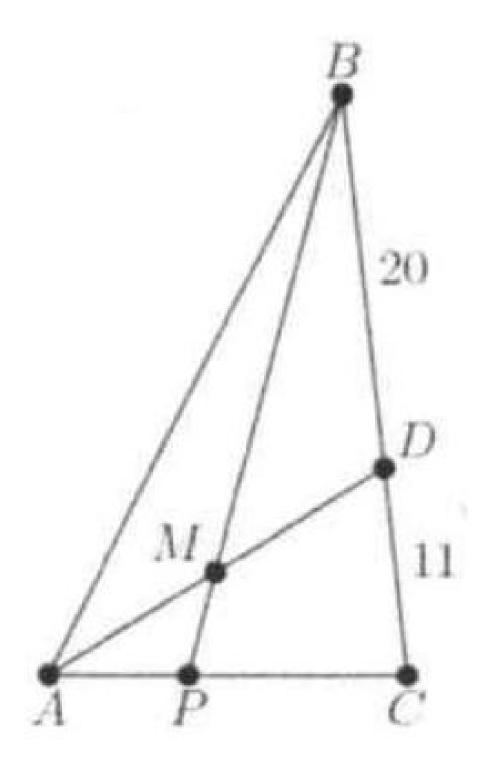
Problem

(2011 AIME II) In triangle ABC, $AB = \frac{20}{11}AC$. The angle bisector of $\angle A$ intersects BC at point D, and point M is the midpoint of AD. Let P be the point of the intersection of AC and BM. The ratio of CP to PA can be expressed in the form $\frac{m}{n}$, where m and n are relatively prime positive integers. Find m+n.



Solution

51. Through D draw a parallel to line BP intersecting line AC at Q. Then PQ=20k, QC=11k, and PA=20k, using the Angle Bisector Theorem and the fact that 3 or more parallel lines divide all transversals in the same proportions. Thus $\frac{CP}{PA}=\frac{20K+11K}{20K}=\frac{31}{20}.$ m+n=31+20=51.

