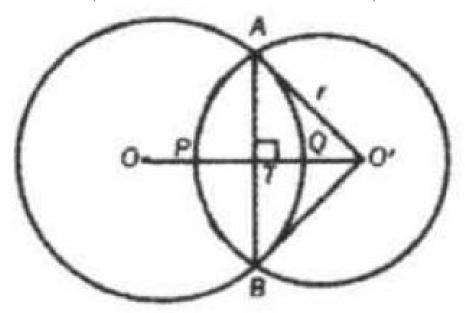
## Problem

Two circles intersect in A and B, and the measure of the common chord AB=10. The line joining the centers cuts the circles in P and Q. If PQ=3 and the measure of the radius of one circle is 13, find the radius of the other circle. (Note that the illustration is not drawn to scale.)



## Solution

 $\frac{41}{8}$ .

Since O'A = O'B and OA = OB, OO' is the perpendicular bisector of AB. Therefore, in right  $\triangle ATO$ , since AO = 13 and AT = 5, we find OT = 12. Since OQ = 13 (also a radius of circle O), and OT = 12, TQ = 1. We Know that PQ = 3. PT = PQ - TQ; therefore, PT = 2. Let O'A = O'P = r, and PT = 2, TO' = r - 2.

Applying the Pythagorean Theorem in tight  $\triangle ATO'$ ,  $(AT)^2 + (TO)^2 = (AO)^2$ . Substituting,  $5^2 + (r-2)^2 = r^2$ , and  $r = \frac{29}{4}$ . PT = PQ + TQ; therefore, PT = 4.

Again, let O'A = O'P = r then TO' = r - 4. Applying the Pythagorean Theorem in right  $\triangle ATO'$ ,  $(AT)^2 + (TO)^2 = (AO)^2$ . Substituting,  $5^2 + (r - 4)^2 = r^2$ , and  $r = \frac{41}{8}$ .

