

Introduction to population genetics

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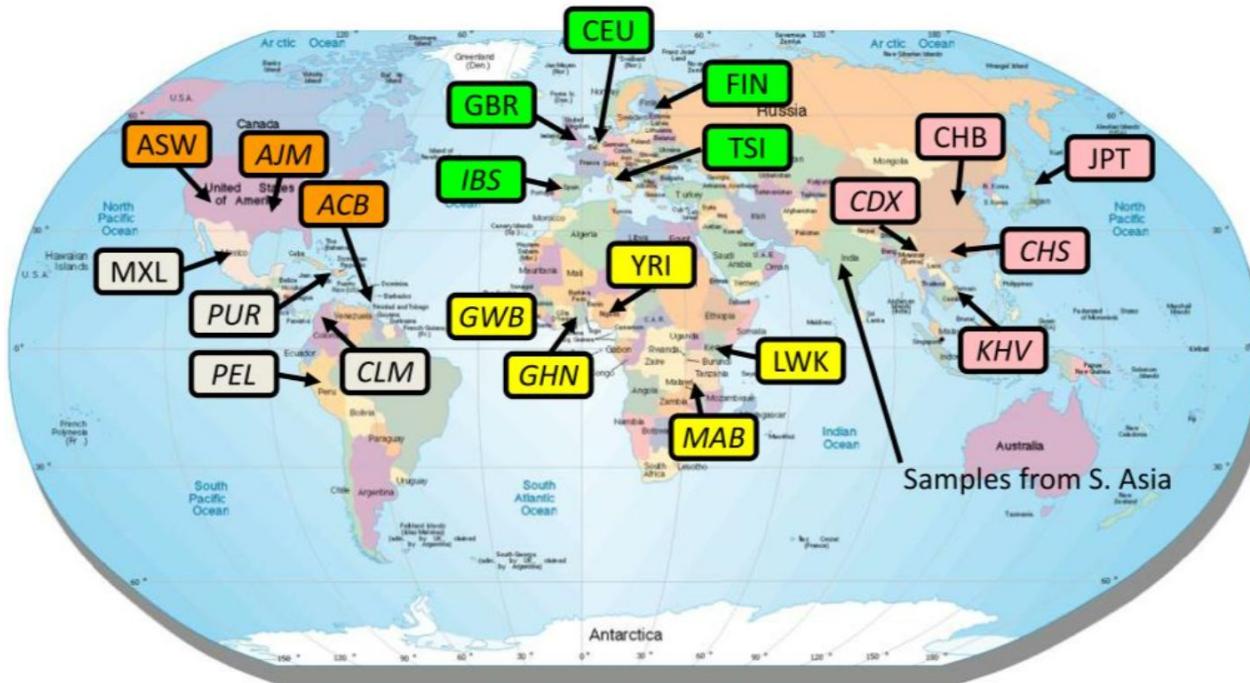
Today's Overview

- i. What is population genomics
- ii. Variation between populations
- iii. Population size
- iv. Sapiens meets Neandertal and Denisovan

What is population genetics?

Population genetics is a subfield of genetics that deals with genetic differences within and among populations.

What is a populations? A group of freely interbreeding individuals.



How many labeled populations are displayed on this map?

Why do population genetics?

- For the love of history (human or non human)
- For medical research
- For research in ecology (conservation genetics)

Genetic variations

Mutations

Human mutation rate is around 1.5×10^{-8} per base pair (bp). Meaning that around 30 new variants will be introduced in each gamete.
The vast majority of mutations are **neutral**.

Genetic variations

Chromosome 1			Population 1				Population 2			
Position	Ref	Alt	Hap1	Hap2	Hap3	Hap4	Hap5	Hap6	Hap7	Hap8
1	A	.	A	A	A	A	A	A	A	A
2	T	.	T	T	T	T	T	T	T	T
4	G	.	G	G	G	G	G	G	G	G
6	G	C	G	G	G	G	G	C	G	C
8	A	.	A	A	A	A	A	A	A	A
	T	.	T	T	T	T	T	T	T	T
	G	A	A	A	G	A	G	G	G	A
	G	.	G	G	G	G	G	G	G	G
	T	A	A	T	T	T	T	T	T	A

Genetic variations

Chromosome 1			Population 1				Population 2			
Position	Ref	Alt	Hap1	Hap2	Hap3	Hap4	Hap5	Hap6	Hap7	Hap8
1	A	.	A	A	A	A	A	A	A	A
2	T	.	T	T	T	T	T	T	T	T
3	G	.	G	G	G	G	G	G	G	G
4	G	.	G	G	G	G	G	G	G	G
5	C	.	G	G	G	G	C	G	C	C
6	A	.	A	A	A	A	A	A	A	A
7	T	.	T	T	T	T	T	T	T	T
8	G	A	A	A	G	A	G	G	G	A
9	C	.	C	C	C	C	C	C	C	C
T	A	.	A	T	T	T	T	T	T	A

Vocab recap!
Positions that
are not identical
for all humans
are called
SNPs or
“variants” or
“segregating
sites”...

Genetic variations: allele frequency

Chromosome 1			Population 1				Population 2			
Position	Ref	Alt	Hap1	Hap2	Hap3	Hap4	Hap5	Hap6	Hap7	Hap8
4	7	G C	G	G	G	G	G C	G	G C	
9		G A	A	A	G	A	G G G	A		
		T A	A	T	T	T	T T T	A		

Genetic variations: allele frequency

Chromosome 1			Population 1				Population 2			
Position	Ref	Alt	Hap1	Hap2	Hap3	Hap4	Hap5	Hap6	Hap7	Hap8
4	G	C	0	0	0	0	0	1	0	1
7										
9	G	A	1	1	0	1	0	0	0	1
	T	A	1	0	0	0	0	0	0	1

The allele frequency is the frequency of an allele in a population

Frequency of the reference allele at position 4:

In population 1 : $4/4 = 1$

In population 2 : $2/4 = 0.5$

Frequency of the reference allele at position 7:

In population 1 : $1/4 = 0.25$

In population 2 : $3/4 = 0.75$

Allele frequencies:

Position	Pop1	Pop2
4	1	0.5
7	0.25	0.75
9	0.75	0.75

Genetic variations: allele frequency

Fixation index (FST)

The FST is a statistic to measure differentiation between two population.

$H_T = 2 * \sum f_i(1-f_i)$ with f_i the allele frequency at position i in both populations. This measure the allele diversity taking both populations together.

$H_S = \sum (f_{i1}^1(1-f_{i1}^1) + f_{i2}^2(1-f_{i2}^2))$ with f_{i1}^1 (resp. f_{i2}^2) the allele frequency at position i in populations 1 and (resp. 2). This measure the allele diversity in both populations separately.

Allele frequencies:

Position	Pop1	Pop2	Pop1&Pop2
4	1	0.5	0.75
7	0.25	0.75	0.5
9	0.75	0.75	0.75

$$FST = \frac{H_T - H_S}{H_T}$$

Genetic variations: allele frequency

Fixation index (FST)

The FST is a statistic to measure differentiation between two population.

$H_T = 2 * \sum f_i(1-f_i)$ with f_i the frequency of allele i in both populations. This measure the allele diversity taking both populations together.

Allele frequencies:

Position	Pop1	Pop2	Pop1&Pop2
4	1	0.5	0.75

$H_S = \sum (f_{i1}^2(1-f_{i1}^2) + f_{i2}^2(1-f_{i2}^2))$ with f_{i1} (resp. f_{i2}) the frequency of allele i in populations 1 and (resp. 2).

7	0.25	0.75	0.5
9	0.75	0.75	0.75

This measure the allele diversity in both populations separately.

$$H_T = 2 * (0.75 * 0.25 + 0.5 * 0.5 + 0.75 * 0.25) = 1.25$$

$$FST = \frac{H_T - H_S}{H_T}$$

Genetic variations: allele frequency

Fixation index (FST)

The FST is a statistic to measure differentiation between two population.

$H_T = 2 * \sum f_i(1-f_i)$ with f_i the frequency of allele i in both populations. This measure the allele diversity taking both populations together.

Allele frequencies:

$H_S = \sum (f_{i1}^1(1-f_{i1}^1) + f_{i2}^2(1-f_{i2}^2))$ with f_{i1}^1 (resp. f_{i2}^2) the frequency of allele i in populations 1 and (resp. 2).

This measure the allele diversity in both populations separately.

Position	Pop1	Pop2	Pop1&Pop2
4	1	0.5	0.75

7	0.25	0.75	0.5
9	0.75	0.75	0.75

$$H_T = 2 * (0.75 * 0.25 + 0.5 * 0.5 + 0.75 * 0.25) = 1.25$$
$$H_S = 1 * 0 + 0.25 * 0.75 + 0.75 * 0.25 + ...$$

$$FST = \frac{H_T - H_S}{H_T}$$

Genetic variations: allele frequency

Fixation index (FST)

The FST is a statistic to measure differentiation between two population.

$H_T = 2 * \sum f_i(1-f_i)$ with f_i the frequency of allele i in both populations. This measure the allele diversity taking both populations together.

Allele frequencies:

Position	Pop1	Pop2	Pop1&Pop2
4	1	0.5	0.75
7	0.25	0.75	0.5
9	0.75	0.75	0.75

$H_S = \sum (f_{i1}^2(1-f_{i1}^2) + f_{i2}^2(1-f_{i2}^2))$ with f_{i1} (resp. f_{i2}) the frequency of allele i in populations 1 and (resp. 2).

This measure the allele diversity in both populations separately.

$$H_T = 2 * (0.75 * 0.25 + 0.5 * 0.5 + 0.75 * 0.25) = 1.25$$
$$H_S = 1 * 0 + 0.25 * 0.75 + 0.75 * 0.25 + 0.5 * 0.5 + 0.75 * 0.25 + 0.75 * 0.25 = 1$$

$$FST = \frac{H_T - H_S}{H_T}$$

Genetic variations: allele frequency

Fixation index (FST)

The FST is a statistic to measure differentiation between two population.

$H_T = 2 * \sum f_i(1-f_i)$ with f_i the frequency of allele i in both populations. This measure the allele diversity taking both populations together.

Allele frequencies:

$H_S = \sum (f_{i1}^1(1-f_{i1}^1) + f_{i2}^2(1-f_{i2}^2))$ with f_{i1}^1 (resp. f_{i2}^2) the frequency of allele i in populations 1 and (resp. 2).

This measure the allele diversity in both populations separately.

$$FST = \frac{H_T - H_S}{H_T}$$

Position	Pop1	Pop2	Pop1&Pop2
4	1	0.5	0.75
7	0.25	0.75	0.5
9	0.75	0.75	0.75

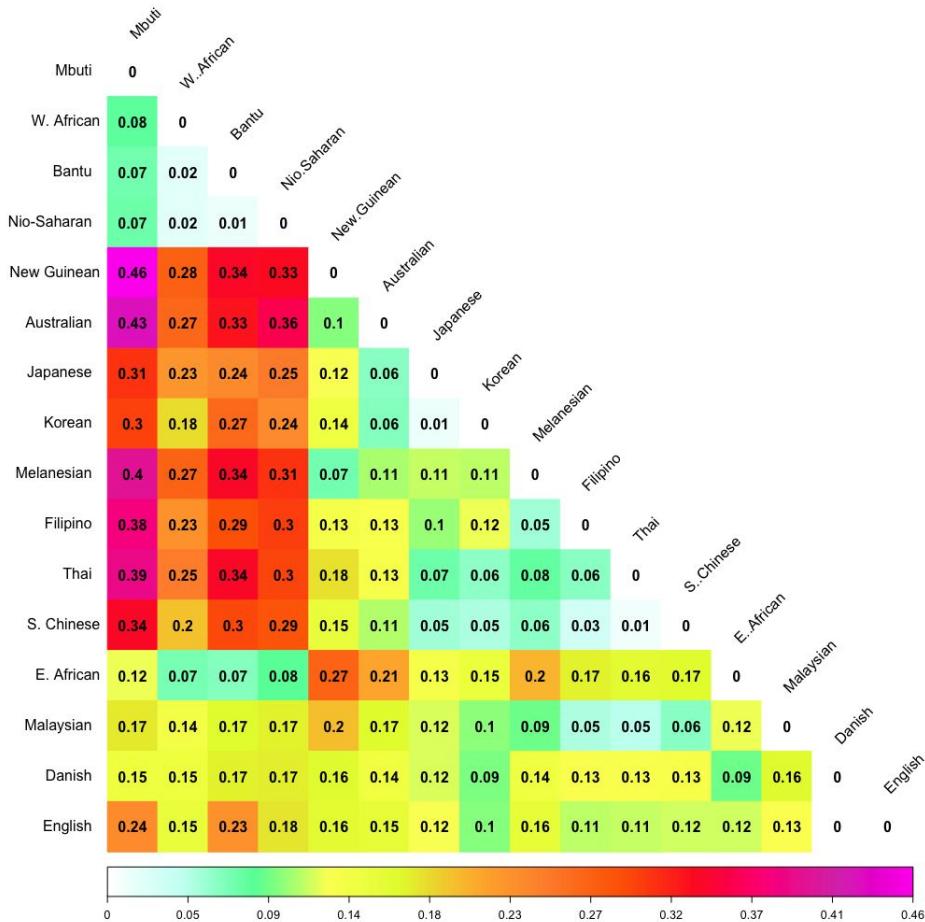
$$H_T = 2 * (0.75 * 0.25 + 0.5 * 0.5 + 0.75 * 0.25) = 1.25$$

$$H_S = 1 * 0 + 0.25 * 0.75 + 0.75 * 0.25 + 0.5 * 0.5 + 0.75 * 0.25 + 0.75 * 0.25 = 1$$

$$FST = (1.25 - 1) / 1.25 = 0.2$$

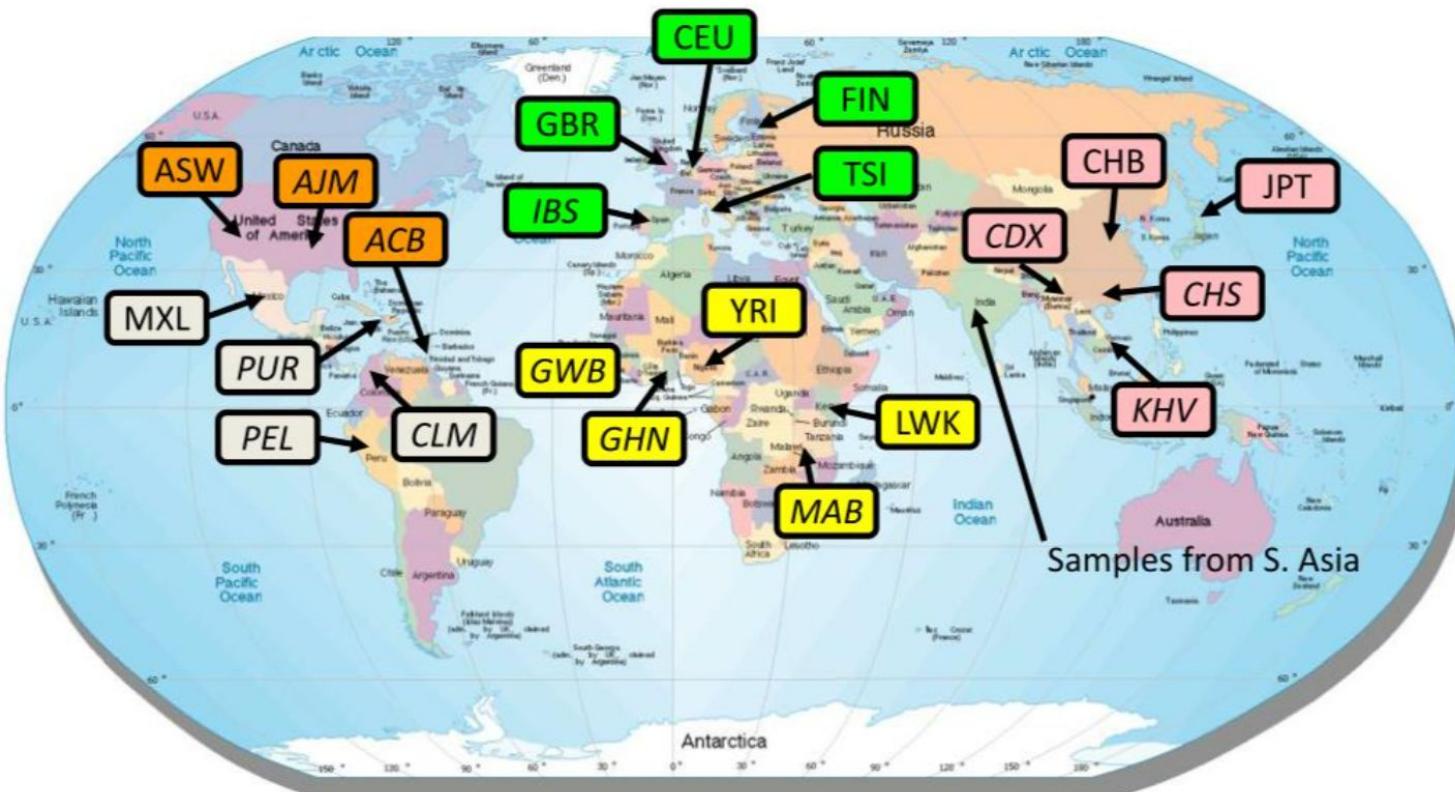
Conclusion: There is 20% more differences between the two populations than within each one.

Genetic variations: allele frequency - (FST)



- The average FST between continent is at around 10%.
- If we were to do an FST-like statistic on skin color, that number would be around 90%.
- The reason is strong selection on genes responsible for the skin color.

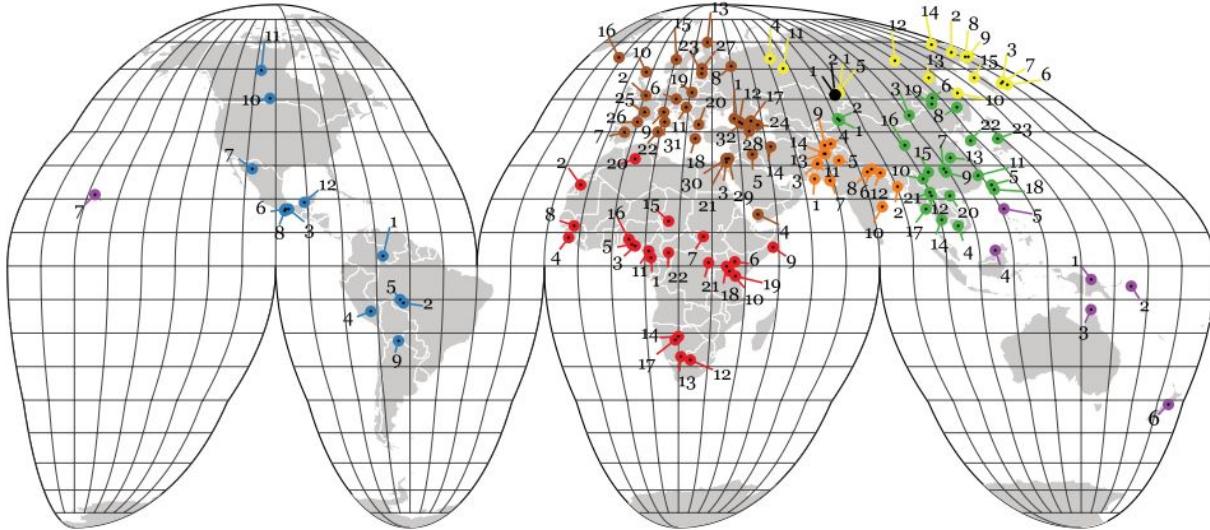
Data availability - 1000 Genome project



Sequencing of around 100 genomes per 12 different populations around the globe.

Data is publicly available.

Data availability - SGDP



- 1 - Neanderthal
- 2 - Denisova
- 1 - Piapeco
- 2 - Surui
- 3 - Mixe
- 4 - Quechua
- 5 - Karitiana
- 6 - Mixtec
- 7 - Pima
- 8 - Zapotec
- 9 - Chane
- 10 - Cree
- 11 - Chipewyan
- 12 - Maya
- 1 - Xibo
- 2 - Uygor
- 3 - Mongola
- 4 - Cambodian
- 5 - Atayal
- 6 - Oroqen
- 7 - Tujia
- 8 - Hezhen

- 9 - Miao
- 10 - Naxi
- 11 - She
- 12 - Dai
- 13 - Han
- 14 - Thai
- 15 - Yi
- 16 - Tu
- 17 - Burmese
- 18 - Ami
- 19 - Daur
- 20 - KinhKVH
- 21 - Lahu
- 22 - Korean
- 23 - Japanese
- 1 - Papuan
- 2 - Bougainville
- 3 - AustraliaECCAC
- 4 - Dusun
- 5 - Igorot
- 6 - Maori
- 7 - Hawaiian

- 1 - Adygei
- 2 - EnglandGBR
- 3 - Bedouin
- 4 - YemeniteJew
- 5 - IraqiJew
- 6 - Czechoslovakian
- 7 - SpainIBS
- 8 - Russian
- 9 - Bergamo
- 10 - Orcadian
- 11 - Hungarian
- 12 - Abkhazian
- 13 - Saami
- 14 - Iranian
- 15 - Norwegian
- 16 - Icelandic
- 17 - Chechen
- 18 - Greek
- 19 - Polish
- 20 - Bulgarian
- 21 - Palestinian
- 22 - Sardinian

- 23 - Estonian
- 24 - Lezgin
- 25 - French
- 26 - Basque
- 27 - FinlandFIN
- 28 - Armenian
- 29 - Jordanian
- 30 - Druze
- 31 - Tuscan
- 32 - Georgian
- 1 - Kongo
- 2 - Saharawi
- 3 - Igbo
- 4 - MendeMSL
- 5 - EsanESN
- 6 - LuhyaLWK
- 7 - Dinka
- 8 - Mandenka
- 9 - Somali
- 10 - MasaiMKK
- 11 - Lemande
- 12 - BantuSETswana

- 13 - KhomaniSan
- 14 - San
- 15 - GambiaGWD
- 16 - Yoruba
- 17 - BantuSEHerero
- 18 - Luo
- 19 - BantuKenya
- 20 - Mozabite
- 21 - Mbuti
- 22 - Biaka
- 1 - Makrani
- 2 - BengaliBEB
- 3 - Igbo
- 4 - Burusho
- 5 - PunjabiPJL
- 6 - Tibetan
- 7 - Sindhi
- 8 - Kusunda
- 9 - Kalash
- 10 - Madiga
- 11 - Brahui
- 12 - Sherpa

236 individual genomes (total) from 125 distinct human populations

Genetic distances

Allele frequencies:

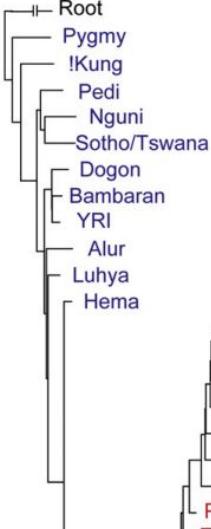
Position	Pop1	Pop2	Pop3
4	1	0.5	0.85
7	0.25	0.75	0.35
9	0.75	0.75	0.8

How to compute the distance
between population i and j at
some position:

$$d_{ij} = |p_i - p_j|$$

With p_i and p_j allele frequencies.

We then compute mean by taking
the average value for all
positions.



Genetic distances - Population trees

Allele frequencies:

Position	Pop1	Pop2	Pop3
4	1	0.5	0.85
7	0.25	0.75	0.35
9	0.75	0.75	0.8

$$d(\text{pop1}, \text{pop2}) = \frac{(|1-0.5| + |0.25-0.75| + |0.75-0.75|)}{3} = 0.33$$

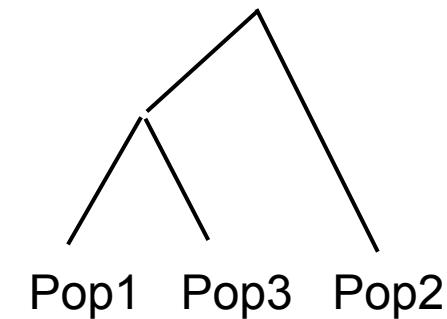
$$d(\text{pop1}, \text{pop3}) = 0.1$$

$$d(\text{pop2}, \text{pop3}) = 0.26$$

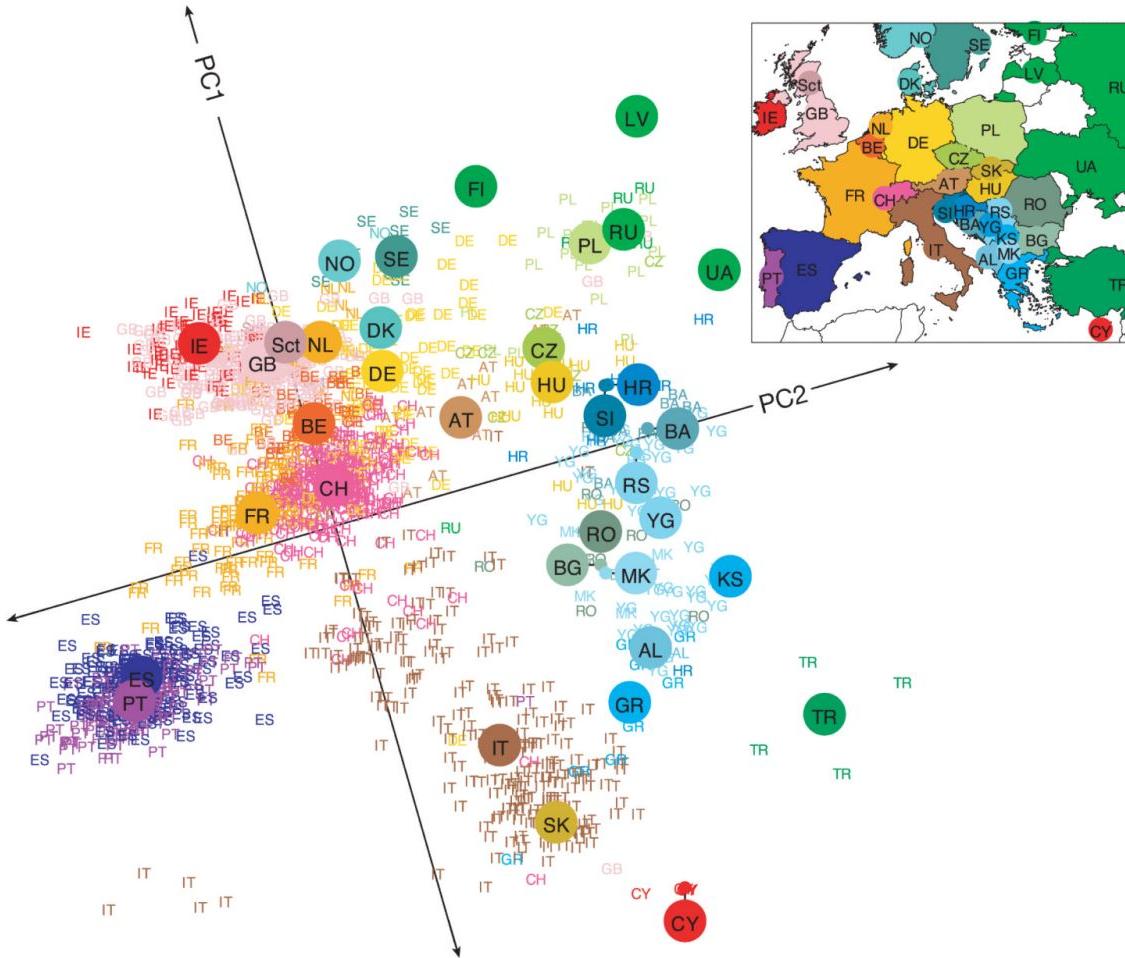
How to compute the distance between population i and j at some position:

$$d_{ij} = |p_i - p_j|$$

With p_i and p_j allele frequencies.
We then compute mean by taking the average value for all positions.

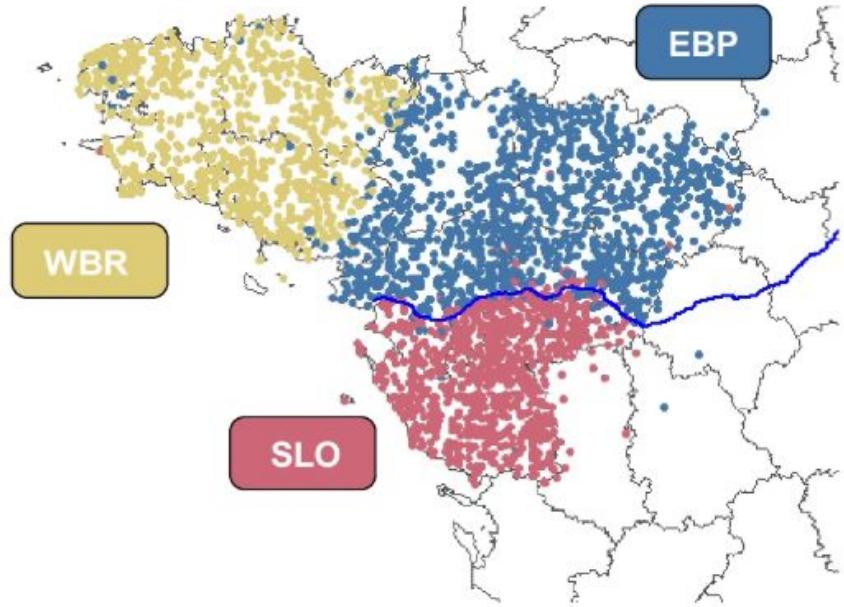


Principal Component Analysis (PCA)

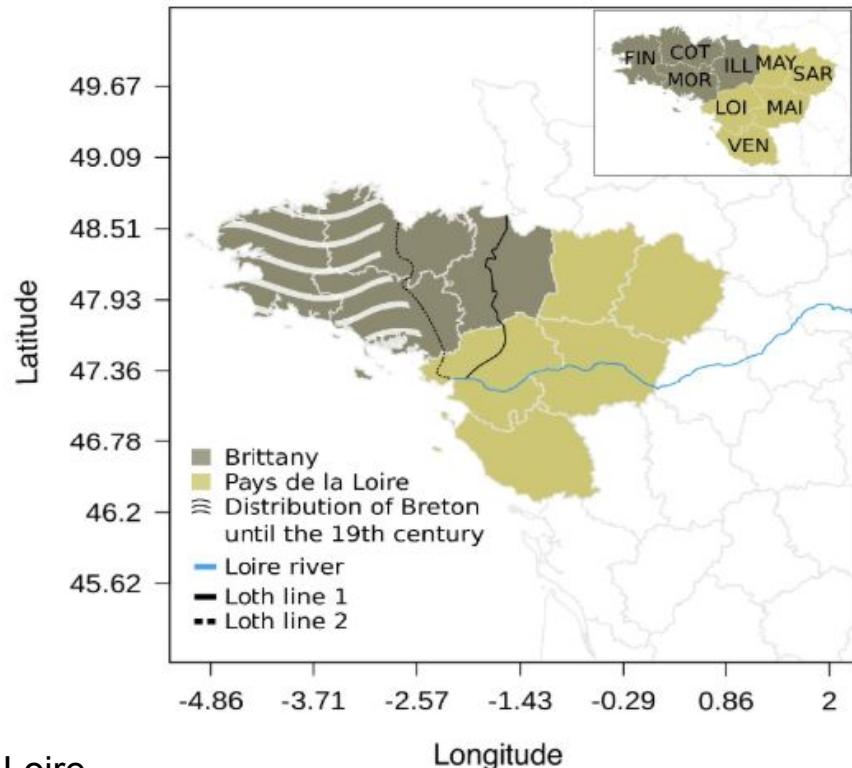


Dataset of 197,146 SNPs per individual projected on 2-d space.

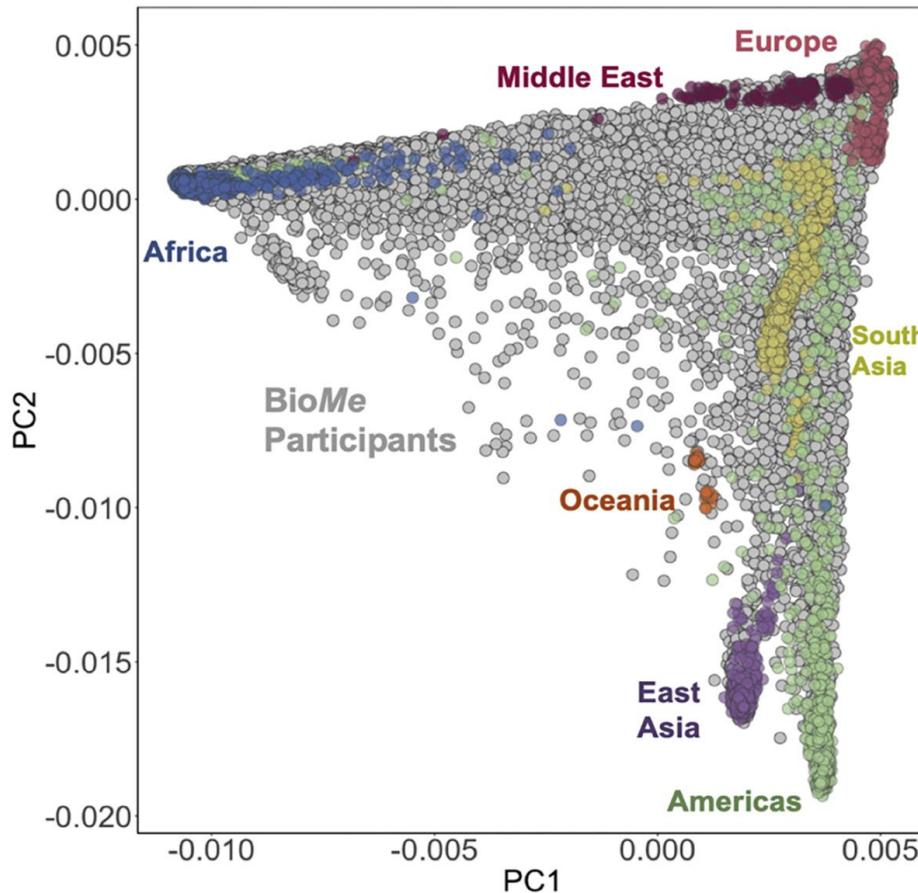
k-clustering



WBR: Western Brittany, EBP: Eastern Brittany and Pays-de-la-Loire,
SLO:South Loire. 3234 present day individuals.
Alves et al. (2024)

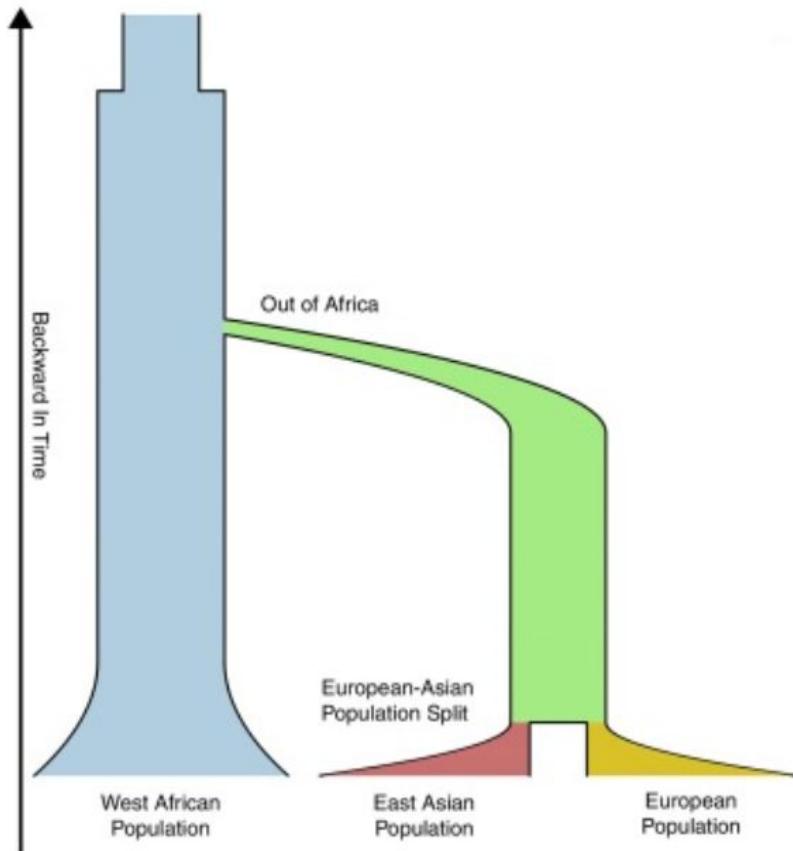


Population as strict categories?



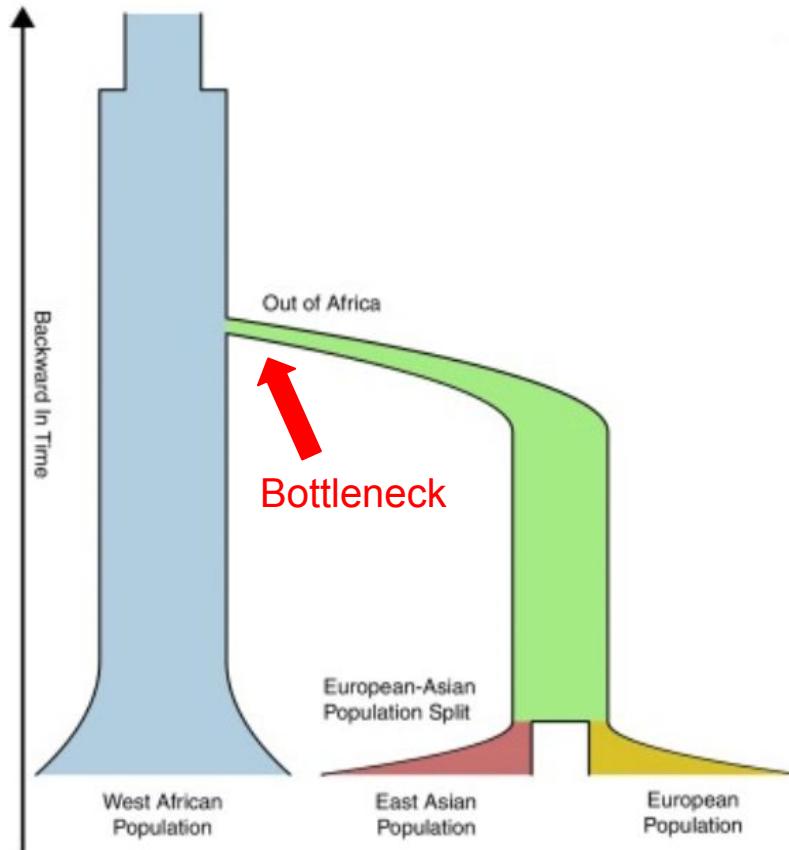
Population size

Population size



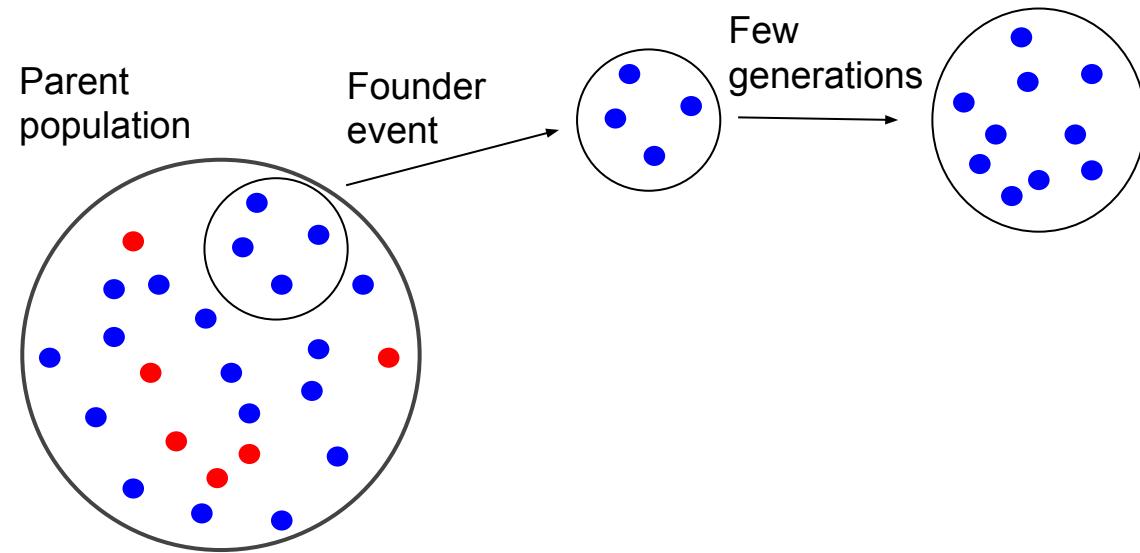
- Population sizes vary through time
- This can be inferred from present day genomes
- First idea:
low genetic diversity \Leftrightarrow low population size

Population size: bottlenecks

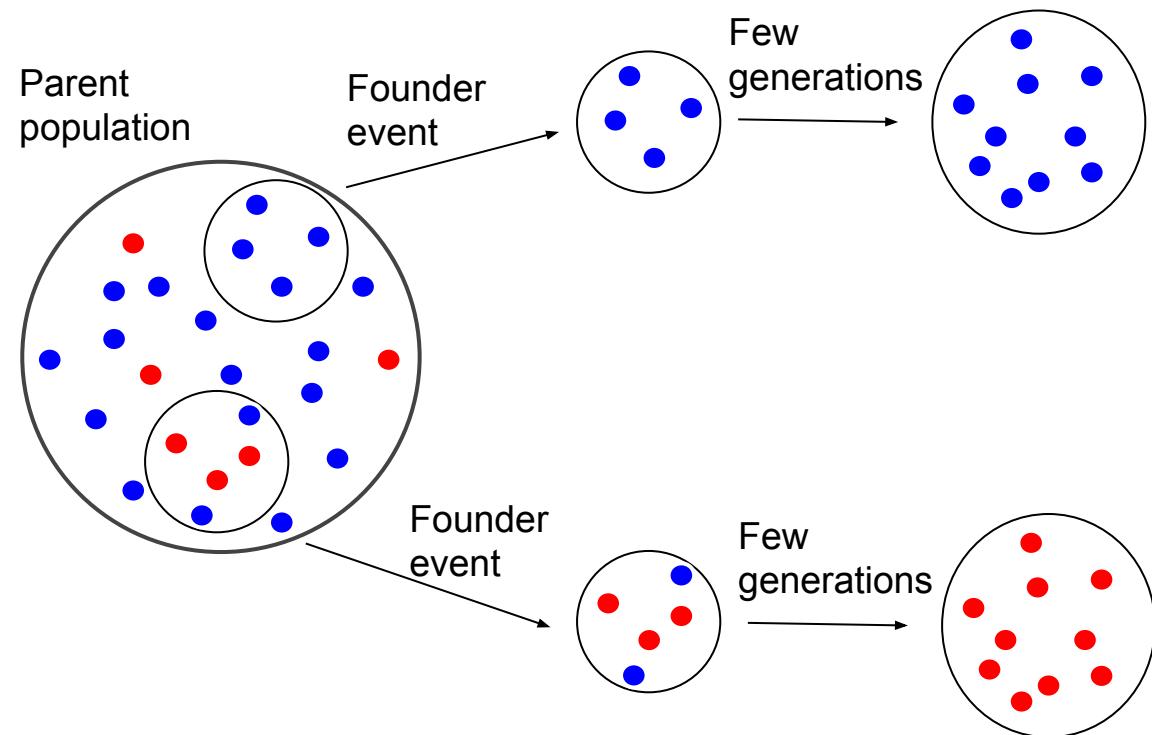


- A bottleneck is a large reduction in population size
- During such events, lots of variants are lost and genetic diversity suddenly decreases

Population size - bottlenecks and founder effect



Population size - bottlenecks and founder effect



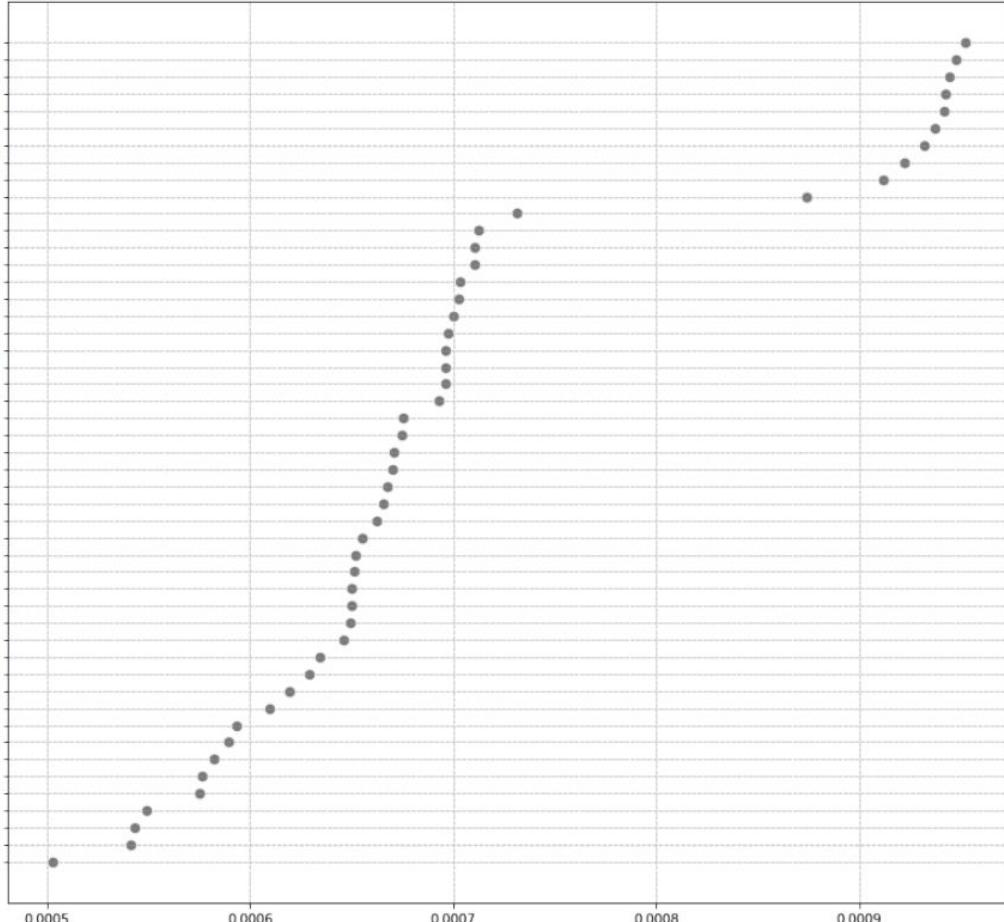
- A bottleneck can be caused by migrations (e.g. the Out of Africa event or the peopling of the Americas) or by environmental events.
- Due to the **founder effect**, a bottleneck will cause a loss of genetic diversity that cannot be recovered even if the population grows afterward.

Population size - bottlenecks consequences

African populations

Biaka
Mende
Luo
Yoruba
Mandenka
Lemande
Gambian
Mbuti
Masai
Dinka
Palestinian
Norwegian
North_Ossetian
Iranian
Spanish
Tlingit
Georgian
Bulgarian
Madiga
Icelandic
Armenian
Greek
Aleut
Naxi
Polish
Daur
Tu
Tajik
Tibetan
Balochi
Hezhen
Uchi
Xibo
Japanese
Yi
Lahu
She
Dusun
Bougainville
Onge
Igorot
Zapotec
Chipewyan
Quechua
Nahua
Papuan
Piapoco
Pima
Karitiana

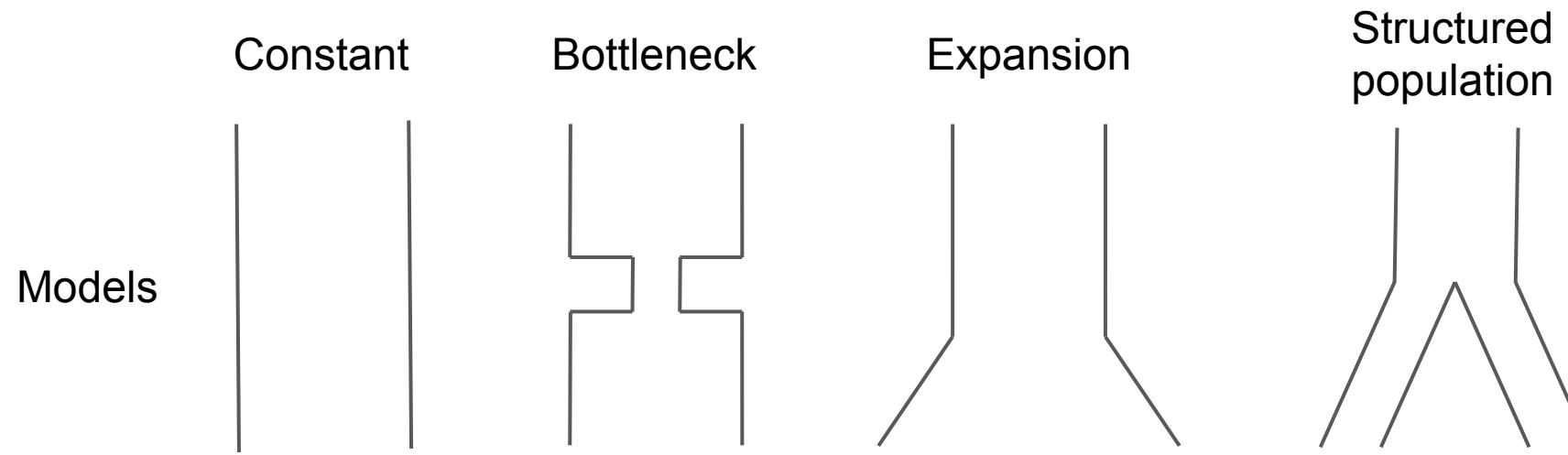
Native Americans
Papuans



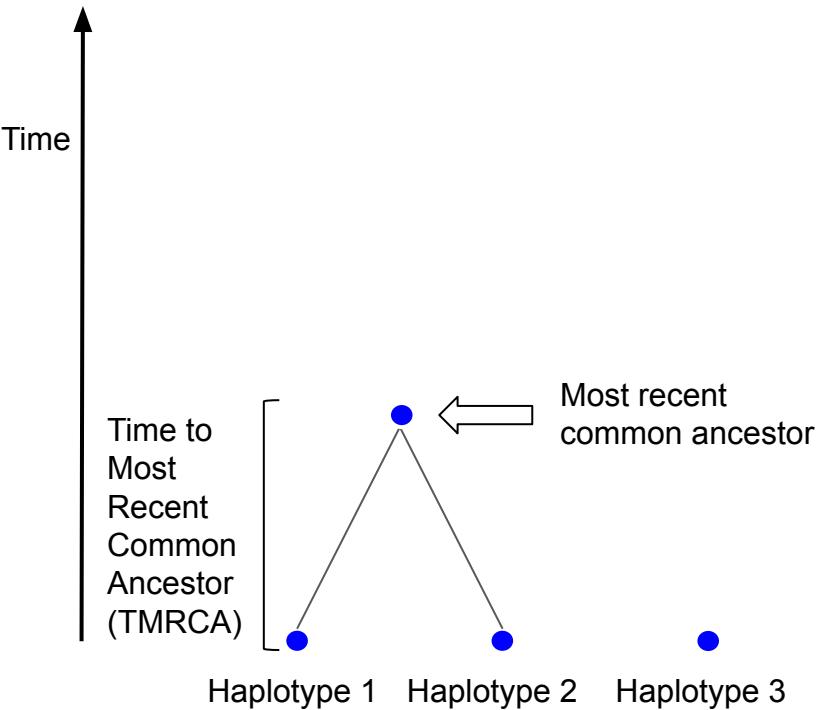
- African populations have the highest amount of genetic diversity.
- Native Americans have the least genetic diversity due to multiple consecutive bottlenecks.

x-axis: heterozygosity proportion (higher -> more genetic diversity)

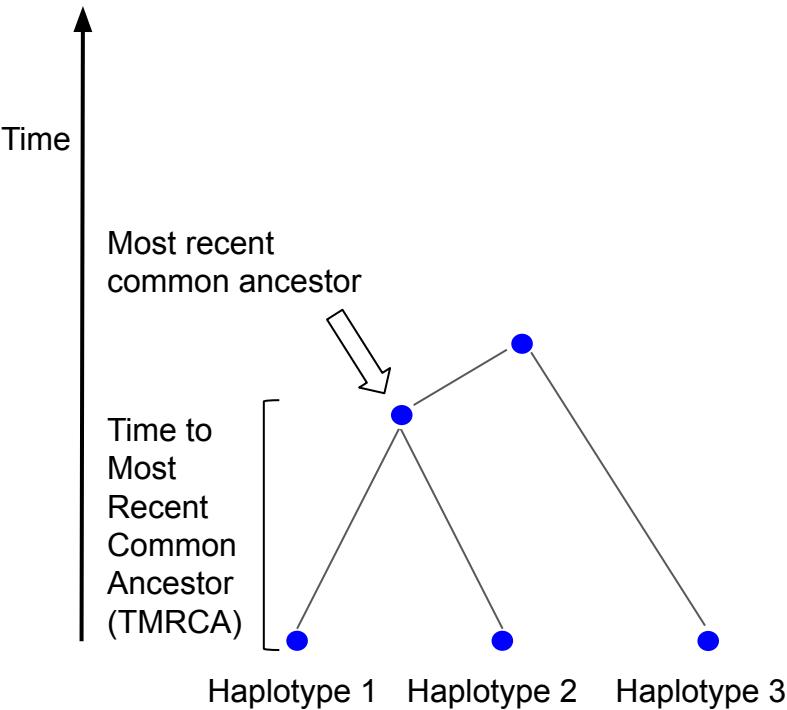
Inferring population size history



Inferring population size - Coalescence trees



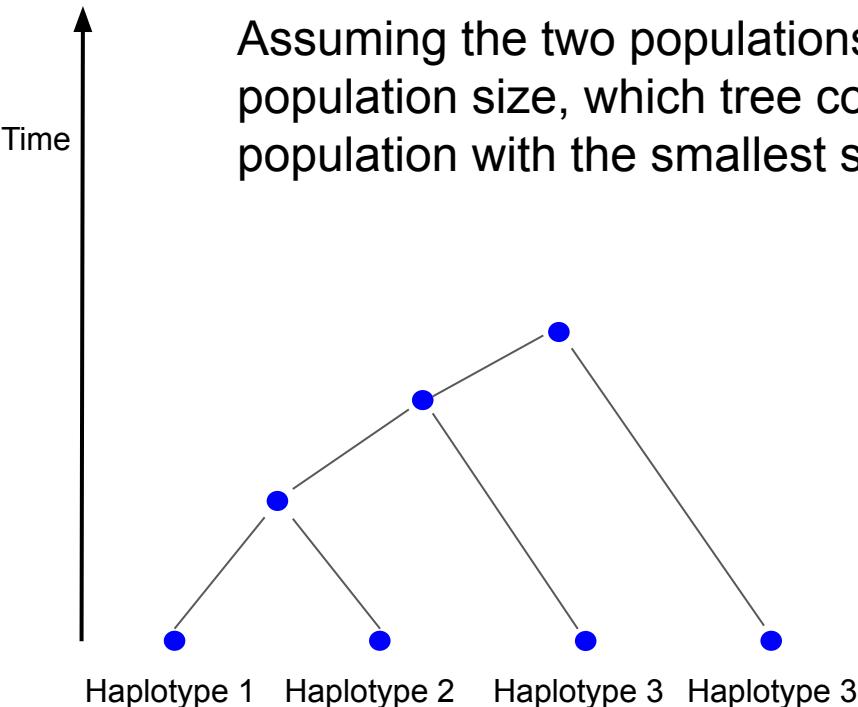
Inferring population size - Coalescence trees



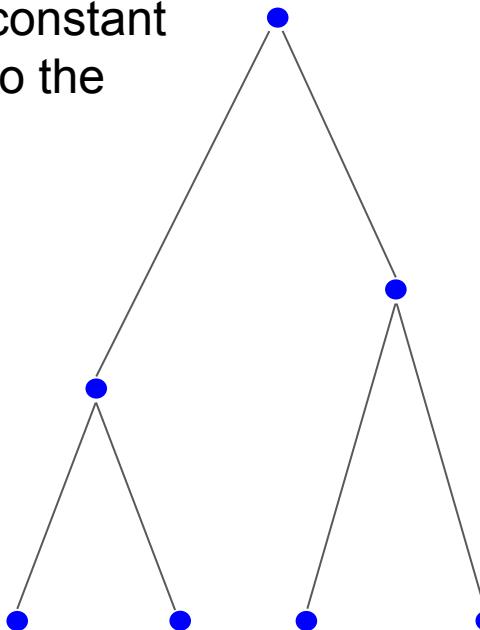
Some vocabulary:

- Any two haplotypes must come from the same ancestral haplotype at some point in the past.
- We say that the haplotypes **coalesce** (merge) together at time **TMRCA**.
- If we take multiple haplotypes, we can build a tree from this, it is called a **coalescence tree**.

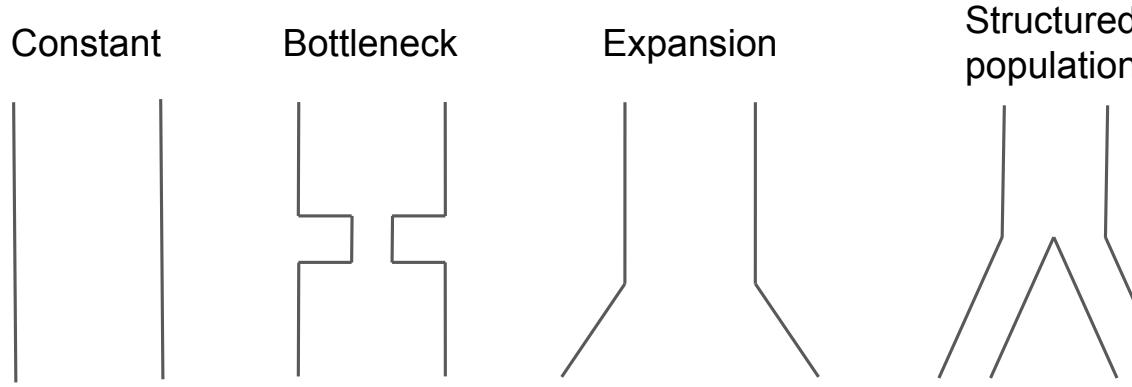
Inferring population size - Coalescence trees



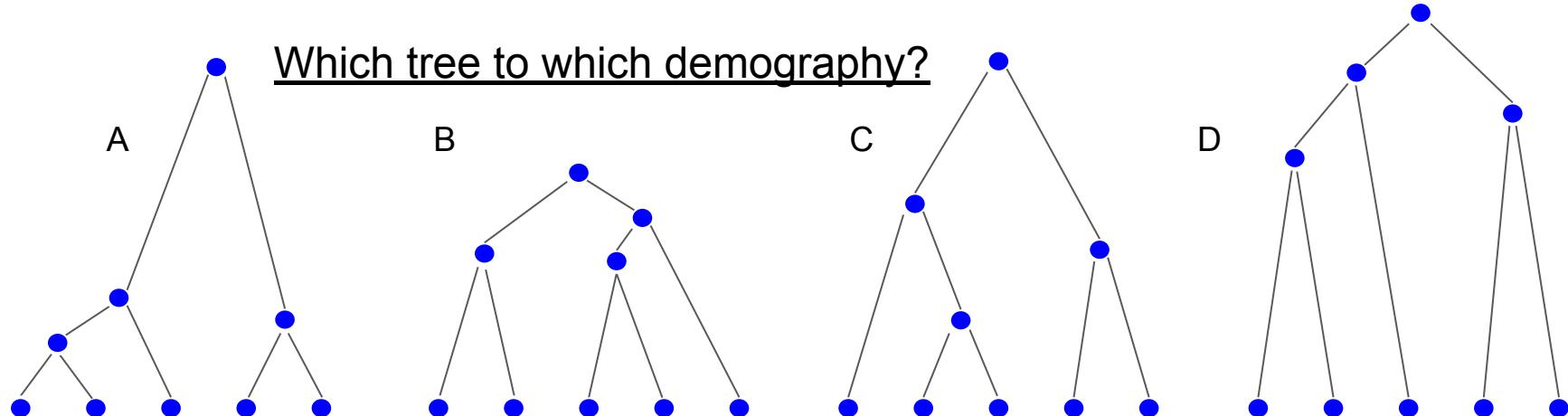
Assuming the two populations are with constant population size, which tree correspond to the population with the smallest size ?



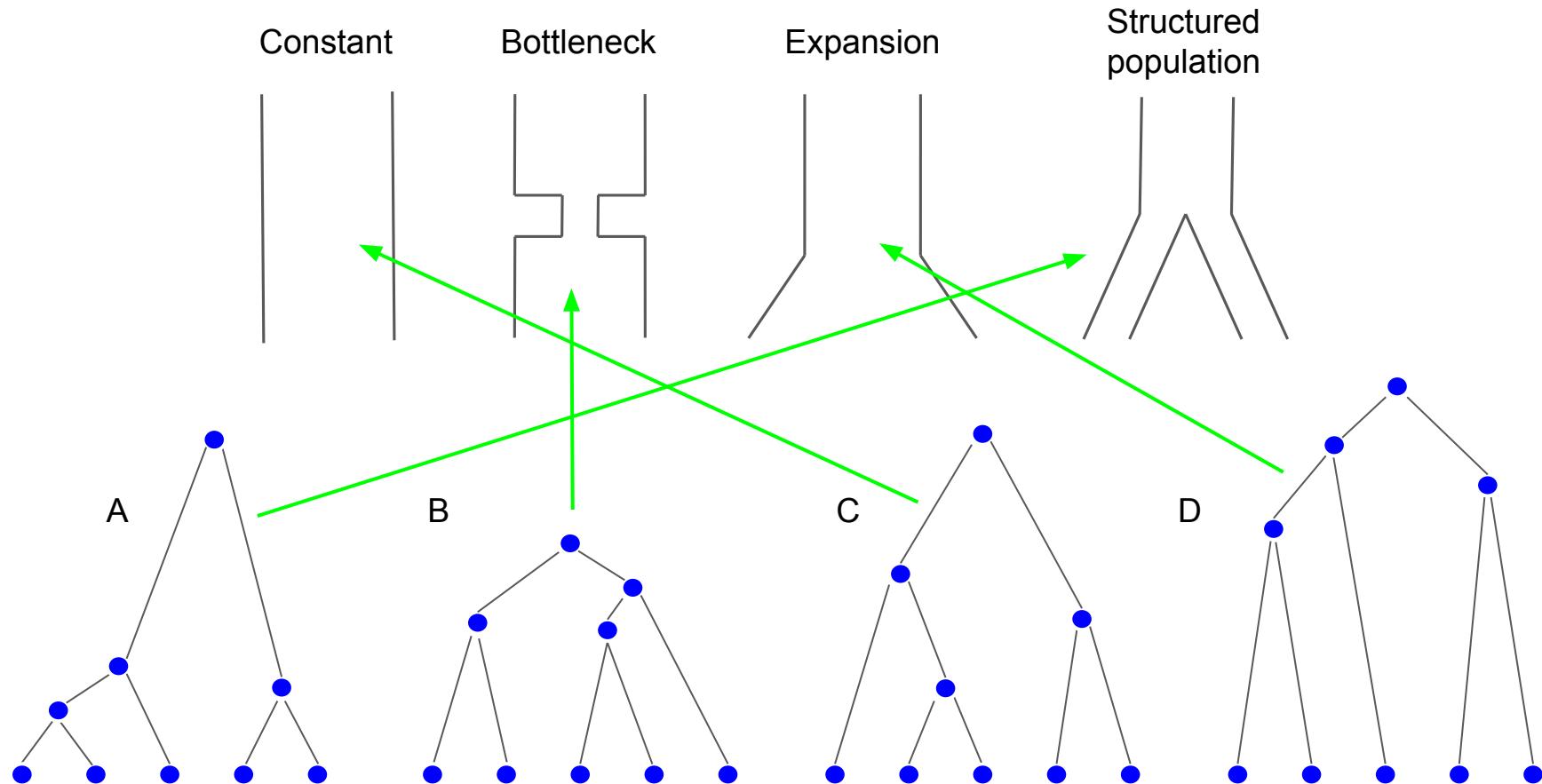
Inferring population size history



Which tree to which demography?



Inferring population size history



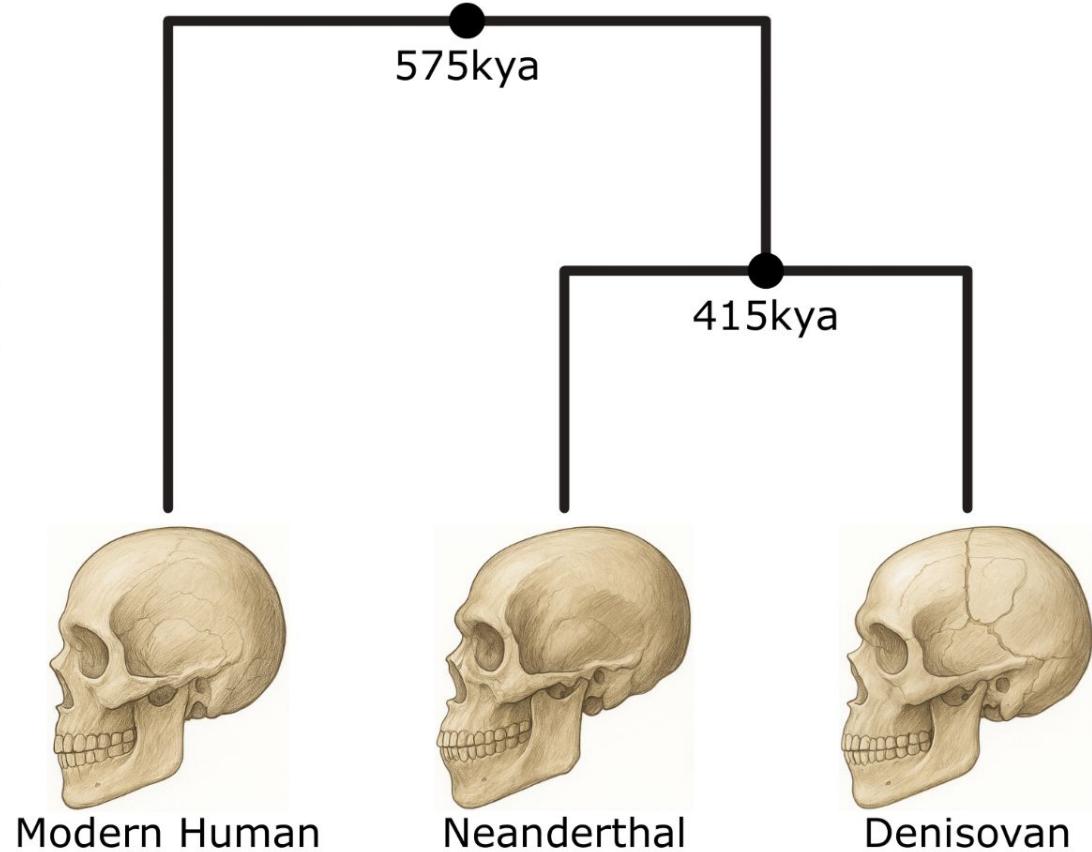
Inferring population size history

Conclusion:

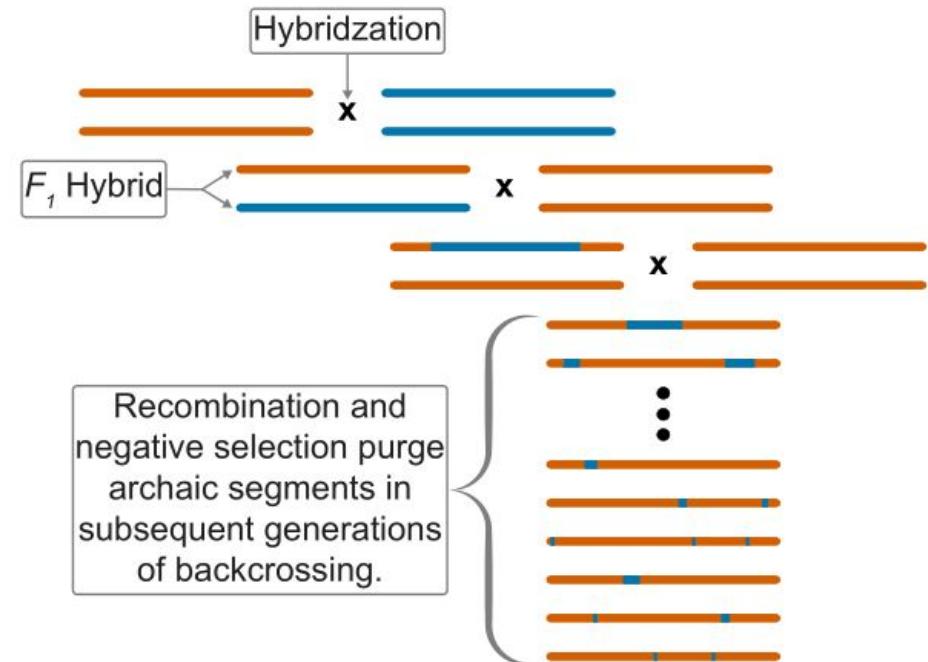
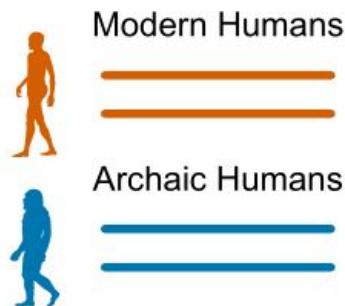
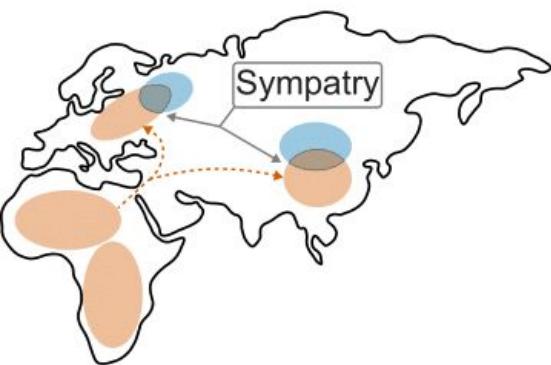
- If we are able to construct the coalescence tree from a population, we can know its whole population size history.
- Population size history can notably inform us about past migrations or ecological events.
- Still, how do we construct this coalescence tree from genomic data?
- The full answer is not for today! Key idea: If two individuals are closely genetically related, then they have a recent common ancestor and conversely.

Archaic ancestry

Archaic Humans



Archaic Introgression



Archaic Introgression

Possible questions:

- Do we have archaic DNA, if so, how much and in which populations?
- Can we locate where archaic DNA is present in our genomes?
- Was there positive or negative selection for archaic DNA in Sapiens?
- If Archaic DNA is found in multiple contemporary populations (i.e Europe and Asia), does it have the same source?
- Can we date the introgression(s) event(s)?
- How did this archaic DNA spread through time?

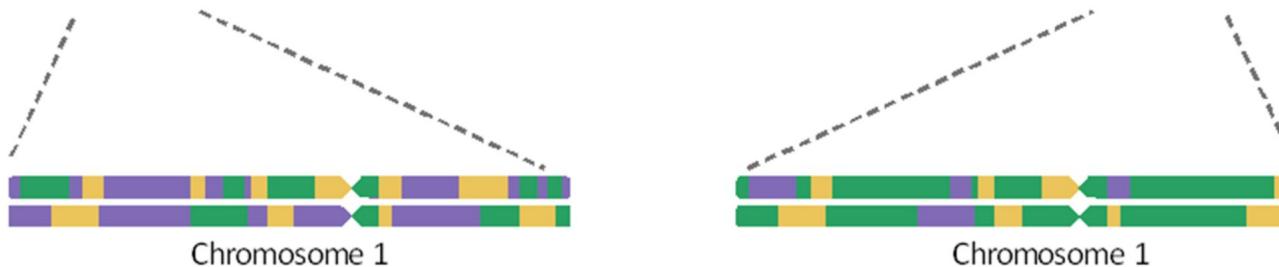
Global and Local ancestry inference

A.

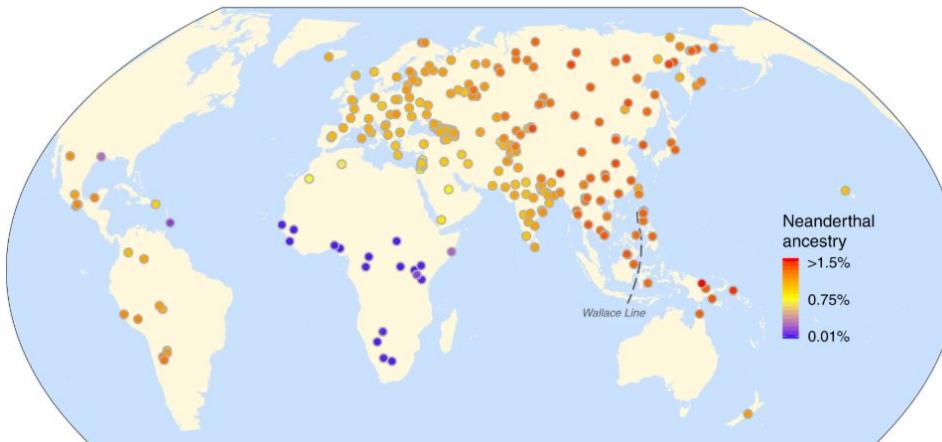
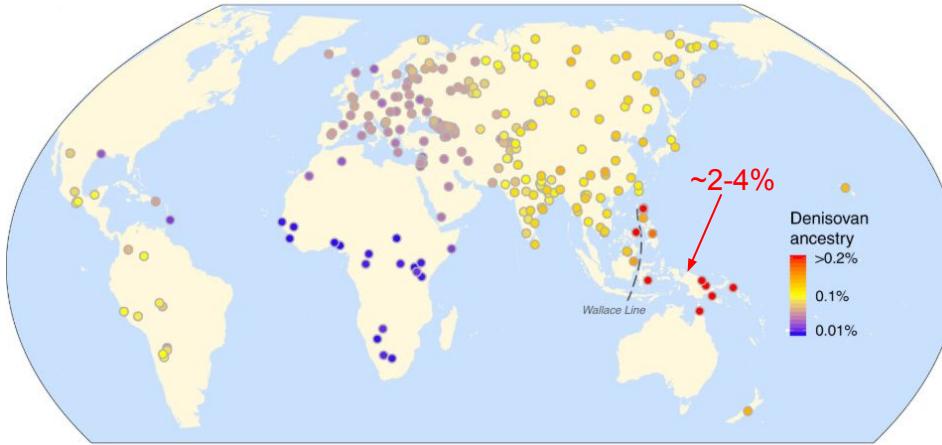


- A. Global ancestry inference.
- B. Local ancestry inference (LAI)

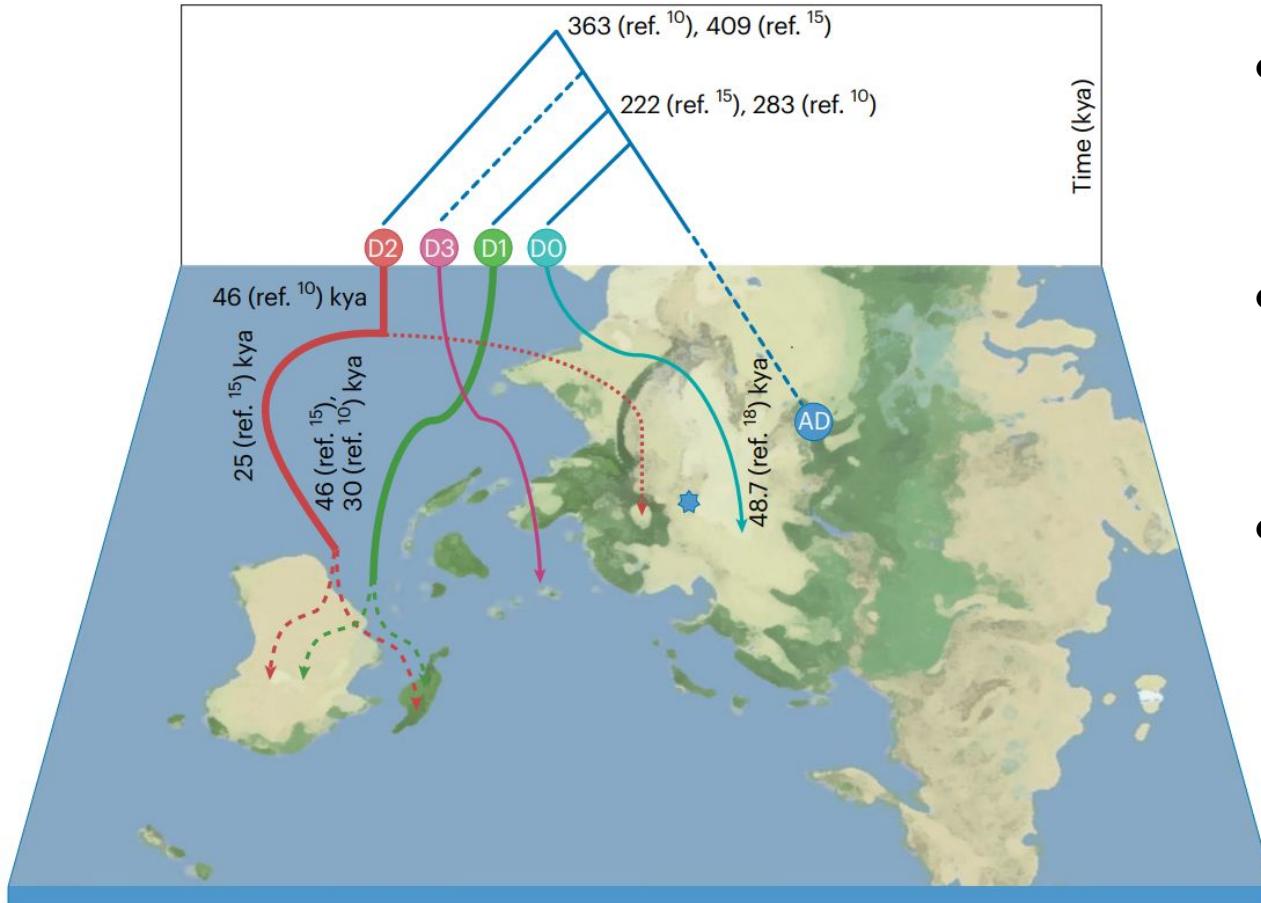
B.



Archaic Introgression - Global ancestry



Archaic Introgression - Multiple sources



- Most likely a single Neanderthal introgression event
- Multiple Denisovan introgression events, the number is still debated
- This can be deduced by comparing Denisovan segments in modern humans to the Denisovan reference genome

Archaic Introgression - Adaptively introgressed genes

