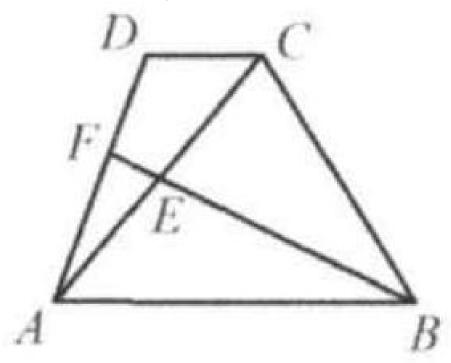
Problem

In trapezoid ABCD, AB = 3CD and AB//CD. E is the midpoint of the diagonal AC. BE meets AD at F. Find the value of AF : FD.

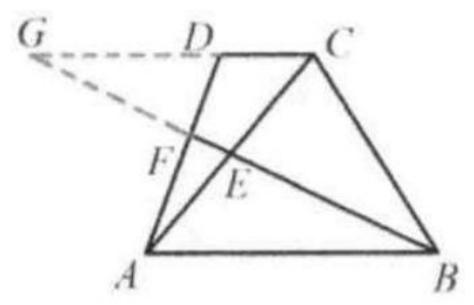
- (A) $\frac{5}{3}$ (B) $\frac{3}{2}$ (C) $\frac{10}{7}$ (D) (E) $\frac{12}{5}$.



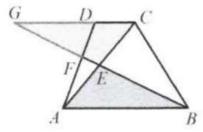
Solution

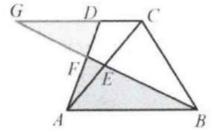
(B). Method 1:

Extend CD and BF to meet at G. Since $CG//AB, \triangle ABE \sim \triangle CGE$. So



$$\begin{array}{l} \frac{CG}{AB} = \frac{CE}{AE} = 1 \Rightarrow CG = AB \Rightarrow \\ GD + CD = 3CD \Rightarrow GD = 2CD \\ \text{Since } DG//AB, \triangle ABF \sim \triangle DGE. \end{array}$$

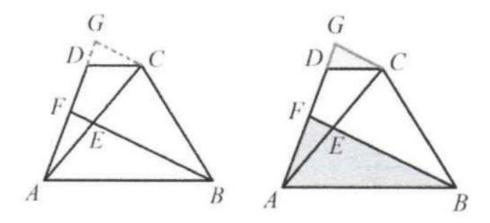




$$\frac{AF}{FD} = \frac{AB}{DG} \Rightarrow \frac{AF}{FD} = \frac{3CD}{2CD} = \frac{3}{2}.$$
Method 2:

Draw CG//BF to meet the extension of AD at G. Since AB//CD, CG//BF,

$$\triangle ABF \sim \triangle DCG$$
. So $\frac{AF}{DG} = \frac{AB}{CD} = 3$
 $\Rightarrow AF = 3DG$.



Since CG//EF, AE=EC, AF=FG. Therefore FD=2DG, $\frac{AF}{FD}=\frac{3}{2}$.