

Josephus Algorithm



The problem

According to the legend, during **the Great Jewish Revolt against the Romans**, a group of **40 Jewish soldiers** found themselves trapped in **a cave**.

Instead of surrendering to the Romans, they decided to **commit suicide**, forming a **circle** and killing each other **every third man** until all were dead.

The mathematical problem :

If there are n people numbered from 1 to n in a group, and every k -th person is eliminated in a circle,

what person will be the last one **remaining alive?**

A
I
g
O
r
i
t
h
m

Let Qc a circular Queue

Let len(Qc) = n

Let r the distance to choose a player that will die

(Note: In common or popular J.A , r=1)

from i=1 to i<= len (Qc) ; i++

 | enqueue (Qc,i)

Let x=s where s is the start index Pi starts J.A

P = x - 1

while len(Qc)>1 :

 | u = P + r % len(Qc)

 | if u==P then

 | u = u+1

 | P = u % len (Qc)

 | Dequeue (Qc)

 | P = u % len(Qc)

A
I
g
O
r
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o

Sea Qc una cola circular.

Sea $\text{len}(Qc) = n$.

Sea r la distancia para elegir un jugador que morirá.

(Nota: En el común o popular J.A, $r=1$).

desde $i=1$ hasta $i \leq \text{len}(Qc)$; $i++$

 encolar(Qc, i)

Sea $x=s$ donde s es el índice de inicio donde P_i comienza el J.A

$P = x - 1$

mientras $\text{len}(Qc) > 1$:

$u = P + r \% \text{len}(Qc)$

 si $u == P$ entonces

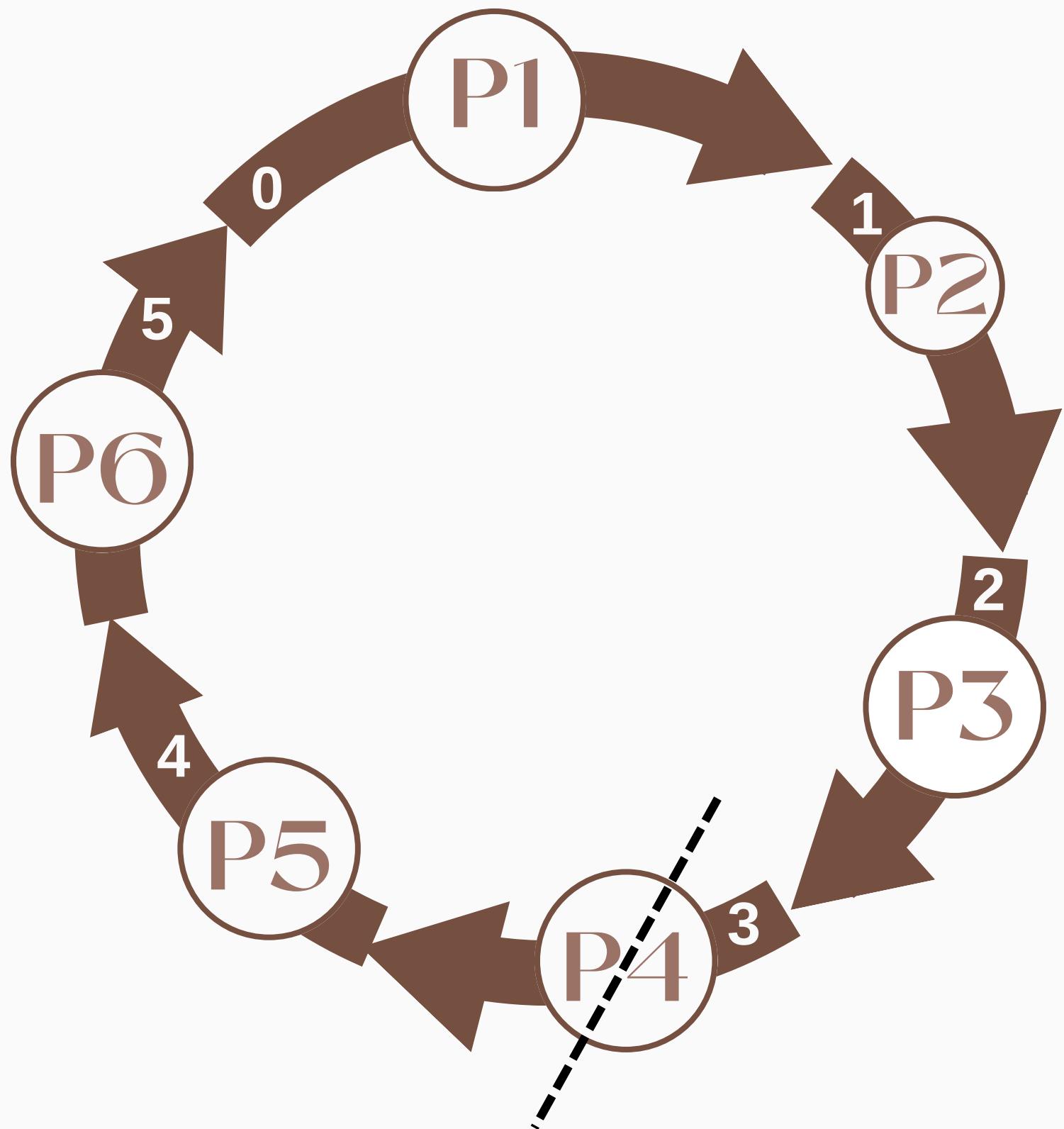
$u = u + 1$

$P = u \% \text{len}(Qc)$

 desencolar(Qc)

$P = u \% \text{len}(Qc)$

1.



Let $r = 3$

start P1

$P = 0$

$u = 0 + 3 \% 6 = 3$

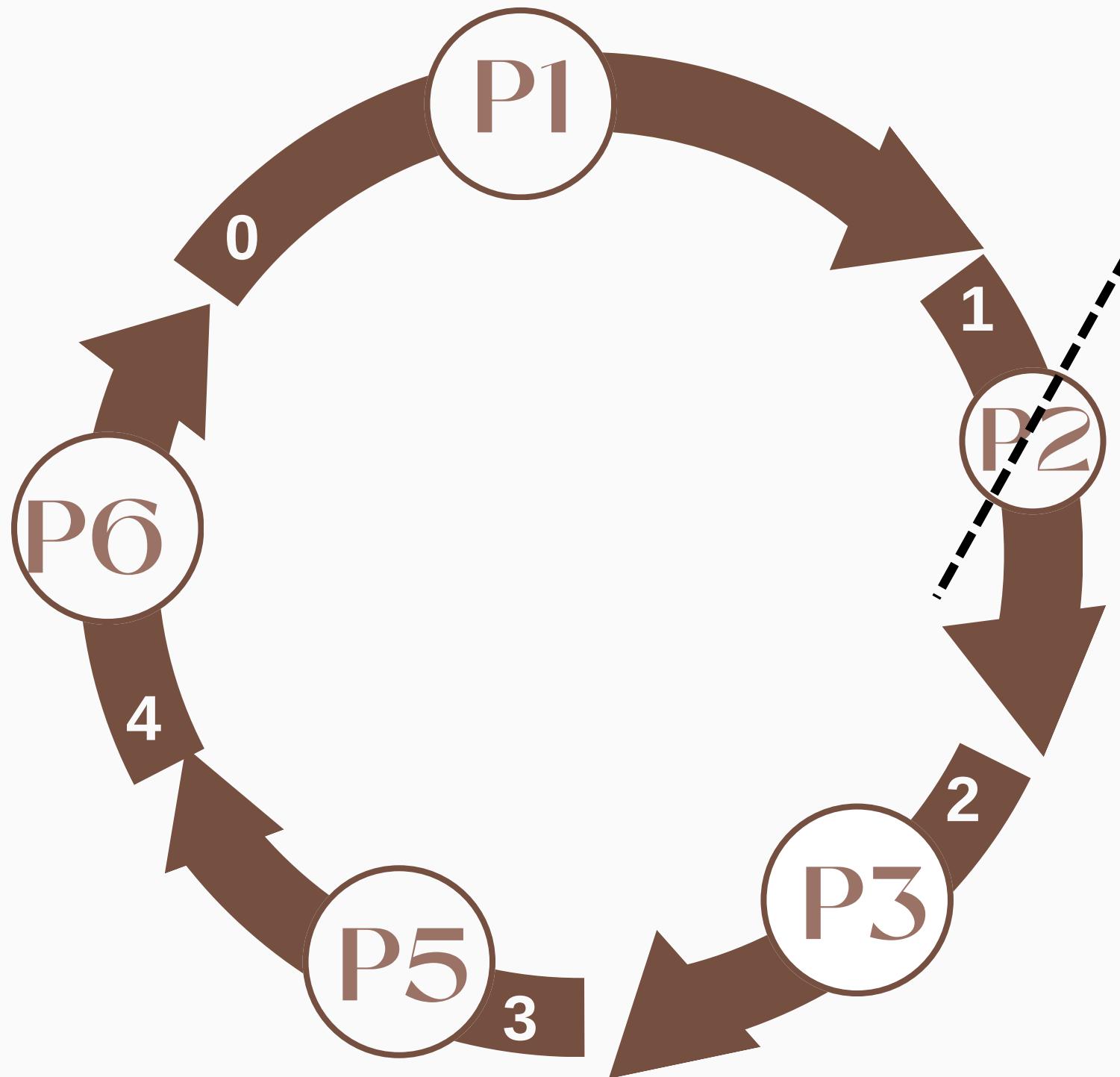
$3 == 0 ? \text{ No}$

$P = 3 \% 6 = 3$

Dequeue

$P = 3 \% 5 = 3$

2.



$$P = 3$$

$$u = 3 + 3 \% 5 =$$

$$6 \% 5 = 1$$

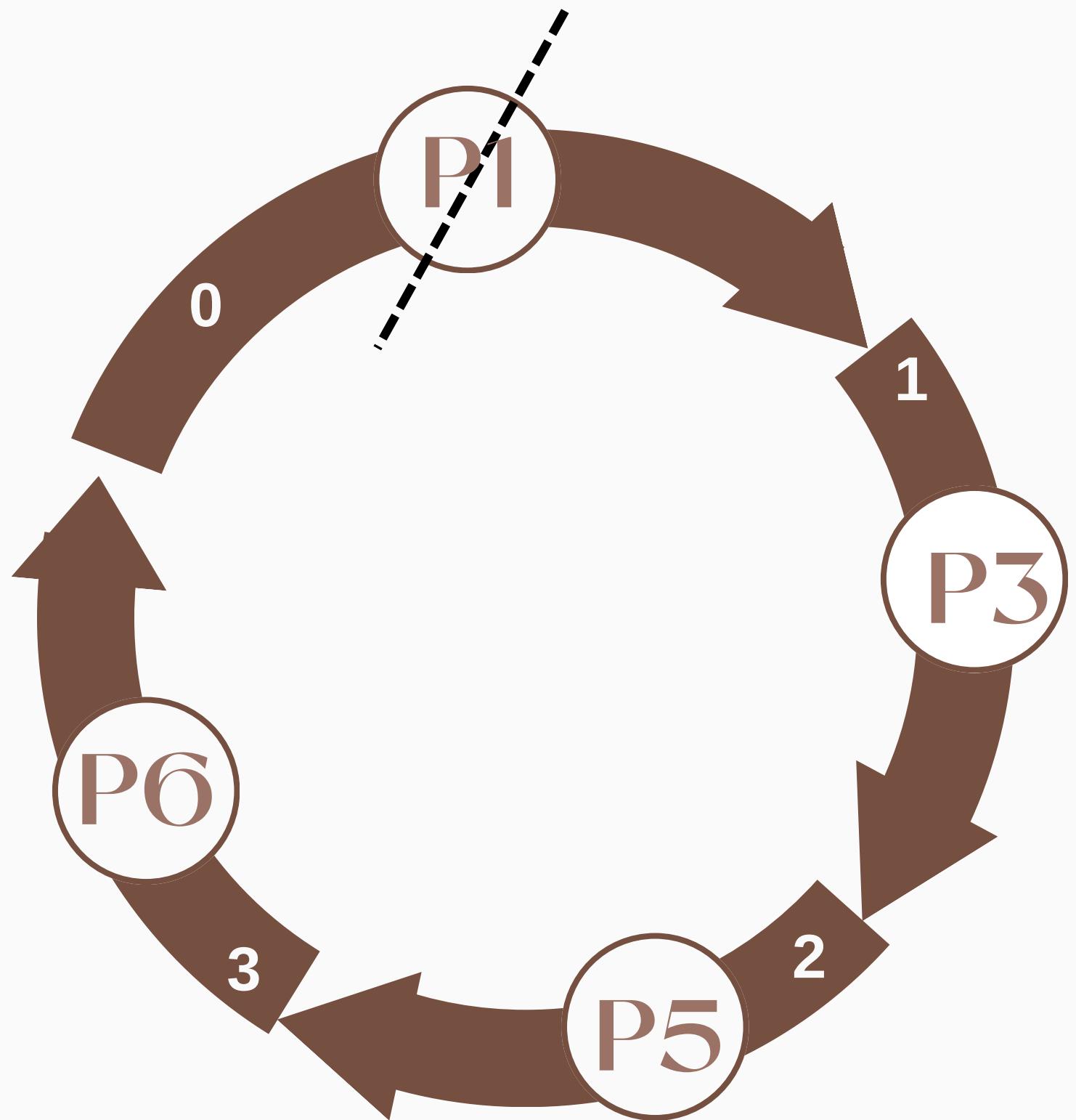
$1 == 3$? No

Dequeue

$$P = 1 \% 5 = 1$$

$$P = 1 \% 4 = 1$$

3.



$$P = 1$$

$$u = 1 + 3 \% 4 = 4 \% 4 = 0$$

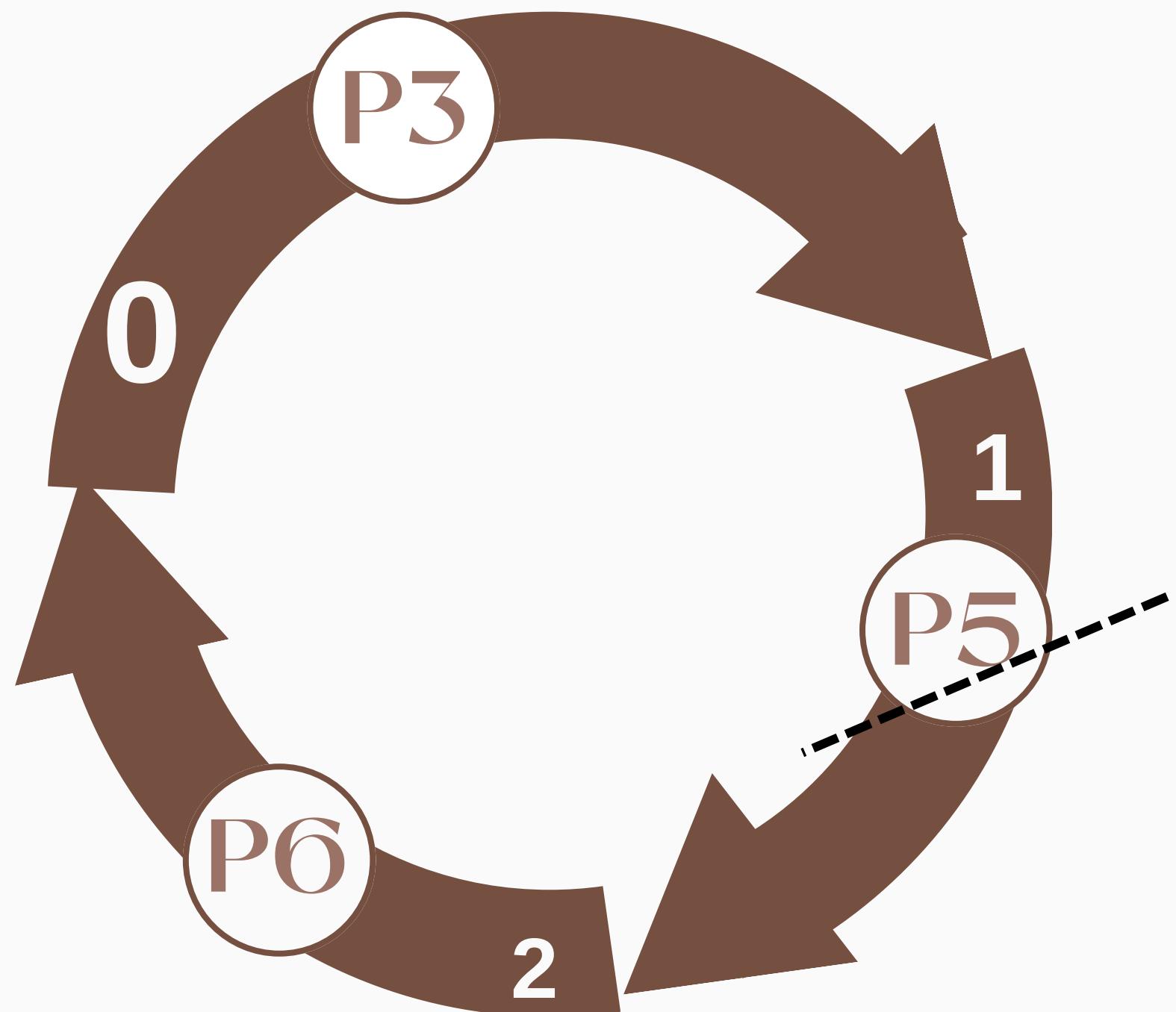
$4 == 1$? No

$$P = 0 \% 4 = 0$$

Dequeue

$$P = 0 \% 3 = 0$$

4.



$$P = 0$$

$$u = 0 \% 3 = 3 \% 3 = 0$$

$$0 == 0 ? \text{ sí}$$

$$u = u + 1$$

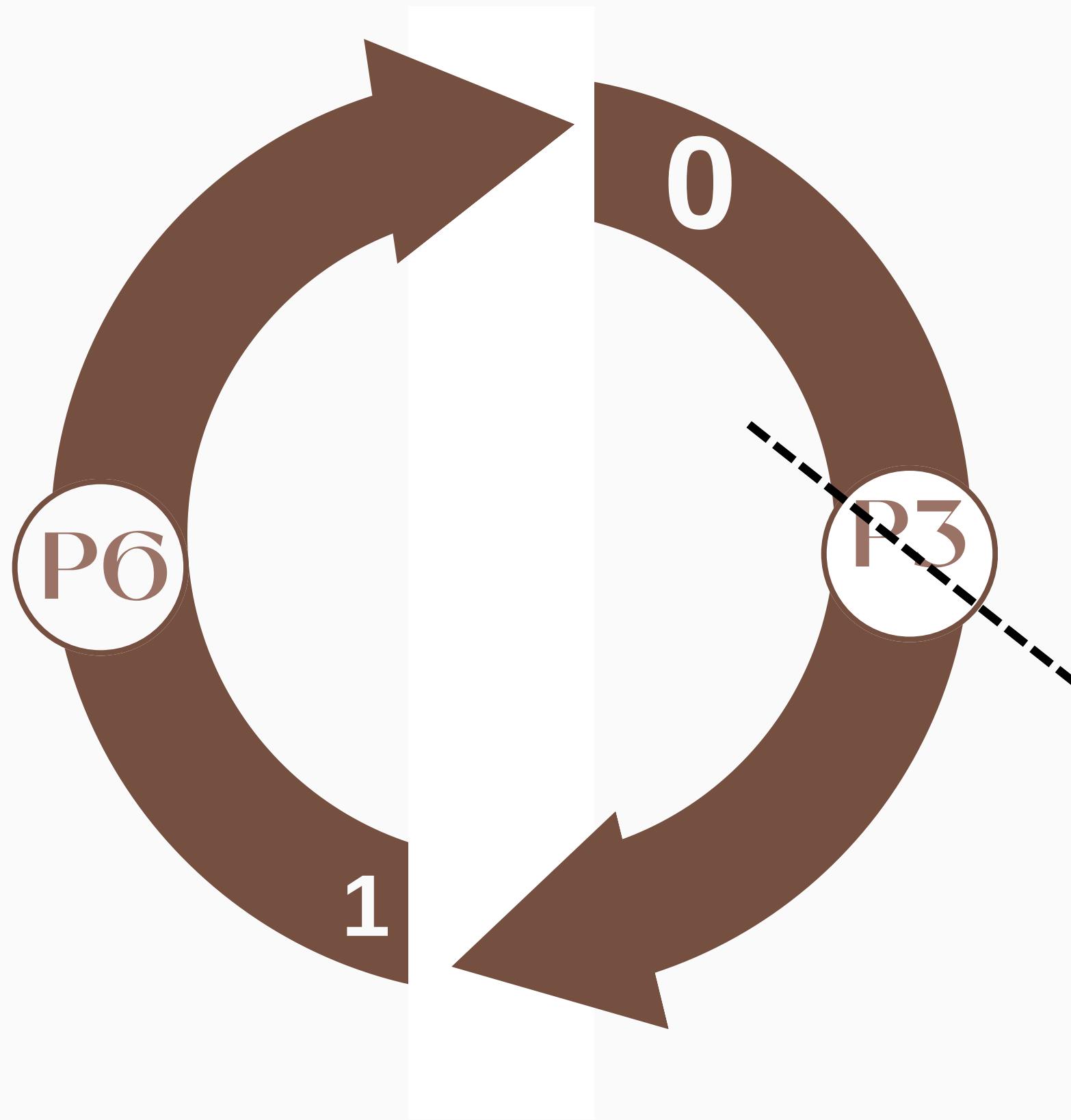
$$u = 1$$

$$P = 1 \% 3 = 1$$

Dequeue

$$P = 1 \% 2 = 1$$

5.



$$P = 1$$

$$u = 1 + 3 \% 2 = 4 \% 2 = 0$$

$0 == 1$? no

$$P = 0 \% 2 = 0$$

Dequeue

$$P = 0 \% 1 = 0$$

$s(6) = P6$

$r = 3$

Practice Exercise

s(7) = P1

r=2
