## Example 8

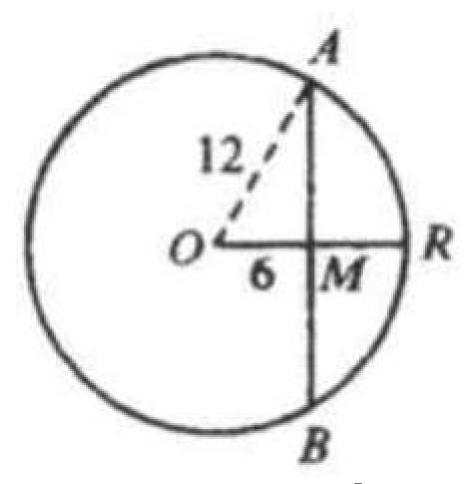
(AMC) A chord which is the perpendicular bisector of radius of length 12 in a circle, has length

- (A)  $3\sqrt{3}$
- (B) 27
- $(C) 6\sqrt{3}$
- (D)  $12\sqrt{3}$
- (E) none of these

Solution: (D).

Let O denote the center of the circle, and let OR and AB be the radius and the chord which are perpendicular bisectors of each other at M . Applying the

Pythagorean theorem to right triangle OMA yields  $(AM)^2 = (OA)^2 - (OM)^2 = 12^2 - 6^2 = 108, AM = 6\sqrt{3}.$ 



Thus the required chord has length  $12\sqrt{3}$ .