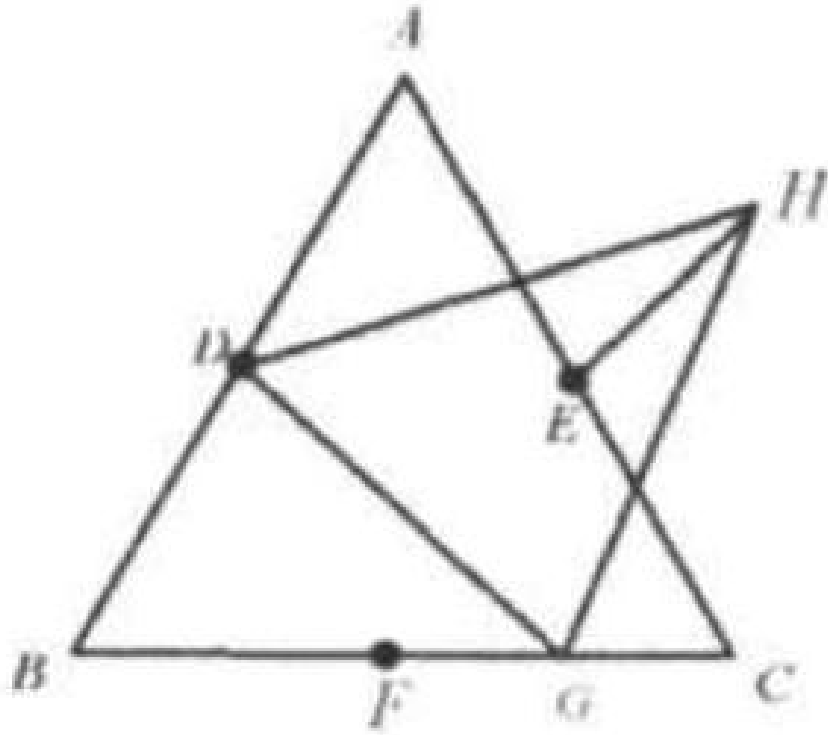


Problem

In equilateral $\triangle ABC$, points D, E, F are the midpoints of AB, AC, BC , respectively. G is a point of FC . Show that $FG = EH$ if $\triangle DGH$ is an equilateral triangle as well.



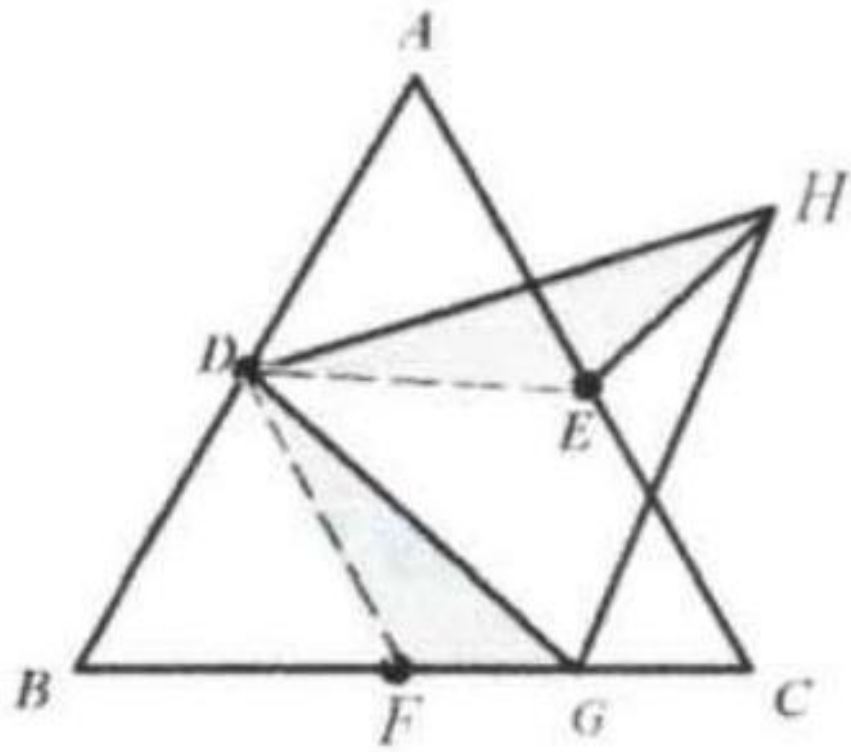
Solution

Connect DE, DF .

Since $\triangle ABC$ is an equilateral triangle, $DE = \frac{1}{2}BC = \frac{1}{2}AC = DF$.

$DE \parallel BC, DF \parallel AC$.

$\angle EDF = \angle ACB = 60^\circ$.



Since $\triangle DGH$ is an equilateral triangle, $DH = DG$, $\angle HDG = 60^\circ$.
 Thus $\angle FDG = 60^\circ - \angle GDE = \angle EDH$.
 So $\triangle FDG \cong \triangle EDH$. $FG = EH$.