

Rock Lee do Pagode Namora D+

University of Brasilia

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nmap <C-down> :m+1<CR>
nmap <C-up> :m-2<CR>
nmap <C-a> ggVG
vmap <C-c> "+y
syntax on
alias comp='g++ -std=c++14 -Wshadow -fsanitize=address -
Wall -Wconversion -fsanitize=undefined -fno-sanitize-
recover -Wformat=2'

```

Template

```

#include <bits/stdc++.h>

#define ff first
#define ss second
#define pb push_back

using namespace std;
using ll = long long;
using ii = pair<int, int>;

const int N = 100005;

int main() {

    return 0;
}

```

Data Structures

Merge Sort Tree

```

struct MergeTree{
    int n;
    vector<vector<int>>> st;

    void build(int p, int L, int R, const int v[]){
        if(L == R){
            st[p].push_back(v[L]);
            return;
        }
        int mid = (L+R)/2;
        build(2*p, L, mid, v);

```

```

        build(2*p+1, mid+1, R, v);
        st[p].resize(R-L+1);
        merge(st[2*p].begin(), st[2*p].end(),
              st[2*p+1].begin(), st[2*p+1].end(),
              st[p].begin());
    }

    int query(int p, int L, int R, int i, int j, int x)
    const{
        if(L > j || R < i) return 0;
        if(L >= i && R <= j){
            int id = lower_bound(st[p].begin(), st[p].end
                                (), x) - st[p].begin();
            return int(st[p].size()) - id;
        }
        int mid = (L+R)/2;
        return query(2*p, L, mid, i, j, x) +
               query(2*p+1, mid+1, R, i, j, x);
    }
};

public:
    MergeTree(int sz, const int v[]): n(sz), st(4*sz){
        build(1, 1, n, v);

        //number of elements >= x on segment [i, j]
        int query(int i, int j, int x) const{
            if(i > j) swap(i, j);
            return query(1, 1, n, i, j, x);
        }
    };

```

Fenwick Tree 2D

```

vector<int> go[N];
vector<int> ft[N];

void prec_add(int x, int y) {
    for(; x < N; x += x & -x) {
        go[x].push_back(y);
    }
}

void init() {
    for(int i = 1; i < N; i++) {
        sort(go[i].begin(), go[i].end());
        ft[i].assign(go[i].size() + 1, 0);
    }
}

void add(int x, int y, int val) {
    for(; x < N; x += x & -x) {
        int id = int(upper_bound(go[x].begin(), go[x].end
                                (), y) - go[x].begin());
        for(; id < (int)ft[x].size(); id += id & -id)
            ft[x][id] += val;
    }
}

int sum(int x, int y) {
    int ans = 0;
    for(; x > 0; x -= x & -x) {
        int id = int(upper_bound(go[x].begin(), go[x].end
                                (), y) - go[x].begin());
        for(; id > 0; id -= id & -id)
            ans += ft[x][id];
    }
    return ans;
}

```

Wavelet Tree

```

template<typename T>
class wavelet{
    T L, R;
    vector<int> l;
    vector<T> sum; // <<
    wavelet *lef, *rig;

    int r(int i) const{ return i - l[i]; }

public:
    template<typename ITER>
    wavelet(ITER bg, ITER en){
        lef = rig = nullptr;
        L = *bg, R = *en;

        for(auto it = bg; it != en; it++){
            L = min(L, *it), R = max(R, *it);
            if(L == R) return;

            T mid = L + (R - L)/2;
            l.reserve(std::distance(bg, en) + 1);
            sum.reserve(std::distance(bg, en) + 1);
            l.push_back(0), sum.push_back(0);
            for(auto it = bg; it != en; it++){
                l.push_back(l.back() + (*it <= mid)),
                sum.push_back(sum.back() + *it);

                auto tmp = stable_partition(bg, en, [mid](T x){
                    return x <= mid;
                });

                if(bg != tmp) lef = new wavelet(bg, tmp);
                if(tmp != en) rig = new wavelet(tmp, en);
            }
        }
        ~wavelet(){
            delete lef;
            delete rig;
        }
        // 1 index, first is 1st
        T kth(int i, int j, int k) const{
            if(L >= R) return L;
            int c = l[j] - l[i-1];
            if(c >= k) return lef->kth(l[i-1]+1, l[j], k);
            else return rig->kth(r(i-1)+1, r(j), k - c);
        }
        // # elements > x on [i, j]
        int cnt(int i, int j, T x) const{
            if(L > x) return j - i + 1;
            if(R <= x || L == R) return 0;
            int ans = 0;
            if(lef) ans += lef->cnt(l[i-1]+1, l[j], x);
            if(rig) ans += rig->cnt(r(i-1)+1, r(j), x);
            return ans;
        }
        // sum of elements <= k on [i, j]
        T sumk(int i, int j, T k){
            if(L == R) return R <= k ? L * (j - i + 1) : 0;
            if(R <= k) return sum[j] - sum[i-1];
            int ans = 0;
            if(lef) ans += lef->sumk(l[i-1]+1, l[j], k);
            if(rig) ans += rig->sumk(r(i-1)+1, r(j), k);
            return ans;
        }
        // swap (i, i+1) just need to update "array" l[i]
    };
};

```

Order Set

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>

#include <ext/pb_ds/detail/standard_policies.hpp>

using namespace __gnu_pbds; // or pb_ds;

template<typename T, typename B = null_type>
using oset = tree<T, B, less<T>, rb_tree_tag,
    tree_order_statistics_node_update>;
// find_by_order / order_of_key

Hash table

#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;

struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }

    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM = chrono::
            steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};

gp_hash_table<long long, int, custom_hash> table;
unordered_map<long long, int, custom_hash> uhash;
uhash.reserve(1 << 15);
uhash.max_load_factor(0.25);

Convex Hull Trick Simple

struct Line{
    ll m, b;
    inline ll eval(ll x) const{
        return x * m + b;
    }
};

// min => cht.back().m >= L.m
// max => cht.back().m <= L.m
void push_line(vector<Line> &cht, Line L){
    while((int)cht.size() >= 2){
        int sz = (int)cht.size();
        if((long double)(L.b-cht[sz-1].b)*(cht[sz-2].m-L.m)
            <= (long double)(L.b-cht[sz-2].b)*(cht[sz-1].m-L.m)){
            cht.pop_back();
        }
        else break;
    }
    cht.push_back(L);
}

// x increasing; pos = 0 in first call
ll linear_search(const vector<Line> &cht, ll x, int &pos){
    while(pos+1 < (int)cht.size()){
        /*>>*/ if(cht[pos].eval(x) >= cht[pos+1].eval(x)) pos++;
        else break;
    }
    return cht[pos].eval(x);
}

```

```

ll binary_search(const vector<Line> &cht, ll x){
    int L = 0, R = (int)cht.size()-2;
    int bans = (int)cht.size()-1;
    while(L <= R){
        int mid = (L+R)/2;
        if(cht[mid].eval(x) >= cht[mid+1].eval(x)) // <<<
            L = mid + 1;
        else bans = mid, R = mid - 1;
    }
    return cht[bans].eval(x);
}

```

Convex Hull Trick

```

const ll is_query = -(1LL<<62);
struct Line{
    ll m, b;
    mutable function<const Line*> succ;
    bool operator<(const Line& rhs) const{
        if(rhs.b != is_query) return m < rhs.m;
        const Line* s = succ();
        if(!s) return 0;
        ll x = rhs.m;
        return b - s->b < (s->m - m) * x;
    }
};

struct Cht : public multiset<Line>{ // maintain max
    bool bad(iterator y){
        auto z = next(y);
        if(y == begin()){
            if(z == end()) return 0;
            return y->m == z->m && y->b <= z->b;
        }
        auto x = prev(y);
        if(z == end()) return y->m == x->m && y->b <= x->b;
        return (long double)(x->b - y->b)*(z->m - y->m)
            >= (long double)(y->b - z->b)*(y->m - x->m);
    }

    void insert_line(ll m, ll b){
        auto y = insert({m, b});
        y->succ = [=]{ return next(y) == end() ? 0 : &*next(y); };
        if(bad(y)){ erase(y); return; }
        while(next(y) != end() && bad(next(y))) erase(next(y));
        while(y != begin() && bad(prev(y))) erase(prev(y));
    }

    ll eval(ll x){
        auto l = *lower_bound((Line) { x, is_query });
        return l.m * x + l.b;
    }
};

```

Convex Hull Trick

```

/**
 * Author: Simon Lindholm
 * source: https://github.com/kth-competitive-programming/kactl/blob/master/content/data-structures/LineContainer.h
 * License: CC0
 */

struct Line {
    mutable ll m, b, p;
    bool operator<(const Line& o) const { return m < o.m

```

```

        ; }
        bool operator<(ll x) const { return p < x; }
};

struct LineContainer : multiset<Line, less<>> { // CPP14 only
    // (for doubles, use inf = 1/.0, div(a,b) = a/b)
    const ll inf = LLONG_MAX;
    ll div(ll a, ll b) { // floored division
        return a / b - ((a ^ b) < 0 && a % b); }
    bool isect(iterator x, iterator y) {
        if (y == end()) { x->p = inf; return false; }
        if (x->m == y->m) x->p = x->b > y->b ? inf : -inf;
        else x->p = div(y->b - x->b, x->m - y->m);
        return x->p >= y->p;
    }

    void add(ll m, ll b) {
        auto z = insert({m, b, 0}), y = z++, x = y;
        while (isect(y, z)) z = erase(z);
        if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
        while ((y = x) != begin() && (--x)->p >= y->p)
            isect(x, erase(y));
    }

    ll query(ll x) {
        assert(!empty());
        auto l = *lower_bound(x);
        return l.m * x + l.b;
    }
};

```

Min queue

```

template<typename T>
class minQ{
    deque<tuple<T, int, int> > p;
    T delta;
    int sz;
public:
    minQ() : delta(0), sz(0) {}
    inline int size() const{ return sz; }
    inline void add(T x){ delta += x; }
    inline void push(T x, int id){
        x -= delta, sz++;
        int t = 1;
        while(p.size() > 0 && get<0>(p.back()) >= x)
            t += get<1>(p.back()), p.pop_back();
        p.emplace_back(x, t, id);
    }
    inline void pop(){
        get<1>(p.front())--, sz--;
        if(!get<1>(p.front())) p.pop_front();
    }
    T getmin() const{ return get<0>(p.front())+delta; }
    int getid() const{ return get<2>(p.front()); }
};

```

Sparse Table

```

int fn(int i, int j){
    if(j == 0) return v[i];
    if(~dn[i][j]) return dn[i][j];
    return dn[i][j] = min(fn(i, j-1), fn(i + (1 << (j-1)), j-1));
}

int getmn(int l, int r){ // [l, r]
    int lz = lg(r - l + 1);

```

```
    return min(fn(l, lz), fn(r - (1 << lz) + 1, lz));
}
```

Treap

```
// source: https://github.com/victorsenam/caderno/blob/
// master/code/treap.cpp
//const int N = ; typedef int num;
num X[N]; int en = 1, Y[N], sz[N], L[N], R[N];
void calc (int u) { // update node given children info
    if(!u) return;
    sz[u] = sz[L[u]] + 1 + sz[R[u]];
    // code here, no recursion
}
void unlaze (int u) {
    if(!u) return;
    // code here, no recursion
}
void split_val(int u, num x, int &l, int &r) { // l gets
    <= x, r gets > x
    unlaze(u); if(!u) return (void) (l = r = 0);
    if(X[u] <= x) { split_val(R[u], x, l, r); R[u] = l;
        l = u; }
    else { split_val(L[u], x, l, r); L[u] = r; r = u; }
    calc(u);
}
void split_sz(int u, int s, int &l, int &r) { // l gets
    first s, r gets remaining
    unlaze(u); if(!u) return (void) (l = r = 0);
    if(sz[L[u]] < s) { split_sz(R[u], s - sz[L[u]] - 1,
        l, r); R[u] = l; l = u; }
    else { split_sz(L[u], s, l, r); L[u] = r; r = u; }
    calc(u);
}
int merge(int l, int r) { // els on l <= els on r
    unlaze(l); unlaze(r); if(!l || !r) return l + r; int
    u;
    if(Y[l] > Y[r]) { R[l] = merge(R[l], r); u = l; }
    else { L[r] = merge(l, L[r]); u = r; }
    calc(u); return u;
}
void init(int n=N-1) { // XXX call before using other
    funcs
    for(int i = en = 1; i <= n; i++) { Y[i] = i; sz[i] =
        1; L[i] = R[i] = 0; }
    random_shuffle(Y + 1, Y + n + 1);
}
void insert(int &u, int it){
    unlaze(u);
    if(!u) u = it;
    else if(Y[it] > Y[u]) split_val(u, X[it], L[it], R[
        it]), u = it;
    else insert(X[it] < X[u] ? L[u] : R[u], it);
    calc(u);
}
void erase(int &u, num key){
    unlaze(u);
    if(!u) return;
    if(X[u] == key) u = merge(L[u], R[u]);
    else erase(key < X[u] ? L[u] : R[u], key);
    calc(u);
}
int create_node(num key){
    X[en] = key;
    sz[en] = 1;
    L[en] = R[en] = 0;
    return en++;
}
```

```
int query(int u, int l, int r){//0 index
    unlaze(u);
    if(u! or r < 0 or l >= sz[u]) return
        identity_element;
    if(l <= 0 and r >= sz[u] - 1) return subt_data[u];
    int ans = query(L[u], l, r);
    if(l <= sz[ L[u] ] and sz[ L[u] ] <= r)
        ans = max(ans, st[u]);
    ans = max(ans, query(R[u], l-sz[L[u]]-1, r-sz[L[u]
        ]-1));
    return ans;
}
```

ColorUpdate

// source: <https://github.com/tfg50/Competitive-Programming/tree/master/Biblioteca/Data%20Structures>

```
#include <set>
#include <vector>

template <class Info = int>
class ColorUpdate {
public:
    struct Range {
        Range(int l = 0) { this->l = l; }
        Range(int l, int r, Info v) {
            this->l = l;
            this->r = r;
            this->v = v;
        }
        int l, r;
        Info v;

        bool operator < (const Range &b) const { return l
            < b.l; }
    };

    std::vector<Range> upd(int l, int r, Info v) {
        std::vector<Range> ans;
        if(l >= r) return ans;
        auto it = ranges.lower_bound(l);
        if(it != ranges.begin()) {
            it--;
            if(it->r > l) {
                auto cur = *it;
                ranges.erase(it);
                ranges.insert(Range(cur.l, l, cur.v));
                ranges.insert(Range(l, cur.r, cur.v));
            }
        }
        it = ranges.lower_bound(r);
        if(it != ranges.begin()) {
            it--;
            if(it->r > r) {
                auto cur = *it;
                ranges.erase(it);
                ranges.insert(Range(cur.l, r, cur.v));
                ranges.insert(Range(r, cur.r, cur.v));
            }
        }
        for(it = ranges.lower_bound(l); it != ranges.end
            () && it->l < r; it++) {
            ans.push_back(*it);
        }
        ranges.erase(ranges.lower_bound(l), ranges.
            lower_bound(r));
        ranges.insert(Range(l, r, v));
    }
};
```

```

        return ans;
    }
private:
    std::set<Range> ranges;
};

Heavy Light Decomposition

void dfs_sz(int u){
    sz[u] = 1;
    for(auto &v : g[u]) if(v == p[u]){
        swap(v, g[u].back()); g[u].pop_back();
        break;
    }
    for(auto &v : g[u]){
        p[v] = u; dfs_sz(v); sz[u] += sz[v];
        if(sz[v] > sz[ g[u][0] ])
            swap(v, g[u][0]);
    }
}
// nxt[u] = start of path with u
// set nxt[root] = root beforehand
void dfs_hld(int u){
    in[u] = t++;
    rin[in[u]] = u;
    for(auto v : g[u]){
        nxt[v] = (v == g[u][0] ? nxt[u] : v); dfs_hld(v);
    }
    out[u] = t;
}
// subtree of u => [ in[u], out[u] )
// path from nxt[u] to u => [ in[ nxt[u] ], in[u] ]

```

Iterative Segtree

```

T query(int l, int r){ // [l, r]
    T rl, rr;
    for(l += n, r += n+1; l < r; l >>= 1, r >>= 1){
        if(l & 1) rl = merge(rl, st[l++]);
        if(r & 1) rr = merge(st[--r], rr);
    }
    return merge(rl, rr);
}

// initially save v[i] in st[n+i] for all i in [0, n)
void build(){
    for(int p = n-1; p > 0; p--){
        st[p] = merge(st[2*p], st[2*p+1]);
    }
}

```

```

void update(int p, T val){
    st[p += n] = val;
    while(p >>= 1) st[p] = merge(st[2*p], st[2*p+1]);
}

```

Recursive Segtree + lazy

```

class SegTree{
    vi st;
    vi lazy;
    int size;

    int el_neutro = -oo;

    inline int f(int a, int b){
        return max(a,b);
    }
    inline int left(int i) {return 2 * i + 1;};
    inline int right(int i) {return 2 * i + 2;};
    void build(int sti, int stl, int str, vi& nums) {

```

```

        if(stl == str) {
            st[sti] = nums[sti];
            return;
        }
        int mid = (stl + str) / 2;
        build(left(sti), stl, mid, nums);
        build(right(sti), mid + 1, str, nums);
        st[sti] = f(st[left(sti)], st[right(sti)]);
    }

    void propagate(int sti, int stl, int str){
        if(lazy[sti]){
            st[sti] += lazy[sti];
            if(stl != str)
            {
                lazy[left(sti)] += lazy[sti];
                lazy[right(sti)] += lazy[sti];
            }
            lazy[sti] = 0;
        }
    }

    int query(int sti, int stl, int str, int l, int r){
        propagate(sti, stl, str);

        if(str < l || r < stl)
            return el_neutro;

        if(stl >= l and str <= r)
            return st[sti];

        int mid = (str+stl)/2;

        return f(query(left(sti),stl,mid,l,r),query(right
            (sti),mid+1,str,l,r));
    }

    void update_range(int sti, int stl, int str, int l,
        int r, int amm){
        propagate(sti, stl, str);
        if(stl >= l and str <= r){
            lazy[sti] = amm;
            propagate(sti, stl, str);
            return;
        }
        if(stl > r or str < l)
            return;
        int mid = (stl + str)/2;
        update_range(left(sti),stl,mid,l,r,amm);
        update_range(right(sti),mid+1,str,l,r,amm);
        st[sti] = f(st[left(sti)],st[right(sti)]);
    }

    void update(int sti, int stl, int str, int i, int
        amm){
        propagate(sti, stl, str);
        if(stl == i and str == i){
            st[sti] = amm;
            return;
        }
        if(stl > i or str < i)
            return;
        int mid = (stl + str)/2;
        update(left(sti),stl,mid,i,amm);
        update(right(sti),mid+1,str,i,amm);
        st[sti] = f(st[left(sti)],st[right(sti)]);
    }

public:
    SegTree(vi& v) : st(4*v.size(),0), lazy(4*v.size

```

```

    (),0) {size = v.size(); build(0,0,size - 1, v)
    };
    SegTree(int n) : st(4*n,0), lazy(4*n,0){size = n
    };
    int query(int l, int r){return query(0,0,size-1,l
    ,r);}
    void update_range(int l, int r, int amm){
        update_range(0,0,size-1,l,r,amm);}
    void update(int i, int amm){update(0,0,size-1,i,
        amm);}
};

```

LiChao's Segtree

```

void add_line(line nw, int v = 1, int l = 0, int r =
    maxn) { // [l, r)
    int m = (l + r) / 2;
    bool lef = nw.eval(l) < st[v].eval(l);
    bool mid = nw.eval(m) < st[v].eval(m);
    if(mid) swap(st[v], nw);
    if(r - l == 1) {
        return;
    } else if(lef != mid) {
        add_line(nw, 2 * v, l, m);
    } else {
        add_line(nw, 2 * v + 1, m, r);
    }
}

int get(int x, int v = 1, int l = 0, int r = maxn) {
    int m = (l + r) / 2;
    if(r - l == 1) {
        return st[v].eval(x);
    } else if(x < m) {
        return min(st[v].eval(x), get(x, 2*v, l, m));
    } else {
        return min(st[v].eval(x), get(x, 2*v+1, m, r));
    }
}

```

Palindromic tree

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```

const int maxn = 3e5 + 1, sigma = 26;
int len[maxn], link[maxn], to[maxn][sigma];
int slink[maxn], diff[maxn], series_ans[maxn];
int sz, last, n;
char s[maxn];

```

```
void init()
```

```

{
    s[n++] = -1;
    link[0] = 1;
    len[1] = -1;
    sz = 2;
}

```

```
int get_link(int v)
```

```

{
    while(s[n - len[v] - 2] != s[n - 1]) v = link[v];
    return v;
}

```

```
void add_letter(char c)
```

```

{
    s[n++] = c == 'a';
}

```

```

last = get_link(last);
if(!to[last][c])
{
    len[sz] = len[last] + 2;
    link[sz] = to[get_link(link[last])][c];
    diff[sz] = len[sz] - len[link[sz]];
    if(diff[sz] == diff[link[sz]])
        slink[sz] = slink[link[sz]];
    else
        slink[sz] = link[sz];
    to[last][c] = sz++;
}
last = to[last][c];
}

```

```
int main()
```

```

{
    ios::sync_with_stdio(0);
    cin.tie(0);
    init();
    string s;
    cin >> s;
    int n = s.size();
    int ans[n + 1];
    memset(ans, 63, sizeof(ans));
    ans[0] = 0;
    for(int i = 1; i <= n; i++)
    {
        add_letter(s[i - 1]);
        for(int v = last; len[v] > 0; v = slink[v])
        {
            series_ans[v] = ans[i - (len[slink[v]] + diff
            [v])];
            if(diff[v] == diff[link[v]])
                series_ans[v] = min(series_ans[v],
                series_ans[link[v]]);
            ans[i] = min(ans[i], series_ans[v] + 1);
        }
        cout << ans[i] << "\n";
    }
    return 0;
}

```

Segtree Beats

```
const int oo = 1e9+7;
```

```
struct SegBeats {
```

```

    int n;
    struct node {
        ll sum;
        int mx, smx, cnt;
    };
    node comb(const node &a, const node &b) {
        node ans{a.sum + b.sum, max(a.mx, b.mx),
            max(a.smx, b.smx), 0};
        if(a.mx == ans.mx) ans.cnt += a.cnt;
        else ans.smx = max(ans.smx, a.mx);
        if(b.mx == ans.mx) ans.cnt += b.cnt;
        else ans.smx = max(ans.smx, b.mx);

        return ans;
    }
    vector<node> st;

```

```
void build(int p, int L, int R) {
```

```

    if(L == R) {
        st[p] = {oo, oo, -oo, 1};
    }
}

```

```

    return;
}
int mid = (L + R) / 2;
build(2 * p, L, mid);
build(2 * p + 1, mid + 1, R);
st[p] = comb(st[2 * p], st[2 * p + 1]);
}

void propx(int p, int L, int R) {
    if(L == R) return;
    if(st[p].mx < st[2 * p].mx) {
        st[2 * p].sum -= 1LL * (st[2 * p].mx - st[p].mx) *
            st[2 * p].cnt;
        st[2 * p].mx = st[p].mx;
    }
    if(st[p].mx < st[2 * p + 1].mx) {
        st[2 * p + 1].sum -= 1LL * (st[2 * p + 1].mx - st[p].mx) *
            st[2 * p + 1].cnt;
        st[2 * p + 1].mx = st[p].mx;
    }
}

void updmin(int p, int L, int R, int i, int j, int x)
{
    if(i > R or j < L) return;
    if(st[p].mx <= x) return;
    if(L >= i and R <= j and st[p].smx < x) {
        st[p].sum -= 1LL * (st[p].mx - x) * st[p].cnt;
        st[p].mx = x;
        return;
    }
    propx(p, L, R);
    int mid = (L + R) / 2;
    updmin(2 * p, L, mid, i, j, x);
    updmin(2 * p + 1, mid + 1, R, i, j, x);
    st[p] = comb(st[2 * p], st[2 * p + 1]);
}

ll querysum(int p, int L, int R, int i, int j) {
    if(i > R or j < L) return 0;
    if(L >= i and R <= j) return st[p].sum;
    propx(p, L, R);
    int mid = (L + R) / 2;
    return querysum(2 * p, L, mid, i, j) +
        querysum(2 * p + 1, mid + 1, R, i, j);
}

void upd(int p, int L, int R, int i, int val) {
    if(i < L or i > R) return;
    if(L == R) {
        st[p].sum = val;
        st[p].cnt = 1;
        st[p].mx = val;
        return;
    }
    propx(p, L, R);
    int mid = (L + R) / 2;
    upd(2 * p, L, mid, i, val);
    upd(2 * p + 1, mid + 1, R, i, val);
    st[p] = comb(st[2 * p], st[2 * p + 1]);
}

SegBeats(int sz) : n(sz), st(4 * sz) {
    build(1, 1, n);
}

void upd(int i, int val) {
    upd(1, 1, n, i, val);
}

```

```

}
// make a[id] = min(a[id], x) for i in [i, j]
void updmin(int i, int j, int x) {
    updmin(1, 1, n, i, j, x);
}

ll querysum(int i, int j) {
    return querysum(1, 1, n, i, j);
}
};

KD Tree

int d;
long long getValue(const PT &a) {return (d & 1) == 0 ? a
    .x : a.y; }
bool comp(const PT &a, const PT &b) {
    if((d & 1) == 0) { return a.x < b.x; }
    else { return a.y < b.y; }
}
long long sqrDist(PT a, PT b) { return (a - b) * (a - b)
    ; }

class KD_Tree {
public:
    struct Node {
        PT point;
        Node *left, *right;
    };

    void init(std::vector<PT> pts) {
        if(pts.size() == 0) {
            return;
        }
        int n = 0;
        tree.resize(2 * pts.size());
        build(pts.begin(), pts.end(), n);
        //assert(n <= (int) tree.size());
    }

    long long nearestNeighbor(PT point) {
        // assert(tree.size() > 0);
        long long ans = (long long) 1e18;
        nearestNeighbor(&tree[0], point, 0, ans);
        return ans;
    }

private:
    std::vector<Node> tree;

    Node* build(std::vector<PT>::iterator l, std::vector
        <PT>::iterator r, int &n, int h = 0) {
        int id = n++;
        if(r - l == 1) {
            tree[id].left = tree[id].right = NULL;
            tree[id].point = *l;
        } else if(r - l > 1) {
            std::vector<PT>::iterator mid = l + ((r - l)
                / 2);
            d = h;
            std::nth_element(l, mid - 1, r, comp);
            tree[id].point = *(mid - 1);
            // BE CAREFUL!
            // DO EVERYTHING BEFORE BUILDING THE LOWER
            PART!
            tree[id].left = build(l, mid, n, h^1);
            tree[id].right = build(mid, r, n, h^1);
        }
        return &tree[id];
    }
}

```



```

void nearestNeighbor(Node* node, PT point, int h,
long long &ans) {
    if(!node) {
        return;
    }
    if(point != node->point) {
        // THIS WAS FOR A PROBLEM
        // THAT YOU DON'T CONSIDER THE DISTANCE TO
        ITSELF!
        ans = std::min(ans, sqrDist(point, node->
        point));
    }
    d = h;
    long long delta = getValue(point) - getValue(node
    ->point);
    if(delta <= 0) {
        nearestNeighbor(node->left, point, h^1, ans);
        if(ans > delta * delta) {
            nearestNeighbor(node->right, point, h^1,
            ans);
        }
    } else {
        nearestNeighbor(node->right, point, h^1, ans)
        ;
        if(ans > delta * delta) {
            nearestNeighbor(node->left, point, h^1,
            ans);
        }
    }
}
};

```

Math

Extended Euclidean Algorithm

```

// a*x + b*y = gcd(a, b), <gcd, x, y>
tuple<int, int, int> gcd(int a, int b) {
    if(b == 0) return make_tuple(a, 1, 0);
    int q, w, e;
    tie(q, w, e) = gcd(b, a % b);
    return make_tuple(q, e, w - e * (a / b));
}

```

Chinese Remainder Theorem

```

// x = vet[i].first (mod vet[i].second)
ll crt(const vector<pair<ll, ll>> &vet){
    ll ans = 0, lcm = 1;
    ll a, b, g, x, y;
    for(const auto &p : vet) {
        tie(a, b) = p;
        tie(g, x, y) = gcd(lcm, b);
        if((a - ans) % g != 0) return -1; // no solution
        ans = ans + x * ((a - ans) / g) % (b / g) * lcm;
        lcm = lcm * (b / g);
        ans = (ans % lcm + lcm) % lcm;
    }
    return ans;
}

```

Diophantine Solver

```

template<typename T>
T extgcd(T a, T b, T &x, T &y) {
    if (a == 0) {
        x = 0;
        y = 1;
    }
}

```

```

        return b;
    }
    T p = b / a;
    T g = extgcd(b - p * a, a, y, x);
    x -= p * y;
    return g;
}

```

```

template<typename T>
bool diophantine(T a, T b, T c, T &x, T &y, T &g) {
    if (a == 0 && b == 0) {
        if (c == 0) {
            x = y = g = 0;
            return true;
        }
        return false;
    }
    if (a == 0) {
        if (c % b == 0) {
            x = 0;
            y = c / b;
            g = abs(b);
            return true;
        }
        return false;
    }
    if (b == 0) {
        if (c % a == 0) {
            x = c / a;
            y = 0;
            g = abs(a);
            return true;
        }
        return false;
    }
    g = extgcd(a, b, x, y);
    if (c % g != 0) {
        return false;
    }
    T dx = c / a;
    c -= dx * a;
    T dy = c / b;
    c -= dy * b;
    x = dx + mulmod(x, c / g, b);
    y = dy + mulmod(y, c / g, a);
    g = abs(g);
    return true;
}

```

Prefix inverse

```

inv[1] = 1;
for(int i = 2; i < p; i++)
    inv[i] = (p - (p/i) * inv[p%i] % p) % p;

```

Pollard Rho

```

ll rho(ll n){
    if(n % 2 == 0) return 2;
    ll d, c, x, y;
    do{
        c = llrand() % n, x = llrand() % n, y = x;
        do{
            x = add(mul(x, x, n), c, n);
            y = add(mul(y, y, n), c, n);
            y = add(mul(y, y, n), c, n);
            d = __gcd(abs(x - y), n);
        }while(d == 1);
    }while(d == n);
}

```

```

    return d;
}
ll pollard_rho(ll n){
    ll x, c, y, d, k;
    int i;
    do{
        i = 1;
        x = llrand() % n, c = llrand() % n;
        y = x, k = 4;
        do{
            if(++i == k) y = x, k *= 2;
            x = add(mul(x, x, n), c, n);
            d = __gcd(abs(x - y), n);
        }while(d == 1);
    }while(d == n);
    return d;
}
void factorize(ll val, map<ll, int> &fac){
    if(rabin(val)) fac[ val ]++;
    else{
        ll d = pollard_rho(val);
        factorize(d, fac);
        factorize(val / d, fac);
    }
}
map<ll, int> factor(ll val){
    map<ll, int> fac;
    if(val > 1) factorize(val, fac);
    return fac;
}

```

Miller Rabin

```

bool rabin(ll n){
    if(n <= 1) return 0;
    if(n <= 3) return 1;
    ll s = 0, d = n - 1;
    while(d % 2 == 0) d /= 2, s++;
    for(int k = 0; k < 64; k++){
        ll a = (llrand() % (n - 3)) + 2;
        ll x = fexp(a, d, n);
        if(x != 1 && x != n-1){
            for(int r = 1; r < s; r++){
                x = mul(x, x, n);
                if(x == 1) return 0;
                if(x == n-1) break;
            }
            if(x != n-1) return 0;
        }
    }
    return 1;
}

```

Totiente

```

ll totiente(ll n){
    ll ans = n;
    for(ll i = 2; i*i <= n; i++){
        if(n % i == 0){
            ans = ans / i * (i - 1);
            while(n % i == 0) n /= i;
        }
    }
    if(n > 1) ans = ans / n * (n - 1);
    return ans;
}

```

Primitive root

```

// a primitive root modulo n is any number g such that
// any c coprime to n is congruent to a power of g modulo
// n.
bool exists_root(ll n){
    if(n == 1 || n == 2 || n == 4) return true;
    if(n % 2 == 0) n /= 2;
    if(n % 2 == 0) return false;
    // test if n is a power of only one prime
    for(ll i = 3; i * i <= n; i += 2) if(n % i == 0){
        while(n % i == 0) n /= i;
        return n == 1;
    }
    return true;
}
ll primitive_root(ll n){
    if(n == 1 || n == 2 || n == 4) return n - 1;
    if(not exists_root(n)) return -1;
    ll x = phi(n);
    auto pr = factorize(x);
    auto check = [x, n, pr](ll m){
        for(ll p : pr) if(fexp(m, x / p, n) == 1)
            return false;
        return true;
    };
    for(ll m = 2; ; m++) if(__gcd(m, n) == 1)
        if(check(m)) return m;
}

```

// Let's denote $R(n)$ as the set of primitive roots modulo n , p is prime
 $g \in R(p) \Rightarrow (g^{p-1} \equiv 1 \pmod{p} \wedge g \not\equiv 1 \pmod{p})$
 $g \in R(p^k) \Rightarrow (g^{p^{k-1}} \equiv 1 \pmod{p^k} \wedge g \not\equiv 1 \pmod{p^k})$
 $g \in R(2 \cdot p^k) \Rightarrow (g^{p^{k-1}} \equiv -1 \pmod{2 \cdot p^k})$

Mobius Function

```

memset(mu, 0, sizeof mu);
mu[1] = 1;
for(int i = 1; i < N; i++){
    for(int j = i + i; j < N; j += i)
        mu[j] -= mu[i];
}
// g(n) = sum{f(d)} => f(n) = sum{mu(d)*g(n/d)}

```

Mulmod TOP

```

constexpr uint64_t mod = (1ull<<61) - 1;
uint64_t modmul(uint64_t a, uint64_t b){
    uint64_t l1 = (uint32_t)a, h1 = a>>32, l2 = (
        uint32_t)b, h2 = b>>32;
    uint64_t l = l1*l2, m = l1*h2 + l2*h1, h = h1*h2;
    uint64_t ret = (l&mod) + (l>>61) + (h << 3) + (m >>
        29) + (m << 35 >> 3) + 1;
    ret = (ret & mod) + (ret>>61);
    ret = (ret & mod) + (ret>>61);
    return ret-1;
}

```

Modular multiplication TOPPER

```

ll mulmod(ll a, ll b, ll mod) {
    ll q = ll((long double)a * (long double)b / (long
        double)mod);
    ll r = (a * b - mod * q) % mod;
    if(r < 0) r += mod;
    return r;
}

```

Division Trick

```

for(int l = 1, r; l <= n; l = r + 1) {

```

```

    r = n / (n / l);
    // n / x yields the same value for l <= x <= r
}
for(int l, r = n; r > 0; r = l - 1) {
    int tmp = (n + r - 1) / r;
    l = (n + tmp - 1) / tmp;
    // (n+x-1) / x yields the same value for l <= x <= r
}

```

Matrix Determinant

```

int n;
long double a[n][n];

long double gauss(){
    long double det = 1;
    for(int i = 0; i < n; i++){
        int q = i;
        for(int j = i+1; j < n; j++){
            if(abs(a[j][i]) > abs(a[q][i]))
                q = j;
        }
        if(abs(a[q][i]) < EPS){
            det = 0;
            break;
        }
        if(i != q){
            for(int w = 0; w < n; w++){
                swap(a[i][w], a[q][w]);
                det = -det;
            }
            det *= a[i][i];
            for(int j = i+1; j < n; j++) a[i][j] /= a[i][i];

            for(int j = 0; j < n; j++) if(j != i){
                if(abs(a[j][i]) > EPS)
                    for(int k = i+1; k < n; k++)
                        a[j][k] -= a[i][k] * a[j][i];
            }
        }

        return det;
    }
}

```

Simplex Method

```

typedef long double dbl;
const dbl eps = 1e-6;
const int N = , M = ;

mt19937 rng(chrono::steady_clock::now().time_since_epoch
().count());
struct simplex {
    int X[N], Y[M];
    dbl A[M][N], b[M], c[N];
    dbl ans;
    int n, m;
    dbl sol[N];

    void pivot(int x, int y){
        swap(X[y], Y[x]);
        b[x] /= A[x][y];
        for(int i = 0; i < n; i++){
            if(i != y)
                A[x][i] /= A[x][y];
            A[x][y] = 1. / A[x][y];
            for(int i = 0; i < m; i++){
                if(i != x && abs(A[i][y]) > eps) {
                    b[i] -= A[i][y] * b[x];

```

```

                for(int j = 0; j < n; j++) if(j != y)
                    A[i][j] -= A[i][y] * A[x][j];
                    A[i][y] = -A[i][y] * A[x][y];
                }
            ans += c[y] * b[x];
            for(int i = 0; i < n; i++){
                if(i != y)
                    c[i] -= c[y] * A[x][i];
                c[y] = -c[y] * A[x][y];
            }

            // maximiza sum(x[i] * c[i])
            // sujeito a
            // sum(a[i][j] * x[j]) <= b[i] para 0 <= i < m (Ax
            <= b)
            // x[i] >= 0 para 0 <= i < n (x >= 0)
            // (n variaveis, m restricoes)
            // guarda a resposta em ans e retorna o valor otimo
            dbl solve(int _n, int _m) {
                this->n = _n; this->m = _m;

                for(int i = 1; i < m; i++){
                    int id = uniform_int_distribution<int>(0, i)(
                        rng);
                    swap(b[i], b[id]);
                    for(int j = 0; j < n; j++)
                        swap(A[i][j], A[id][j]);
                }

                ans = 0.;
                for(int i = 0; i < n; i++) X[i] = i;
                for(int i = 0; i < m; i++) Y[i] = i + n;
                while(true) {
                    int x = min_element(b, b + m) - b;
                    if(b[x] >= -eps)
                        break;
                    int y = find_if(A[x], A[x] + n, [](dbl d) {
                        return d < -eps; }) - A[x];
                    if(y == n) throw 1; // no solution
                    pivot(x, y);
                }
                while(true) {
                    int y = max_element(c, c + n) - c;
                    if(c[y] <= eps) break;
                    int x = -1;
                    dbl mn = 1. / 0.;
                    for(int i = 0; i < m; i++){
                        if(A[i][y] > eps && b[i] / A[i][y] < mn)
                            mn = b[i] / A[i][y], x = i;
                        if(x == -1) throw 2; // unbounded
                    }
                    pivot(x, y);
                }
                memset(sol, 0, sizeof(dbl) * n);
                for(int i = 0; i < m; i++){
                    if(Y[i] < n)
                        sol[Y[i]] = b[i];
                }
                return ans;
            }
        };
    };
}

```

FFT

```

void fft(vector<base> &a, bool inv){
    int n = (int)a.size();

    for(int i = 1, j = 0; i < n; i++){
        int bit = n >> 1;
        for(; j >= bit; bit >>= 1) j -= bit;

```

```

    j += bit;
    if(i < j) swap(a[i], a[j]);
}

for(int sz = 2; sz <= n; sz <= 1) {
    double ang = 2 * PI / sz * (inv ? -1 : 1);
    base wlen(cos(ang), sin(ang));
    for(int i = 0; i < n; i += sz){
        base w(1, 0);
        for(int j = 0; j < sz / 2; j++){
            base u = a[i+j], v = a[i+j + sz/2] * w;
            a[i+j] = u + v;
            a[i+j+sz/2] = u - v;
            w *= wlen;
        }
    }
}
if(inv) for(int i = 0; i < n; i++) a[i] /= 1.0 * n;
}

```

FFT Tourist

```

namespace fft {
    typedef double dbl;

    struct num {
        dbl x, y;
        num() { x = y = 0; }
        num(dbl x, dbl y) : x(x), y(y) {}
    };

    inline num operator+(num a, num b) { return num(a.x + b.x, a.y + b.y); }
    inline num operator-(num a, num b) { return num(a.x - b.x, a.y - b.y); }
    inline num operator*(num a, num b) { return num(a.x * b.x - a.y * b.y, a.x * b.y + a.y * b.x); }
    inline num conj(num a) { return num(a.x, -a.y); }

    int base = 1;
    vector<num> roots = {{0, 0}, {1, 0}};
    vector<int> rev = {0, 1};

    const dbl PI = acos(-1.0);

    void ensure_base(int nbase) {
        if(nbase <= base) return;

        rev.resize(1 << nbase);
        for(int i = 0; i < (1 << nbase); i++) {
            rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
        }
        roots.resize(1 << nbase);

        while(base < nbase) {
            dbl angle = 2*PI / (1 << (base + 1));
            for(int i = 1 << (base - 1); i < (1 << base); i++) {
                roots[i << 1] = roots[i];
                dbl angle_i = angle * (2 * i + 1 - (1 << base));
                roots[(i << 1) + 1] = num(cos(angle_i), sin(angle_i));
            }
            base++;
        }
    }
}

```

```

void fft(vector<num> &a, int n = -1) {
    if(n == -1) {
        n = a.size();
    }
    assert((n & (n-1)) == 0);
    int zeros = __builtin_ctz(n);
    ensure_base(zeros);
    int shift = base - zeros;
    for(int i = 0; i < n; i++) {
        if(i < (rev[i] >> shift)) {
            swap(a[i], a[rev[i] >> shift]);
        }
    }
    for(int k = 1; k < n; k <= 1) {
        for(int i = 0; i < n; i += 2 * k) {
            for(int j = 0; j < k; j++) {
                num z = a[i+j+k] * roots[j+k];
                a[i+j+k] = a[i+j] - z;
                a[i+j] = a[i+j] + z;
            }
        }
    }
}

vector<num> fa, fb;
vector<int> multiply(vector<int> &a, vector<int> &b) {
    int need = a.size() + b.size() - 1;
    int nbase = 0;
    while((1 << nbase) < need) nbase++;
    ensure_base(nbase);
    int sz = 1 << nbase;
    if(sz > (int) fa.size()) {
        fa.resize(sz);
    }
    for(int i = 0; i < sz; i++) {
        int x = (i < (int) a.size() ? a[i] : 0);
        int y = (i < (int) b.size() ? b[i] : 0);
        fa[i] = num(x, y);
    }
    fft(fa, sz);
    num r(0, -0.25 / sz);
    for(int i = 0; i <= (sz >> 1); i++) {
        int j = (sz - i) & (sz - 1);
        num z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
        if(i != j) {
            fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
            fa[i] = z;
        }
    }
    fft(fa, sz);
    vector<int> res(need);
    for(int i = 0; i < need; i++) {
        res[i] = fa[i].x + 0.5;
    }
    return res;
}

vector<int> multiply_mod(vector<int> &a, vector<int> &b, int m, int eq = 0) {
    int need = a.size() + b.size() - 1;
    int nbase = 0;
    while ((1 << nbase) < need) nbase++;
    ensure_base(nbase);
    int sz = 1 << nbase;
    if (sz > (int) fa.size()) {
        fa.resize(sz);
    }
}

```

```

}
for (int i = 0; i < (int) a.size(); i++) {
    int x = (a[i] % m + m) % m;
    fa[i] = num(x & ((1 << 15) - 1), x >> 15);
}
fill(fa.begin() + a.size(), fa.begin() + sz, num {0,
    0});
fft(fa, sz);
if (sz > (int) fb.size()) {
    fb.resize(sz);
}
if (eq) {
    copy(fa.begin(), fa.begin() + sz, fb.begin());
} else {
    for (int i = 0; i < (int) b.size(); i++) {
        int x = (b[i] % m + m) % m;
        fb[i] = num(x & ((1 << 15) - 1), x >> 15);
    }
    fill(fb.begin() + b.size(), fb.begin() + sz, num
        {0, 0});
    fft(fb, sz);
}
dbl ratio = 0.25 / sz;
num r2(0, -1);
num r3(ratio, 0);
num r4(0, -ratio);
num r5(0, 1);
for (int i = 0; i <= (sz >> 1); i++) {
    int j = (sz - i) & (sz - 1);
    num a1 = (fa[i] + conj(fa[j]));
    num a2 = (fa[i] - conj(fa[j])) * r2;
    num b1 = (fb[i] + conj(fb[j])) * r3;
    num b2 = (fb[i] - conj(fb[j])) * r4;
    if (i != j) {
        num c1 = (fa[j] + conj(fa[i]));
        num c2 = (fa[j] - conj(fa[i])) * r2;
        num d1 = (fb[j] + conj(fb[i])) * r3;
        num d2 = (fb[j] - conj(fb[i])) * r4;
        fa[i] = c1 * d1 + c2 * d2 * r5;
        fb[i] = c1 * d2 + c2 * d1;
    }
    fa[j] = a1 * b1 + a2 * b2 * r5;
    fb[j] = a1 * b2 + a2 * b1;
}
fft(fa, sz);
fft(fb, sz);
vector<int> res(need);
for (int i = 0; i < need; i++) {
    long long aa = fa[i].x + 0.5;
    long long bb = fb[i].x + 0.5;
    long long cc = fa[i].y + 0.5;
    res[i] = (aa + ((bb % m) << 15) + ((cc % m) << 30))
        % m;
}
return res;
}

vector<int> square_mod(vector<int> &a, int m) {
    return multiply_mod(a, a, m, 1);
}
}

```

NTT

```

const int mod = 7340033;
const int root = 5;
const int root_1 = 4404020;
const int root_pw = 1<<20;

```

```

void fft (vector<int> &a, bool invert) {
    int n = (int) a.size();

    for (int i=1, j=0; i<n; ++i) {
        int bit = n >> 1;
        for (; j>=bit; bit>>=1)
            j -= bit;
        j += bit;
        if (i < j)
            swap (a[i], a[j]);
    }

    for (int len=2; len<=n; len<=1) {
        int wlen = invert ? root_1 : root;
        for (int i=len; i<root_pw; i<=1)
            wlen = int (wlen * 111 * wlen % mod);
        for (int i=0; i<n; i+=len) {
            int w = 1;
            for (int j=0; j<len/2; ++j) {
                int u = a[i+j], v = int (a[i+j+len/2] * 1
                    11 * w % mod);
                a[i+j] = u+v < mod ? u+v : u+v-mod;
                a[i+j+len/2] = u-v >= 0 ? u-v : u-v+mod;
                w = int (w * 111 * wlen % mod);
            }
        }
    }
    if (invert) {
        int nrev = reverse (n, mod);
        for (int i=0; i<n; ++i)
            a[i] = int (a[i] * 111 * nrev % mod);
    }
}

```

Gauss

// Solves systems of linear equations.
// To use, build a matrix of coefficients and call run(
mat, R, C). If the i-th variable is free, row[i] will
be -1, otherwise it's value will be ans[i].

```

namespace Gauss {
    const int MAXC = 1001;
    int row[MAXC];
    double ans[MAXC];

    void run(double mat[][MAXC], int R, int C) {
        REP(i, C) row[i] = -1;

        int r = 0;
        REP(c, C) {
            int k = r;
            FOR(i, r, R) if(fabs(mat[i][c]) > fabs(mat[k][c]))
                k = i;
            if(fabs(mat[k][c]) < eps) continue;

            REP(j, C+1) swap(mat[r][j], mat[k][j]);
            REP(i, R) if (i != r) {
                double w = mat[i][c] / mat[r][c];
                REP(j, C+1) mat[i][j] -= mat[r][j] * w;
            }
            row[c] = r++;
        }

        REP(i, C) {
            int r = row[i];
            ans[i] = r == -1 ? 0 : mat[r][C] / mat[r][i];
        }
    }
}

```

```

    }
}
}

```

Gauss Xor

```

const ll MAX = 1e9;
const int LOG_MAX = 64 - __builtin_clzll((ll)MAX);

struct Gauss {
    array<ll, LOG_MAX> vet;
    int size;
    Gauss() size(0) {}
    Gauss(vector<ll> vals) size(0) {
        for(ll val : vals) add(val);
    }
    bool add(ll val) {
        for(int i = 0; i < LOG_MAX; i++) if(val & (1LL <<
            i)) {
            if(vet[i] == 0) {
                vet[i] = val;
                size++;
                return true;
            }
            val ^= vet[i];
        }
        return false;
    }
};

```

Simpson

```

inline double simpson(double fl,double fr,double fmid,
    double l,double r) {
    return (fl + fr + 4.0 * fmid) * (r - l) / 6.0;
}
double rsimpson(double slr,double fl,double fr,double
    fmid,double l,double r) {
    double mid = (l+r)*0.5;
    double fml = f((l+mid)*0.5), fmr = f((mid+r)*0.5);
    double slm = simpson(fl, fmid, fml, l, mid);
    double smr = simpson(fmid, fr, fmr, mid, r);
    if(fabs(slr-slm-smr) < eps and r - l < delta) return
        slr;
    return rsimpson(slm,fl,fmid,fml,l,mid) + rsimpson(
        smr,fmid,fr,fmr,mid,r);
}
double integrate(double l,double r) {
    double mid = (l+r)*0.5;
    double fl = f(l), fr = f(r), fmid = f(mid);
    return rsimpson(simpson(fl,fr,fmid,l,r),fl,fr,fmid,l
        ,r);
}

```

Modular Arithmetic

```

template <int mod = MOD>
struct modBase {
    modBase(int val = 0) : val(val) {}
    int val;

    modBase<mod> operator*(modBase<mod> o) {
        return (long long)val * o.val % mod;
    }
    modBase<mod> operator+(modBase<mod> o) {
        return val + o.val > mod ? val + o.val - mod : val +
            o.val;
    }
};

```

```

template <class T>
T fexp(T x, long long e) {
    T ans(1);
    for (; e > 0; e /= 2) {
        if (e & 1) ans = ans * x;
        x = x * x;
    }
    return ans;
}

```

Matrix

```

template <const size_t n, const size_t m, class T =
    modBase<>>
struct Matrix {
    T v[n][m];

    Matrix(int d = 0) {
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < m; j++) {
                v[i][j] = T(0);
            }
            if (i < m) {
                v[i][i] = T(d);
            }
        }
    }

    template <size_t mm>
    Matrix<n, mm, T> operator*(Matrix<m, mm, T> &o) {
        Matrix<n, mm, T> ans;
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < mm; j++) {
                for (int k = 0; k < m; k++) {
                    ans.v[i][j] = ans.v[i][j] + v[i][k] * o.v[k][j];
                }
            }
        }
        return ans;
    }
};

```

Graphs

Bipartite Matching

```

// O(V * E)
int match[N];
int vis[N], pass;
vector<int> g[N];

bool dfs(int u) {
    vis[u] = pass;

    for(int v : g[u]) if(vis[v] != pass) {
        vis[v] = pass;
        if(match[v] == -1 or dfs(match[v])) {
            match[v] = u;
            match[u] = v;
            return true;
        }
    }
    return false;
}

int max_maching() {
    memset(match, -1, sizeof match);
    int max_matching_size = 0;
}

```

```

    for(int u : vertices_on_side_A) {
        pass++;
        if(dfs(i)) max_matching_size++;
    }
    return max_matching_size;
}

```

Dinic

```

const int N = 1000005;
const int E = 2 * 10000006;
vector<int> g[N];
int ne;
struct Edge{
    int from, to; ll flow, cap;
} edge[E];
int lvl[N], vis[N], pass, start = N-2, target = N-1;
int qu[N], qt, px[N];

ll run(int s, int sink, ll minE){
    if(s == sink) return minE;

    ll ans = 0;

    for(; px[s] < (int)g[s].size(); px[s]++){
        int e = g[s][px[s]];
        auto &v = edge[e], &rev = edge[e^1];
        if(lvl[v.to] != lvl[s]+1 || v.flow >= v.cap)
            continue; // v.cap - v.flow < lim
        ll tmp = run(v.to, sink, min(minE, v.cap-v.flow));
        v.flow += tmp, rev.flow -= tmp;
        ans += tmp, minE -= tmp;
        if(minE == 0) break;
    }
    return ans;
}

bool bfs(int source, int sink){
    qt = 0;
    qu[qt++] = source;
    lvl[source] = 1;
    vis[source] = ++pass;
    for(int i = 0; i < qt; i++){
        int u = qu[i];
        px[u] = 0;
        if(u == sink) return true;
        for(auto& ed : g[u]) {
            auto v = edge[ed];
            if(v.flow >= v.cap || vis[v.to] == pass)
                continue; // v.cap - v.flow < lim
            vis[v.to] = pass;
            lvl[v.to] = lvl[u]+1;
            qu[qt++] = v.to;
        }
    }
    return false;
}

ll flow(int source = start, int sink = target){
    ll ans = 0;
    //for(lim = (1LL << 62); lim >= 1; lim /= 2)
    while(bfs(source, sink))
        ans += run(source, sink, oo);
    return ans;
}

void addEdge(int u, int v, ll c = 1, ll rc = 0){
    edge[ne] = {u, v, 0, c};
    g[u].push_back(ne++);
    edge[ne] = {v, u, 0, rc};
    g[v].push_back(ne++);
}

```

```

}
void reset_flow(){
    for(int i = 0; i < ne; i++){
        edge[i].flow = 0;
    }
}

Push relabel

// Push relabel in  $O(V^2 E^{0.5})$  with gap heuristic
// It's quite fast
template<typename flow_t = long long>
struct PushRelabel {
    struct Edge { int to, rev; flow_t f, c; };
    vector<vector<Edge> > g;
    vector<flow_t> ec;
    vector<Edge*> cur;
    vector<vector<int> > hs;
    vector<int> H;
    PushRelabel(int n) : g(n), ec(n), cur(n), hs(2*n), H
        (n) {}
    void add_edge(int s, int t, flow_t cap, flow_t rcap
        = 0) {
        if (s == t) return;
        Edge a = {t, (int)g[t].size(), 0, cap};
        Edge b = {s, (int)g[s].size(), 0, rcap};
        g[s].push_back(a);
        g[t].push_back(b);
    }
    void add_flow(Edge& e, flow_t f) {
        Edge &back = g[e.to][e.rev];
        if (!ec[e.to] && f)
            hs[H[e.to]].push_back(e.to);
        e.f += f, ec[e.to] += f;
        back.f -= f, ec[back.to] -= f;
    }
    flow_t max_flow(int s, int t) {
        int v = g.size();
        H[s] = v; ec[t] = 1;
        vector<int> co(2 * v);
        co[0] = v-1;
        for(int i = 0; i < v; ++i) cur[i] = g[i].data();
        for(auto &e : g[s]) add_flow(e, e.c);

        if(hs[0].size())
            for (int hi = 0; hi >= 0; ) {
                int u = hs[hi].back();
                hs[hi].pop_back();
                while (ec[u] > 0) // discharge u
                    if (cur[u] == g[u].data() + g[u].size()) {
                        H[u] = 1e9;
                        for(auto &e:g[u])
                            if (e.c - e.f && H[u] > H[e.to]+1)
                                H[u] = H[e.to]+1, cur[u] = &e;
                        if (++co[H[u]], !--co[hi] && hi < v)
                            for(int i = 0; i < v; ++i)
                                if (hi < H[i] && H[i] < v){
                                    --co[H[i]];
                                    H[i] = v + 1;
                                }
                        hi = H[u];
                    }
                else if (cur[u]->c - cur[u]->f && H[u]
                    == H[cur[u]->to]+1)
                    add_flow(*cur[u], min(ec[u], cur[u]->c
                        - cur[u]->f));
                else ++cur[u];
                while (hi >= 0 && hs[hi].empty()) --hi;
            }
        return -ec[s];
    }
}

```

```

    }
};

Min Cost Max Flow

const ll oo = 1e18;
const int N = 222, E = 2 * 1000006;

vector<int> g[N];
int ne;
struct Edge{
    int from, to; ll cap, cost;
} edge[E];
int start = N-1, target = N-2, p[N]; int inqueue[N];
ll d[N];
bool spfa(int source, int sink){
    for(int i = 0; i < N; i++) d[i] = oo;
    inqueue[i] = 0;

    d[source] = 0; queue<int> q; q.push(source);
    inqueue[source] = 1;

    while(!q.empty()){
        int u = q.front(); q.pop();
        inqueue[u] = 0;
        for(int e : g[u]){
            auto v = edge[e];
            if(v.cap > 0 and d[u] + v.cost < d[v.to]){
                d[v.to] = d[u] + v.cost; p[v.to] = e;
                if(!inqueue[v.to]){
                    q.push(v.to); inqueue[v.to] = 1;
                }
            }
        }
    }
    return d[sink] != oo;
}

// <max flow, min cost>
pair<ll, ll> mincost(int source = start, int sink =
target){
    ll ans = 0, mf = 0;
    while(spfa(source, sink)){
        ll f = oo;
        for(int u = sink; u != source; u = edge[ p[u] ].
            from)
            f = min(f, edge[ p[u] ].cap);
        for(int u = sink; u != source; u = edge[ p[u] ].
            from){
            edge[ p[u] ].cap -= f;
            edge[ p[u] ^ 1 ].cap += f;
        }
        mf += f;
        ans += f * d[sink];
    }
    return {mf, ans};
}

void addEdge(int u, int v, ll c, ll cost){
    edge[ne] = {u, v, c, cost};
    g[u].push_back(ne++);
    edge[ne] = {v, u, 0, -cost};
    g[v].push_back(ne++);
}

```

Blossom Algorithm for General Matching

```

const int MAXN = 2020 + 1;
// 1-based Vertex index
int vis[MAXN], par[MAXN], orig[MAXN], match[MAXN], aux[
    MAXN], t, N;

```

```

vector<int> conn[MAXN];
queue<int> Q;
void addEdge(int u, int v) {
    conn[u].push_back(v); conn[v].push_back(u);
}
void init(int n) {
    N = n; t = 0;
    for(int i=0; i<=n; ++i)
        conn[i].clear(), match[i] = aux[i] = par[i] = 0;
}
void augment(int u, int v) {
    int pv = v, nv;
    do {
        pv = par[v]; nv = match[pv];
        match[v] = pv; match[pv] = v;
        v = nv;
    } while(u != pv);
}
int lca(int v, int w) {
    ++t;
    while(true) {
        if(v) {
            if(aux[v] == t) return v; aux[v] = t;
            v = orig[par[match[v]]];
        }
        swap(v, w);
    }
}
void blossom(int v, int w, int a) {
    while(orig[v] != a) {
        par[v] = w; w = match[v];
        if(vis[w] == 1) Q.push(w), vis[w] = 0;
        orig[v] = orig[w] = a; v = par[w];
    }
}
bool bfs(int u) {
    fill(vis+1, vis+1+N, -1); iota(orig + 1, orig + N +
        1, 1);
    Q = queue<int>(); Q.push(u); vis[u] = 0;
    while(!Q.empty()) {
        int v = Q.front(); Q.pop();
        for(int x: conn[v]) {
            if(vis[x] == -1) {
                par[x] = v; vis[x] = 1;
                if(!match[x]) return augment(u, x), true;
                Q.push(match[x]); vis[match[x]] = 0;
            }
            else if(vis[x] == 0 && orig[v] != orig[x]) {
                int a = lca(orig[v], orig[x]);
                blossom(x, v, a); blossom(v, x, a);
            }
        }
    }
    return false;
}

int Match() {
    int ans = 0;
    // find random matching (not necessary, constant
    improvement)
    vector<int> V(N-1); iota(V.begin(), V.end(), 1);
    shuffle(V.begin(), V.end(), mt19937(0x9494949));
    for(auto x: V) if(!match[x]){
        for(auto y: conn[x]) if(!match[y]) {
            match[x] = y, match[y] = x;
            ++ans; break;
        }
    }
}

```



```

    for(int i=1; i<=N; ++i) if(!match[i] && bfs(i)) ++
        ans;
    return ans;
}

```

Blossom Algorithm for Weighted General Matching

```

// N^3 (but fast in practice)
static const int INF = INT_MAX;
static const int N = 514;
struct edge{
    int u,v,w; edge(){}
    edge(int ui,int vi,int wi)
        :u(ui),v(vi),w(wi){}
};
int n,n_x;
edge g[N*2][N*2];
int lab[N*2];
int match[N*2],slack[N*2],st[N*2],pa[N*2];
int flo_from[N*2][N+1],S[N*2],vis[N*2];
vector<int> flo[N*2];
queue<int> q;
int e_delta(const edge &e){
    return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
}
void update_slack(int u,int x){
    if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]][x]))
        slack[x]=u;
}
void set_slack(int x){
    slack[x]=0;
    for(int u=1;u<=n;++u)
        if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)
            update_slack(u,x);
}
void q_push(int x){
    if(x<=n)q.push(x);
    else for(size_t i=0;i<flo[x].size();i++)
        q_push(flo[x][i]);
}
void set_st(int x,int b){
    st[x]=b;
    if(x>n)for(size_t i=0;i<flo[x].size();++i)
        set_st(flo[x][i],b);
}
int get_pr(int b,int xr){
    int pr=find(flo[b].begin(),flo[b].end(),xr)-flo[b].begin();
    if(pr%2==1){
        reverse(flo[b].begin()+1,flo[b].end());
        return (int)flo[b].size()-pr;
    }else return pr;
}
void set_match(int u,int v){
    match[u]=g[u][v].v;
    if(u<=n) return;
    edge e=g[u][v];
    int xr=flo_from[u][e.u],pr=get_pr(u,xr);
    for(int i=0;i<pr;++i)set_match(flo[u][i],flo[u][i]^1);
    set_match(xr,v);
    rotate(flo[u].begin(),flo[u].begin()+pr,flo[u].end());
}
void augment(int u,int v){
    for(;;){
        int xnv=st[match[u]];

```

```

        set_match(u,v);
        if(!xnv)return;
        set_match(xnv,st[pa[xnv]]);
        u=st[pa[xnv]],v=xnv;
    }
}
int get_lca(int u,int v){
    static int t=0;
    for(++t;u||v;swap(u,v)){
        if(u==0)continue;
        if(vis[u]==t)return u;
        vis[u]=t;
        u=st[match[u]];
        if(u)u=st[pa[u]];
    }
    return 0;
}
void add_blossom(int u,int lca,int v){
    int b=n+1;
    while(b<=n_x&&st[b])++b;
    if(b>n_x)++n_x;
    lab[b]=0,S[b]=0;
    match[b]=match[lca];
    flo[b].clear();
    flo[b].push_back(lca);
    for(int x=u,y;x!=lca;x=st[pa[y]])
        flo[b].push_back(x),flo[b].push_back(y=st[match[x]]),q_push(y);
    reverse(flo[b].begin()+1,flo[b].end());
    for(int x=v,y;x!=lca;x=st[pa[y]])
        flo[b].push_back(x),flo[b].push_back(y=st[match[x]]),q_push(y);
    set_st(b,b);
    for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w=0;
    for(int x=1;x<=n_x;++x)flo_from[b][x]=0;
    for(size_t i=0;i<flo[b].size();++i){
        int xs=flo[b][i];
        for(int x=1;x<=n_x;++x)
            if(g[b][x].w==0||e_delta(g[xs][x])<e_delta(g[b][x]))
                g[b][x]=g[xs][x],g[x][b]=g[x][xs];
        for(int x=1;x<=n_x;++x)
            if(flo_from[xs][x])flo_from[b][x]=xs;
    }
    set_slack(b);
}
void expand_blossom(int b){
    for(size_t i=0;i<flo[b].size();++i)
        set_st(flo[b][i],flo[b][i]);
    int xr=flo_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
    for(int i=0;i<pr;i+=2){
        int xs=flo[b][i],xns=flo[b][i+1];
        pa[xs]=g[xns][xs].u;
        S[xs]=1,S[xns]=0;
        slack[xs]=0,set_slack(xns);
        q_push(xns);
    }
    S[xr]=1,pa[xr]=pa[b];
    for(size_t i=pr+1;i<flo[b].size();++i){
        int xs=flo[b][i];
        S[xs]=-1,set_slack(xs);
    }
    st[b]=0;
}
bool on_found_edge(const edge &e){
    int u=st[e.u],v=st[e.v];
    if(S[v]==-1){

```

```

    pa[v]=e.u,S[v]=1;
    int nu=st[match[v]];
    slack[v]=slack[nu]=0;
    S[nu]=0,q_push(nu);
} else if(S[v]==0){
    int lca=get_lca(u,v);
    if(!lca) return augment(u,v),augment(v,u),true;
    else add_blossom(u,lca,v);
}
return false;
}
bool matching(){
    memset(S+1,-1,sizeof(int)*n_x);
    memset(slack+1,0,sizeof(int)*n_x);
    q=queue<int>();
    for(int x=1;x<=n_x;++x)
        if(st[x]==x&&!match[x]) pa[x]=0,S[x]=0,q_push(x);
    if(q.empty()) return false;
    for(;;){
        while(q.size()){
            int u=q.front();q.pop();
            if(S[st[u]]==1) continue;
            for(int v=1;v<=n;++v)
                if(g[u][v].w>0&&st[u]!=st[v]){
                    if(e_delta(g[u][v])==0){
                        if(on_found_edge(g[u][v])) return true;
                    } else update_slack(u,st[v]);
                }
        }
        int d=INF;
        for(int b=n+1;b<=n_x;++b)
            if(st[b]==b&&S[b]==1) d=min(d,lab[b]/2);
        for(int x=1;x<=n_x;++x)
            if(st[x]==x&&slack[x]){
                if(S[x]==-1) d=min(d,e_delta(g[slack[x]][x]));
                else if(S[x]==0) d=min(d,e_delta(g[slack[x]][x])/2);
            }
        for(int u=1;u<=n;++u){
            if(S[st[u]]==0){
                if(lab[u]<=d) return 0;
                lab[u]-=d;
            } else if(S[st[u]]==1) lab[u]+=d;
        }
        for(int b=n+1;b<=n_x;++b)
            if(st[b]==b){
                if(S[st[b]]==0) lab[b]+=d*2;
                else if(S[st[b]]==1) lab[b]-=d*2;
            }
        q=queue<int>();
        for(int x=1;x<=n_x;++x)
            if(st[x]==x&&slack[x]&&st[slack[x]]!=x&&
                e_delta(g[slack[x]][x])==0)
                if(on_found_edge(g[slack[x]][x])) return true;
        for(int b=n+1;b<=n_x;++b)
            if(st[b]==b&&S[b]==1&&lab[b]==0)
                expand_blossom(b);
        }
    }
    return false;
}
pair<long long,int> solve(){
    memset(match+1,0,sizeof(int)*n);
    n_x=n;
    int n_matches=0;

```

```

    long long tot_weight=0;
    for(int u=0;u<=n;++u) st[u]=u,flo[u].clear();
    int w_max=0;
    for(int u=1;u<=n;++u)
        for(int v=1;v<=n;++v){
            flo_from[u][v]=(u==v?0:0);
            w_max=max(w_max,g[u][v].w);
        }
    for(int u=1;u<=n;++u) lab[u]=w_max;
    while(matching()) ++n_matches;
    for(int u=1;u<=n;++u)
        if(match[u]&&match[u]<u)
            tot_weight+=g[u][match[u]].w;
    return make_pair(tot_weight,n_matches);
}
void add_edge( int ui , int vi , int wi ){
    g[ui][vi].w = g[vi][ui].w = wi;
}
void init( int _n ){
    n = _n;
    for(int u=1;u<=n;++u)
        for(int v=1;v<=n;++v)
            g[u][v]=edge(u,v,0);
}

```

Small to Large

```

void cnt_sz(int u, int p = -1){
    sz[u] = 1;
    for(int v : g[u]) if(v != p)
        cnt_sz(v, u), sz[u] += sz[v];
}
void add(int u, int p, int big = -1){
    // Update info about this vx in global answer
    for(int v : g[u]) if(v != p && v != big)
        add(v, u);
}
void dfs(int u, int p, int keep){
    int big = -1, mmx = -1;
    for(int v : g[u]) if(v != p && sz[v] > mmx)
        mmx = sz[v], big = v;
    for(int v : g[u]) if(v != p && v != big)
        dfs(v, u, 0);
    if(big != -1) dfs(big, u, 1);
    add(u, p, big);
    for(auto x : q[u]){
        // answer all queries for this vx
    }
    if(!keep){ /*Remove data from this subtree*/ }
}

```

Centroid Decomposition

```

void decomp(int v, int p){
    int treesize = calc_sz(v, v);
    if(treesize < k) return;
    int cent = centroid(v, v, treesize);
    erased[cent] = 1;

    for(int i = 1; i <= treesize; i++) dist[i] = 1e18;

    for(pair<int,int> x : G[cent]) if(!erased[x.ff]){
        procurar_ans(x.ff, cent, 1, x.ss); // linear
        atualiza_dist(x.ff, cent, 1, x.ss); // linear
    }

    for(pair<int,int> x : G[cent]) if(!erased[x.ff])
        decomp(x.ff, cent);
}

```

Kosaraju

```
vector<int> g[N], gt[N], S; int vis[N], cor[N];
void dfs(int u){
    vis[u] = 1; for(int v : g[u]) if(!vis[v]) dfs(v);
    S.push_back(u);
}
void dfst(int u, int e){
    cor[u] = e;
    for(int v : gt[u]) if(!cor[v]) dfst(v, e);
}
void kosaraju(){
    for(int i = 1; i <= n; i++) if(!vis[i]) dfs(i);
    for(int i = 1; i <= n; i++) for(int j : g[i])
        gt[j].push_back(i);
    int e = 0; reverse(S.begin(), S.end());
    for(int u : S) if(!cor[u]) dfst(u, ++e);
}
```

Tarjan

```
int cnt = 0, root;
void dfs(int u, int p = -1){
    low[u] = num[u] = ++t;
    for(int v : g[u]){
        if(!num[v]){
            dfs(v, u);
            if(u == root) cnt++;
            if(low[v] >= num[u]) u PONTO DE ARTICULACAO;
            if(low[v] > num[u]) ARESTA u->v PONTE;
            low[u] = min(low[u], low[v]);
        }
        else if(v != p) low[u] = min(low[u], num[v]);
    }
}
```

root PONTO DE ARTICULACAO <=> cnt > 1

```
void tarjanSCC(int u){
    low[u] = num[u] = ++cnt;
    vis[u] = 1;
    S.push_back(u);
    for(int v : g[u]){
        if(!num[v]) tarjanSCC(v);
        if(vis[v]) low[u] = min(low[u], low[v]);
    }
    if(low[u] == num[u]){
        ssc[u] = ++ssc_cnt; int v;
        do{
            v = S.back(); S.pop_back(); vis[v] = 0;
            ssc[v] = ssc_cnt;
        }while(u != v);
    }
}
```

Max Clique

long long adj[N], dp[N];

```
for(int i = 0; i < n; i++){
    for(int j = 0; j < n; j++){
        int x;
        scanf("%d", &x);
        if(x || i == j)
            adj[i] |= 1LL << j;
    }
}
```

int resto = n - n/2;

```
int C = n/2;
for(int i = 1; i < (1 << resto); i++){
    int x = i;
    for(int j = 0; j < resto; j++){
        if(i & (1 << j))
            x &= adj[j + C] >> C;
    }
    if(x == i){
        dp[i] = __builtin_popcount(i);
    }
}

for(int i = 1; i < (1 << resto); i++){
    for(int j = 0; j < resto; j++){
        if(i & (1 << j))
            dp[i] = max(dp[i], dp[i ^ (1 << j)]);
    }
}

int maxCliq = 0;
for(int i = 0; i < (1 << C); i++){
    int x = i, y = (1 << resto) - 1;
    for(int j = 0; j < C; j++){
        if(i & (1 << j))
            x &= adj[j] & ((1 << C) - 1), y &= adj[j] >> C;
    }
    if(x != i) continue;
    maxCliq = max(maxCliq, __builtin_popcount(i) + dp[y]);
}
```

Dominator Tree

```
vector<int> g[N], gt[N], T[N];
vector<int> S;
int dsu[N], label[N];
int sdom[N], idom[N], dfs_time, id[N];
```

vector<int> bucket[N];
vector<int> down[N];

```
void prep(int u){
    S.push_back(u);
    id[u] = ++dfs_time;
    label[u] = sdom[u] = dsu[u] = u;

    for(int v : g[u]){
        if(!id[v])
            prep(v), down[u].push_back(v);
        gt[v].push_back(u);
    }
}
```

```
int fnd(int u, int flag = 0){
    if(u == dsu[u]) return u;
    int v = fnd(dsu[u], 1), b = label[ dsu[u] ];
    if(id[ sdom[b] ] < id[ sdom[ label[u] ] ])
        label[u] = b;
    dsu[u] = v;
    return flag ? v : label[u];
}
```

```
void build_dominator_tree(int root, int sz){
    // memset(id, 0, sizeof(int) * (sz + 1));
    // for(int i = 0; i <= sz; i++) T[i].clear();
    prep(root);
    reverse(S.begin(), S.end());

    int w;
    for(int u : S){
        for(int v : gt[u]){
```

```

        w = fnd(v);
        if(id[ sdom[w] ] < id[ sdom[u] ])
            sdom[u] = sdom[w];
    }
    gt[u].clear();

    if(u != root) bucket[ sdom[u] ].push_back(u);

    for(int v : bucket[u]){
        w = fnd(v);
        if(sdom[w] == sdom[v]) idom[v] = sdom[v];
        else idom[v] = w;
    }
    bucket[u].clear();

    for(int v : down[u]) dsu[v] = u;
    down[u].clear();
}

reverse(S.begin(), S.end());
for(int u : S) if(u != root){
    if(idom[u] != sdom[u]) idom[u] = idom[ idom[u] ];
    T[ idom[u] ].push_back(u);
}
S.clear();
}

```

Min Cost Matching

```

// Min cost matching
// O(n^2 * m)
// n == nro de linhas
// m == nro de colunas
// n <= m | flow == n
// a[i][j] = custo pra conectar i a j
vector<int> u(n + 1), v(m + 1), p(m + 1), way(m + 1);
for(int i = 1; i <= n; ++i){
    p[0] = i;
    int j0 = 0;
    vector<int> minv(m + 1, oo);
    vector<char> used(m + 1, false);
    do{
        used[j0] = true;
        int i0 = p[j0], delta = oo, j1;
        for(int j = 1; j <= m; ++j)
            if(!used[j]){
                int cur = a[i0][j] - u[i0] - v[j];
                if(cur < minv[j])
                    minv[j] = cur, way[j] = j0;
                if(minv[j] < delta)
                    delta = minv[j], j1 = j;
            }
        for(int j = 0; j <= m; ++j)
            if(used[j])
                u[p[j]] += delta, v[j] -= delta;
            else
                minv[j] -= delta;
        j0 = j1;
    }while(p[j0] != 0);

    do{
        int j1 = way[j0];
        p[j0] = p[j1];
        j0 = j1;
    }while(j0);
}

// match[i] = coluna escolhida para linha i

```

```

vector<int> match(n + 1);
for(int j = 1; j <= m; ++j)
    match[p[j]] = j;

```

int cost = -v[0];

mjhum's flow

```

#include <bits/stdc++.h>
#ifdef DEMETRIO
#define deb(...) fprintf(stderr, __VA_ARGS__)
#define deb1(x) cerr << #x << " = " << x << endl
#else
#define deb(...) 0
#define deb1(x) 0
#endif
#define pb push_back
#define mp make_pair
#define fst first
#define snd second
#define fore(i,a,b) for(int i=a,ThxDem=b;i<ThxDem;++i)
#define SZ(x) ((int)(x).size())
#define mset(a,v) memset(a,v,sizeof(a))
#define mcpy(a,b) memcpy(a,b,sizeof(a))
using namespace std;
typedef long long ll;

#define MAXN 100055

int nodes,src,dst;
int dist[MAXN],q[MAXN],work[MAXN];
struct edge {int to,rev;ll f,cap;};
vector<edge> g[MAXN];
void add_edge(int s, int t, ll cap){
    g[s].pb((edge){t,SZ(g[t]),0,cap});
    g[t].pb((edge){s,SZ(g[s])-1,0,0});
}
bool dinic_bfs(){
    fill(dist,dist+nodes,-1);dist[src]=0;
    int qt=0;q[qt++]=src;
    for(int qh=0;qh<qt;qh++){
        int u=q[qh];
        fore(i,0,SZ(g[u])){
            edge& e=g[u][i];int v=g[u][i].to;
            if(dist[v]<0&&e.f<e.cap)dist[v]=dist[u]+1,q[
                qt++]=v;
        }
    }
    return dist[dst]>=0;
}
ll dinic_dfs(int u, ll f){
    if(u==dst)return f;
    for(int& i=work[u];i<SZ(g[u]);i++){
        edge& e=g[u][i];
        if(e.cap<=e.f)continue;
        int v=e.to;
        if(dist[v]==dist[u]+1){
            ll df=dinic_dfs(v,min(f,e.cap-e.f));
            if(df>0){e.f+=df;g[v][e.rev].f-=df;return df
                ;}
        }
    }
    return 0;
}
ll max_flow(int _src, int _dst){
    src=_src;dst=_dst;
    ll result=0;
    while(dinic_bfs()){

```

```

        fill(work,work+nodes,0);
        while(ll d=dinic_dfs(src,1LL<<60))result+=d;
    }
    return result;
}

int n,m,s;ll all;
map<int,ll> pingo;
vector<pair<int,ll> > ss;
ll p[100005];
ll d[11][100005];

vector<ll> qwe;

bool can(ll t){
    fore(i,0,nodes)g[i].clear();
    fore(i,0,s)add_edge(0,2+i,ss[i].snd);
    fore(i,0,n)add_edge(2+s+i,1,p[i]);
    fore(i,0,s)fore(j,0,n)if(d[i][j]<=t){
        //printf(" %lld %d %d\n",t,ss[i].fst+1,j+1);
        add_edge(2+i,2+s+j,1LL<<60);
    }
    ll asd=max_flow(0,1);
    //printf(" %lld %lld %lld\n",t,asd,all);
    return asd==all;
}

vector<pair<int,ll> > gg[100005];
priority_queue<pair<ll,int> > qq;

void dijkstra(int x, ll* d){
    fore(i,0,n)d[i]=-1;
    d[x]=0;
    qq.push(mp(0,x));
    while(!qq.empty()){
        int x=qq.top().snd;ll asd=-qq.top().fst;qq.pop();
        if(d[x]!=asd)continue;
        for(auto p:gg[x]){
            int y=p.fst;ll c=p.snd;
            if(d[y]<0||d[x]+c<d[y]){
                d[y]=d[x]+c;
                qq.push(mp(-d[y],y));
            }
        }
    }
}

int main(){
    scanf("%d%d%d",&n,&m,&s);
    fore(i,0,n)scanf("%lld",p+i),all+=p[i];
    while(m--){
        int x,y;ll c;
        scanf("%d%d%lld",&x,&y,&c);x--;y--;
        gg[x].pb(mp(y,c));
        gg[y].pb(mp(x,c));
    }
    fore(_,0,s){
        int x;ll c;
        scanf("%d%lld",&x,&c);x--;
        pingo[x]+=c;
    }
    ss=vector<pair<int,ll> >(pingo.begin(),pingo.end());
    s=SZ(ss);
    fore(i,0,s)dijkstra(ss[i].fst,d[i]);
    nodes=2+s+n;
    fore(i,0,s)fore(j,0,n)qwe.pb(d[i][j]);
    sort(qwe.begin(),qwe.end());

```

```

    qwe.erase(unique(qwe.begin(),qwe.end()),qwe.end());
    fore(i,0,s)g[2+i].reserve(n);
    int s=0,e=SZ(qwe);
    while(e-s>1){
        int m=(s+e)/2;
        if(can(qwe[m-1]))e=m;
        else s=m;
    }
    printf("%lld\n",qwe[s]);
    return 0;
}

```

Strings

Aho Corasick

```

int to[N][A];
int ne = 2, fail[N], term[N];
void add_string(const char *str, int id){
    int p = 1;
    for(int i = 0; str[i]; i++){
        int ch = str[i] - 'a';
        if(!to[p][ch]) to[p][ch] = ne++;
        p = to[p][ch];
    }
    term[p]++;
}

void init(){
    for(int i = 0; i < ne; i++) fail[i] = 1;
    queue<int> q; q.push(1);
    int u, v; char c;
    while(!q.empty()){
        u = q.front(); q.pop();
        for(int i = 0; i < A; i++){
            if(to[u][i]){
                v = to[u][i]; q.push(v);
                if(u != 1){
                    fail[v] = to[ fail[u] ][i];
                    term[v] += term[ fail[v] ];
                }
            }
            else if(u != 1) to[u][i] = to[ fail[u] ][i];
            else to[u][i] = 1;
        }
    }
}

void clean() {
    memset(to, 0, ne * sizeof(to[0]));
    memset(fail, 0, ne * sizeof(fail[0]));
    memset(term, 0, ne * sizeof(term[0]));
    memset(to, 0, ne * sizeof(to[0]));
    ne = 2;
}

// Suffix Array

int lcp[N], c[N];

// Caractere final da string '\0' esta sendo considerado
// parte da string s
void build_sa(char s[], int n, int a[]){
    const int A = 300; // Tamanho do alfabeto
    int c1[n], a1[n], h[n + A];
    memset(h, 0, sizeof h);

    for(int i = 0; i < n; i++) {
        c[i] = s[i];
        h[c[i] + 1]++;
    }
}

```

```

partial_sum(h, h + A, h);
for(int i = 0; i < n; i++)
    a[h[c[i]]++] = i;
for(int i = 0; i < n; i++)
    h[c[i]]--;

for(int L = 1; L < n; L <= 1) {
    for(int i = 0; i < n; i++) {
        int j = (a[i] - L + n) % n;
        a1[h[c[j]]++] = j;
    }

    int cc = -1;
    for(int i = 0; i < n; i++) {
        if(i == 0 || c[a1[i]] != c[a1[i-1]] || c[(a1[i] + L) % n] != c[(a1[i-1] + L) % n])
            h[++cc] = i;
        c1[a1[i]] = cc;
    }

    memcpy(a, a1, sizeof a1);
    memcpy(c, c1, sizeof c1);

    if(cc == n-1) break;
}

void build_lcp(char s[], int n, int a[]){ // lcp[i] =
    lcp(s[:i], s[:i+1])
    int k = 0;

    //memset(lcp, 0, sizeof lcp);
    for(int i = 0; i < n; i++){
        if(c[i] == n-1) continue;
        int j = a[c[i]+1];
        while(i+k < n && j+k < n && s[i+k] == s[j+k]) k
            ++;
        lcp[c[i]] = k;
        if(k) k--;
    }

}

int comp_lcp(int i, int j){
    if(i == j) return n - i;
    if(c[i] > c[j]) swap(i, j);
    return min(lcp[k] for k in [c[i], c[j]-1]);
}

```

Adamant Suffix Tree

```

namespace sf {

const int inf = 1e9;
const int maxn = 200005;
char s[maxn];
map<int, int> to[maxn];
int len[maxn], fpos[maxn], link[maxn];
int node, pos;
int sz = 1, n = 0;

int make_node(int _pos, int _len) {
    fpos[sz] = _pos;
    len[sz] = _len;
    return sz++;
}

void go_edge() {
    while (pos > len[to[node][s[n - pos]]]) {

```

```

        node = to[node][s[n - pos]];
        pos -= len[node];
    }
}

void add_letter(int c) {
    s[n++] = (char)c;
    pos++;
    int last = 0;
    while (pos > 0) {
        go_edge();
        int edge = s[n - pos];
        int &v = to[node][edge];
        int t = s[fpos[v] + pos - 1];
        if (v == 0) {
            v = make_node(n - pos, inf);
            link[last] = node;
            last = 0;
        } else if (t == c) {
            link[last] = node;
            return;
        } else {
            int u = make_node(fpos[v], pos - 1);
            to[u][c] = make_node(n - 1, inf);
            to[u][t] = v;
            fpos[v] += pos - 1;
            len[v] -= pos - 1;
            v = u;
            link[last] = u;
            last = u;
        }
    }
    if (node == 0)
        pos--;
    else
        node = link[node];
}

void add_string(char *str) {
    for (int i = 0; str[i]; i++) add_letter(str[i]);
    add_letter('$');
}

bool is_leaf(int u) { return len[u] > n; }
int get_len(int u) {
    if (!u) return 0;
    if (is_leaf(u)) return n - fpos[u];
    return len[u];
}

int leafs[maxn];
int calc_leafs(int u = 0) {
    leafs[u] = is_leaf(u);
    for (const auto &c : to[u]) leafs[u] += calc_leafs(c.second);
    return leafs[u];
}
}; // namespace sf

int main() { sf::len[0] = sf::inf; }

```

Z Algorithm

```

vector<int> z_algo(const string &s) {
    int n = s.size(), L = 0, R = 0;
    vector<int> z(n, 0);
    for(int i = 1; i < n; i++){
        if(i <= R) z[i] = min(z[i-L], R - i + 1);
        while(z[i]+i < n && s[z[i]+i] == s[z[i]])
            z[i]++;
        if(i+z[i]-1 > R) L = i, R = i + z[i] - 1;
    }
}

```

```
    return z;
}
```

Prefix function/KMP

```
vector<int> prefix_function(const string &s){
    int n = s.size(); vector<int> b(n+1);
    b[0] = -1; int i = 0, j = -1;
    while(i < n){
        while(j >= 0 && s[i] != s[j]) j = b[j];
        b[++i] = ++j;
    }
    return b;
}

void kmp(const string &t, const string &p){
    vector<int> b = prefix_function(p);
    int n = t.size(), m = p.size();
    int j = 0;
    for(int i = 0; i < n; i++){
        while(j >= 0 && t[i] != p[j]) j = b[j];
        j++;
        if(j == m){
            //patern of p found on t
            j = b[j];
        }
    }
}
```

Min rotation

```
int min_rotation(int *s, int N) {
    REP(i, N) s[N+i] = s[i];

    int a = 0;
    REP(b, N) REP(i, N) {
        if (a+i == b || s[a+i] < s[b+i]) { b += max(0, i-1);
            break; }
        if (s[a+i] > s[b+i]) { a = b; break; }
    }
    return a;
}
```

Manacher

```
// rad[2 * i] = largest palindrome cetered at char i
// rad[2 * i + 1] = largest palindrome cetered between
// chars i and i+1
void manacher(char *s, int n, int *rad) {
    static char t[2*MAX];
    int m = 2 * n - 1;

    for(int i = 0; i < m; i++) t[i] = -1;
    for(int i = 0; i < n; i++) t[2 * i] = s[i];

    int x = 0;
    for(int i = 1; i < m; i++) {
        int &r = rad[i] = 0;
        if(i <= x+rad[x]) r = min(rad[x+x-i], x+rad[x]-i);
        while(i - r - 1 >= 0 and i + r + 1 < m and
            t[i - r - 1] == t[i + r + 1]) ++r;
        if(i + r >= x + rad[x]) x = i;
    }

    for(int i = 0; i < m; i++) {
        if(i-rad[i] == 0 || i+rad[i] == m-1) ++rad[i];
    }
    // for(int i = 0; i < m; i++) rad[i] /= 2;
}
```

Suffix Automaton

```
map<char, int> to[2*N];
int link[2*N], len[2*N], last = 0, sz = 1;

void add_letter(char c){
    int p = last;
    last = sz++;
    len[last] = len[p] + 1;
    for(; !to[p][c]; p = link[p]) to[p][c] = last;
    if(to[p][c] == last){
        link[last] = 0;
        return;
    }
    int u = to[p][c];
    if(len[u] == len[p]+1){
        link[last] = u;
        return;
    }
    int c1 = sz++;
    to[c1] = to[u];
    link[c1] = link[u];
    len[c1] = len[p]+1;
    link[last] = link[u] = c1;
    for(; to[p][c] == u; p = link[p]) to[p][c] = c1;
}
```

Suffix Tree

```
namespace sf {
    // const int NS = ; const int N = * 2;
    int cn, cd, ns, en = 1, lst;
    string S[NS]; int si = -1;
    vector<int> sufn[N]; // sufn[si][i] no do sufixo S[si][i]
    ...
    struct node {
        int l, r, si, p, suf;
        map<char, int> adj;
        node() : l(0), r(-1), suf(0), p(0) {}
        node(int L, int R, int S, int P) : l(L), r(R), si(S),
            p(P) {}
        inline int len() { return r - l + 1; }
        inline int operator[](int i) { return S[si][l + i]; }
        inline int& operator()(char c) { return adj[c]; }
    } t[N];
    inline int new_node(int L, int R, int S, int P) { t[en]
        = node(L, R, S, P); return en++; }
    void add_string(string s) {
        s += '$'; S[++si] = s; sufn[si].resize(s.size() + 1)
            ; cn = cd = 0;
        int i = 0; const int n = s.size();
        for(int j = 0; j < n; j++)
            for(; i <= j; i++) {
                if(cd == t[cn].len() && t[cn][s[j]]) { cn = t
                    [cn][s[j]]; cd = 0; }
                if(cd < t[cn].len() && t[cn][cd] == s[j]) {
                    cd++;
                    if(j < s.size() - 1) break;
                }
                else {
                    if(i) t[lst].suf = cn;
                    for(; i <= j; i++) { sufn[si][i] = cn;
                        cn = t[cn].suf; }
                }
            }
        else if(cd == t[cn].len()) {
            sufn[si][i] = en;
            if(i) t[lst].suf = en; lst = en;
            t[cn][s[j]] = new_node(j, n - 1, si, cn);
        }
    }
}
```

```

        cn = t[cn].suf; cd = t[cn].len();
    } else {
        int mid = new_node(t[cn].l, t[cn].l + cd -
            1, t[cn].si, t[cn].p);
        t[t[cn].p][t[cn][0]] = mid;
        if(ns) t[ns].suf = mid;
        if(i) t[lst].suf = en; lst = en;
        sufn[si][i] = en;
        t[mid](s[j]) = new_node(j, n - 1, si, mid);
        ;
        t[mid](t[cn][cd]) = cn;
        t[cn].p = mid; t[cn].l += cd; cn = t[mid].
            p;
        int g = cn? j - cd : i + 1; cn = t[cn].suf
            ;
        while(g < j && g + t[t[cn](S[si][g])].len
            () <= j) {
            cn = t[cn](S[si][g]); g += t[cn].len();
        }
        if(g == j) { ns = 0; t[mid].suf = cn; cd =
            t[cn].len(); }
        else { ns = mid; cn = t[cn](S[si][g]); cd
            = j - g; }
    }
}
}
};

```

Geometry

2D basics

```

typedef double cod;
double eps = 1e-7;
bool eq(cod a, cod b){ return abs(a - b) <= eps; }

```

```

struct vec{
    cod x, y; int id;
    vec(cod a = 0, cod b = 0) : x(a), y(b) {}
    vec operator+(const vec &o) const{
        return {x + o.x, y + o.y};
    }
    vec operator-(const vec &o) const{
        return {x - o.x, y - o.y};
    }
    vec operator*(cod t) const{
        return {x * t, y * t};
    }
    vec operator/(cod t) const{
        return {x / t, y / t};
    }
    cod operator*(const vec &o) const{ // cos
        return x * o.x + y * o.y;
    }
    cod operator^(const vec &o) const{ // sin
        return x * o.y - y * o.x;
    }
    bool operator==(const vec &o) const{
        return eq(x, o.x) && eq(y, o.y);
    }
    bool operator<(const vec &o) const{
        if(!eq(x, o.x)) return x < o.x;
        return y < o.y;
    }
    cod cross(const vec &a, const vec &b) const{
        return (a-(*this)) ^ (b-(*this));
    }
    int ccw(const vec &a, const vec &b) const{

```

```

        cod tmp = cross(a, b);
        return (tmp > eps) - (tmp < -eps);
    }
    cod dot(const vec &a, const vec &b) const{
        return (a-(*this)) * (b-(*this));
    }
    cod len() const{
        return sqrt(x * x + y * y); // <
    }
    double angle(const vec &a, const vec &b) const{
        return atan2(cross(a, b), dot(a, b));
    }
    double tan(const vec &a, const vec &b) const{
        return cross(a, b) / dot(a, b);
    }
    vec unit() const{
        return operator/(len());
    }
    int quad() const{
        if(x > 0 && y >=0) return 0;
        if(x <=0 && y > 0) return 1;
        if(x < 0 && y <=0) return 2;
        return 3;
    }
    bool comp(const vec &a, const vec &b) const{
        return (a - *this).comp(b - *this);
    }
    bool comp(vec b){
        if(quad() != b.quad()) return quad() < b.quad();
        if(!eq(operator^(b), 0)) return operator^(b) > 0;
        return (*this) * (*this) < b * b;
    }
    template<class T>
    void sort_by_angle(T first, T last) const{
        std::sort(first, last, [=](const vec &a, const
            vec &b){
            return comp(a, b);
        });
    }
    vec rot90() const{ return {-y, x}; }
    vec rot(double a) const{
        return {cos(a)*x -sin(a)*y, sin(a)*x +cos(a)*y};
    }
    vec proj(const vec &b) const{ // proj of *this onto
        b
        cod k = operator*(b) / (b * b);
        return b * k;
    }
    // proj of (*this) onto the plane orthogonal to b
    vec rejection(vec b) const{
        return (*this) - proj(b);
    }
};

struct line{
    cod a, b, c; vec n;
    line(vec q, vec w){ // q.cross(w, (x, y)) = 0
        a = -(w.y-q.y);
        b = w.x-q.x;
        c = -(a * q.x + b * q.y);
        n = {a, b};
    }
    cod dist(const vec &o) const{
        return abs(eval(o)) / n.len();
    }
    bool contains(const vec &o) const{
        return eq(a * o.x + b * o.y + c, 0);
    }

```



```

}
cod dist(const line &o) const{
    if(!parallel(o)) return 0;
    if(!eq(o.a * b, o.b * a)) return 0;
    if(!eq(a, 0))
        return abs(c - o.c * a / o.a) / n.len();
    if(!eq(b, 0))
        return abs(c - o.c * b / o.b) / n.len();
    return abs(c - o.c);
}
bool parallel(const line &o) const{
    return eq(n ^ o.n, 0);
}
bool operator==(const line &o) const{
    if(!eq(a*o.b, b*o.a)) return false;
    if(!eq(a*o.c, c*o.a)) return false;
    if(!eq(c*o.b, b*o.c)) return false;
    return true;
}
bool intersect(const line &o) const{
    return !parallel(o) || *this == o;
}
vec inter(const line &o) const{
    if(parallel(o)){
        if(*this == o){ }
        else{ /* dont intersect */ }
    }

    auto tmp = n ^ o.n;
    return {(o.c*b -c*o.b)/tmp, (o.a*c -a*o.c)/tmp};
}
vec at_x(cod x) const{
    return {x, (-c-a*x)/b};
}
vec at_y(cod y) const{
    return {(-c-b*y)/a, y};
}
cod eval(const vec &o) const{
    return a * o.x + b * o.y + c;
}
};

struct segment{
    vec p, q;
    segment(vec a = vec(), vec b = vec()): p(a), q(b) {}
    bool onstrip(const vec &o) const{ // onstrip strip
        return p.dot(o, q) >= -eps && q.dot(o, p) >= -eps;
    }
    cod len() const{
        return (p-q).len();
    }
    cod dist(const vec &o) const{
        if(onstrip(o)) return line(p, q).dist(o);
        return min((o-q).len(), (o-p).len());
    }
    bool contains(const vec &o) const{
        return eq(p.cross(q, o), 0) && onstrip(o);
    }
    bool intersect(const segment &o) const{
        if(contains(o.p)) return true;
        if(contains(o.q)) return true;
        if(o.contains(q)) return true;
        if(o.contains(p)) return true;
        return p.ccw(q, o.p) * p.ccw(q, o.q) == -1
        && o.p.ccw(o.q, q) * o.p.ccw(o.q, p) == -1;
    }
}

```

```

bool intersect(const line &o) const{
    return o.eval(p) * o.eval(q) <= 0;
}
cod dist(const segment &o) const{
    if(line(p, q).parallel(line(o.p, o.q))){
        if(onstrip(o.p) || onstrip(o.q)
        || o.onstrip(p) || o.onstrip(q))
            return line(p, q).dist(line(o.p, o.q));
    }
    else if(intersect(o)) return 0;
    return min(min(dist(o.p), dist(o.q)),
        min(o.dist(p), o.dist(q)));
}
cod dist(const line &o) const{
    if(line(p, q).parallel(o))
        return line(p, q).dist(o);
    else if(intersect(o)) return 0;
    return min(o.dist(p), o.dist(q));
}
};

struct hray{
    vec p, q;
    hray(vec a = vec(), vec b = vec()): p(a), q(b){}
    bool onstrip(const vec &o) const{ // onstrip strip
        return p.dot(q, o) >= -eps;
    }
    cod dist(const vec &o) const{
        if(onstrip(o)) return line(p, q).dist(o);
        return (o-p).len();
    }
    bool intersect(const segment &o) const{
        if(!o.intersect(line(p,q))) return false;
        if(line(o.p, o.q).parallel(line(p,q)))
            return contains(o.p) || contains(o.q);
        return contains(line(p,q).inter(line(o.p,o.q)));
    }
    bool contains(const vec &o) const{
        return eq(line(p, q).eval(o), 0) && onstrip(o);
    }
    cod dist(const segment &o) const{
        if(line(p, q).parallel(line(o.p, o.q))){
            if(onstrip(o.p) || onstrip(o.q))
                return line(p, q).dist(line(o.p, o.q));
            return o.dist(p);
        }
        else if(intersect(o)) return 0;
        return min(min(dist(o.p), dist(o.q)),
            o.dist(p));
    }
    bool intersect(const hray &o) const{
        if(!line(p, q).parallel(line(o.p, o.q)))
            return false;
        auto pt = line(p, q).inter(line(o.p, o.q));
        return contains(pt) && o.contains(pt); // <<
    }
    bool intersect(const line &o) const{
        if(line(p, q).parallel(o)) return line(p, q) == o;
        if(o.contains(p) || o.contains(q)) return true;
        return (o.eval(p) >= -eps)^(o.eval(p)<o.eval(q));
        return contains(o.inter(line(p, q)));
    }
    cod dist(const line &o) const{
        if(line(p,q).parallel(o))
            return line(p,q).dist(o);
        else if(intersect(o)) return 0;
        return o.dist(p);
    }
}

```

```

    }
    cod dist(const hray &o) const{
        if(line(p, q).parallel(line(o.p, o.q))){
            if(onstrip(o.p) || o.onstrip(p))
                return line(p,q).dist(line(o.p, o.q));
            return (p-o.p).len();
        }
        else if(intersect(o)) return 0;
        return min(dist(o.p), o.dist(p));
    }
};

double heron(cod a, cod b, cod c){
    cod s = (a + b + c) / 2;
    return sqrt(s * (s - a) * (s - b) * (s - c));
}

line mediatrix(const vec &a, const vec &b) {
    auto tmp = (b - a) * 2;
    return line(tmp.x, tmp.y, a * a - b * b);
}

struct circle {
    vec c; cod r;
    circle() : c(0, 0), r(0) {}
    circle(const vec o) : c(o), r(0) {}
    circle(const vec &a, const vec &b) {
        c = (a + b) * 0.5; r = (a - c).len();
    }
    circle(const vec &a, const vec &b, const vec &cc) {
        c = mediatrix(a, b).inter(mediatrix(b, cc));
        r = (a - c).len();
    }
    bool inside(const vec &a) const {
        return (a - c).len() <= r;
    }
};

circle min_circle_cover(vector<vec> v) {
    random_shuffle(v.begin(), v.end());
    circle ans;
    int n = (int)v.size();
    for(int i = 0; i < n; i++) if(!ans.inside(v[i])) {
        ans = circle(v[i]);
        for(int j = 0; j < i; j++) if(!ans.inside(v[j])){
            ans = circle(v[i], v[j]);
            for(int k=0; k<j; k++)if(!ans.inside(v[k])){
                ans = circle(v[i], v[j], v[k]);
            }
        }
    }
    return ans;
}

```

Circle line intersection

```

// intersection of line a * x + b * y + c = 0
// and circle centered at the origin with radius r
double r, a, b, c; // given as input
double x0 = -a*c/(a*a+b*b), y0 = -b*c/(a*a+b*b);
if(c*c > r*r*(a*a+b*b)+EPS)
    puts("no points");
else if(abs(c*c - r*r*(a*a+b*b)) < EPS){
    puts("1 point");
    cout << x0 << ' ' << y0 << '\n';
}
else {
    double d = r*r - c*c/(a*a+b*b);
    double mult = sqrt(d / (a*a+b*b));
    double ax, ay, bx, by;
    ax = x0 + b * mult;

```

```

    bx = x0 - b * mult;
    ay = y0 - a * mult;
    by = y0 + a * mult;
    puts ("2 points");
    cout<<ax<< ' ' <<ay<<'\n'<<bx<< ' ' <<by<<'\n';
}

```

Half plane intersection

```

const double eps = 1e-8;
typedef pair<long double, long double> pi;
bool z(long double x){ return fabs(x) < eps; }
struct line{
    long double a, b, c;
    bool operator<(const line &l)const{
        bool flag1 = pi(a, b) > pi(0, 0);
        bool flag2 = pi(l.a, l.b) > pi(0, 0);
        if(flag1 != flag2) return flag1 > flag2;
        long double t = ccw(pi(0, 0), pi(a, b), pi(l.a, l.b));
        return z(t) ? c * hypot(l.a, l.b) < l.c * hypot(a, b) : t > 0;
    }
    pi slope(){ return pi(a, b); }
};
pi cross(line a, line b){
    long double det = a.a * b.b - b.a * a.b;
    return pi((a.c * b.b - a.b * b.c) / det, (a.a * b.c - a.c * b.a) / det);
}
bool bad(line a, line b, line c){
    if(ccw(pi(0, 0), a.slope(), b.slope()) <= 0) return false;
    pi crs = cross(a, b);
    return crs.first * c.a + crs.second * c.b >= c.c;
}
bool solve(vector<line> v, vector<pi> &solution){ // ax
+ by <= c;
    sort(v.begin(), v.end());
    deque<line> dq;
    for(auto &i : v){
        if(!dq.empty() && z(ccw(pi(0, 0), dq.back().slope(), i.slope()))) continue;
        while(dq.size() >= 2 && bad(dq[dq.size()-2], dq.back(), i)) dq.pop_back();
        while(dq.size() >= 2 && bad(i, dq[0], dq[1])) dq.pop_front();
        dq.push_back(i);
    }
    while(dq.size() > 2 && bad(dq[dq.size()-2], dq.back(), dq[0])) dq.pop_back();
    while(dq.size() > 2 && bad(dq.back(), dq[0], dq[1])) dq.pop_front();
    vector<pi> tmp;
    for(int i=0; i<dq.size(); i++){
        line cur = dq[i], nxt = dq[(i+1)%dq.size()];
        if(ccw(pi(0, 0), cur.slope(), nxt.slope()) <= eps)
            return false;
        tmp.push_back(cross(cur, nxt));
    }
    solution = tmp;
    return true;
}

```

Detect empty Half plane intersection

```

// abs(point a) = absolute value of a
// ccw(a, b, c) = a.ccw(b, c)
pair<bool, point> half_inter(vector<pair<point,point> >

```

```

&vet){
    random_shuffle(all(vet));
    point p;
    rep(i,0,sz(vet)) if(ccw(vet[i].x,vet[i].y,p) != 1){
        point dir = (vet[i].y - vet[i].x) / abs(vet[i].y
            - vet[i].x);
        point l = vet[i].x - dir*1e15;
        point r = vet[i].x + dir*1e15;
        if(r < l) swap(l, r);
        rep(j, 0, i){
            if(ccw(point(), vet[i].x-vet[i].y, vet[j].x-
                vet[j].y) == 0){
                if(ccw(vet[j].x, vet[j].y, p) == 1)
                    continue;
                return mp(false, point());
            }
            if(ccw(vet[j].x, vet[j].y, l) != 1)
                l = max(l, line_intersect(vet[i].x,vet[i].
                    y,vet[j].x,vet[j].y));
            if(ccw(vet[j].x, vet[j].y, r) != 1)
                r = min(r, line_intersect(vet[i].x,vet[i].
                    y,vet[j].x,vet[j].y));
            if(!(l < r)) return mp(false, point());
        }
        p = r;
    }
    return mp(true, p);
}

```

Delaunay

```

struct triple {
    int i, j, k;
    triple() {}
    triple(int i, int j, int k) : i(i), j(j), k(k) {}
};
int cmp(ld x, ld y = 0, ld tol = EPS) {
    return (x <= y + tol) ? (x + tol < y) ? -1 : 0 : 1;
}

```

```

//Problema se tiver mais de uma triangulacao possivel
vector<triple> delaunayTriangulation(vector<ld>& x,
    vector<ld>& y) {
    int n = x.size();
    vector<ld> z(n);
    vector<triple> ret;
    for (int i = 0; i < n; i++)
        z[i] = x[i] * x[i] + y[i] * y[i];
    rep(i,0,n-2) rep(j,i+1,n) rep(k,i+1,n){
        if (j == k) continue;
        ld xn = (y[j]-y[i])*(z[k]-z[i]) - (y[k]-y[i])*(z[
            j]-z[i]);
        ld yn = (x[k]-x[i])*(z[j]-z[i]) - (x[j]-x[i])*(z[
            k]-z[i]);
        ld zn = (x[j]-x[i])*(y[k]-y[i]) - (x[k]-x[i])*(y[
            j]-y[i]);
        bool flag = (cmp(zn) < 0);
        for (int m = 0; flag && m < n; m++)
            flag &= (cmp((x[m]-x[i])*xn + (y[m]-y[i])*yn
                + (z[m]-z[i])*zn) <= 0);
        if (flag) ret.push_back(triple(i, j, k));
    }
    return ret;
}

```

Simple Triangulate

```

bool isear (vec * p, int n, int i, int prev[], int next
    []) { // aux to triangulate

```

```

    vec a = p[prev[i]], b = p[next[i]];
    if (b.ccw(a,p[i]) <= 0) return false;
    for (int j = 0; j < n; j++) {
        if (j == prev[i] || j == next[i]) continue;
        if (p[j].ccw(a,p[i]) >= 0 && p[j].ccw(p[i],b) >=
            0 && p[j].ccw(b,a) >= 0) return false;
        int k = (j+1)%n;
        if (k == prev[i] || k == next[i]) continue;
        if (inter_seg(p[j],p[k],a,b)) return false;
    }
    return true;
}
int triangulate (vec * p, int n, bool ear[], int prev[],
    int next[], int tri[][3]) { // O(n^2) | n >= 3
    int s = 0, i = 0;
    for (int i = 0, prv = n-1; i < n; i++) { prev[i] =
        prv; prv = i; next[i] = (i+1)%n; ear[i] = isear(p,
            n,i,prev,next); }
    for (int lef = n; lef > 3; lef--, i = next[i]) {
        while (!ear[i]) i = next[i];
        tri[s][0] = prev[i]; tri[s][1] = i; tri[s][2] =
            next[i]; s++; // tri[i][0],i,tri[i][1] inserted
        int c_prev = prev[i], c_next = next[i];
        next[c_prev] = c_next; prev[c_next] = c_prev;
        ear[c_prev] = isear(p,n,c_prev,prev,next); ear[
            c_next] = isear(p,n,c_next,prev,next);
    }
    tri[s][0] = next[next[i]]; tri[s][1] = i; tri[s][2]
        = next[i]; s++; // tri[i][0],i,tri[i][1] inserted
    return s;
}

```

Circle Circle intersection

Assume that the first circle is centered at the origin and second at (x_2, y_2) . Find circle line intersection of first circle and line $Ax + By + C = 0$, where $A = -2x_2$, $B = -2y_2$, $C = x_2^2 + y_2^2 + r_1^2 - r_2^2$.

Be aware of corner case with two circles centered at the same point.

Tangents of two circles

```

// solve first for same circle(and infinitely many
    tangents)
// Find up to four tangents of two circles
void tangents(pt c, double r1, double r2, vector<line> &
    ans){
    double r = r2 - r1;
    double z = c.x * c.x + c.y * c.y;
    double d = z - r * r;
    if(d < -EPS) return;
    d = sqrt(abs(d));
    line l;
    l.a = (c.x * r + c.y * d) / z;
    l.b = (c.y * r - c.x * d) / z;
    l.c = r1;
    ans.push_back (l);
}
vector<line> tangents(circle a, circle b){
    vector<line> ans;
    pt aux = a.center - b.center;
    for(int i = -1; i <= 1; i += 2)
        for(int j = -1; j <= 1; j += 2)
            tangents(aux, a.r * i, b.r * j, ans);
    for(size_t i = 0; i < ans.size(); ++i)
        ans[i].c -= ans[i].a * a.x + ans[i].b * a.y;
}

```

```
    return ans;
}
```

Convex Hull

```
vector<vec> monotone_chain_ch(vector<vec> P){
    sort(P.begin(), P.end());

    vector<vec> L, U;
    for(auto p : P){
        while(L.size() >= 2 && L[L.size() - 2].cross(L.
            back(), p) < 0)
            L.pop_back();

        L.push_back(p);
    }

    reverse(P.begin(), P.end());
    for(auto p : P){
        while(U.size() >= 2 && U[U.size() - 2].cross(U.
            back(), p) < 0)
            U.pop_back();

        U.push_back(p);
    }

    L.pop_back(), U.pop_back();

    L.reserve(L.size() + U.size());
    L.insert(L.end(), U.begin(), U.end());

    return L;
}
```

Check point inside polygon

```
bool below(const vector<vec> &vet, vec p){
    auto it = lower_bound(vet.begin(), vet.end(), p);
    if(it == vet.end()) return false;
    if(it == vet.begin()) return *it == p;
    return prev(it)->cross(*it, p) <= 0;
}

bool above(const vector<vec> &vet, vec p){
    auto it = lower_bound(vet.begin(), vet.end(), p);
    if(it == vet.end()) return false;
    if(it == vet.begin()) return *it == p;
    return prev(it)->cross(*it, p) >= 0;
}

// lowerhull, upperhull and point, borders included
bool inside_poly(const vector<vec> &lo, const vector<vec>
    &hi, vec p){
    return below(hi, p) && above(lo, p);
}
```

Check point inside polygon without lower/upper hull

```
// borders included
// must not have 3 colinear consecutive points
bool inside_poly(const vector<vec> &v, vec p){
    if(v[0].ccw(v[1], p) < 0) return false;
    if(v[0].ccw(v.back(), p) > 0) return 0;
    if(v[0].ccw(v.back(), p) == 0)
        return v[0].dot(p, v.back()) >= 0
            && v.back().dot(p, v[0]) >= 0;

    int L = 1, R = (int)v.size() - 1, ans = 1;
```

```
while(L <= R){
    int mid = (L+R)/2;
    if(v[0].ccw(v[mid], p) >= 0) ans = mid, L = mid
        +1;
    else R = mid-1;
}
```

```
return v[ans].ccw(v[(ans+1)%v.size()], p) >= 0;
}
```

Minkowski sum

```
vector<vec> mk(const vector<vec> &a, const vector<vec> &b){
    int i = 0, j = 0;
    for(int k = 0; k < (int)a.size(); k++){
        if(a[k] < a[i])
            i = k;
        for(int k = 0; k < (int)b.size(); k++){
            if(b[k] < b[j])
                j = k;
        }

        vector<vec> c;
        c.reserve(a.size() + b.size());
        for(int k = 0; k < int(a.size()+b.size()); k++){
            vec pt{a[i] + b[j]};
            if((int)c.size() >= 2
                && c[c.size()-2].ccw(c.back(), pt) == 0)
                c.pop_back();
            c.push_back(pt);
            int q = i+1, w = j+1;
            if(q == int(a.size())) q = 0;
            if(w == int(b.size())) w = 0;
            if(c.back().ccw(a[i]+b[w], a[q]+b[j]) < 0) i = q;
            else j = w;
        }
        c.shrink_to_fit();

        return c;
    }
}
```

Geo Notes

Center of mass

System of points(2D/3D): Mass weighted average of points.

Frame(2D/3D): Get middle point of each segment solve as previously.

Triangle: Average of vertices.

2D Polygon: Compute **signed** area and center of mass of triangle $((0,0), p_i, p_{i+1})$. Then solve as system of points.

Polyhedron surface: Solve each face as a 2D polygon (be aware of $(0,0)$) then replace each face with its center of mass and solve as system of points.

Tetrahedron(Triangular pyramid): As triangles, its the average of points.

Polyhedron: Can be done as 2D polygon, but with tetrahedralization instead of triangulation.

Pick's Theorem

Given a polygon without self-intersections and all its vertices on integer coordinates in some 2D grid. Let A be its area, I the number of points with interger coordinates stricly inside the polygon and B the number of points with interger coordinates in the border of the polygon. The following formula holds: $A = I + \frac{B}{2} - 1$.

Miscellaneous

LIS

```
multiset<int> S;
for(int i = 0; i < n; i++){
    auto it = S.upper_bound(a[i]); // low for inc
    if(it != S.end()) S.erase(it);
    S.insert(a[i]);
}
ans = S.size();
```

DSU rollback

```
struct DSU{
    vector<int> sz, p, change;
    vector<tuple<int, int, int>> modifications;
    vector<size_t> saves;
    bool bipartite;

    DSU(int n): sz(n+1, 1), p(n+1), change(n+1),
        bipartite(true){
        iota(p.begin(), p.end(), 0);
    }

    void add_edge(int u, int v){
        if(!bipartite) return;
        int must_change = get_colour(u) == get_colour(v);
        int a = rep(u), b = rep(v);
        if(sz[a] < sz[b]) swap(a, b);
        if(a != b){
            p[b] = a;
            modifications.emplace_back(b, change[b],
                bipartite);
            change[b] ^= must_change;
            sz[a] += sz[b];
        }
        else if(must_change){
            modifications.emplace_back(0, change[0],
                bipartite);
            bipartite = false;
        }
    }

    int rep(int u){
        return p[u] == u ? u : rep(p[u]);
    }

    int get_colour(int u){
        if(p[u] == u) return change[u];
        return change[u] ^ get_colour(p[u]);
    }

    void reset(){
        modifications.clear();
        saves.clear();
        iota(p.begin(), p.end(), 0);
        fill(sz.begin(), sz.end(), 1);
        fill(change.begin(), change.end(), 0);
        bipartite = true;
    }

    void rollback(){
        int u = get<0>(modifications.back());
        tie(ignore, change[u], bipartite) = modifications
            .back();
        sz[ p[u] ] -= sz[u];
        p[u] = u;
        modifications.pop_back();
    }

    void reload(){
        while(modifications.size() > saves.back())
            rollback();
        saves.pop_back();
    }

    void save(){
        saves.push_back(modifications.size());
    }
};
```

Buildings

```
// count the number of circular arrays of size m, with
// elements on range [1, c**(n*n)]
int n, m, c; cin >> n >> m >> c;
int x = f_exp(c, n * n); int ans = f_exp(x, m);
for(int i = 1; i <= m; i++) if(m % i == 0) {
    int y = f_exp(x, i);
    for(int j = 1; j < i; j++) if(i % j == 0)
        y = sub(y, mult(j, dp[j]));
    dp[i] = mult(y, inv(i));
    ans = sub(ans, mult(i - 1, dp[i]));
}
cout << ans << '\n';
```

Rand

```
#include <random>
#include <chrono>
cout << RAND_MAX << endl;
mt19937 rng(chrono::steady_clock::now().time_since_epoch
    ().count());
vector<int> permutation(N);
iota(permutation.begin(), permutation.end(), 0);
shuffle(permutation.begin(), permutation.end(), rng);
iota(permutation.begin(), permutation.end(), 0);
for(int i = 1; i < N; i++){
    swap(permutation[i], permutation[
        uniform_int_distribution<int>(0, i)(rng)]);
}
```

Klondike

```
// minimum number of moves to make
// all elements equal
// move: change a segment of equal value
// elements to any value

int v[305], dp[305][305], rec[305][305];
```

```
int f(int l, int r){
    if(r == l) return 1;
    if(r < l) return 0;
    if(dp[l][r] != -1) return dp[l][r];
    int ans = f(l+1, r) + 1;
    for(int i = l+1; i <= r; i++){
        if(v[i] == v[l])
            ans = min(ans, f(l, i - 1) + f(i+1, r));
    }
    return dp[l][r] = ans;
}
```

Hilbert Order

```
// maybe use B = n / sqrt(q)
inline int64_t hilbertOrder(int x, int y, int pow = 21,
    int rotate = 0) {
    if(pow == 0) return 0;
```

```

int hpow = 1 << (pow-1);
int seg = (x < hpow) ? (
    (y < hpow) ? 0 : 3
) : (
    (y < hpow) ? 1 : 2
);
seg = (seg + rotate) & 3;
const int rotateDelta[4] = {3, 0, 0, 1};
int nx = x & (x ^ hpow), ny = y & (y ^ hpow);
int nrot = (rotate + rotateDelta[seg]) & 3;
int64_t subSquareSize = int64_t(1) << (2*pow - 2);
int64_t ans = seg * subSquareSize;
int64_t add = hilbertOrder(nx, ny, pow-1, nrot);
ans += (seg == 1 || seg == 2) ? add : (subSquareSize
    - add - 1);
return ans;
}

```

Modular Factorial

```

// Compute (1*2*...*(p-1)*1*(p+1)*(p+2)*...*n) % p
// in O(p*lg(n))
int factmod(int n, int p){
    int ans = 1;
    while(n > 1){
        for(int i = 2; i <= n % p; i++){
            ans = (ans * i) % p;
        }
        n /= p;
        if(n % 2) ans = p - ans;
    }
    return ans % p;
}
int fac_pow(int n, int p){
    int ans = 0;
    while(n) n /= p, ans += n;
    return ans;
}
int C(int n, int k, int p){
    if(fac_pow(n, p) > fac_pow(n-k, p) + fac_pow(k, p))
        return 0;
    int tmp = factmod(k, p) * factmod(n-k, p) % p;
    return (f_exp(tmp, p - 2, p) * factmod(n, p)) % p;
}

```

Enumeration all submasks of a bitmask

```

// loop through all submask of a given bitmask
// it does not include mask 0
for(int sub = mask; sub; sub = (sub-1)&mask){
}

```

Slope Trick

```

///By woqjal25, contest: Codeforces Round #371 (Div. 1),
problem: (C) Sonya and Problem Wihtout a Legend,
Accepted, #
int main() {
    int n, t; long long ans = 0; priority_queue<int> Q;
    scanf("%d%d", &n, &t); Q.push(t);
    for(int i = 1; i < n; i++) {
        scanf("%d", &t); t -= i; Q.push(t);
        if(Q.top() > t) {
            ans += Q.top() - t; Q.pop(); Q.push(t);
        }
    }
    printf("%lld", ans);
}

```

Knapsack Bounded with Cost

```

// menor custo para conseguir peso ate M usando N tipos
diferentes de elementos, sendo que o i-esimo elemento
pode ser usado b[i] vezes, tem peso w[i] e custo c[i]
// O(N * M)

```

```

int b[N], w[N], c[N];
MinQueue Q[M];
int d[M] //d[i] = custo minimo para conseguir peso i

for(int i = 0; i <= M; i++) d[i] = i ? oo : 0;
for(int i = 0; i < N; i++){
    for(int j = 0; j < w[i]; j++){
        Q[j].clear();
        for(int j = 0; j <= M; j++){
            q = Q[j % w[i]];
            if(q.size() >= q.pop());
            q.add(c[i]);
            q.push(d[j]);
            d[j] = q.getmin();
        }
    }
}

```

LCA <O(nlgn), O(1)>

```

int start[N], dfs_time;
int tour[2*N], id[2*N];

void dfs(int u){
    start[u] = dfs_time;
    id[dfs_time] = u;
    tour[dfs_time++] = start[u];
    for(int v : g[u]){
        dfs(v);
        id[dfs_time] = u;
        tour[dfs_time++] = start[u];
    }
}

int LCA(int u, int v){
    if(start[u] > start[v]) swap(u, v);
    return id[min(tour[k] for k in [start[u], start[v]])];
}

```

Buffered reader

```

// source: https://github.com/ngthanhtrung23/
ACM_Notebook_new/blob/master/buffered_reader.h
int INP, AM, REACHEOF;
#define BUFSIZE (1<<12)
char BUF[BUFSIZE+1], *inp=BUF;
#define GETCHAR(INP) { \
    if(!*inp && !REACHEOF) { \
        memset(BUF, 0, sizeof BUF); \
        int inpzzz = fread(BUF, 1, BUFSIZE, stdin); \
        if (inpzzz != BUFSIZE) REACHEOF = true; \
        inp=BUF; \
    } \
    INP=*inp++; \
}
#define DIG(a) (((a)>='0')&&((a)<='9'))
#define GN(j) { \
    AM=0; \
    GETCHAR(INP); while(!DIG(INP) && INP!='-') GETCHAR( \
        INP); \
    if (INP=='-') {AM=1; GETCHAR(INP);} \
    j=INP-'0'; GETCHAR(INP); \
    while(DIG(INP)){j=10*j+(INP-'0'); GETCHAR(INP);} \
}

```

```

    if (AM) j=-j;\
}

```

Modular summation

```

//calcula (sum(0 <= i <= n) P(i)) % mod,
//onde P(i) eh uma PA modular (com outro modulo)
namespace sum_pa_mod{
    ll calc(ll a, ll b, ll n, ll mod){
        assert(a&&b);
        if(a >= b){
            ll ret = ((n*(n+1)/2)%mod)*(a/b);
            if(a%b) ret = (ret + calc(a%b,b,n,mod))%mod;
            else ret = (ret+n+1)%mod;
            return ret;
        }
        return ((n+1)*(((n*a)/b+1)%mod) - calc(b,a,(n*a)/
            b,mod) + mod + n/b + 1)%mod;
    }

    //P(i) = a*i mod m
    ll solve(ll a, ll n, ll m, ll mod){
        a = (a%m + m)%m;
        if(!a) return 0;
        ll ret = (n*(n+1)/2)%mod;
        ret = (ret*a)%mod;
        ll g = __gcd(a,m);
        ret -= m*(calc(a/g,m/g,n,mod)-n-1);
        return (ret%mod + mod)%mod;
    }

    //P(i) = a + r*i mod m
    ll solve(ll a, ll r, ll n, ll m, ll mod){
        a = (a%m + m)%m;
        r = (r%m + m)%m;
        if(!r) return (a*(n+1))%mod;
        if(!a) return solve(r, n, m, mod);
        ll g, x, y;
        g = gcdExtended(r, m, x, y);
        x = (x%m + m)%m;
        ll d = a - (a/g)*g;
        a -= d;
        x = (x*(a/g))%m;
        return (solve(r, n+x, m, mod) - solve(r, x-1, m,
            mod) + mod + d*(n+1))%mod;
    }
};

```

Edge coloring CPP

```

const int MX = 300;
int C[MX][MX] = {}, G[MX][MX] = {};

void solve(vector<pii> &E, int N){
    int X[MX] = {}, a, b;

    auto update = [&](int u){ for(X[u] = 1; C[u][X[u]];
        X[u]++); };
    auto color = [&](int u, int v, int c){
        int p = G[u][v];
        G[u][v] = G[v][u] = c;
        C[u][c] = v; C[v][c] = u;
        C[u][p] = C[v][p] = 0;
        if( p ) X[u] = X[v] = p;
        else update(u), update(v);
        return p; };
    auto flip = [&](int u, int c1, int c2){
        int p = C[u][c1], q = C[u][c2];
        swap(C[u][c1], C[u][c2]);

```

```

        if( p ) G[u][p] = G[p][u] = c2;
        if( !C[u][c1] ) X[u] = c1;
        if( !C[u][c2] ) X[u] = c2;
        return p; };

```

```

for(int i = 1; i <= N; i++) X[i] = 1;
for(int t = 0; t < E.size(); t++){
    int u = E[t].first, v0 = E[t].second, v = v0, c0
        = X[u], c = c0, d;
    vector<pii> L;
    int vst[MX] = {};
    while(!G[u][v0]){
        L.emplace_back(v, d = X[v]);
        if(!C[v][c]) for(a = (int)L.size()-1; a >= 0;
            a--) c = color(u, L[a].first, c);
        else if(!C[u][d])for(a=(int)L.size()-1;a>=0;a
            --)color(u,L[a].first,L[a].second);
        else if( vst[d] ) break;
        else vst[d] = 1, v = C[u][d];
    }
    if( !G[u][v0] ){
        for(;v; v = flip(v, c, d), swap(c, d));
        if(C[u][c0]){
            for(a = (int)L.size()-2; a >= 0 && L[a].
                second != c; a--);
            for(; a >= 0; a--) color(u, L[a].first, L[
                a].second);
        } else t--;
    }
}
}

```

Burnside's Lemma

Let (G, \oplus) be a finite group that acts on a set X . It should hold that $e_g * x = x$ and $g_1 * (g_2 * x) = (g_1 \oplus g_2) * x, \forall x \in X, g_1, g_2 \in G$. For each $g \in G$ let $X^g = \{x \in X \mid g * x = x\}$. The number of orbits its given by:

$$|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$$

Wilson's Theorem

$(n-1)! \equiv -1 \pmod n \iff n$ is prime

Fibonacci

- $F_{n-1}F_{n+1} - F_n^2 = (-1)^n$
- $F_{n+k} = F_k F_{n+1} + F_{k-1} F_n$
- $GCD(F_n, F_m) = F_{GCD(n,m)}$
- $F_n = \frac{(\frac{1+\sqrt{5}}{2})^n - (\frac{1-\sqrt{5}}{2})^n}{\sqrt{5}}$

Lucas's Theorem

For non-negative integers m and n and a prime p , the following congruence holds:

$$\binom{m}{n} \equiv \prod_{i=0}^k \binom{m_i}{n_i} \pmod p$$

where m_i is the i -th digit of m in base p . $\binom{a}{b} = 0$ if $a < b$.

Kirchhoff's Theorem

Laplacian matrix is $L = D - A$, where D is a diagonal matrix with vertex degrees on the diagonals and A is adjacency matrix.

The number of spanning trees is any cofactor of L . i -th cofactor is determinant of the matrix gotten by removing i -th row and column of L .

Multigraphs

In $D[i][i]$ all loops are excluded. $A[i][j]$ = number of edges from i to j .

Directed multigraphs

$D[i][i]$ = indegree of i minus the number of loops at i . $A[i][j]$ = number of edges from i to j .

The number of oriented spanning trees rooted at a vertex i is the determinant of the matrix gotten by removing the i th row and column of L .

Matroid

Let X set of objects, $I \subseteq 2^X$ set of independent sets such that:

1. $\emptyset \in I$
2. $A \in I, B \subseteq A \implies B \in I$
3. Exchange axiom, $A \in I, B \in I, |B| > |A| \implies \exists x \in B \setminus A : A \cup \{x\} \in I$
4. $A \subseteq X$ and I and I' are maximal independent subsets of A then $|I| = |I'|$

Then (X, I) is a matroid. The combinatorial optimization problem associated with it is: Given a weight $w(e) \geq 0 \forall e \in X$, find an independent subset that has the largest possible total weight.

Matroid intersection

```
// Input two matroids (X, I_a) and (X, I_b)
// output set I of maximum size, I \in I_a and I \in I_b
set<> I;
while(1){
    for(e_i : X \ I)
        if(I + e_i \in I_a and I + e_i \in I_b)
            I = I + e_i;
    set<> A, T; queue<> Q;
    for(x : X) label[x] = MARK1;
    for(e_i : X \ I){
        if(I + e_i \in I_a)
            Q.push(e_i), label[e_i] = MARK2;
        else{
            for(x such that I - x + e_i \in I_a)
                A[x].push(e_i);
        }
        if(I + e_i \in I_b)
            T = T + {e_i}
        else{
            for(x such that I - x + e_i \in I_b)
                A[e_i].push(x);
        }
    }
    if(T.empty()) break;
```

```
bool found = false;
while(!Q.empty() and !found){
    auto e = Q.front(); Q.pop();
    for(x : A[e]) if(label[x] == MARK1){
        label[x] = e; Q.push(x);
        if(x \in T){
            found = true; put = 1;
            while(label[x] != MARK2){
                I = put ? (I + x) : (I - x);
                put = 1 - put;
            }
            I = I + x;
            break;
        }
    }
}
if(!found) break;
return I;
```

Where $\text{path}(e) = [e]$ if $\text{label}[e] = \text{MARK2}$, $\text{path}(\text{label}[e]) + [e]$ otherwise.

Matroid Union

Given k matroids over the same set of objects $(X, I_1), (X, I_2), \dots, (X, I_k)$ find $A_1 \in I_1, A_2 \in I_2, \dots, A_k \in I_k$ such that $i \neq j, A_i \cap A_j = \emptyset$ and $|\bigcup_{i=1}^k A_i|$ is maximum. Matroid union can be reduced to matroid intersection as follows.

Let $X' = X \times \{1, 2, \dots, k\}$, ie, k copies of each element of X with different colors. $M1 = (X', Q)$ where $B \in Q \iff \forall 1 \leq i \leq k, \{x \mid (x, i) \in B\} \in I_i$, ie, for each color, B is independent. $M2 = (X', W)$ where $B \in W \iff i \neq j \implies \neg((x, i) \in B \wedge (x, j) \in B)$, ie, each element is picked by at most one color.

Intersection of $M1$ and $M2$ is the answer for the combinatorial problem of matroid union.

Notes

When we repeat something and each time we have probability p to succeed then the expected number of tries is $\frac{1}{p}$, till we succeed.

Small to large

Trick in statement If k sets are given you should note that the amount of different set sizes is $O(\sqrt{s})$ where s is total size of those sets. And no more than \sqrt{s} sets have size greater than \sqrt{s} . For example, a path to the root in Aho-Corasick through suffix links will have at most $O(\sqrt{s})$ vertices.

gcd on subsegment, we have at most $\log(a_i)$ different values in $\{\text{gcd}(a_j, a_{j+1}, \dots, a_i) \text{ for } j < i\}$.

From static set to expandable. To insert, create a new set with the new element. While there are two sets with same size, merge them. There will be at most $\log(n)$ disjoint sets.

Matrix exponentiation optimization. Save binary power of $A_{n \times n}$ and answer q queries $b = A^m x$ in $O((n^3 + qn^2)\log(m))$.

Ternary search on integers into binary search, comparing $f(\text{mid})$ and $f(\text{mid}+1)$, binary search on derivative

Dynamic offline set For each element we will wind segment of time $[a, b]$ such that element is present in the set during this whole segment. Now we can come up with recursive procedure which handles $[l, r]$ time segment considering that all elements such that $[l, r] \subset [a, b]$ are already included into the set. Now, keeping this invariant we recursively go into $[l, m]$ and $[m+1, r]$ subsegments. Finally when we come into segment of length 1.

$$a > b \implies a \bmod b < \frac{a}{2}$$

Convex Hull. The expected number of points in the convex hull of a random set of points is $O(\log(n))$. The number of points in a convex hull with points coordinates limited by L is $O(L^{2/3})$.

Tree path query. Sometimes the linear query is fast enough. Just do adamant's hld sorting subtrees by their size and remap vertices indexes.

Range query offline can be solved by a sweep, ordering queries by R.