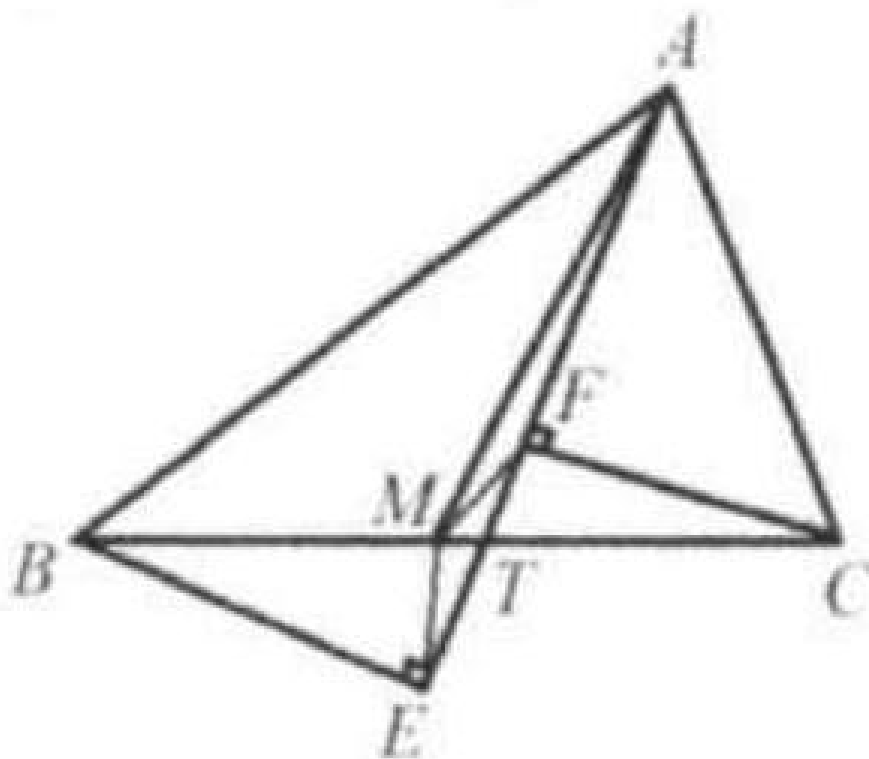


Problem 5

Problem

In $\triangle ABC$, AM is the median. AT is the angle bisector of $\angle A$. $BE \perp AT$ at T and $CF \perp AT$ at F . Show that $ME = MF$.



Solution

Method 1:

Extend CF to meet AB at C' .

Since AT is the angle bisector of $\angle A$, AF is the angle bisector of $\angle A$. AF is the perpendicular bisector of $C'C$ in $\triangle AC'C$, so $\triangle AC'F \cong \triangle ACF$, $CF = FC'$.

Extend CF to meet AB at C' .

Since F is the midpoint of CC' , M is the midpoint of BC , $MF = \frac{1}{2}BC$.

