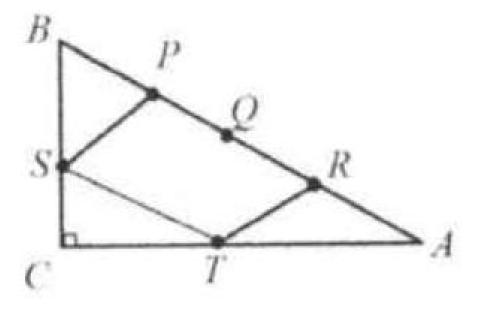
Problem 1

Problem

(Phillips Academy Prize Exam) In right triangle ABC, angle C is the right angle. P,Q and R are points which divide AB into four equal parts. S and Tare the midpoint of BC and AC, respectively. AB equals 24 inches. Find the perimeter of PRST.

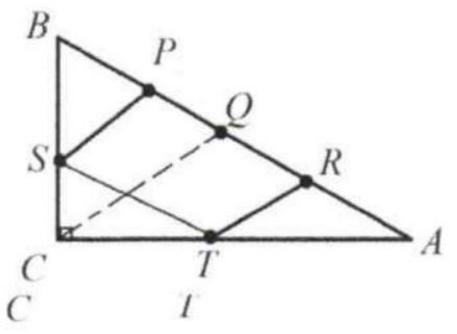


Solution

36.

Draw median CQ. Since the median to the hypotenuse of a right triangle is

half the hypotenuse,
$$CQ = \frac{1}{2}AB = \frac{24}{2} = 12.$$
 Since SP, RT , and ST are midlines,
$$SP = \frac{1}{2}CQ = \frac{12}{2} = 6 = RT \text{ and } ST = \frac{1}{2}AB = \frac{24}{2} = 12.$$



The perimeter of PRST is 36 .