



Autonomous and Mobile Robotics - group project presentation

QUADRUPED GAIT GENERATION BASED ON IS-MPC

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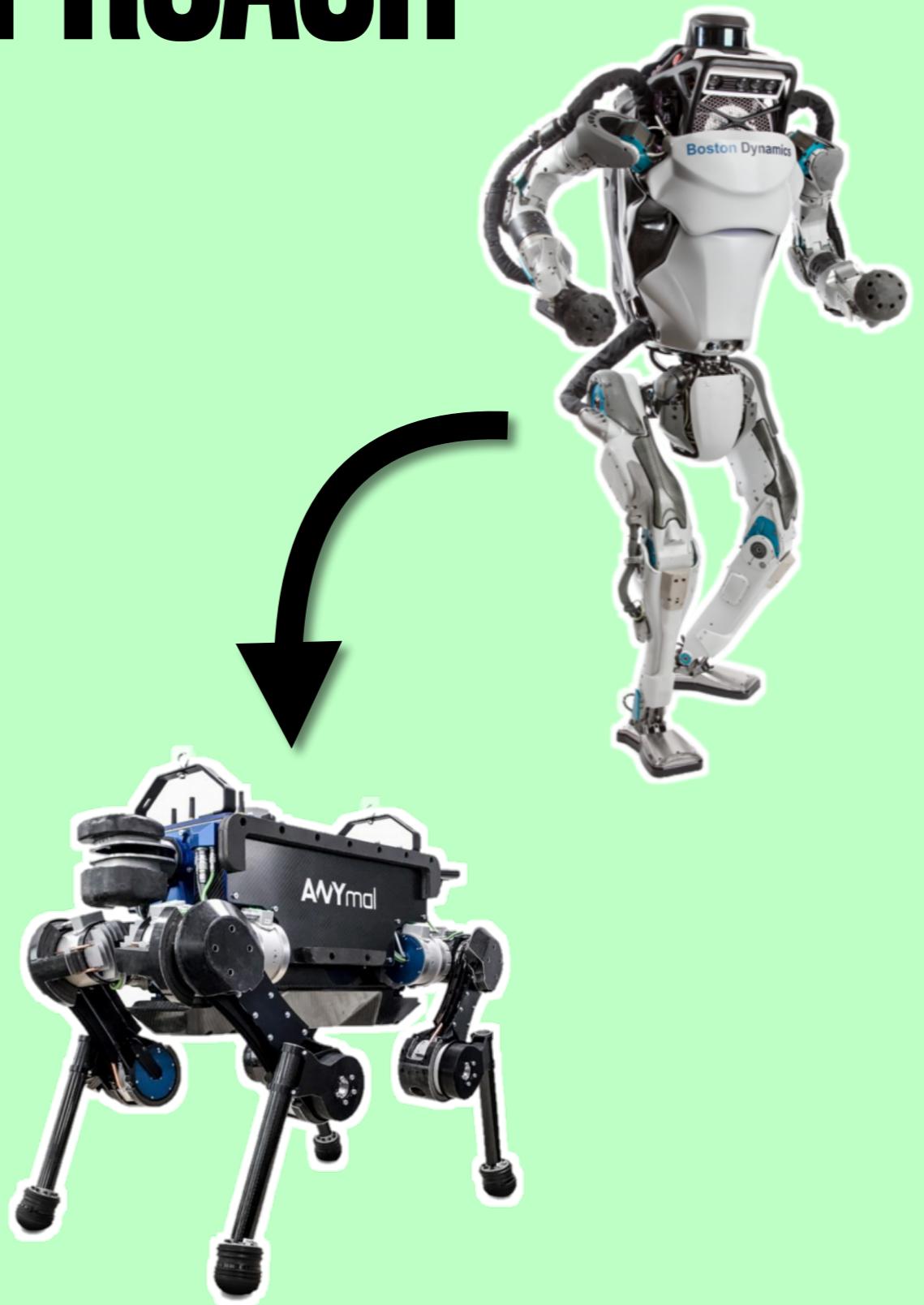
STATE OF THE ART

- Due to non linearity of quadruped simplified model as inverted pendulum is used.
- Commonly the classic approach aims to let the ZMP lie inside the support polygon with vertex in the contact feet, this constraints are generally non linear in the decision variables
- In a MPC framework this will lead to an increase of decision variables.



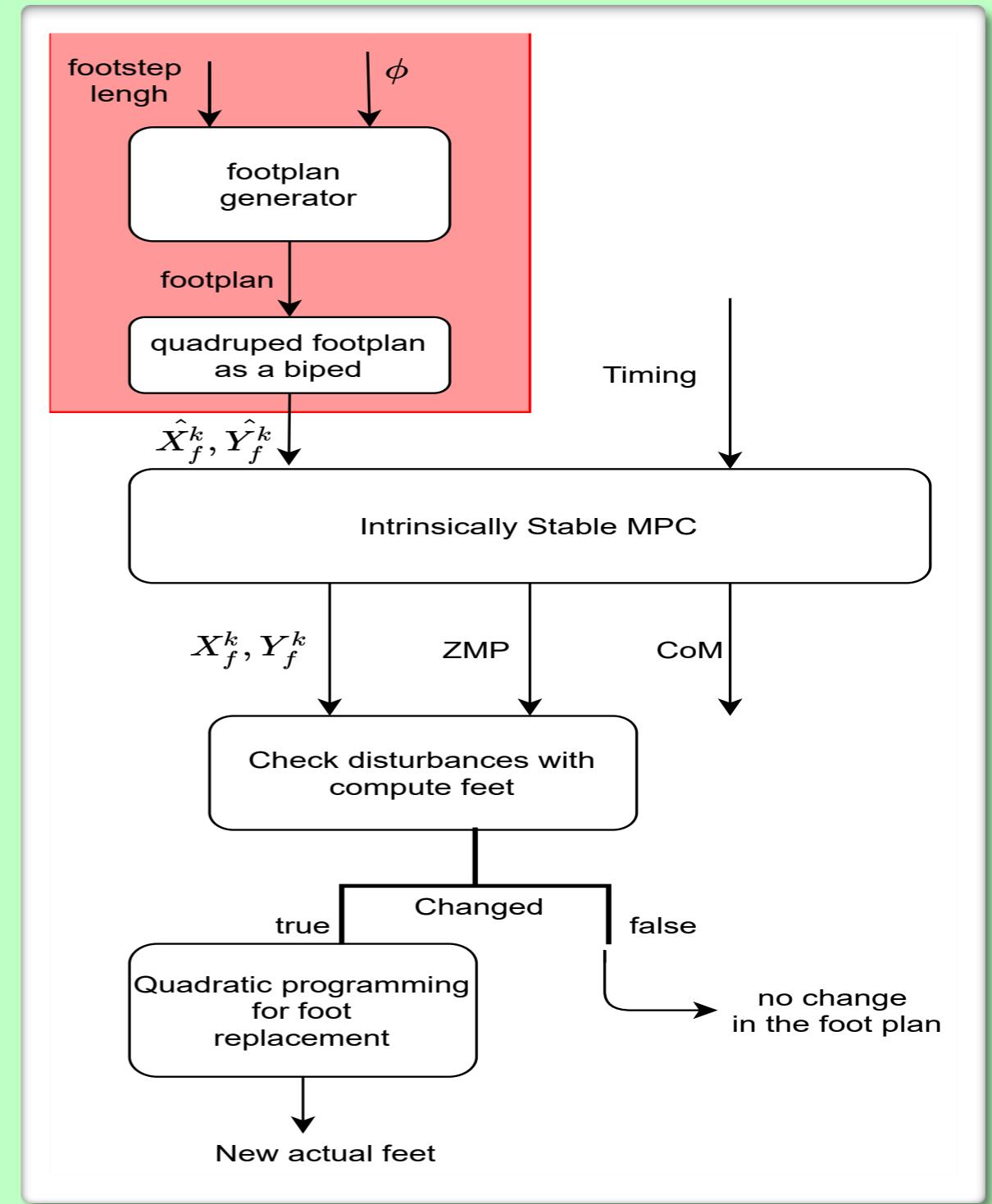
OUR PROBLEM APPROACH

- Approach the quadruped problem, considering an ideal humanoid:
 - Computationally less intensive.
 - Linear ZMP constraints.
 - Restrictive approach case.
- Consider then a second QP for the foot replacement.
- Trotting/Walking scenarios.

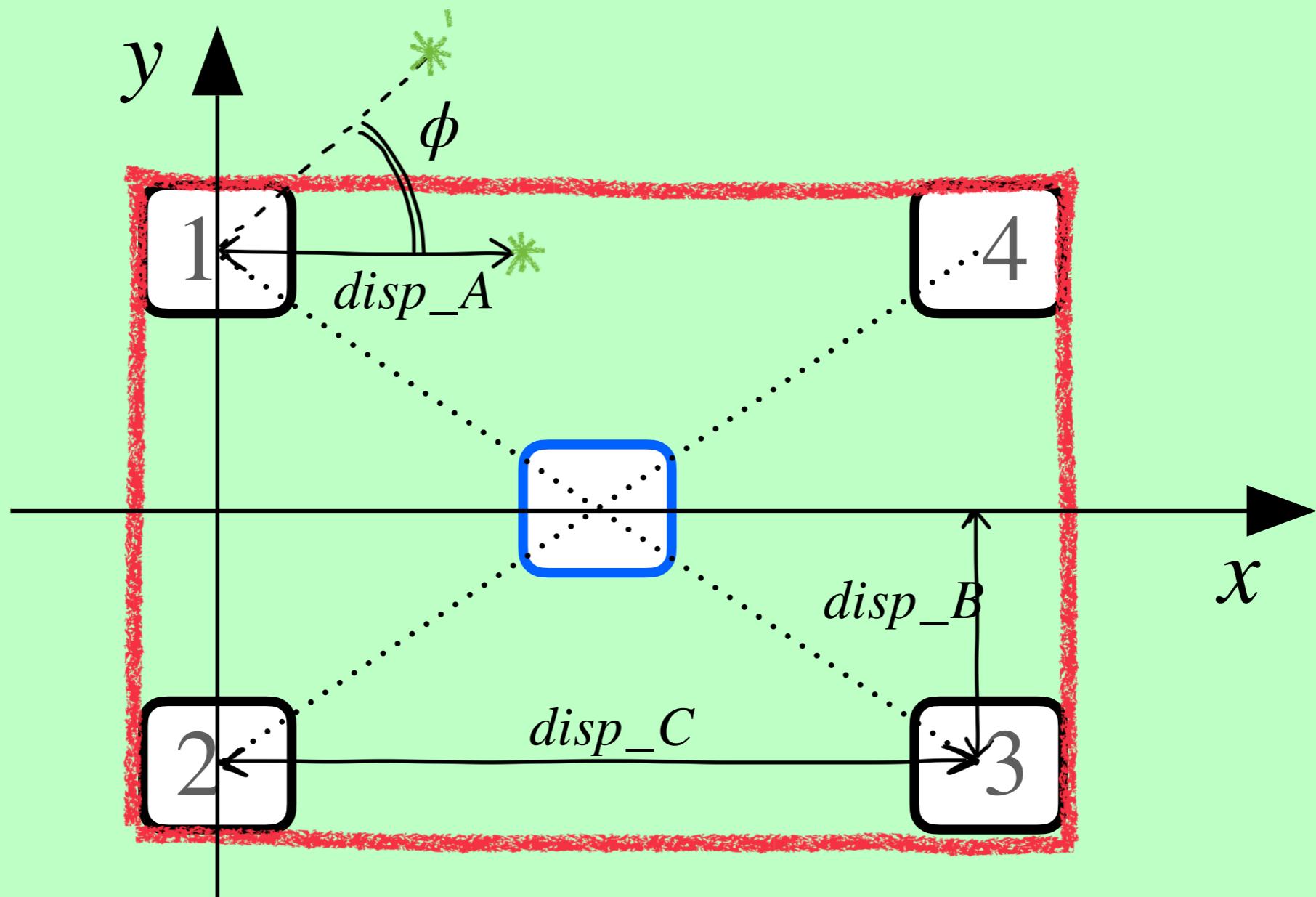


GENERAL BLOCK DIAGRAM

- Initialisation of the foot plan for the quadruped and the ideal biped.
- IS-MPC on the biped.
- Check for eventual disturbances.
- Second QP for the foot replacement.

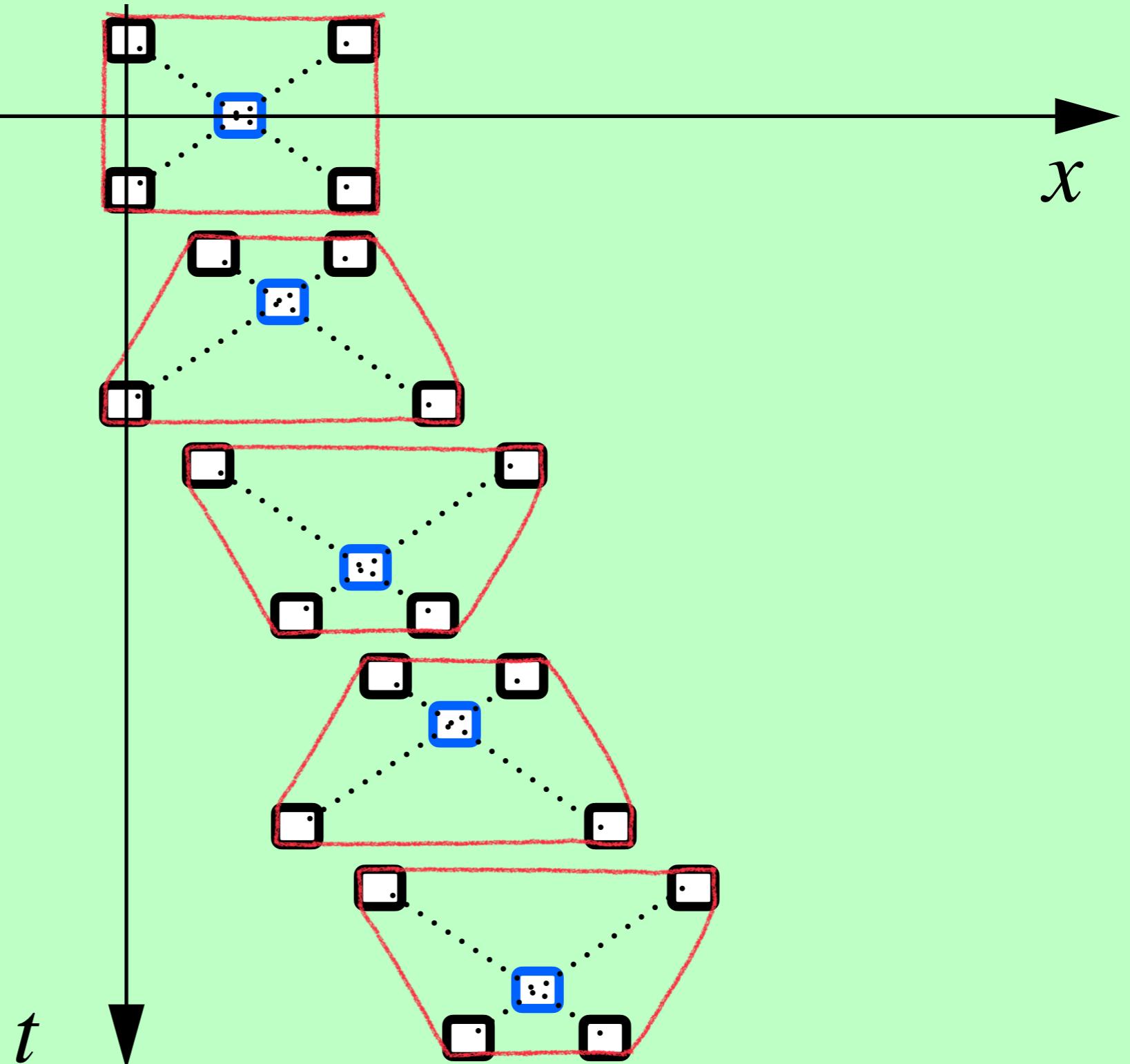


QUADRUPED PARAMETRIZATION

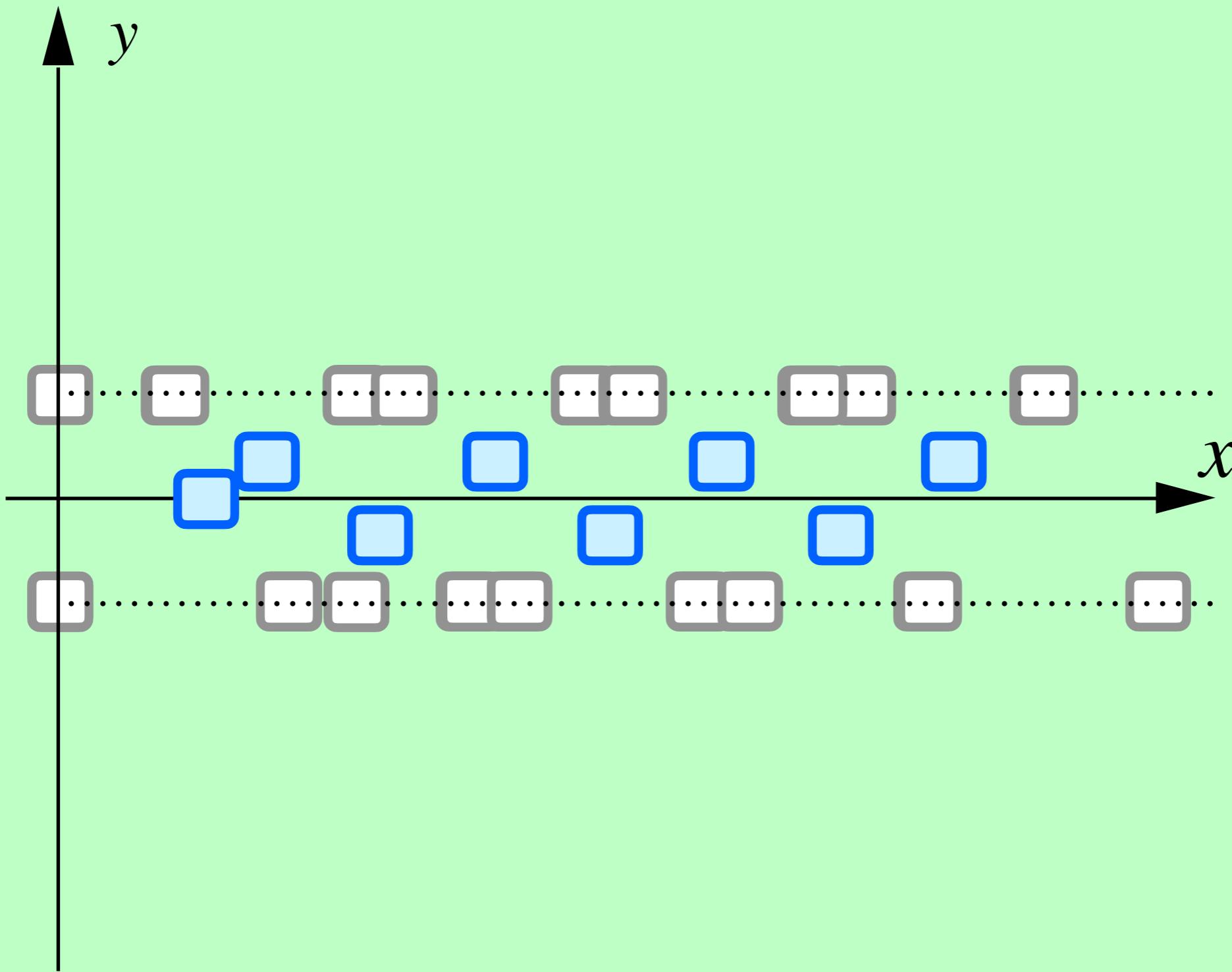


MAIN IDEA

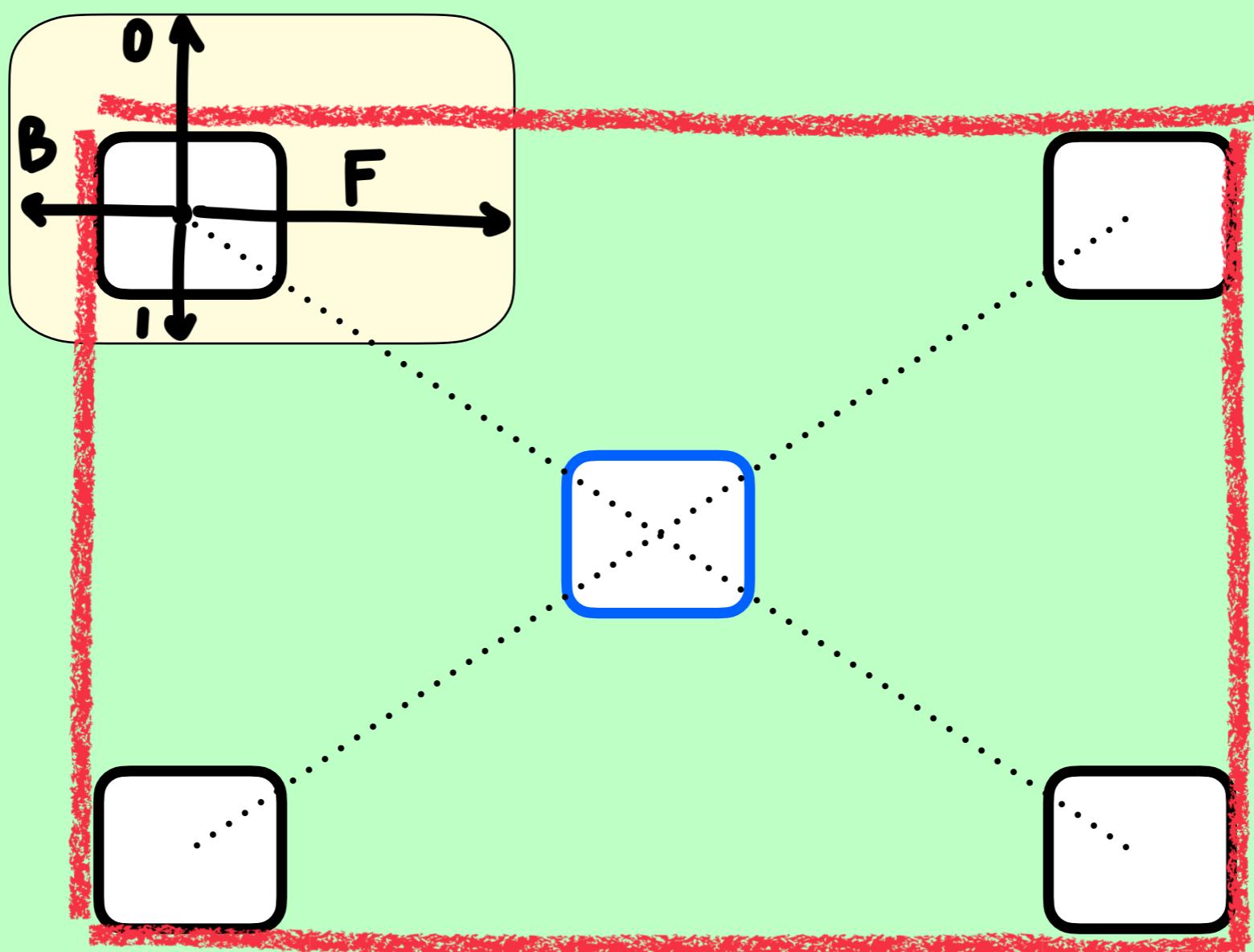
- During time and considering a trotting scenario, the blue squares are the ideal biped steps.
- We exploits these blue squares to feed the IS-MPC QP with a ZMP trajectory that interpolates all them.



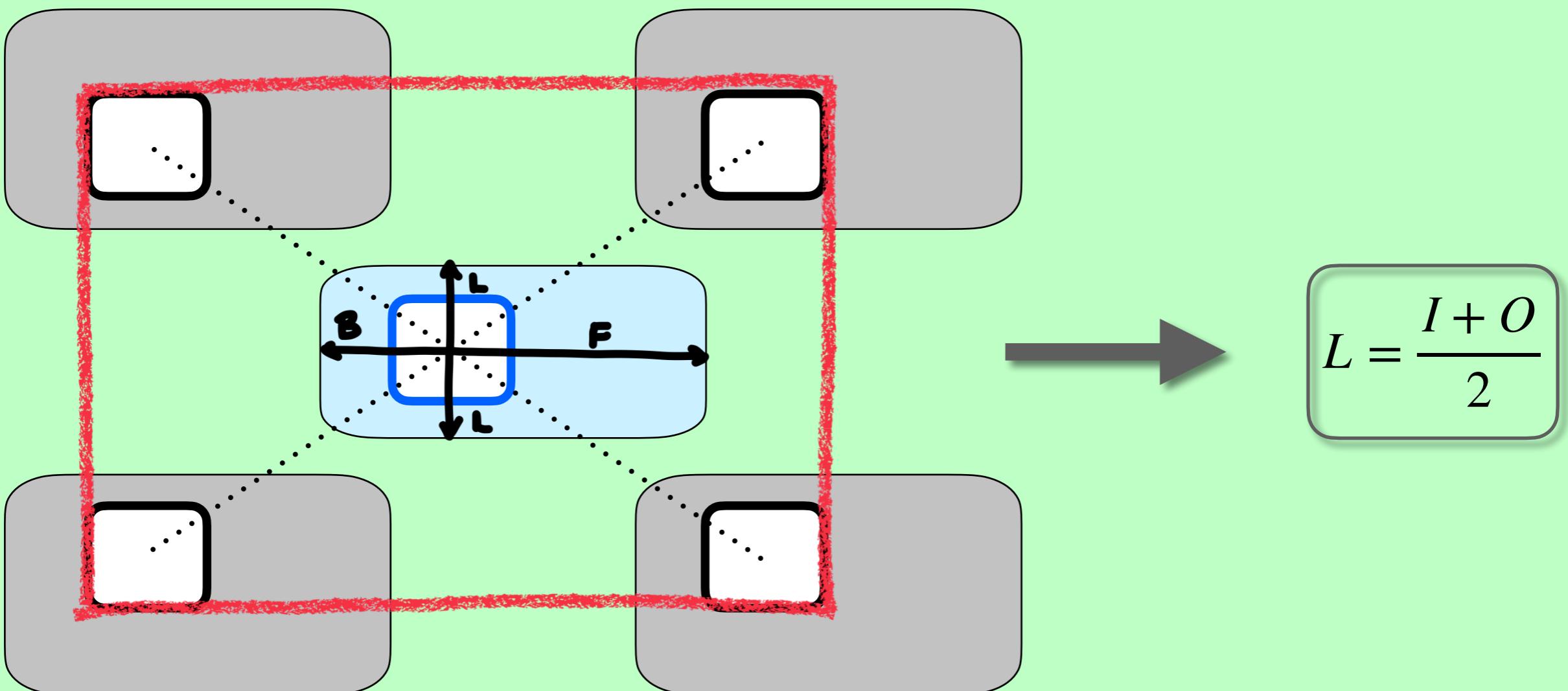
MAIN IDEA



FOOT KINEMATIC LIMITATION



FICTITIOUS FOOT KINEMATIC LIMITATION



IS-MPC FORMULATION

$$\min_{\dot{X}_z^k, \dot{Y}_z^k} \|\dot{X}_z^k\|^2 + \|\dot{Y}_z^k\|^2 + \beta(\|X_f - \hat{X}_f\|^2 + \|Y_f - \hat{Y}_f\|^2)$$
$$X_f^k, Y_f^k$$

Subject to :

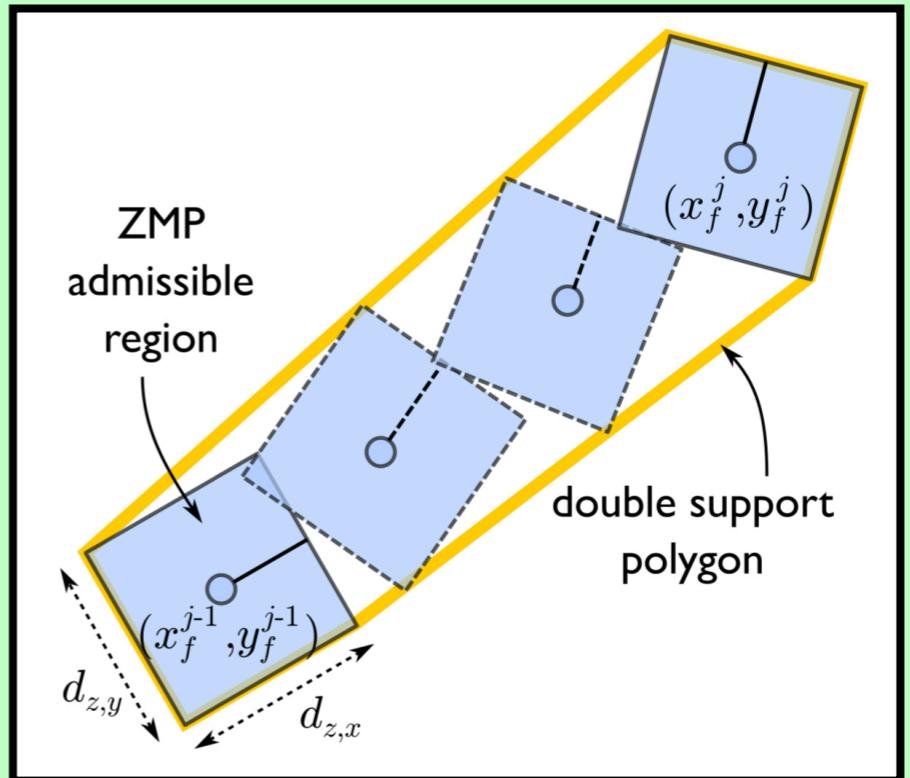
- ZMP constraint
- Kinematic constraint
- Stability constraint for x and y

All the decision variables are collected in vectors, like:

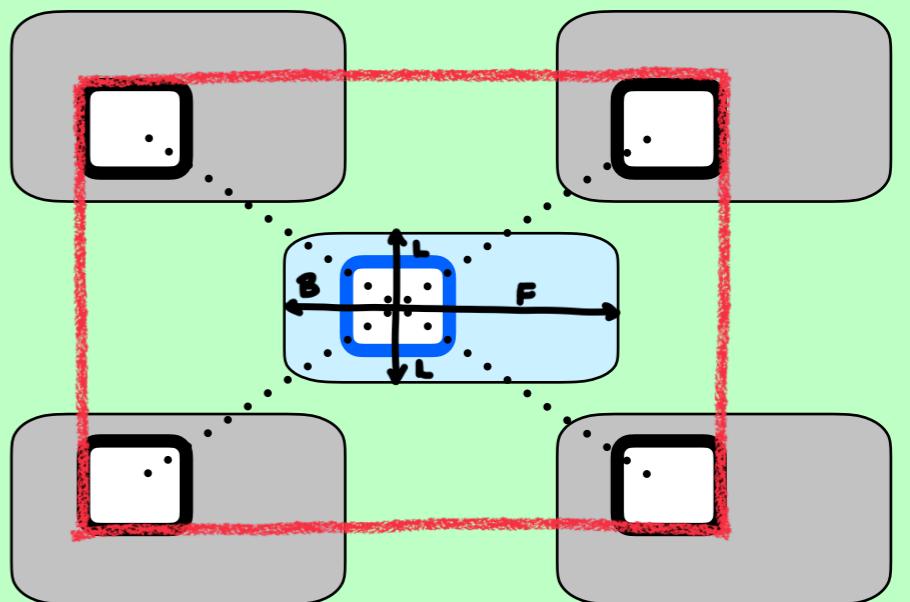
$$\left\{ \begin{array}{lcl} \dot{X}_z^k & = & (\dot{x}_z^k, \dots, \dot{x}_z^{k+C-1})^T \\ \dot{Y}_z^k & = & (\dot{y}_z^k, \dots, \dot{y}_z^{k+C-1})^T \\ X_f^k & = & (x_f^1, \dots, x_f^{F'})^T \\ Y_f^k & = & (y_f^1, \dots, y_f^{F'})^T \end{array} \right.$$

ZMP & KINEMATIC CONSTRAINT

$$R_j^T \begin{pmatrix} \delta \sum_{l=0}^i \dot{x}_z^{k+l} - x_f^j \\ \delta \sum_{l=0}^i \dot{y}_z^{k+l} - y_f^j \end{pmatrix} \leq \frac{1}{2} \begin{pmatrix} d_{z,x} \\ d_{z,y} \end{pmatrix} - R_j^T \begin{pmatrix} x_z^k \\ y_z^k \end{pmatrix}$$



$$R_{j-1}^T \begin{pmatrix} x_f^j - x_f^{j-1} \\ y_f^j - y_f^{j-1} \end{pmatrix} \leq \pm \begin{pmatrix} 0 \\ disp_L/2 \end{pmatrix} + \begin{pmatrix} disp_F \\ disp_L/2 \end{pmatrix}$$



STABILITY CONSTRAINT

- Using a change of coordinates, the LIP can be decoupled in stable and unstable dynamics.

$$\dot{x}_u = x_c + \frac{\dot{x}_c}{\eta}$$

- The decoupled dynamics are:

$$\dot{x}_s = x_c - \frac{\dot{x}_c}{\eta}$$

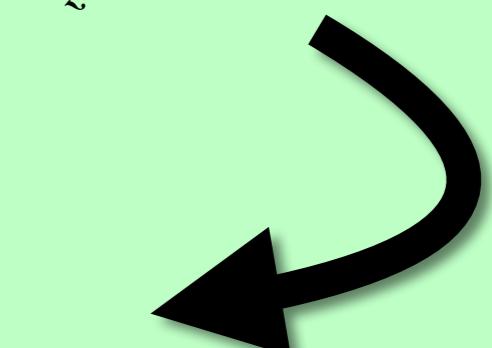
$$\dot{x}_s = \eta(-x_s + x_z) \quad \dot{x}_u = \eta(x_u - x_z)$$

- The CoM is bounded if and only if :

$$x_u^k = \eta \int_{t_k}^{\infty} e^{-\eta(\tau-t_k)} x_z(\tau) d\tau$$

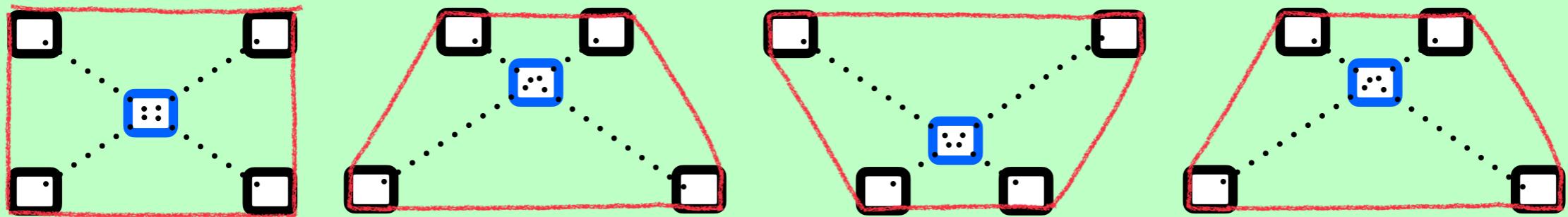
$$\sum_{i=0}^{C-1} e^{-i\eta\delta} \dot{x}_z^{k+1} = - \sum_{i=C}^{\infty} e^{-i\eta\delta} \dot{x}_z^{k+i} + \frac{\eta}{1-e^{-\eta\delta}} (x_u^k - x_z^k)$$

$$\sum_{i=0}^{C-1} e^{-i\eta\delta} \dot{x}_z^{k+1} = - \sum_{i=C}^{P-1} e^{-i\eta\delta} \dot{x}_{z,ant}^{k+i} - \sum_{i=P}^{\infty} e^{-i\eta\delta} \dot{x}_{z,ant}^{k+i} + \frac{\eta}{1-e^{-\eta\delta}} (x_u^k - x_z^k)$$



Anticipative tail

TROTTING



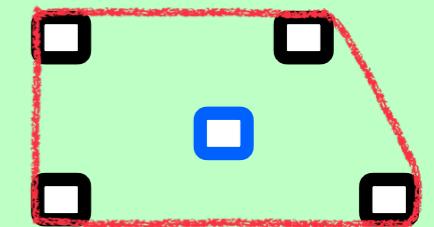
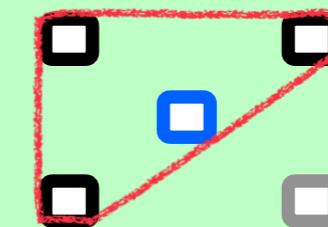
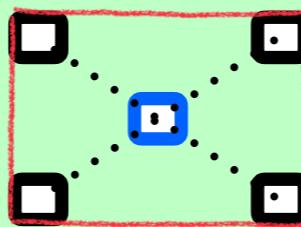
- The idea is to move two opposite leg simultaneously, e.g. **Back_Left with Front_Right** and **Back_Right with Front_Left**.

Back Left		Back Right		Front Right		Front Left	
x	y	x	y	x	y	x	y
0	disp_B	0	-disp_B	disp_C	-disp_B	disp_C	disp_B
+x_pd	+y_pd	•	•	+x_pd	+y_pd	•	•
•	•	+x_p	+y_p	•	•	+x_p	+y_p
+x_p	+y_p	•	•	+x_p	+y_p	•	•

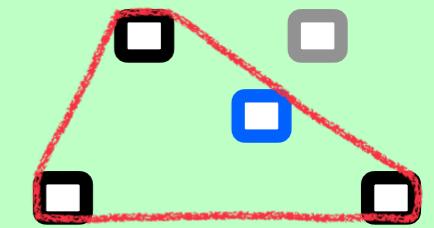
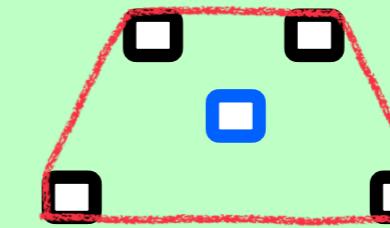
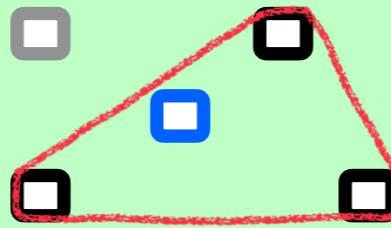
Recursive procedure to generate a trotting gait, starting from an initial feet configuration.

WALKING

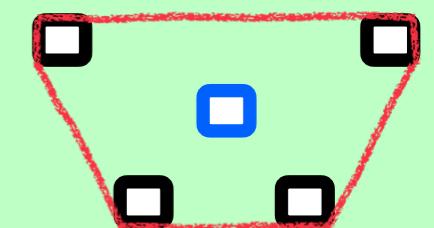
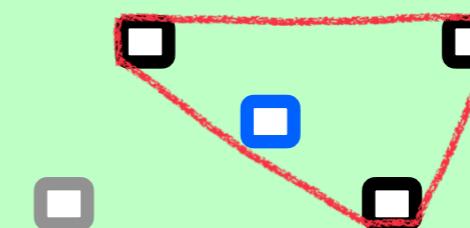
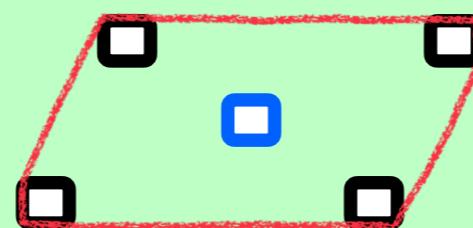
- In the walking scenario instead, the robot is performing the gait just moving one leg at each step.



- It seems to be a static gait.



- During the triangular shape support polygon, we have constrained the ZMP to stay inside the blue square relative to the previous support polygon.

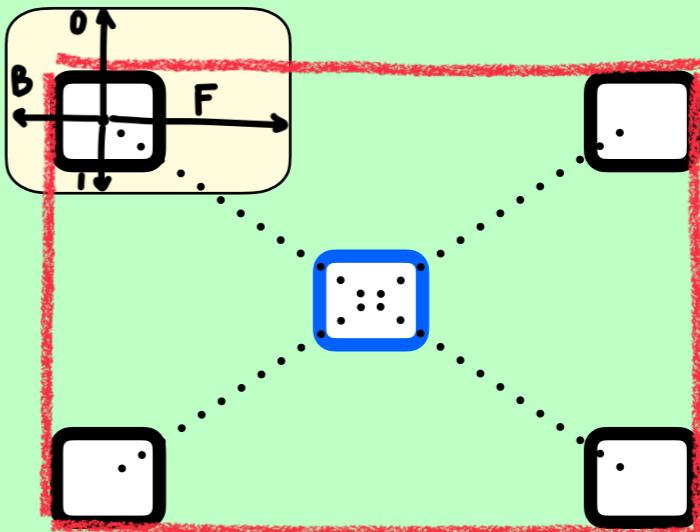


QP FOR FOOT REPLACEMENT

$$\min_{x_{fl}, y_{fl}, x_{fr}, y_{fr}} (X_{fl} - x_{fl})^2 + (Y_{fl} - y_{fl})^2 + (X_{fr} - x_{fr})^2 + (Y_{fr} - y_{fr})^2$$

Subject to :

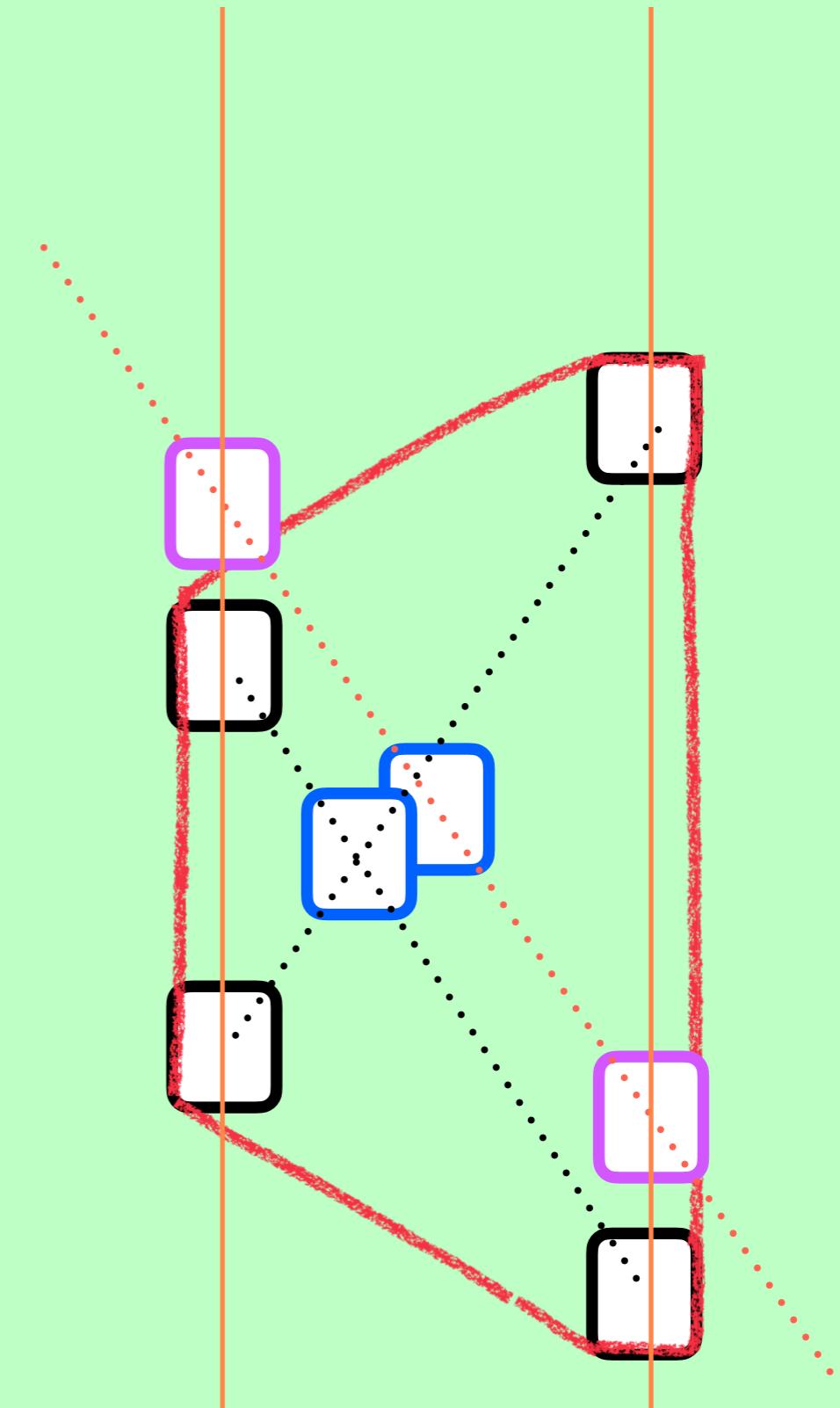
- Kinematic foot constraints



Where the decision variables are the coordinates for left and right feet

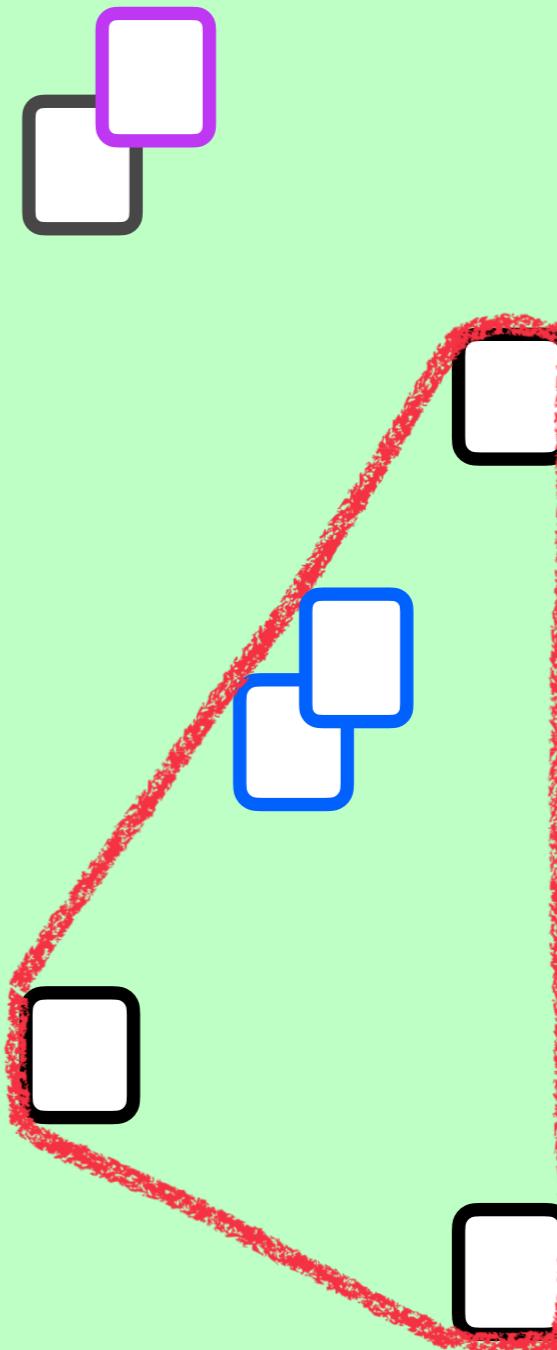
COMPUTE FEET: TROTTING

- When a disturbance is acting on the robot we recompute the feet prioritizing the gait orientation (ϕ angle).
- The aim of this procedure is to impose that the ZMP at the next step lies inside the double support polygon.

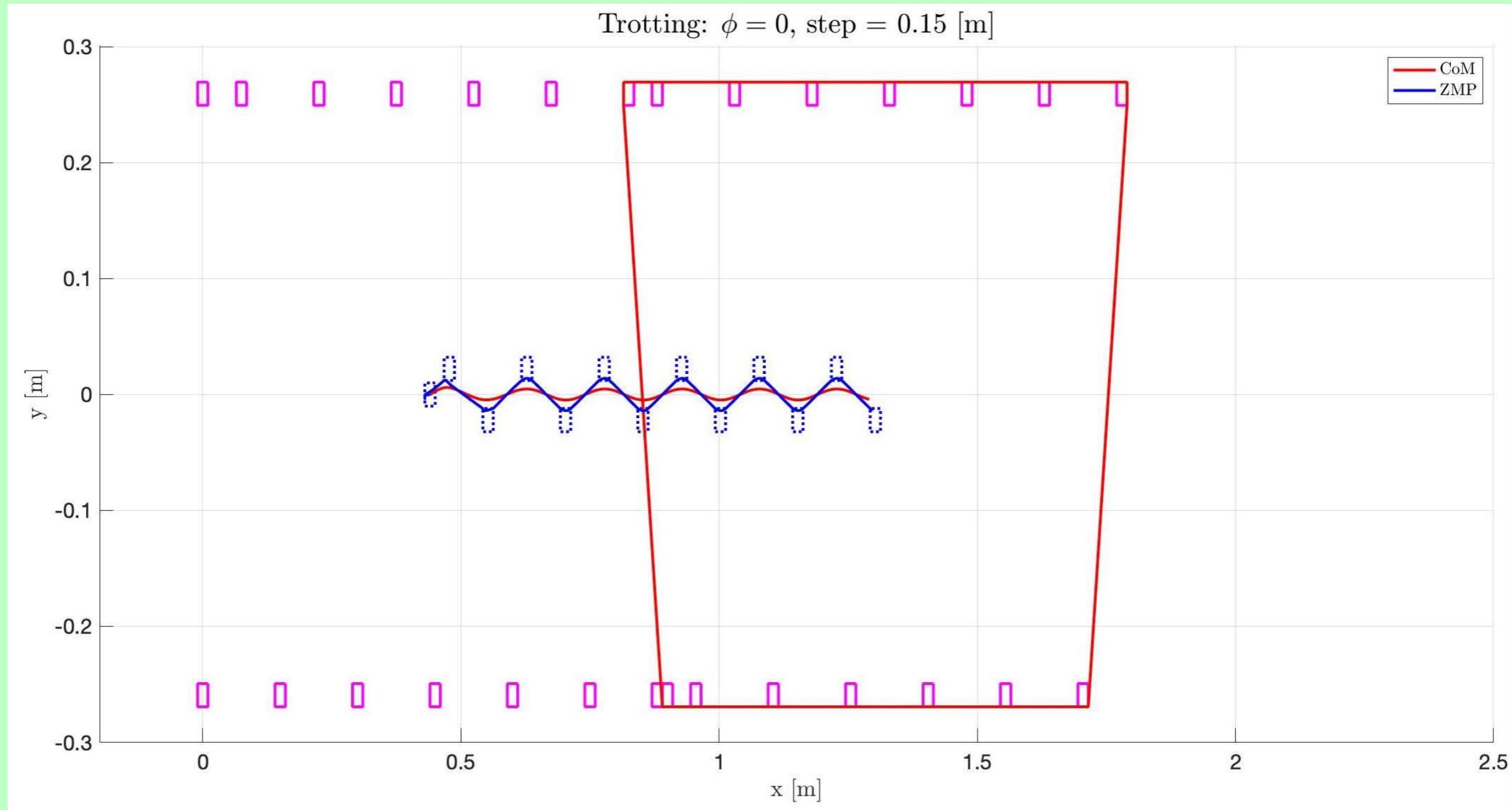


COMPUTE FEET: WALKING

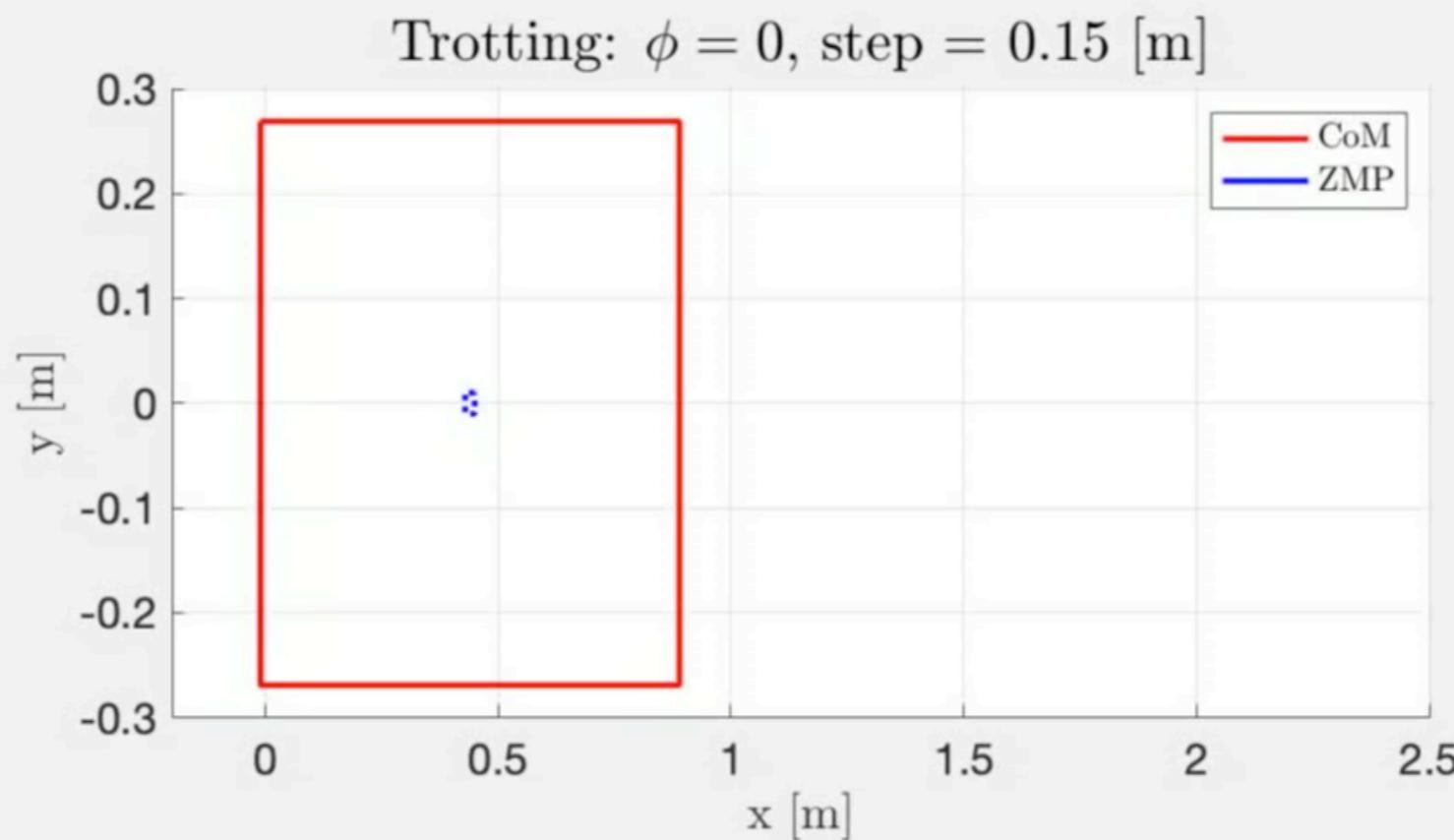
- In the walking case we try to compensate the error between the actual ZMP coordinates and the predicted ones.
- This is done by adding the aforementioned difference to the free-foot coordinate.



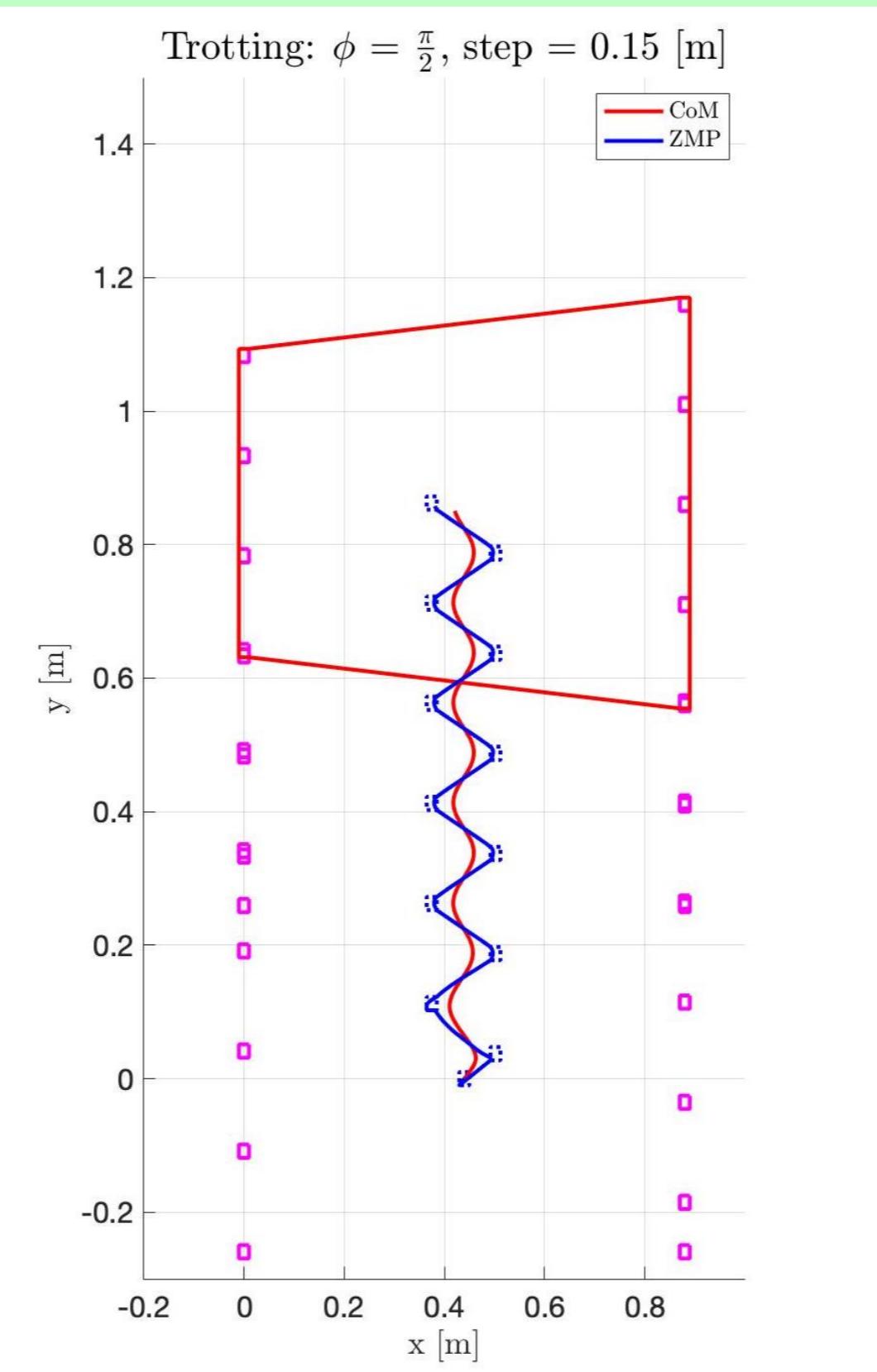
MATLAB



MATLAB

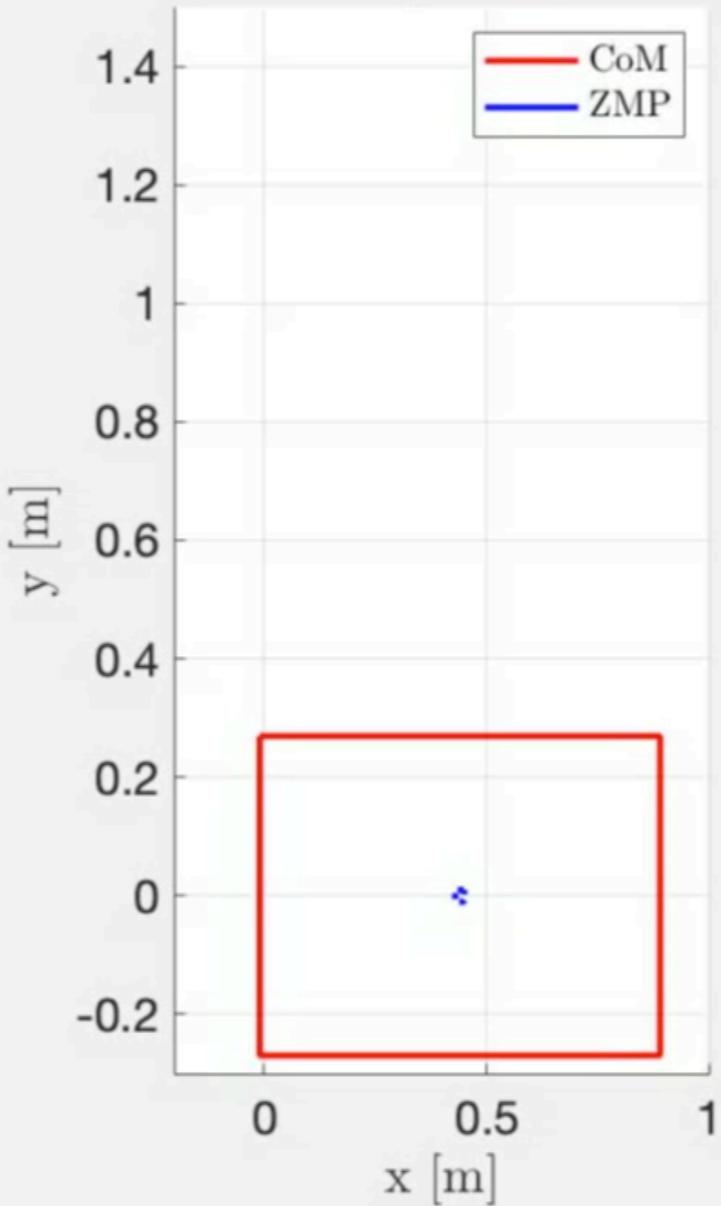


MATLAB

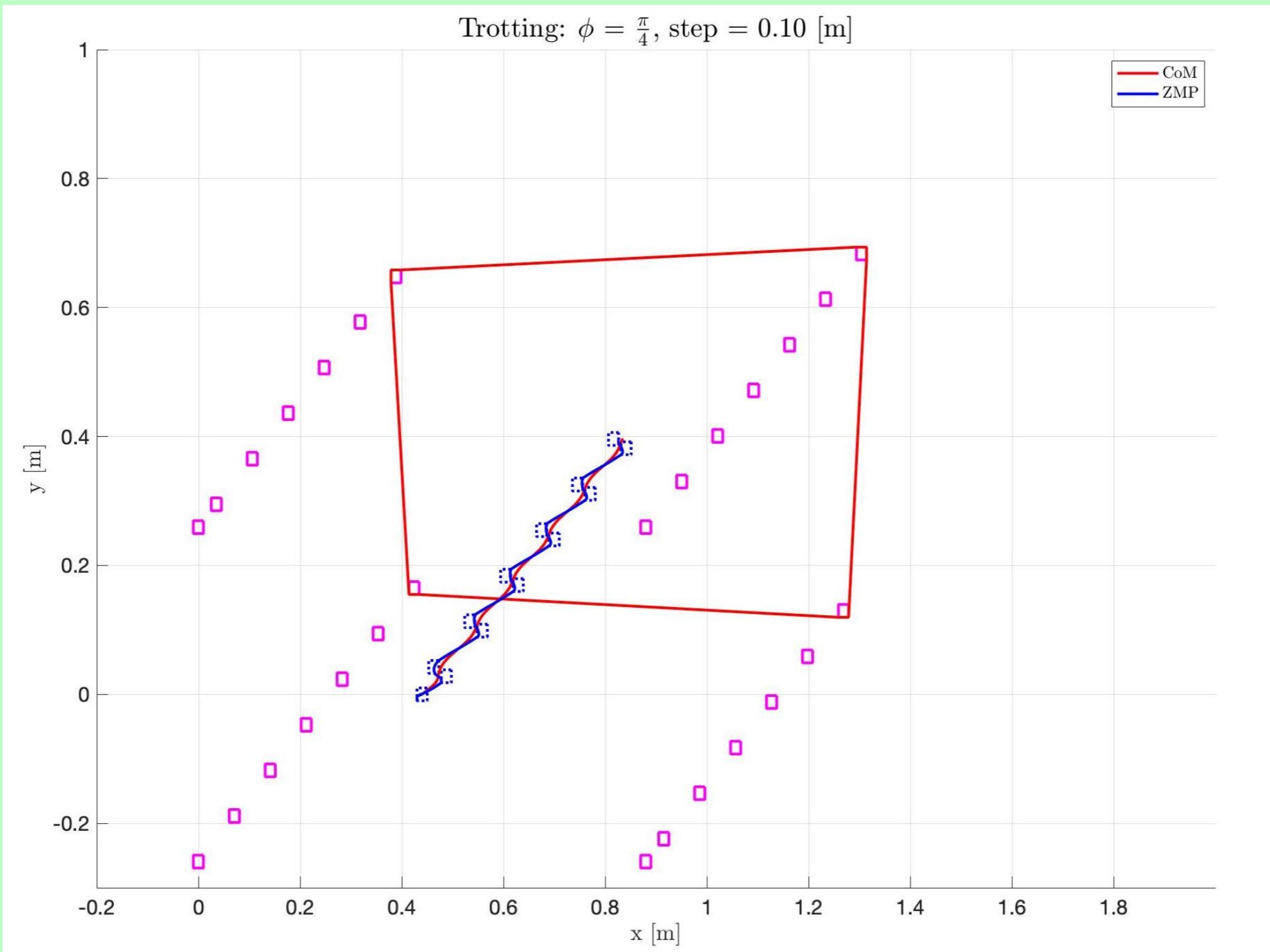


MATLAB

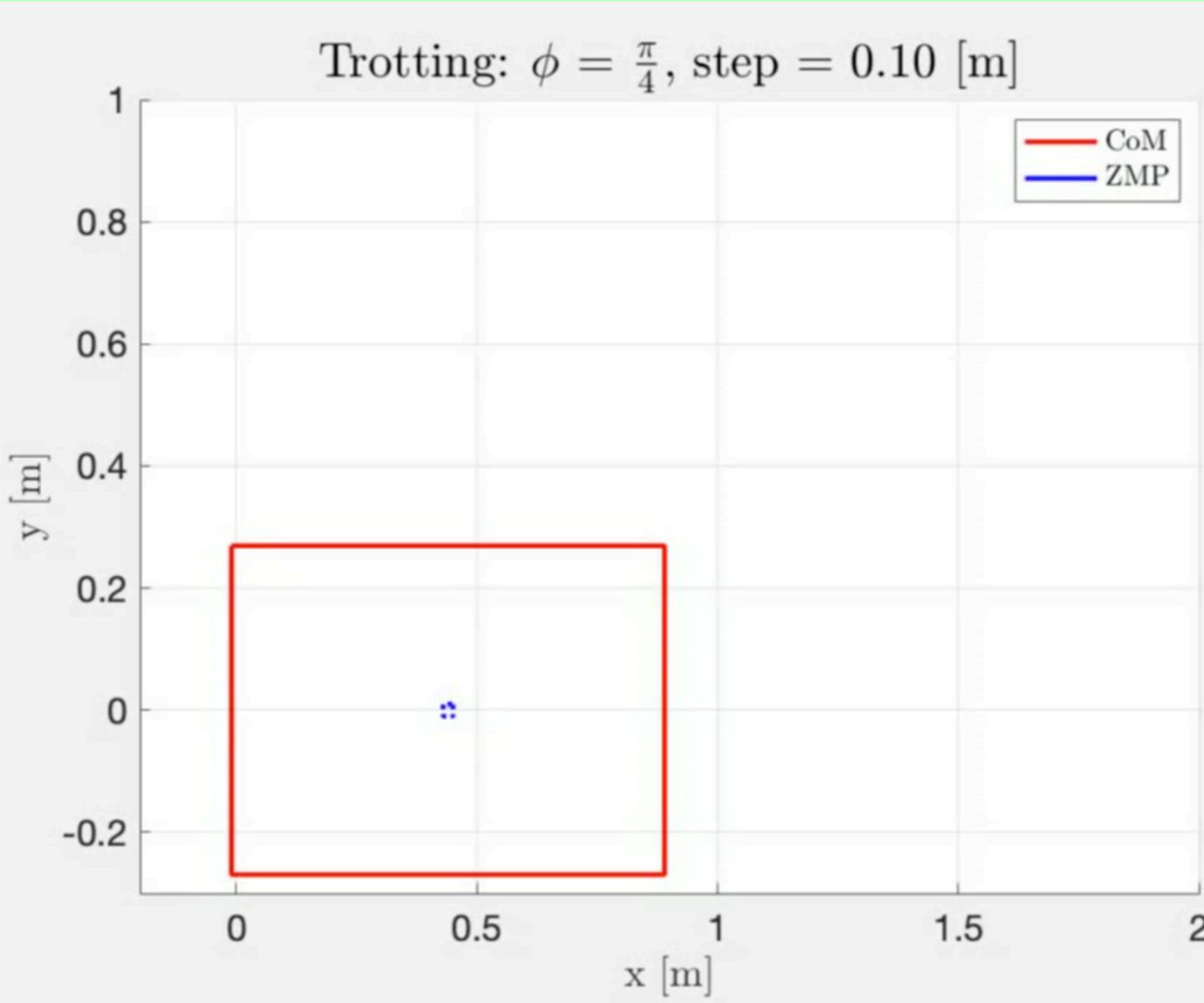
Trotting: $\phi = \frac{\pi}{2}$, step = 0.15 [m]



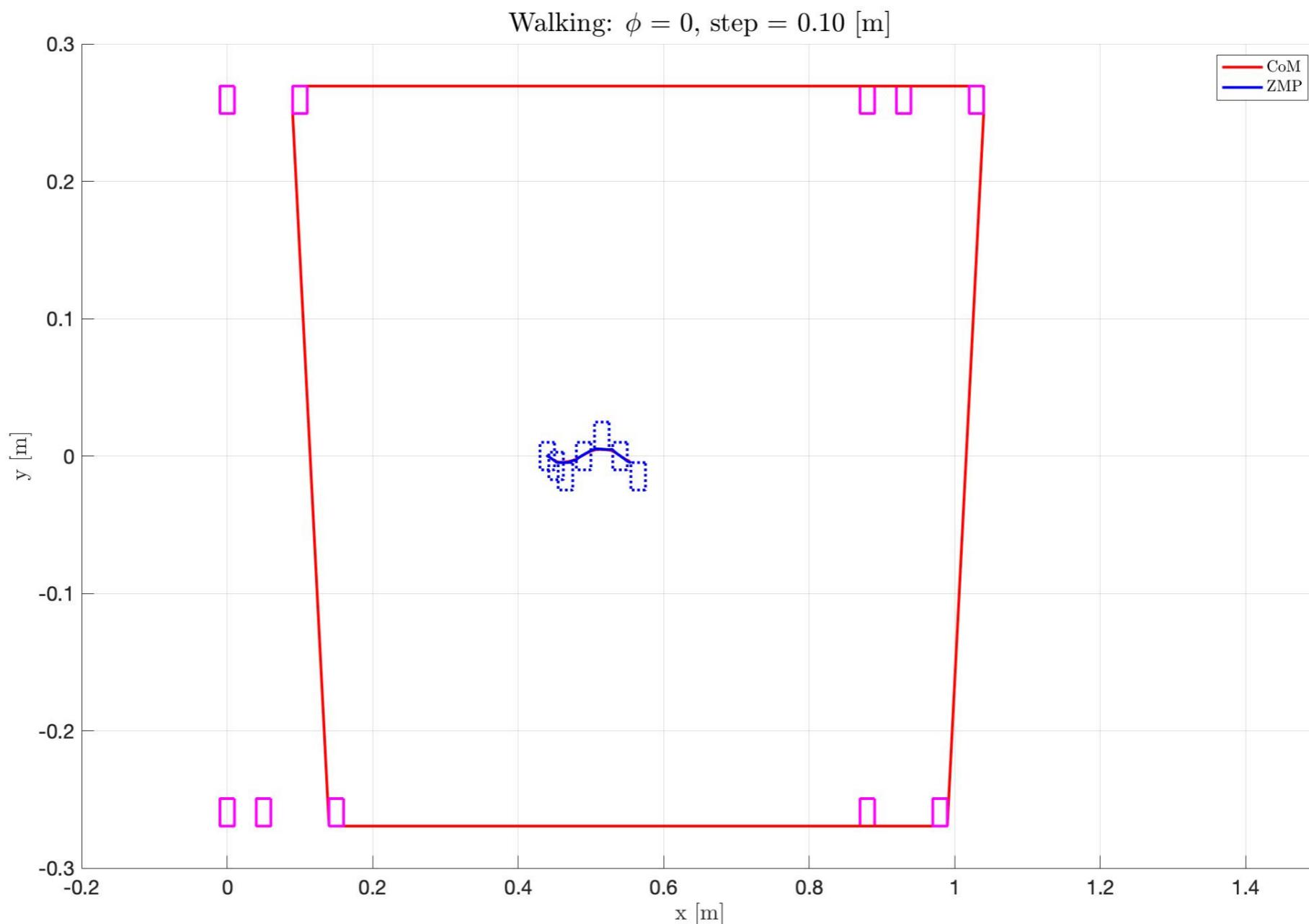
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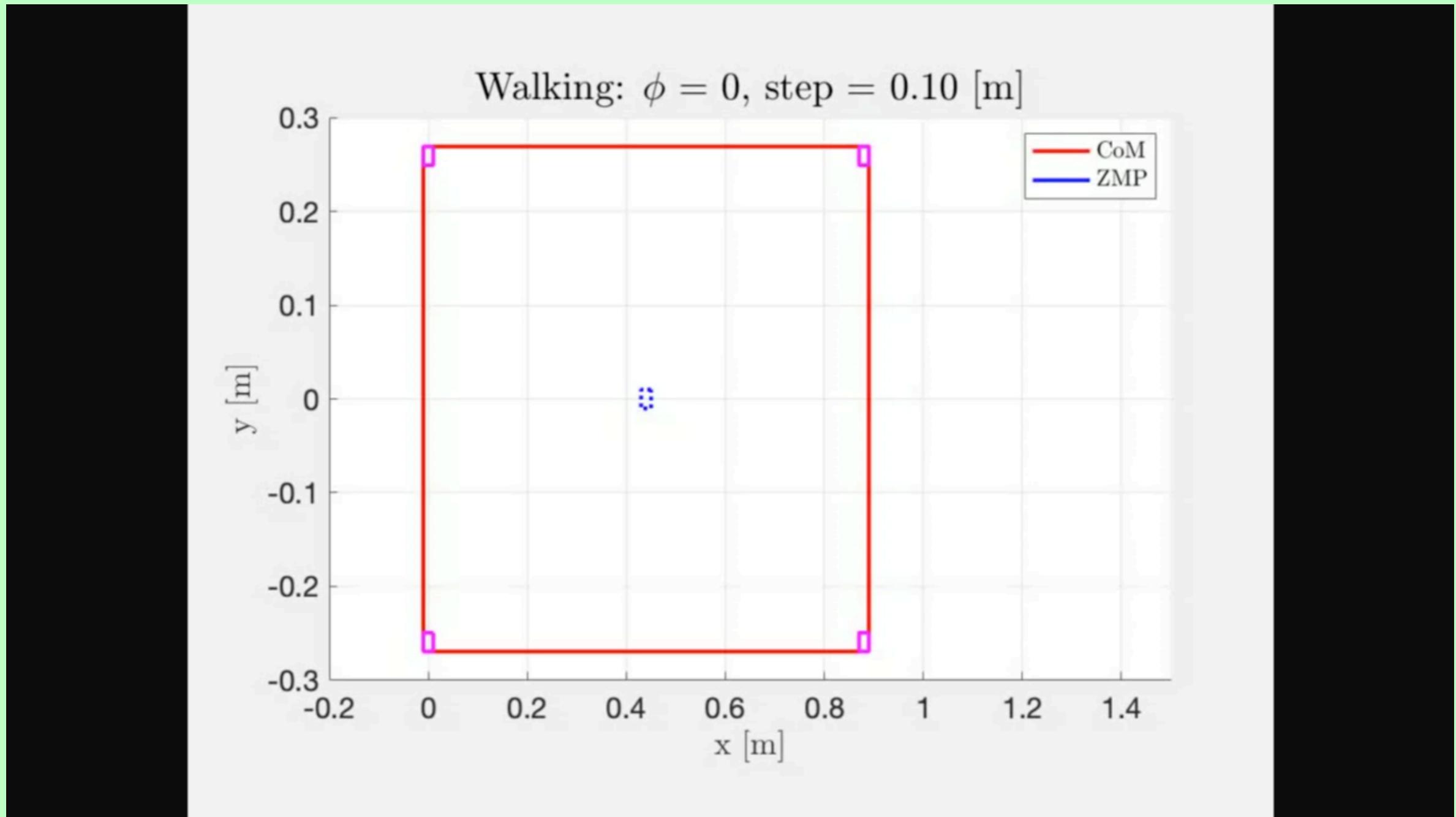
MATLAB



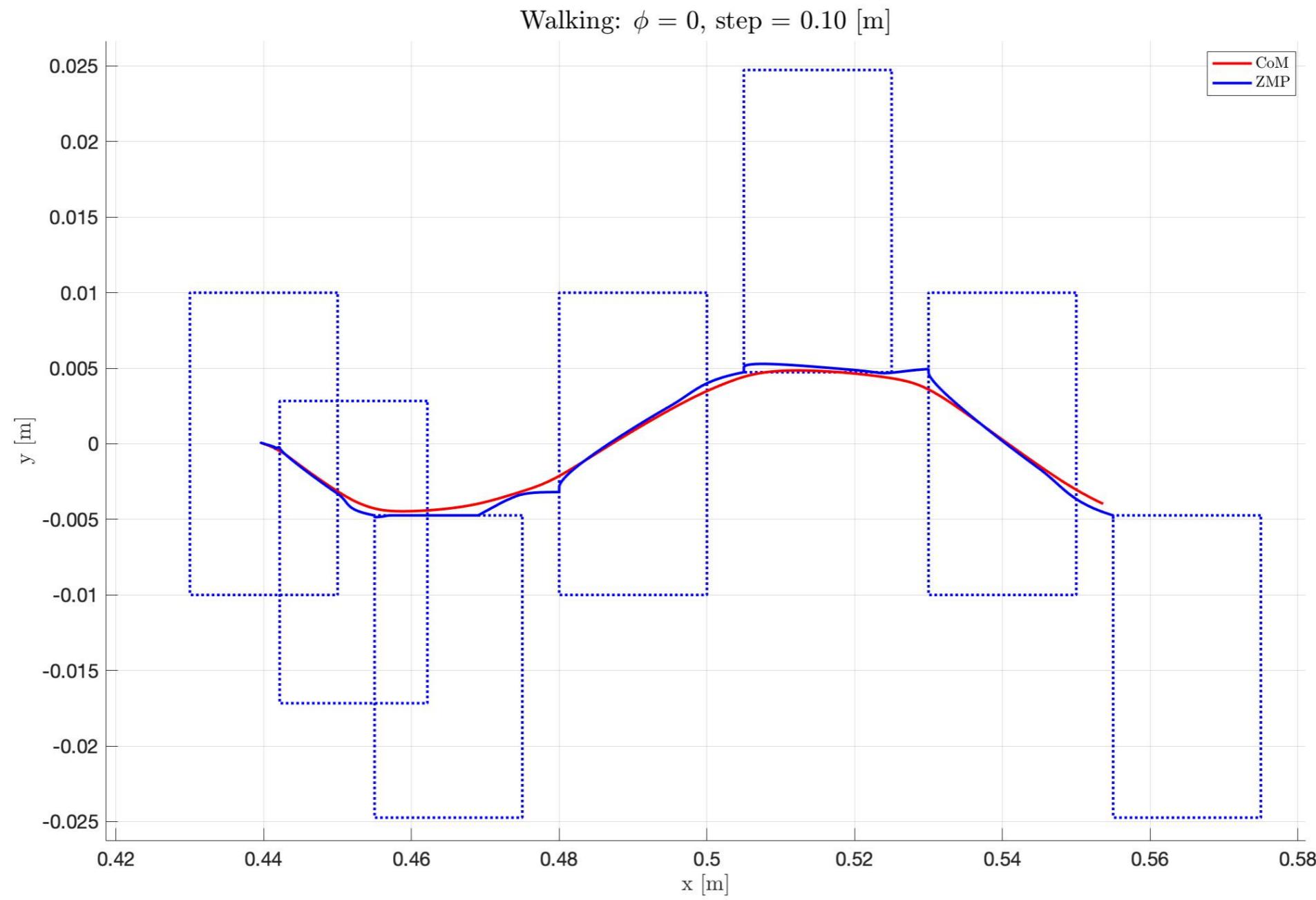
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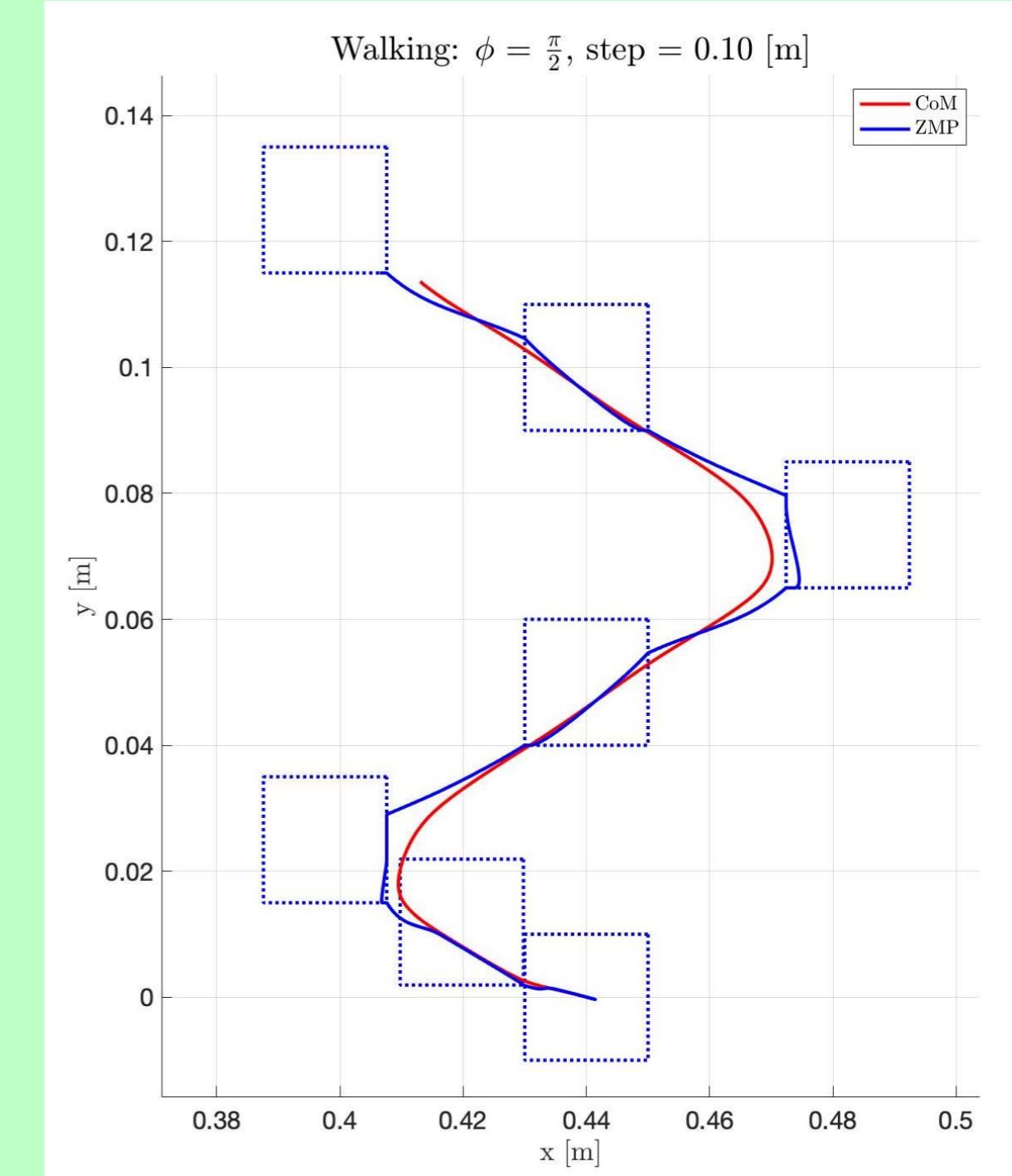
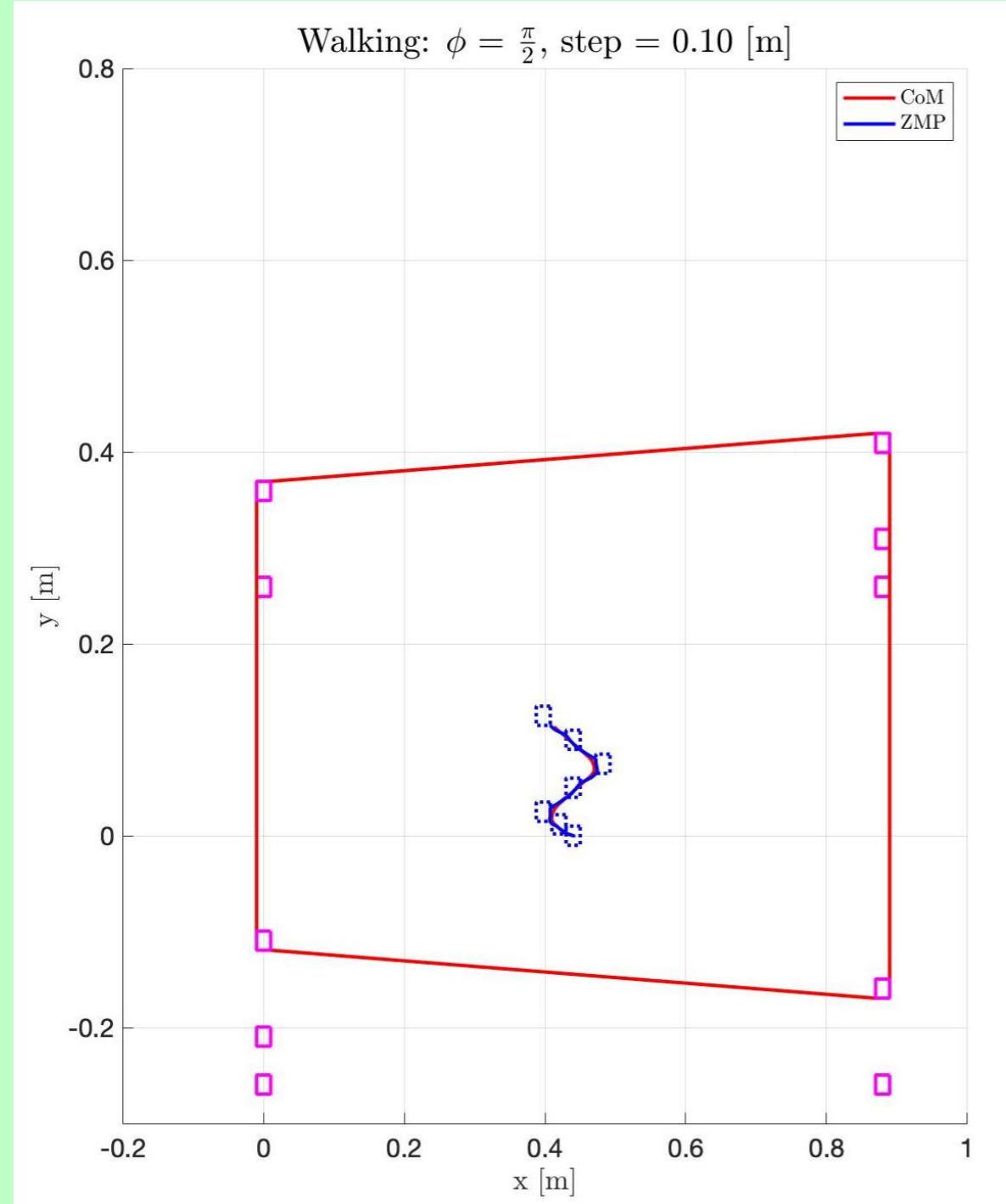
MATLAB



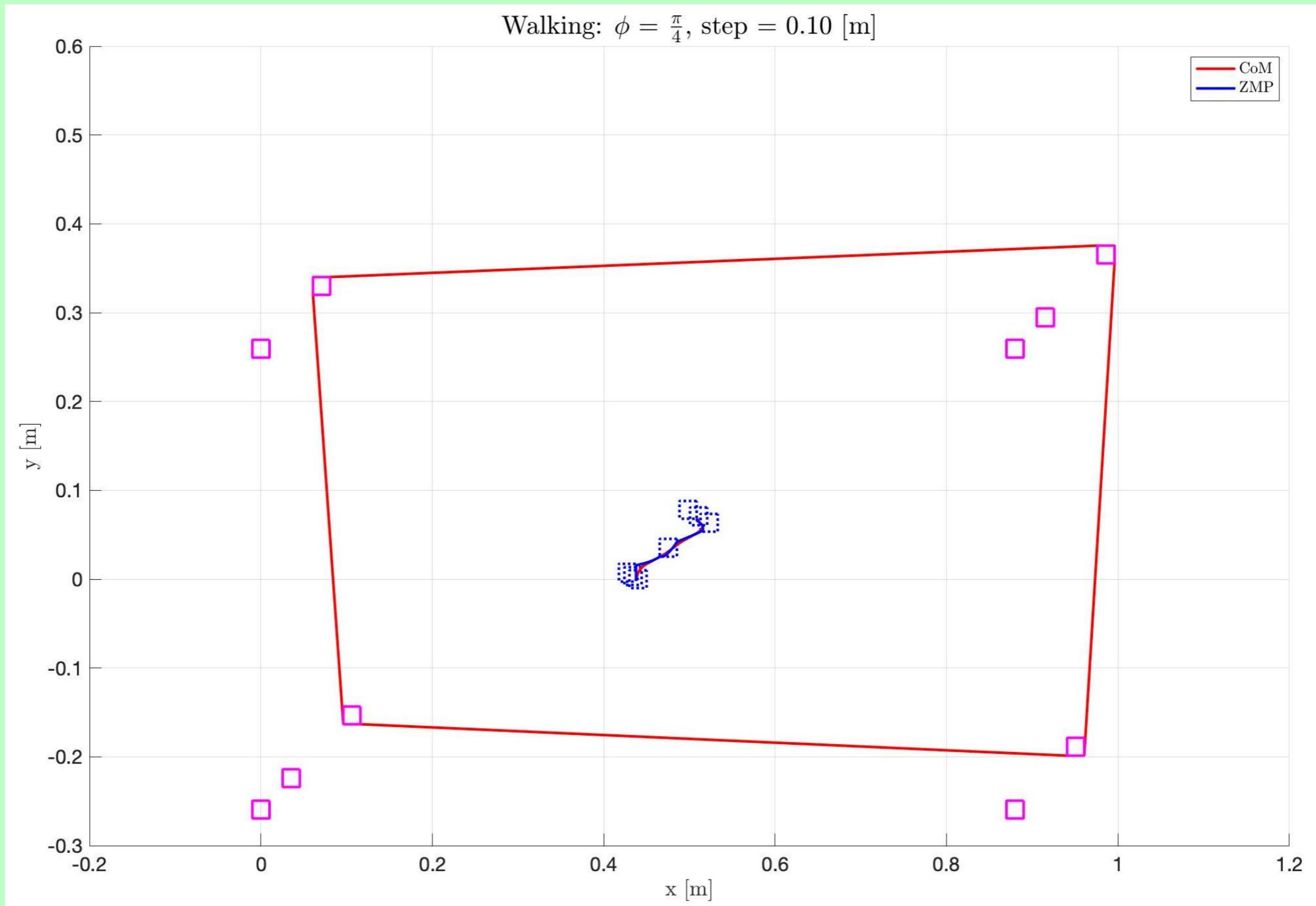
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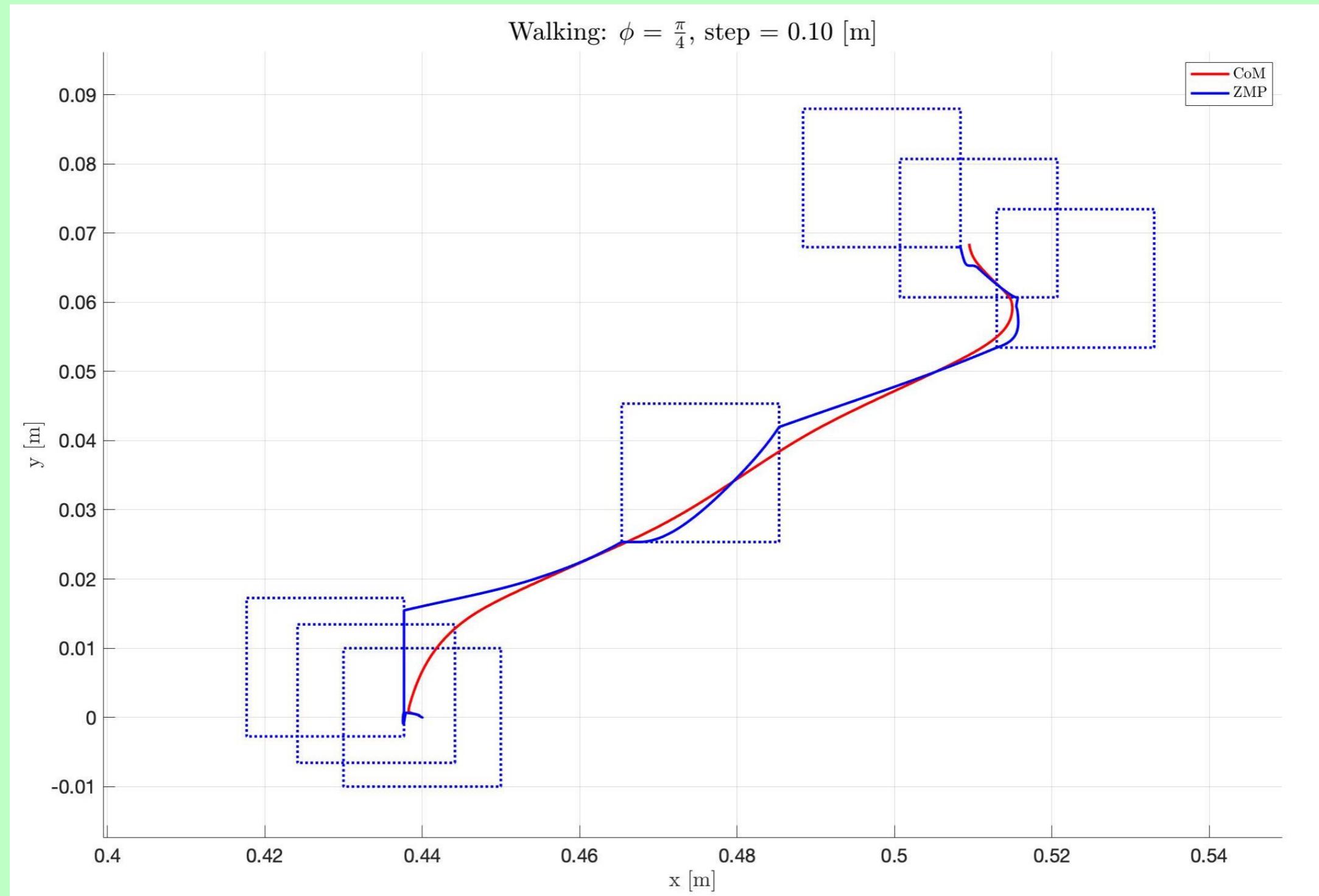
MATLAB



MATLAB

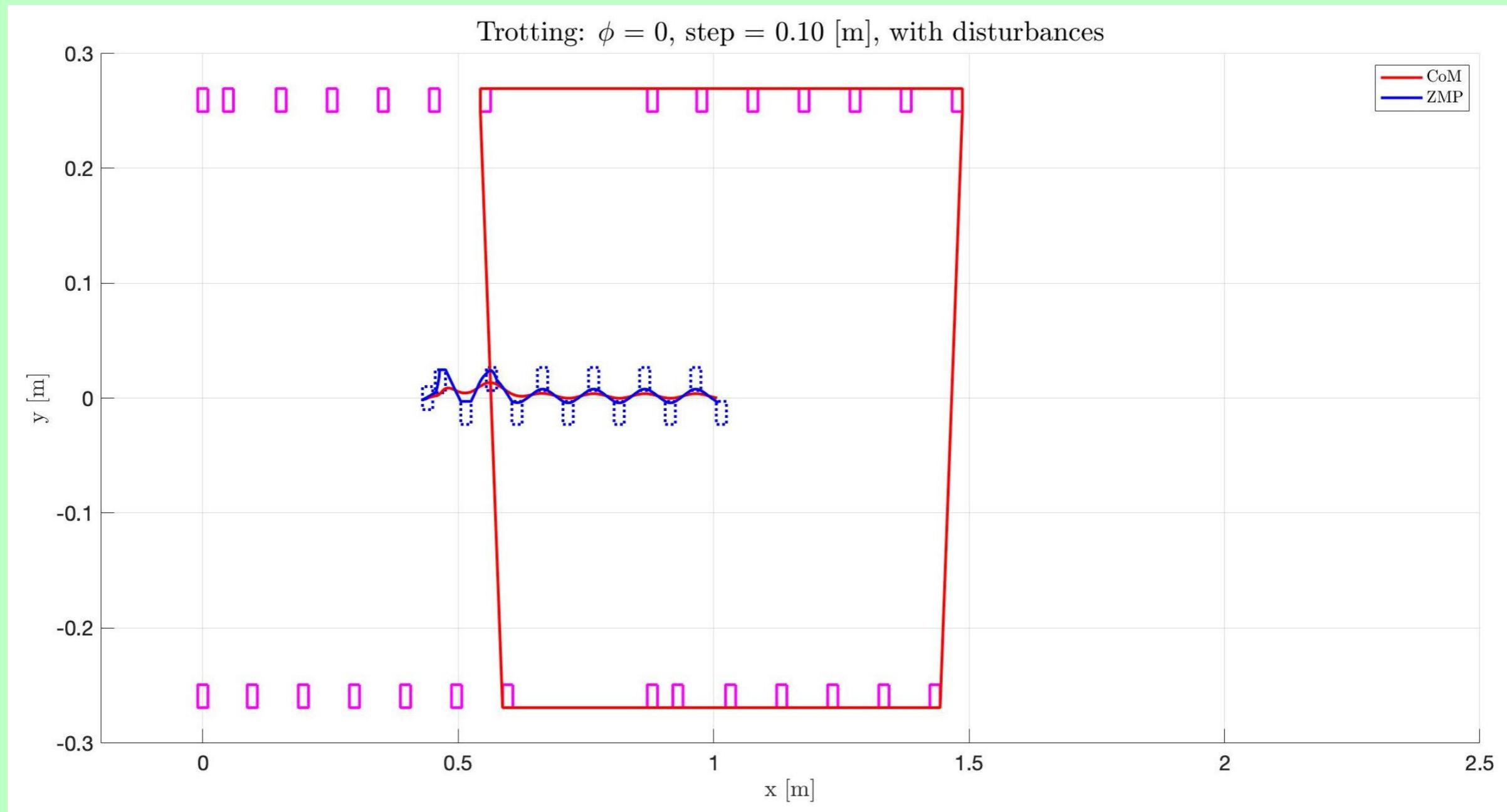


MATLAB



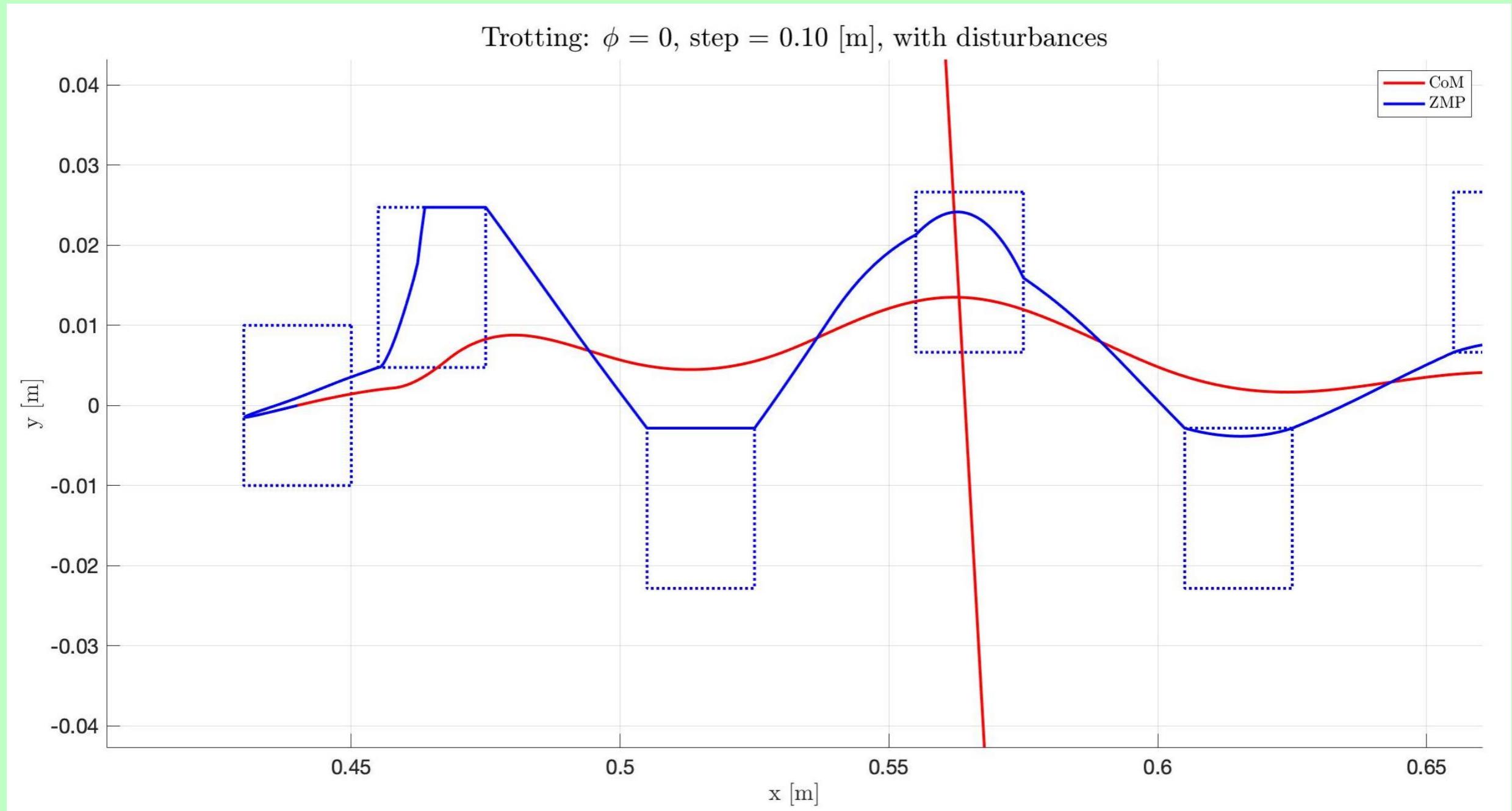
MATLAB

Disturb of 0.4 m/s^2 along y-axis
at the second step.



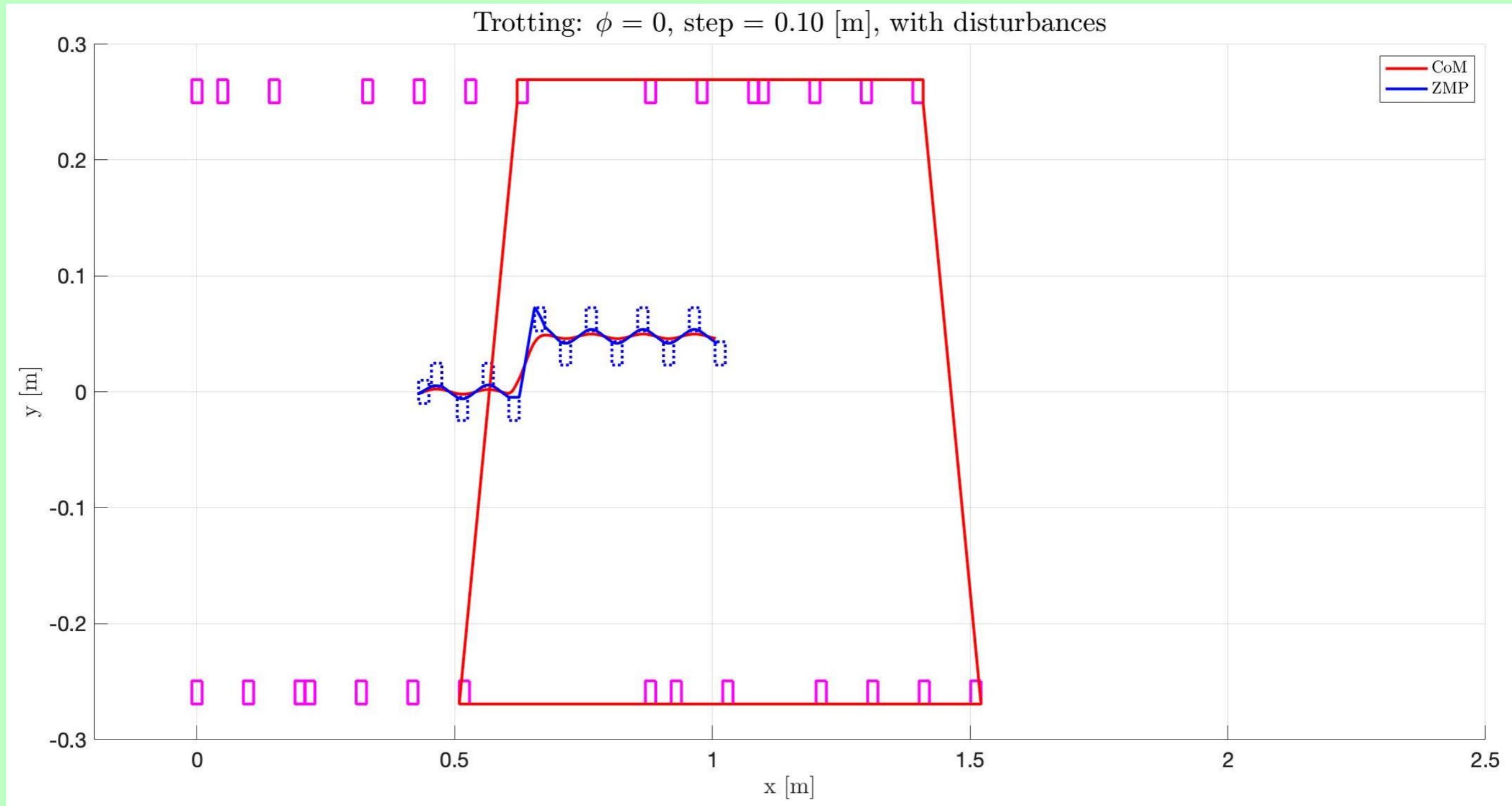
MATLAB

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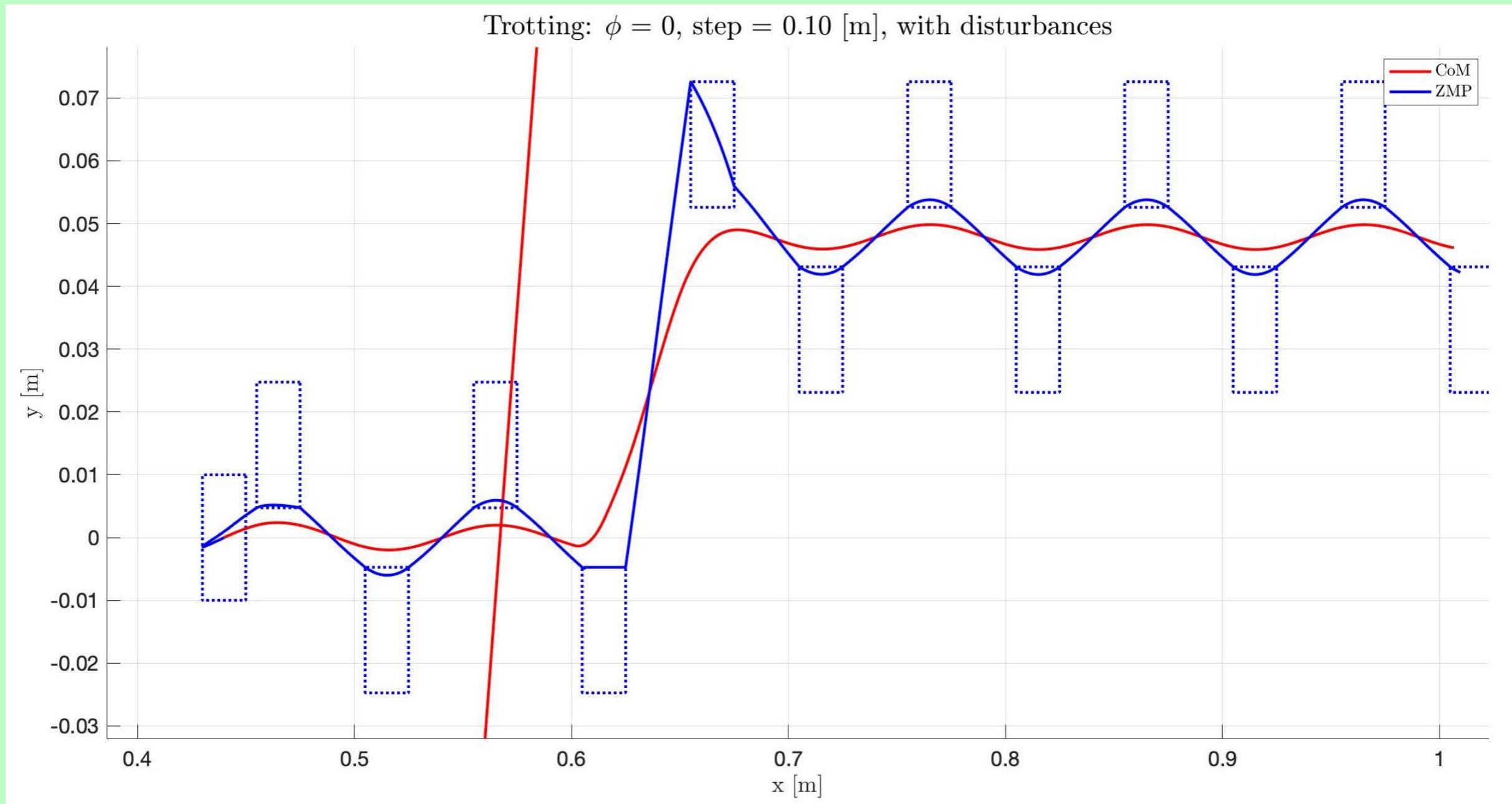
MATLAB

Disturb of 0.5 m/s^2 along y-axis
at the fifth step.



MATLAB

Disturb of 0.5 m/s^2 along y-axis
at the fifth step.

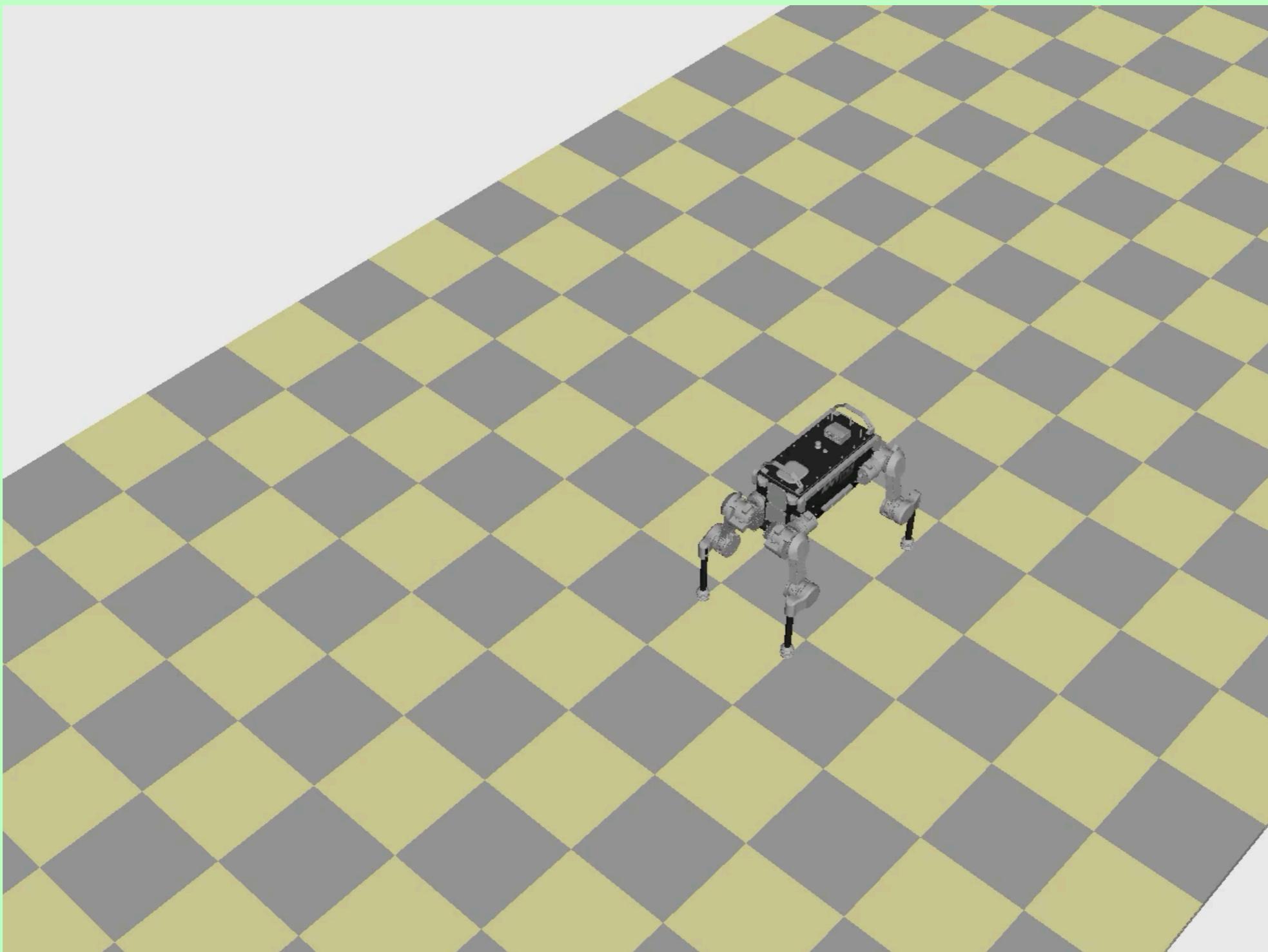


TROTTING:

$\phi = 0$

Step
size = 0.15 [m]

Step
timing = 0.8 [s]

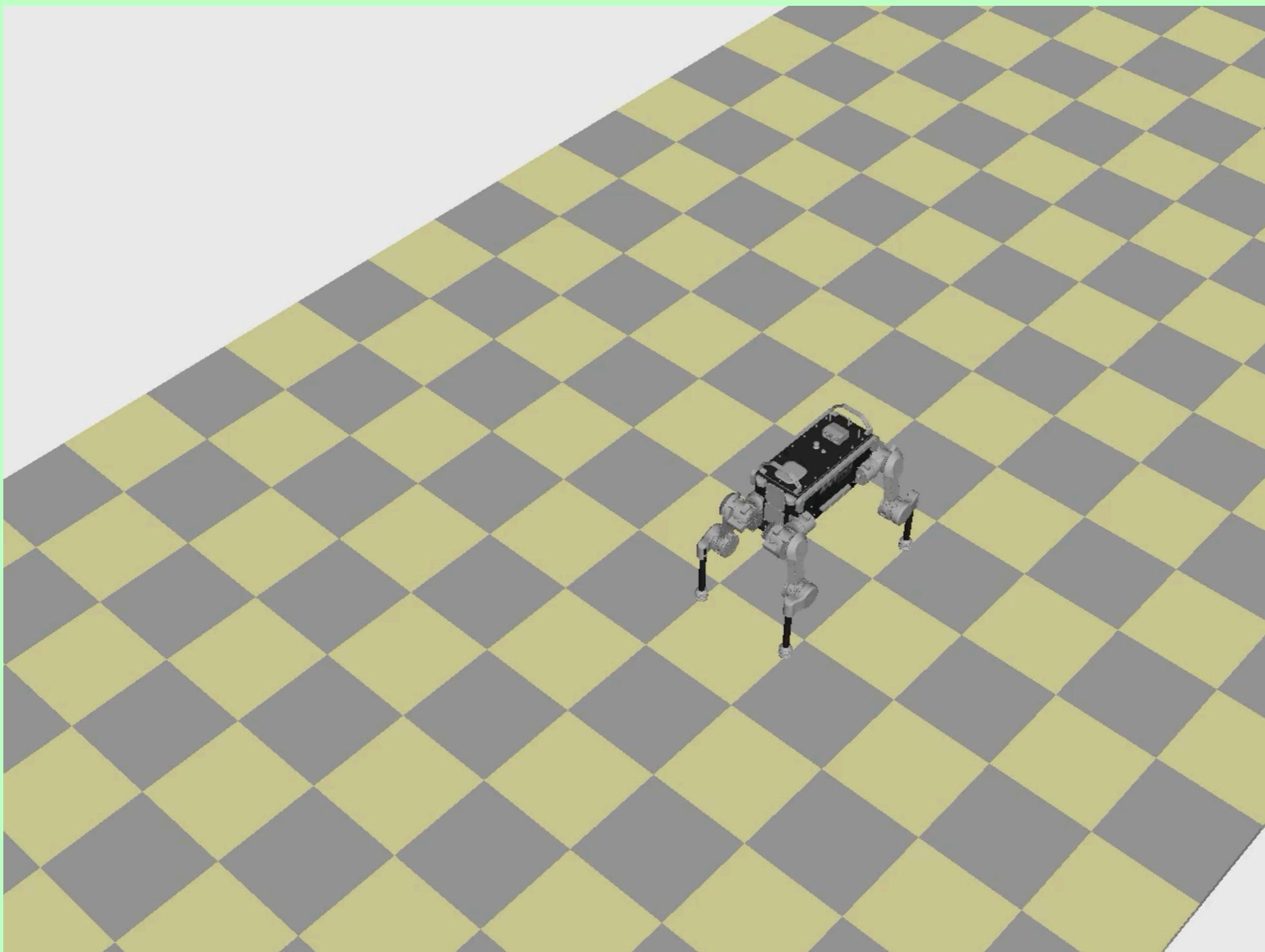


TROTTING:

$$\phi = \frac{\pi}{2}$$

Step
size = 0.15 [m]

Step
timing = 0.8 [s]

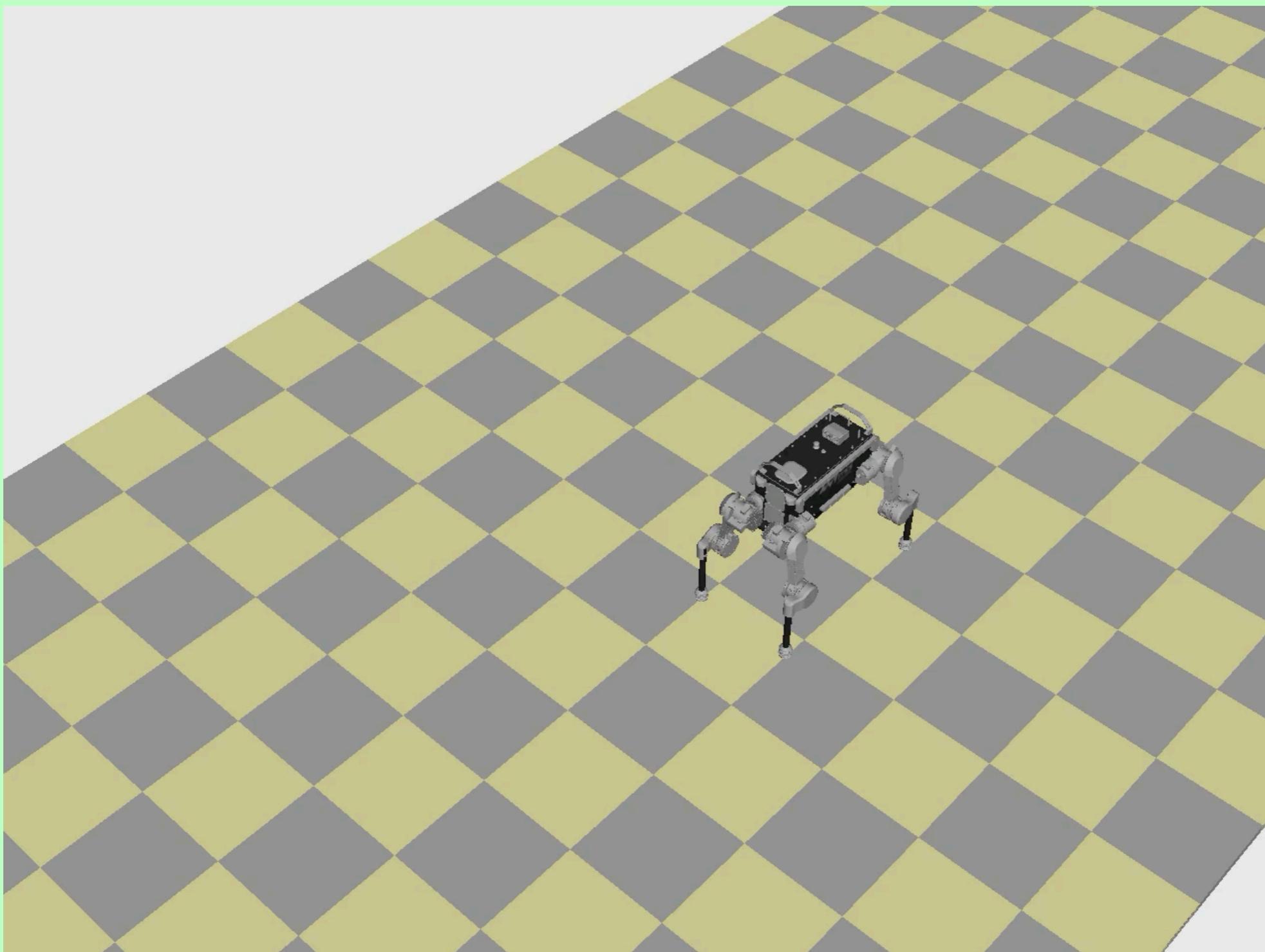


TROTTING:

$$\phi = \frac{\pi}{4}$$

Step
size = 0.10 [m]

Step
timing = 0.8 [s]

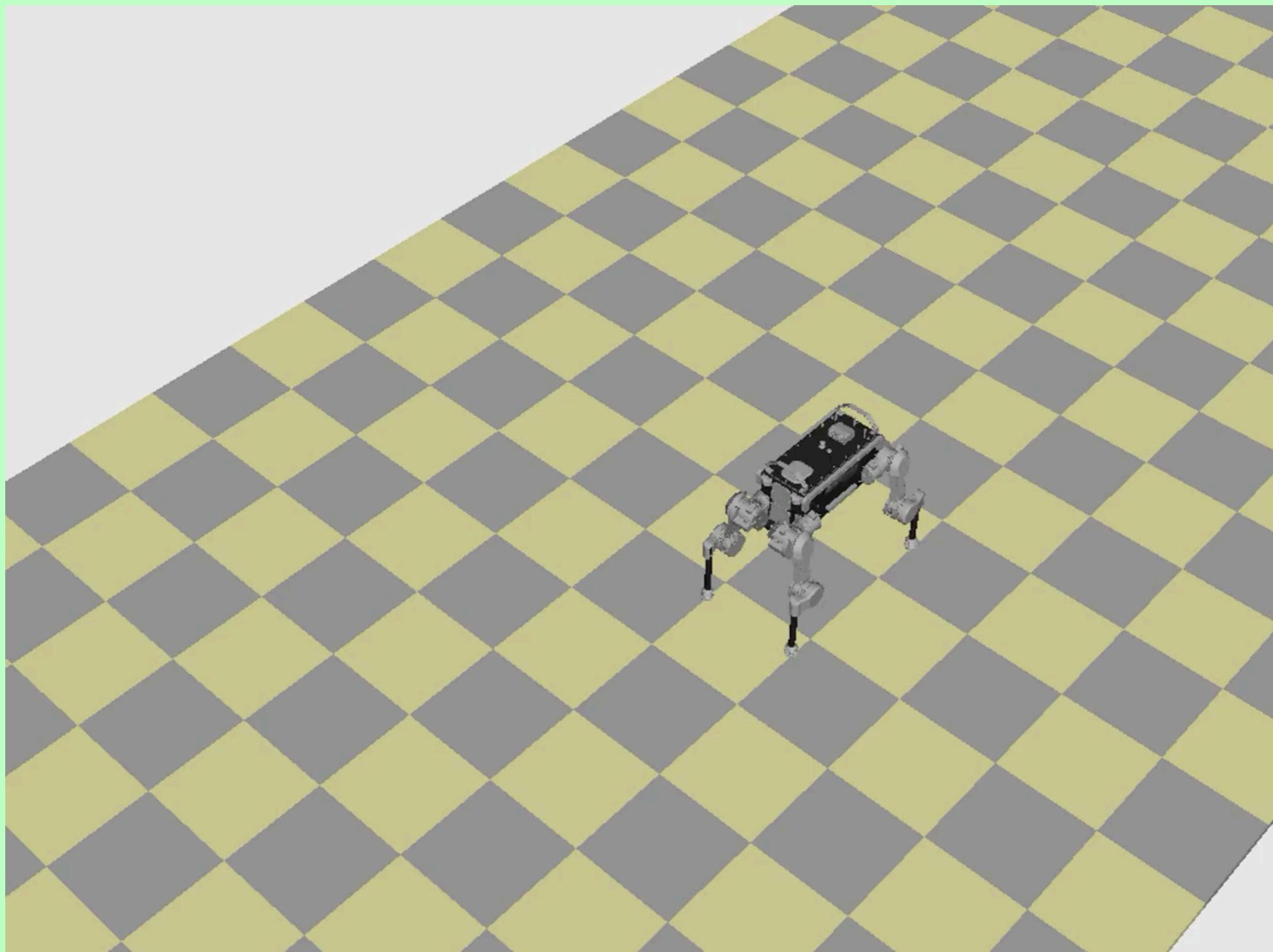


WALKING:

$\phi = 0$

Step
size = 0.10 [m]

Step
timing = 0.5 [s]



CONCLUSIONS

- The approach is very conservative due to the limitation on the ZMP region.
- We have performed dynamic simulation on DART and in absence of disturbances the nominal gait is well performed in any direction.
- The approach that was developed for the trotting gait has shown to be suitable also for walking gait.
- Different foot replacement policies can be investigated in future works.
- Further developments point to the goal of exploring gaits different from trotting and walking with a deeper exploitation of ZMP admissible region and more complex disturbance recovery.



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THANK YOU FOR THE ATTENTION

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