

Session 3 – From Learning Architectures to Decision Profiles

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### From Deduction to Induction

#### Deduction

Learning architectures → decision profiles

Learning architectures 

?
decision profiles

Induction



### Review of Sessions 1 and 2

- > Architectures for decision making
  - > **Learning in human teams** (supervision, interaction)
  - > Reinforcement learning (online-offline, learning with state-action pairs)
  - > Rule-based systems (Finite State Machines, conditional logic)
  - > **Multi-agent learning** (joint-separate, "Policy Geometry")

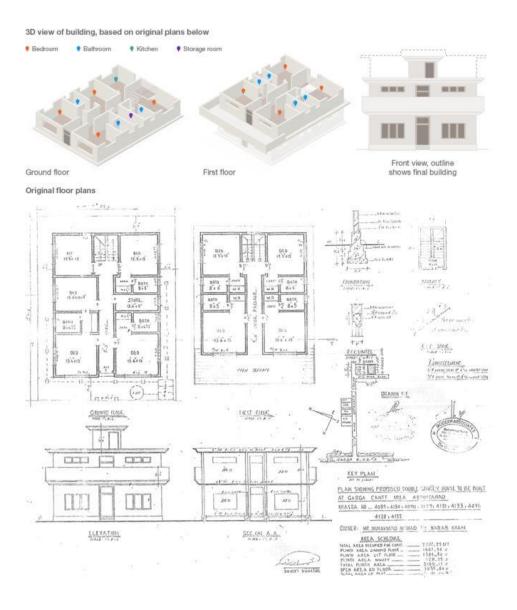


### Outline

- 1. Exercise on Rule-Based Systems
- 2. Recap on Reinforcement Learning
- 3. Q-Learning
- 4. Case on Inferring Learning Architectures from Observed Behavior



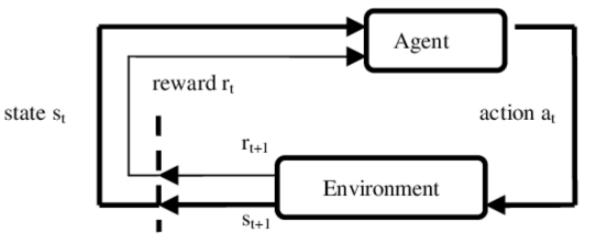
### Location X





## Review of Reinforcement Learning Basics

- > RL is suitable to a class of problems known as the Markov Decision Process (MDP)
  - > Outcome of applying action to any state depends only on this action a and state s (and not on preceding a or s)
  - > Information available to the agent: rewards and subsequent state for each state-action transition



> What are the components of a MDP?

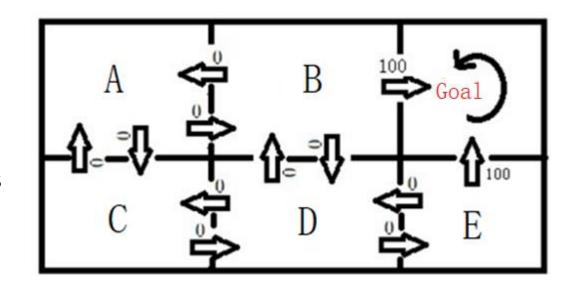


### What is the Total (Cumulative) Reward?

- > After performing action a in state s (state action pair s, a):
  - > The agent receives immediate reward of either 0 or 100
  - > The agent goes to the next state
- > The action that the agent chooses in every state s is dictated by a policy  $\pi$

$$> \pi(s_t) = a_t$$

> The total reward that the agent gets (from  $\pi$ ) is the sum of the sequence of rewards that it gets by following  $\pi$ , discounted by  $\Upsilon$ 

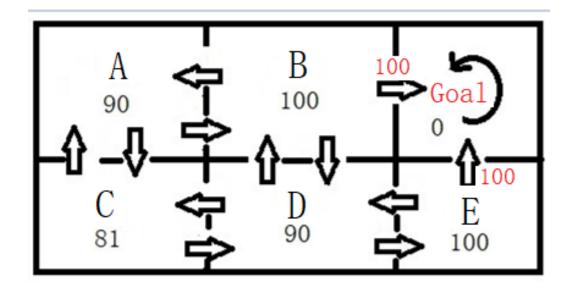


$$V^{\pi}(s_t) = r_t + \gamma r_{t+1} + y^2 r_{t+2} + \cdots$$



## What is the Agent's Goal?

- > What is the goal of an agent that uses RL?
  - > Pick the best policy that will maximize the total rewards that the agent receives
- > How does it do that?
  - > The agent needs to evaluate the "goodness" of each state. How good is it to be in Grid A, in Grid E?
  - > This evaluation can be done if the agent knows the maximum total reward that it can achieve in each state
  - > We call this the "optimal value function" V\*(s)
  - > If we have good estimates of V\*(s), then we can choose the optimal policy



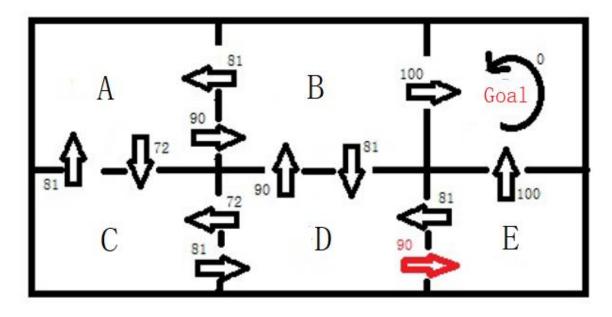
$$V^*(s=A)$$

$$\pi^*(s) = \underset{a}{argmax}[r(s, a) + \gamma V^*(\delta(s, a))]$$



### The Q-Function

- > Rather than evaluating the "goodness" of each state, we can also evaluate the goodness of each state-action pair
  - > How good it is for me to perform RIGHT in state D (as oppose to RIGHT) in state B?
  - > Compare the Q value of doing RIGHT in D and RIGHT in B
  - > Q value is the maximum achievable total reward that the robot get by performing a in s, and then following optimal policy thereafter



$$Q(s,a) = r(s,a) + \gamma V^* (\delta(s,a))$$
$$Q(s = D, a = right) = 0 + 0.9 * 100 = 90$$

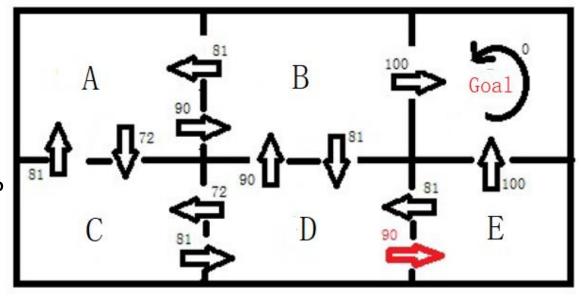


## The Bellman Equation

> The Q-function can be rewritten as the Bellmann Equation:

$$Q(s,a) = r(s,a) + \gamma \max Q(\delta(s,a),a')$$

- > Learning Q corresponds to learning the optimal policy.
- > What is Q(s=D, a=RIGHT) from the Bellmann Equation?
- > Learning Q corresponds to learning the optimal policy. Assuming Q-values are known, what is the optimal strategy starting from A?



$$\pi^*(s) = \underset{a}{argmax} \ Q(s, a)$$



### Learn $V^*(s)$ or Q(s, a)?

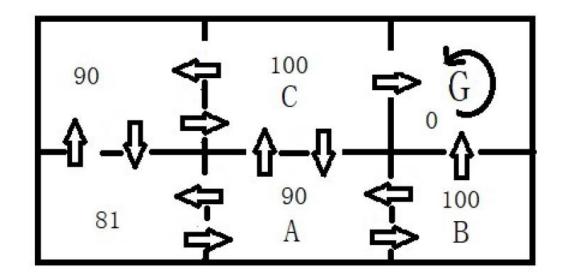
> **Approach 1:** If we know the true V\*(s) values, we know the optimal policy:

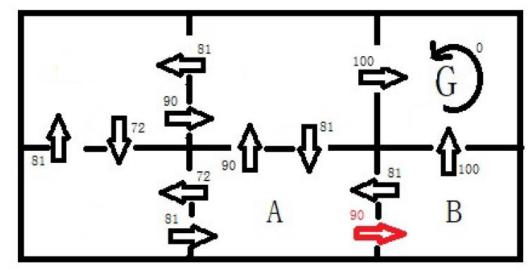
$$\pi^*(s) = \underset{a}{argmax}[r(s, a) + \gamma V^*(\delta(s, a))]$$

> **Approach 2:** If we know the true Q-values, we know the optimal policy:

$$\pi^*(s) = \underset{a}{argmax} \ Q(s, a)$$

> Which approach should we choose?







## Model-based vs. Model-free Learning

#### **Model-Based Learning**

- > Model of the environment : reward and statetransition need to be known
- > The agent interacts with environment, and from the "history" of its interactions, the agent will approximate the reward and state transition
- > After that, the agent learns the V\*(s) using an algorithm called "Value iteration". Once the V\*(s) values are known, the agent can find the optimal policy

$$\pi^*(s) = \underset{a}{argmax}[r(s,a) + \gamma V^*(\delta(s,a))]$$

#### **Model Free Learning**

- > The agent will not try to "guess" the reward and state transition functions. It will only "experience" them as it explores the environment
- > By trail and error, the robot discovers what are the good and bad actions in each state
- > Uses "Q learning" to approximate the Q(s, a) values and find optimal policy

$$\pi^*(s) = \underset{a}{argmax} \ Q(s, a)$$



## The Q-Learning Algorithm

#### > Assumptions:

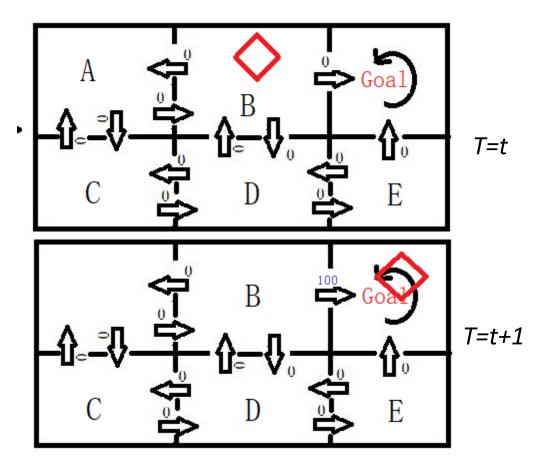
- > (A1) Reward and state-transitions functions are unknown but deterministic.
- > (A2) Robot visit every possible state with non-zero frequency overtime.
- > (A3) Rewards are bounded (not infinite).

#### > Algorithm:

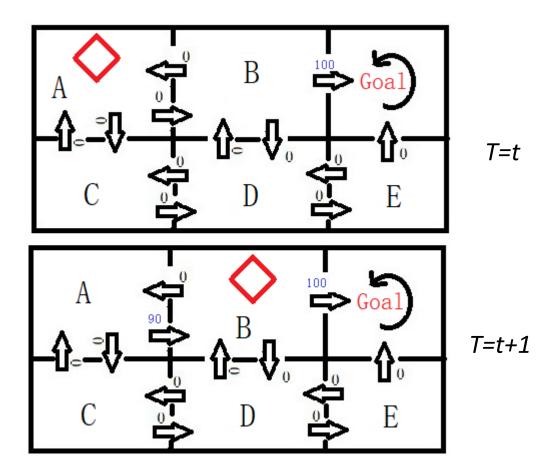
- 1. Initially fill the table of  $\widehat{Q}$  (estimated Q-values) with zeros
- 2. Observe current state s
- 3. Select and action a and executes it
- 4. Receive immediate reward r
- 5. Observe the new state s'
- 6. Update the table entry for  $\widehat{Q}(s, a)$  using the Bellman equation
- 7. Set state s' to s, repeat 2-6 until  $\widehat{Q}$  converges (new  $\widehat{Q}$  values do change much from old values)



## **Example: Information Propagation**



Training Episode 1



Some Training Episode after 1



## Strategies for Experimentation

- > The Q-learning algorithm does not specify how the agent chooses its actions
- > If the agent *always* selects the state-action pair with the highest estimated Q-values, then it will "overcommit" to its actions found in the early training sessions, while failing to explore other state-action pairs that might have even higher Q-values
- > Solution to Exploration vs. Exploitation dilemma:
  - > During early training episodes: All actions have a chance of being executed
  - > During the latter training episodes: Actions with higher  $\hat{Q}$  will be assigned with increasingly higher probabilities, so overtime, the agent will do more exploitation and less exploration



### Decision Profiles in Unbounded Environments

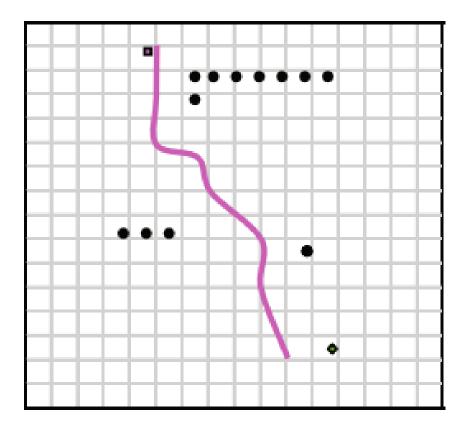
Learning architectures 

? decision profiles

- > Does each architecture correspond to a distinctive decision profile?
- > How can we discern this decision profile?
- > What are the consequences, if we answer the first or second question negatively?



# **AV Flight Trajectory**



> Goerzen, et al. 2009. A Survey of Motion Planning Algorithms from the Perspective of Autonomous UAV Guidance



## Toy Model of Learning Architectures

> Does each architecture correspond to a distinctive decision profile?

**Rule-based** → precise solution, no adaptation

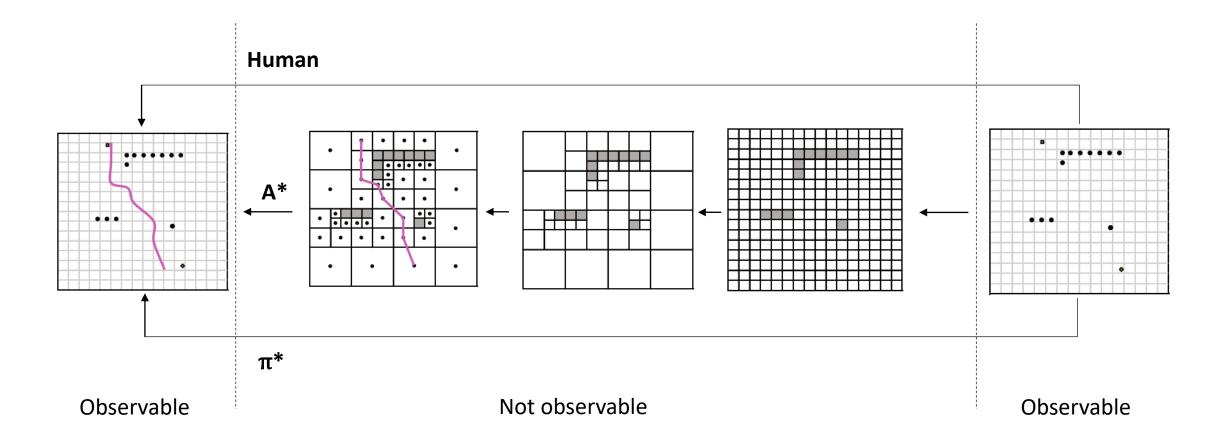
**Reinforcement learner** → multiple degrees of adaptation

**Human** → full adaptation and rule generation

- > Assumes we have perfect information about the environment
- > Real-world is often too complex to justify such an assumption

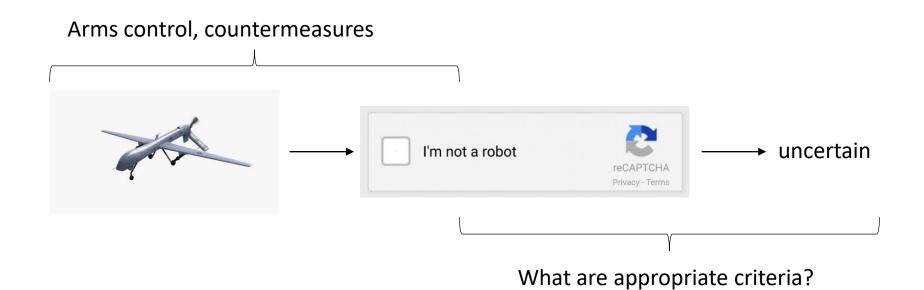


# Possible Architectures for Trajectory



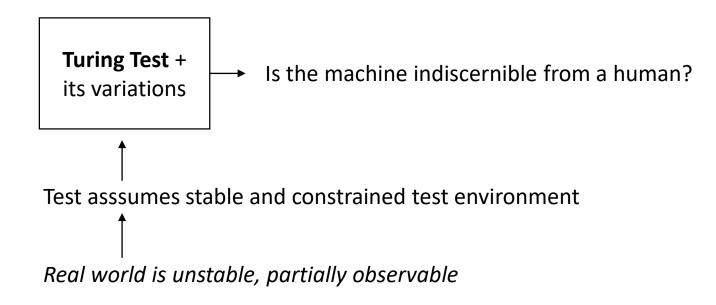


## Why Care about Verification?





## Differentiating Human from Machine



> **Hypothesis**: A system that would not pass the Turing Test in theory might pass it in practice, because the test environment is fuzzy



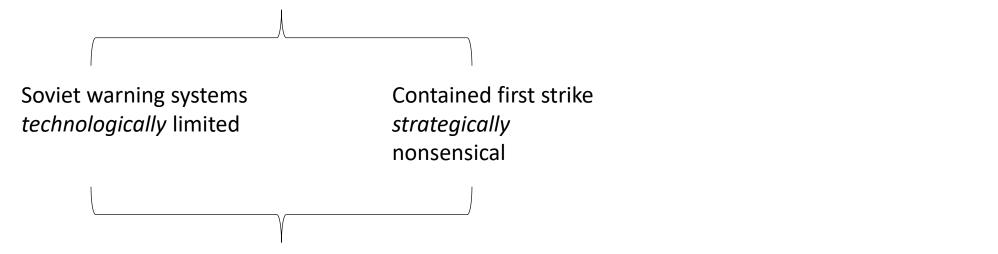
### Other Mechanisms of Verifcation

Performance	Worse than human	Human-level	Better than human
Verifcation	Easy	Hard	Easy; depends
	Clear failure modes	Internal factors:	Unparalleled performance
		Unexpected decision patterns	
		Unexpected failure modes	
		External factors:	
		Change in force structure	
		Change in strategy	
		Introduce disturbances in env.	



### **Petrov Verification**

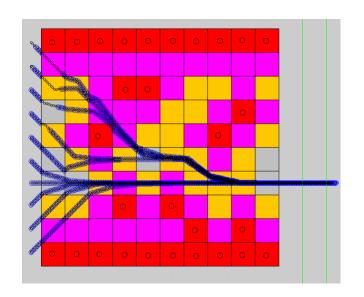
- > September 26, 1983
- > Five U.S. ICBMs surface on Soviet radar, station monitored by Stanislav Petrov
- > Petrov reasons that this is a false alarm, decides not to launch counter-attack

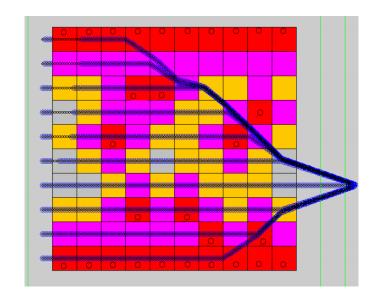


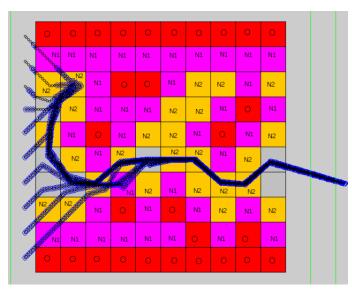
= Petrov Verification: combination of internal and external factors; educated guess *across* domains on limited information



## Appendix on Countermeasures







> Krishna et al. 2005. Parametric Control of Multiple Unmanned Air Vehicles over an Unknown Hostile Territory

