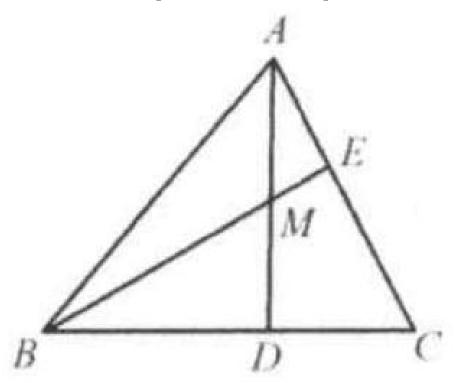
Problem 6

Problem

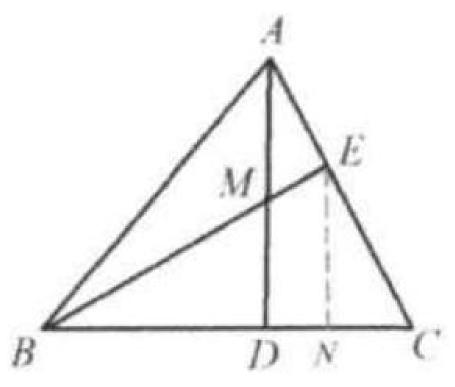
In triangle ABC, a point D is taken on AB and a point E is taken on AC such that BD:DC=3:2, and AE:EC=3:4.AD and BE intersect at M. Find the area of triangle AEM if the area of triangle ABC is 1.



Solution

Draw~EN//AD~to meet~BC~at~N. Since BD:DC=3:2 and AE:EC=3:4,NC:DN:BD=8:6:21. So <math display="inline">EM:MB=6:21=2:7.

We know that $\frac{S_{\triangle ABE}}{S_{\triangle ABC}} = \frac{3}{3+4} \Rightarrow S_{\triangle ABE} = \frac{3}{7}S_{\triangle ABC} = \frac{3}{7}$.



 $S_{\triangle AEM} = \frac{2}{9}S_{\triangle ABE} = \frac{2}{9} \times \frac{3}{7} = \frac{2}{21}$