## Problem 6

## Problem

(AMC) In  $\triangle ABC$ , we have AB=1 and AC=2. Side BC and the median from A to BC have the same length. What is BC?

- (A)  $\frac{1+\sqrt{2}}{2}$ (B)  $\frac{1+\sqrt{3}}{2}$ (C)  $\sqrt{2}$ (D)  $\frac{3}{2}$

- (E)  $\sqrt{3}$

## Solution

(C).

By the median length formula:

$$(AD^{2} + DC^{2}) + (AD^{2} + BD^{2}) = AB^{2} + AC^{2}$$
$$(2m)^{2} + m^{2} + (2m)^{2} + m^{2} = 1^{2} + 2^{2}$$
$$10m^{2} = 5 \Rightarrow m^{2} = \frac{1}{2} \Rightarrow m = \frac{\sqrt{2}}{2}$$
$$BC = 2m = 2 \times \frac{\sqrt{2}}{2} = \sqrt{2}.$$

