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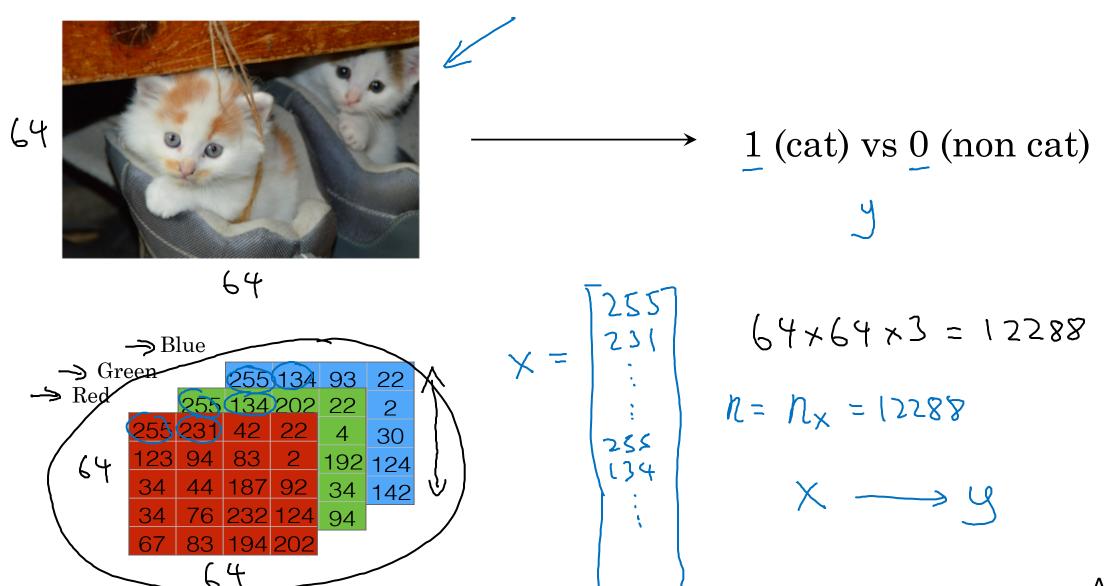
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Basics of Neural Network Programming

Binary Classification

Binary Classification



Andrew Ng

Notation

$$(x,y) \times \mathbb{CR}^{n_{x}}, y \in \{0,1\}$$

$$m \text{ training evarples}: \{(x^{(1)},y^{(1)}), (x^{(1)},y^{(2)}), \dots, (x^{(m)},y^{(m)})\}$$

$$M = M \text{ train} \qquad M \text{ test} = \text{ $\#$ test examples}.$$

$$X = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X = \begin{bmatrix} x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ x^{(m)} & x^{(m)} & \dots & x^{(m)} \end{bmatrix}$$

$$X \in \mathbb{R}^{n_{x} \times m}$$



Basics of Neural Network Programming

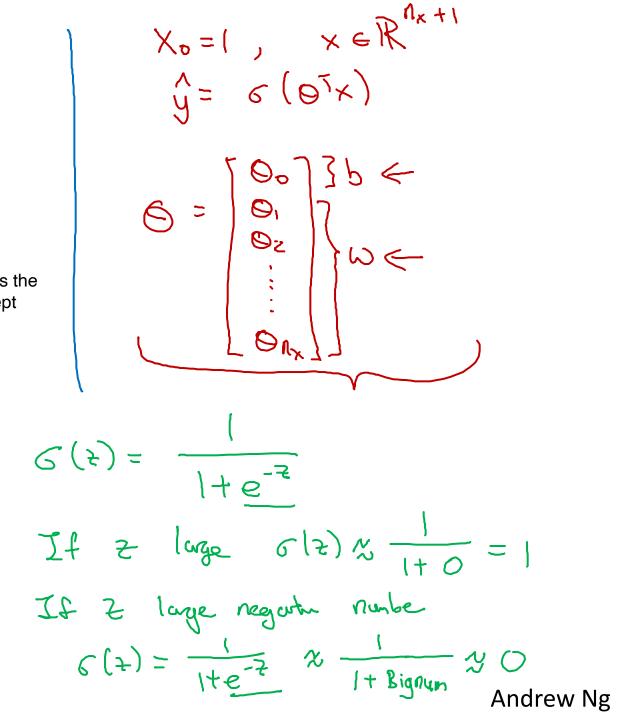
Logistic Regression

Logistic Regression

Given
$$\times$$
, want $\hat{y} = P(y=1|x)$
 $\times \in \mathbb{R}^{n_{\times}}$

$$\times \in \mathbb{R}^{n_{\times}}$$
Parameters: $\omega \in \mathbb{R}^{n_{\times}}$, $\omega \in \mathbb{R}$, where $\omega \in \mathbb{R}$ where $\omega \in \mathbb{R}$ interconstant $\omega \in \mathbb{R}$ and $\omega \in \mathbb{R}$ where $\omega \in \mathbb{R}$ interconstant $\omega \in \mathbb{R}$ and $\omega \in \mathbb{R}$ in $\omega \in \mathbb{R}$ in $\omega \in \mathbb{R}$ and $\omega \in \mathbb{R}$ in $\omega \in \mathbb{R}$

Logistic regression utilises the sigmoid function to fulfill probability bounds





Basics of Neural Network Programming

Logistic Regression cost function

Logistic Regression cost function

Given
$$\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$$
, want $\hat{y}^{(i)} \approx y^{(i)}$.

Loss (error) function:
$$\int_{a}^{b} (\hat{y}, y) = \frac{1}{2} (\hat{y},$$

training observations m

Andrew Ng



Basics of Neural Network Programming

Gradient Descent

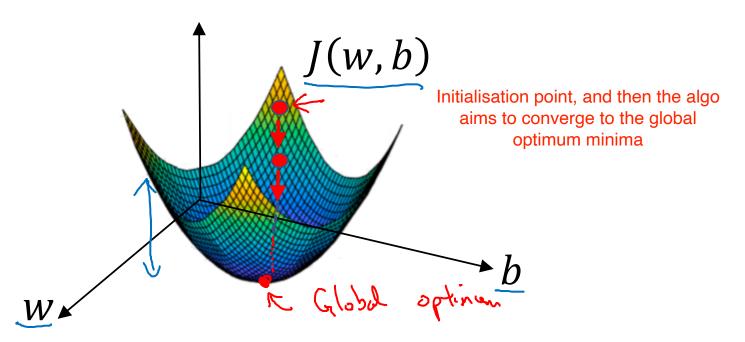
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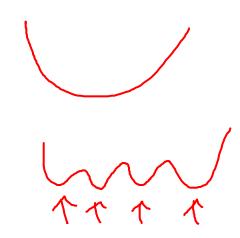
Gradient Descent

Recap:
$$\hat{y} = \sigma(w^T x + b)$$
, $\sigma(z) = \frac{1}{1 + e^{-z}}$

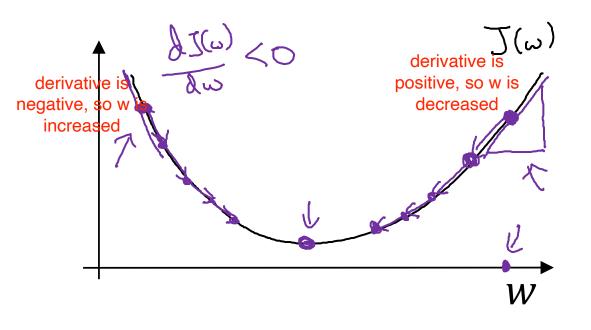
$$\underline{J(w,b)} = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = -\frac{1}{m} \sum_{i=1}^{m} y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

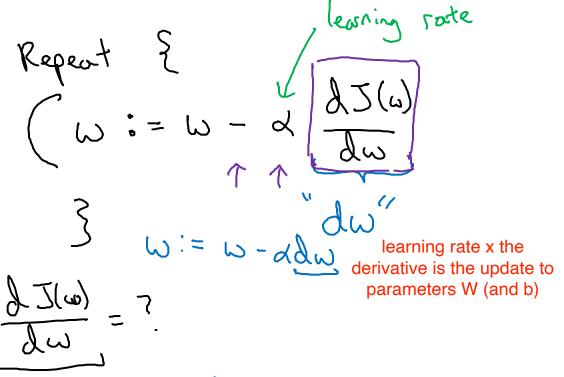
Want to find w, b that minimize J(w, b)

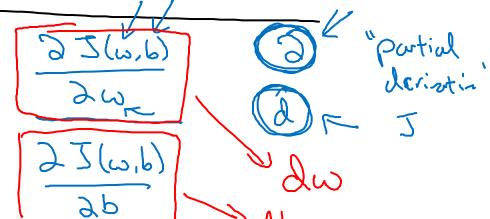




Gradient Descent





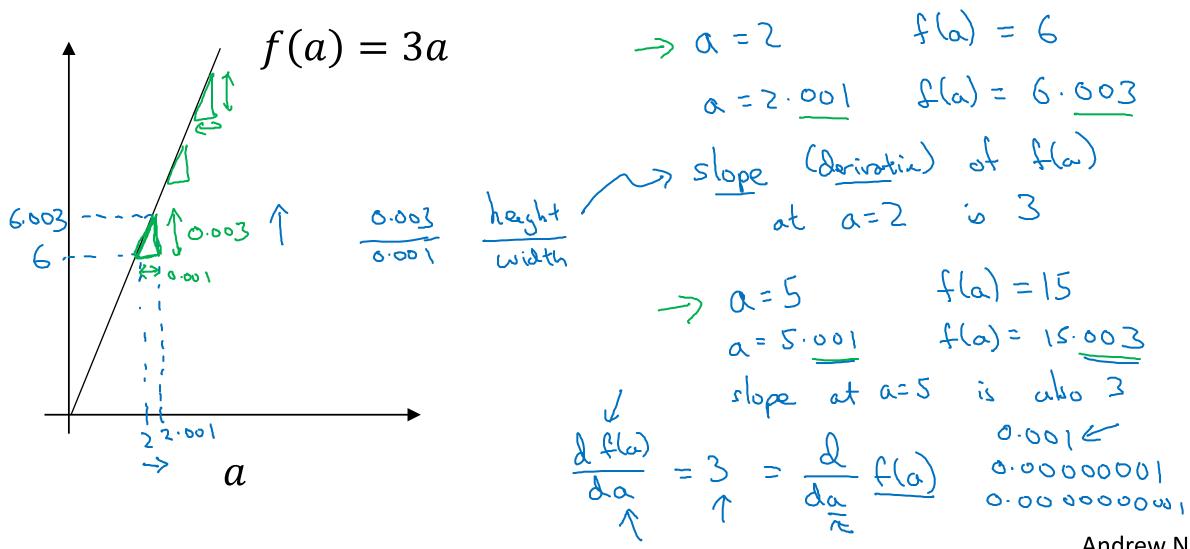




Basics of Neural Network Programming

Derivatives

Intuition about derivatives



Andrew Ng



Basics of Neural Network Programming

More derivatives examples

Intuition about derivatives







More derivative examples

$$f(a) = a^2$$

$$f(\omega) = \alpha^3$$

$$\frac{\lambda}{\lambda a} (a) = 3a^{2}$$
 $3x2^{3} = 12$

$$\sigma = 5.001$$
 $t(r) = 8$

$$Q = 5.001 \quad \text{fm} \approx 0.64312$$

$$Q = 5.001 \quad \text{fm} \approx 0.64362$$



Basics of Neural Network Programming

Computation Graph

Computation Graph

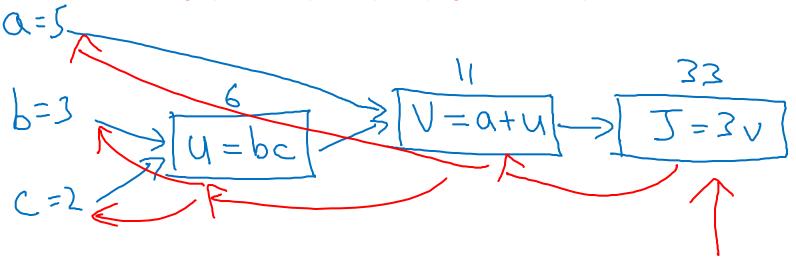
$$J(a,b,c) = 3(a+bc) = 3(5+3x^2) = 33$$

$$U = bc$$

$$V = atu$$

$$T = 3v$$

left to right pass to compute outputs (J), right to left to compute the derivatives



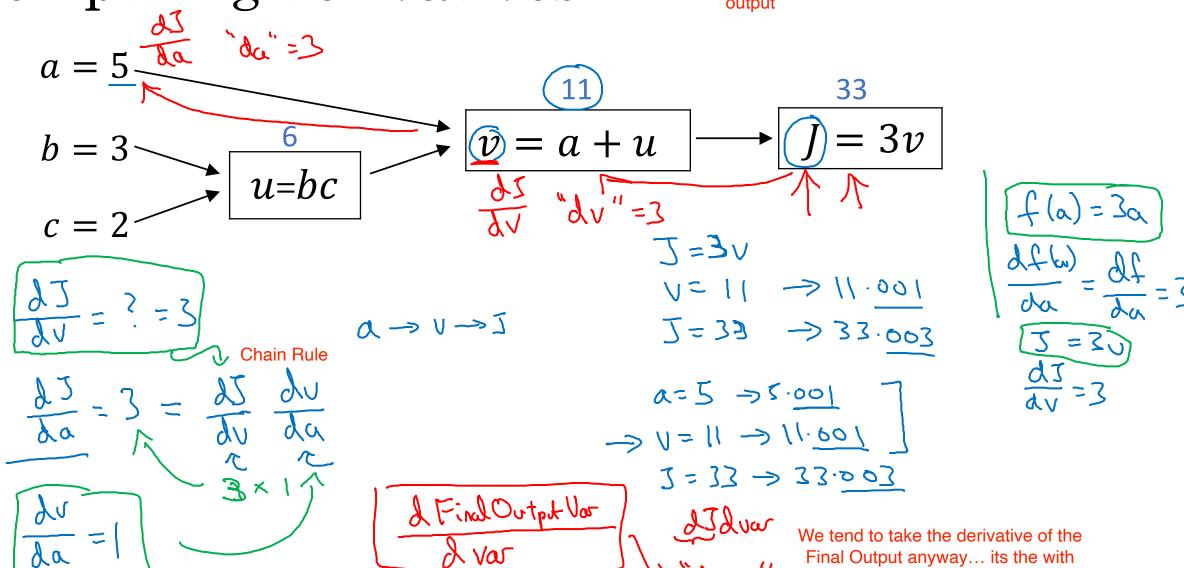


Basics of Neural Network Programming

Derivatives with a Computation Graph

Computing derivatives

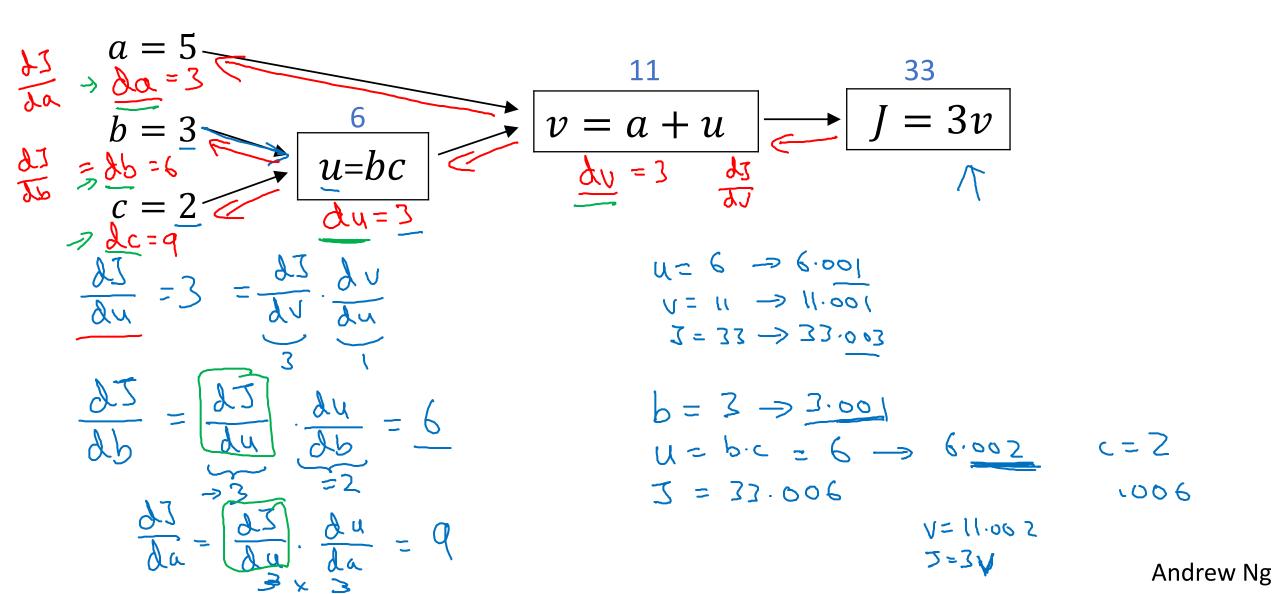
Back propogation to identify derivatives, by breaking down the impact of the net change of a value and how it affects the output



Andrew Ng

respect to what that changes

Computing derivatives





Basics of Neural Network Programming

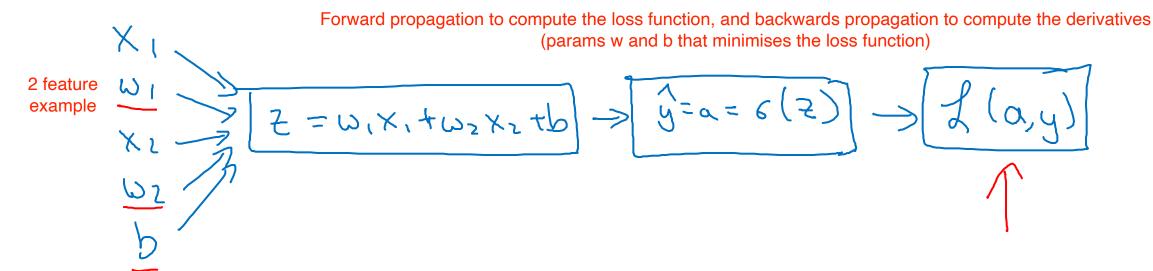
Logistic Regression Gradient descent

Logistic regression recap

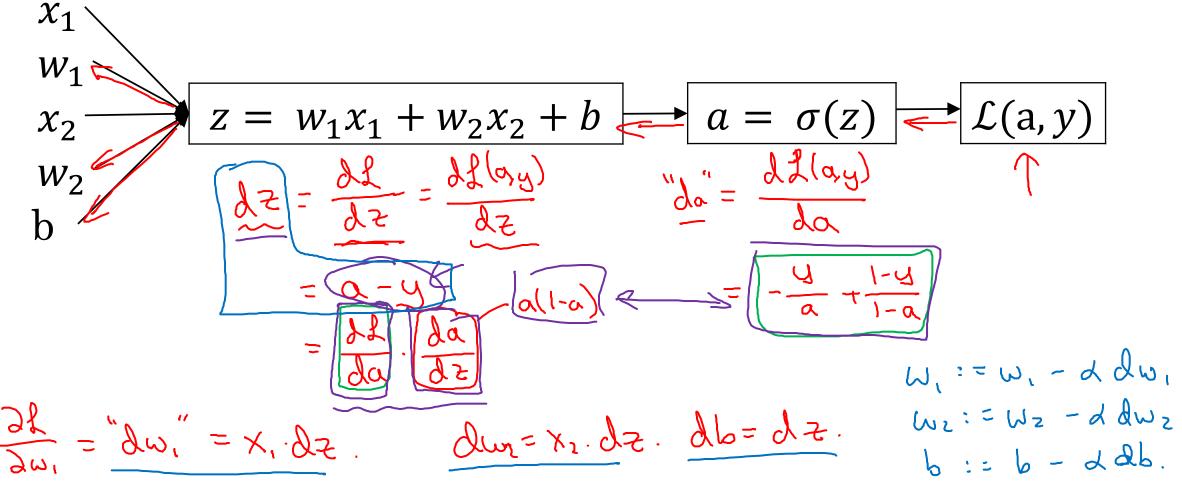
$$\Rightarrow z = w^T x + b$$

$$\Rightarrow \hat{y} = a = \sigma(z)$$

$$\Rightarrow \mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$$



Logistic regression derivatives



The final goal of back propagation - calculate how much we need to change the params w and b.

The params then get updated by this calculated change (derivatives)N



Basics of Neural Network Programming

Gradient descent on m examples

Logistic regression on m examples

$$\frac{J(\omega,b)}{J(\omega,b)} = \frac{1}{m} \sum_{i=1}^{m} \chi(\alpha^{(i)}, y^{(i)}) \\
= \chi(\alpha^{(i)},$$

Now we expand the calculation from 1 example to across the entire training set (Cost function)

$$\frac{\partial}{\partial \omega_{i}} \mathcal{I}(\omega, b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} \mathcal{I}(a^{(i)}, y^{(i)})$$

$$\frac{\partial}{\partial \omega_{i}} \mathcal{I}(\omega, b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial \omega_{i}} \mathcal{I}(a^{(i)}, y^{(i)})$$

Logistic regression on m examples

$$J=0$$
; $d\omega_{i}=0$; $d\omega_{z}=0$; $db=0$
 $Z^{(i)}=\omega^{T}x^{(i)}+b$
 $a^{(i)}=6(z^{(i)})$
 $J+=-[y^{(i)}(\log a^{(i)}+(1-y^{(i)})\log(1-a^{(i)})]$
 $dz^{(i)}=a^{(i)}-y^{(i)}$
 $d\omega_{z}+=x^{(i)}dz^{(i)}$
 $d\omega_{z}+=x^{(i)}dz^{(i)}$
 $d\omega_{z}+=dz^{(i)}$
 $d\omega_{z}+=dz^{(i)}$
 $d\omega_{z}+=dz^{(i)}$
 $d\omega_{z}+=m$; $d\omega_{z}/=m$; $d\omega_{z}/=m$. $d\omega_{z}/=m$. $d\omega_{z}/=m$.

$$d\omega_1 = \frac{\partial J}{\partial \omega}$$

Vectorization

instead of For loops, for more efficiency and speed



Basics of Neural Network Programming

Vectorization

What is vectorization?

for i in ray
$$(n-x)$$
:
 $2+= \omega [1] + x [1]$



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More vectorization examples

Neural network programming guideline

Whenever possible, avoid explicit for-loops.

$$U = AV$$

$$U_{i} = \sum_{i} \sum_{j} A_{ij} V_{ij}$$

$$U = np. zevos((n, i))$$

$$for i \dots \subseteq ACIT_{i} \exists *vC_{i} \exists$$

$$uCi \exists t = ACIT_{i} \exists *vC_{i} \exists$$

Vectors and matrix valued functions

Say you need to apply the exponential operation on every element of a matrix/vector.

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow \mathbf{u} = \begin{bmatrix} \mathbf{e}^{\mathbf{v}_1} \\ \mathbf{e}^{\mathbf{v}_2} \end{bmatrix}$$

$$v = \begin{bmatrix} v_1 \\ \vdots \\ v_n \end{bmatrix} \rightarrow u = \begin{bmatrix} e^{v_1} \\ e^{v_n} \end{bmatrix}$$

$$u = np \cdot exp(v) \leftarrow 1$$

$$np \cdot log(v)$$

$$np \cdot abs(v)$$

$$np \cdot abs(v)$$

$$np \cdot haximum(v, 0)$$

$$np \cdot haximum(v, 0)$$

$$v \neq v = [v_1] + [v_1] + [v_2] + [v_2] + [v_3] + [v_3] + [v_4] + [v_4] + [v_5] + [v_5]$$

Logistic regression derivatives

$$J = 0, \quad dw1 = 0, \quad dw2 = 0, \quad db = 0$$

$$\Rightarrow \text{ for } i = 1 \text{ to } n:$$

$$z^{(i)} = w^{T}x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J + = -[y^{(i)}\log\hat{y}^{(i)} + (1 - y^{(i)})\log(1 - \hat{y}^{(i)})]$$

$$dz^{(i)} = a^{(i)}(1 - a^{(i)})$$

$$dw_{1} + x_{1}^{(i)}dz^{(i)}$$

$$dw_{2} + x_{2}^{(i)}dz^{(i)}$$

$$db + dz^{(i)}$$

$$J = J/m, \quad dw_{1} = dw_{1}/m, \quad dw_{2} = dw_{2}/m, \quad db = db/m$$

$$d\omega / = m$$



Basics of Neural Network Programming

Vectorizing Logistic Regression

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Vectorizing Logistic Regression

$$Z^{(1)} = w^{T}x^{(1)} + b$$

$$Z^{(2)} = w^{T}x^{(2)} + b$$

$$Z^{(3)} = w^{T}x^{(3)} + b$$

$$Z^{(3)} = \sigma(z^{(3)})$$

$$Z^$$



Basics of Neural Network Programming

Vectorizing Logistic Regression's Gradient Computation

Vectorizing Logistic Regression

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = a^{(2)} - y^{(2)}$$

$$\frac{dz^{(1)} = a^{(1)} - y^{(1)}}{dz^{(2)}} = a^{(2)} - y^{(2)}$$

$$A = [a^{(1)} - a^{(1)}] \quad Y = [y^{(1)} - y^{(2)}]$$

$$A = [a^{(1)} - a^{(1)}] \quad Y = [y^{(1)} - y^{(2)}]$$

$$A = [a^{(1)} - y^{(1)}] \quad a^{(2)} - y^{(2)}$$

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$$A = [a^{(1)} - y^{(1)}] \quad a^{(1)} - y^{(1)}$$

$$A = [a^{(1)} - y^{(1)}] \quad a$$

$$db = \frac{1}{m} \sum_{i=1}^{n} dz^{(i)}$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

$$= \frac{1}{m} \left[x^{(i)} + \dots + x^{(n)} dz^{(m)} \right]$$

Implementing Logistic Regression

J = 0,
$$dw_1 = 0$$
, $dw_2 = 0$, $db = 0$

for i = 1 to m:

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)}) \checkmark$$

$$J += -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$$

$$dz^{(i)} = a^{(i)} - y^{(i)} \checkmark$$

$$dw_1 += x_1^{(i)} dz^{(i)}$$

$$dw_2 += x_2^{(i)} dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_1 += dz^{(i)}$$

$$dw_2 += dz^{(i)}$$

$$dw_3 += dz^{(i)}$$

$$dw_4 += dz^{(i)}$$

$$dw_4 += dz^{(i)}$$

$$dw_5 += dz^{(i)}$$

$$dw_6 += dz^{(i)}$$

$$dw_7 += dw_7 / m$$

$$dw_8 == dw_8 / m$$

iter in range (1000)!
$$\angle$$

$$Z = \omega^{T} X + b$$

$$= n p \cdot dot (\omega \cdot T \cdot X) + b$$

$$A = \epsilon (Z)$$

$$A = \epsilon (Z)$$

$$A = \Delta - Y$$

$$A$$



Basics of Neural Network Programming

Broadcasting in Python

Broadcasting example

Calories from Carbs, Proteins, Fats in 100g of different foods:

Apples Beef Eggs Potatoes

Carb
$$56.0$$
 0.0 4.4 68.0

Protein 1.2 104.0 52.0 8.0

Fat 1.8 135.0 99.0 0.9 (3,4)

Squal Section from Cab, Poten, Fort. Can you do the arphint for-loop?

Cal = A.sum(axis = 0)

percentage = $100*A/(cal Abstrace(1.6))$

Broadcasting example

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} + \begin{bmatrix} 100 \\ 100 \\ 100 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 200 & 300 \\ 100 & 200 & 300 \end{bmatrix}$$

$$(m,n) \quad (2,3)$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 100 & 100 & 100 \\ 200 & 200 \end{bmatrix} = \begin{bmatrix} (m,n) & 2 & 100 \\ (m,n) & 2 & 100 \end{bmatrix}$$

General Principle

$$(m, n)$$
 $\frac{t}{x}$ (n, i) m (m, n) $($

Mathab/Octave: bsxfun



Basics of Neural Network Programming

Explanation of logistic regression cost function (Optional)

Logistic regression cost function

Logistic regression cost function

If
$$y = 1$$
: $p(y|x) = \hat{y}$

If $y = 0$: $p(y|x) = 1 - \hat{y}$

$$p(y|x) = \hat{y} \cdot (1 - \hat{y})$$

Cost on *m* examples

log
$$p(lolods)$$
 in troops set) = log $\prod_{i=1}^{m} p(y^{(i)}|\chi^{(i)})$

log $p(----) = \sum_{i=1}^{m} log p(y^{(i)}|\chi^{(i)})$

Movimum likelihood setiment

$$- \chi(y^{(i)}, y^{(i)})$$

$$= -\sum_{i=1}^{m} \chi(y^{(i)}, y^{(i)})$$

(ost: $J(w, b) = \frac{1}{m} \sum_{i=1}^{m} \chi(y^{(i)}, y^{(i)})$

(minimize)