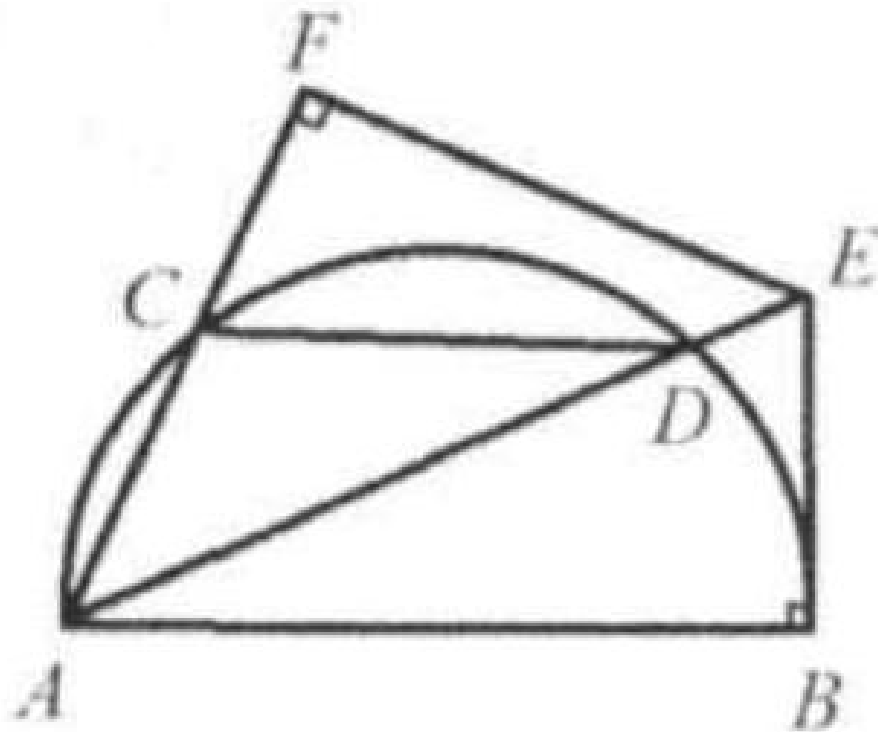


Problem

As shown in the figure, AB is the diameter of a semicircle and CD is a chord parallel to AB . Connect AD and extend it to meet BE of the perpendicular of AB at E . Draw $EF \perp AC$ and meets the extension of AC at F , F is the foot of perpendicular. Show that $AC = CF$.



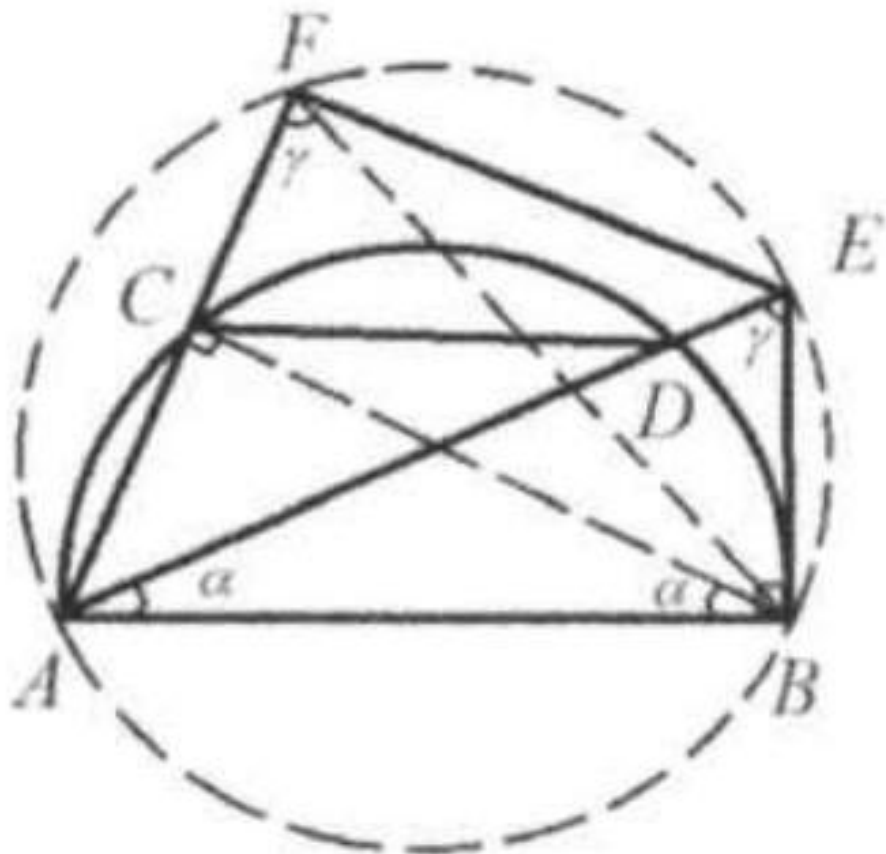
Solution

Since $\angle F = \angle B = 90^\circ$, points A, B, E , and F are concyclic.

$$\angle AFB = \angle AEB = \gamma.$$

Since $CD \parallel AB$, arcs $AC = BD$, $\angle DAB = \angle CBA = \alpha$.

In Rt $\triangle ABE$, $\alpha + \gamma = 90^\circ$.



In Rt $\triangle BCF$, $\angle FBC + \gamma = 90^\circ$. So $\angle FBC = \alpha$. BC is the perpendicular bisector of AF in $\triangle BAF$. So $AC = CF$.