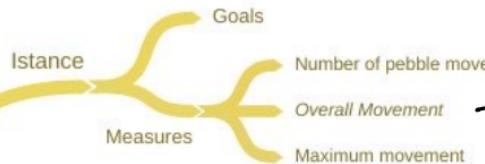


DS MINDMAPS

2^a PARTE

26 TH
10 ALGOs



$\text{OVERALL_MOVEMENT} = \sum_{p \in P} d_p(O(p), A(p))$
 $\text{MAXIMUM_MOVEMENT} = \max_{p \in P} d_p(O(p), A(p))$
 $\# \text{PEBBLE MOVED} = \sum_{p \in P} \mathbb{1}_{\{O(p) \neq A(p)\}}$
 $\text{NUH}(u) = \left\{ p \in P \mid O(p) \neq A(p) \right\}$

IND-MAX hardness

Movement on graph

5 th
1 Algo

IS
max IS
 $3\text{-SAT} \rightarrow \text{IND-MAX}$
Claim

$\{ \text{SODDISFAZIBILE} \Leftrightarrow \exists \text{ SOL PER IND-MAX DI COSTO } 1 \}$

INd-MAX approximability

Theorem hall's matching

$\Rightarrow \text{3 MATCHING} \leq \text{THEOREM HALL'S MATCHING}$

Lemma

$\forall U \subseteq V \subseteq G \quad |U| \cap N_G(U) \geq |U|$

Lemma

$\forall V \subseteq U \subseteq G \quad \exists U' \subseteq U \text{ INIZIALE T/C}$
 $d_G(U, U') \leq 1$

Theorem

$\text{SO UN MINISUBSET } U \subseteq G \text{ TROVABILE IN POI, T/AB}$
 $\text{ES SU CIRCA 90\%} \rightarrow \text{IND-MAX TROVABILE CON}$
 $\lambda\text{-ADDING GRAPH}$

ALGO



Vertex coloring
Valid vertex coloring
k-coloring
chromatic number

Delta+1 coloring ALGO

palette(v)

ALGO
 $\forall v \in V$ $c(v) = \min\{c_i \mid i \in \text{color}(v)\}$
 $\text{while } \exists v \in V \text{ non colorato}$
 $\quad \text{coloro } v \text{ con } c(v) + 1$
 $\quad \text{coloro } v \text{ con } c(v) + 1$
 $\quad \dots$

Claim

Ogni $v \in V$ ha almeno $\Delta+1$ colorazioni, cioè
 $|\text{color}(v)| \leq \Delta+1 \quad \forall v \in V$

Distributed Vertex coloring

2 Th
1 Algo

Mis Coloring ALGO

Complexity $O(\Delta \log \Delta \log n)$

Coloring and IS

Lemma MASSIMO $\Delta+1$ ITERAZIONI

ALGO
 $C := 1$
 $\text{WHILE } \exists v \in V \text{ non colorato}$
 $\quad \text{TECO MIS I DEI SOTTOSETTI INDUSTRIALI } \{v \mid v \in V \text{ non colorato}\}$
 $\quad \text{ASSEGNA } C \text{ AD OGNI } v \in I$
 $C := C + 1$

2 -Delta Coloring ALGO

Complexity $O(\log n)$ high prob
 $\text{palette}(v) = 2 \cdot \sigma(v)$
 candidates colors

Analysis
 $A(v), u(v), A'(v)$

ALGO
 UNIFORM
 $\text{STEGO } c_1 \text{ PER OGNI } v \in V$
 $\text{LETTA } c_2$
 $\text{SE } c_1 \neq c_2$
 $\quad \text{UNIFORM } c_1 \text{ E } c_2$
 $\quad \text{UNIFORM } c_1 \text{ E } c_2$

Prob(v accetta)
 $\text{prob}(v \text{ rigetta in log n fasi})$
 $\text{Prob(almeno un } v \text{ rigetta in log n fasi)}$
 $\text{prob(tutti accettano in log n fasi)}$

$\text{Prob}(v \text{ accetta } c_1) = \frac{1}{2} \text{ and } \frac{\Delta-1}{\Delta}$
 $\text{Prob}(v \text{ rigetta } c_1) > (1 - \frac{1}{2})^{\log n} = \frac{1}{2^{\log n}} = \frac{1}{n}$
 $\text{Prob}(v \text{ rigetta } c_2) < (1 - \frac{1}{2})^{\log n} = \frac{1}{2^{\log n}} = \frac{1}{n}$
 $\text{Prob(v rigetta } c_1 \text{ e } c_2) \geq 1 - \frac{1}{n}$

Mutex

2 Th 3 algo

Mutex problem

Liveness condition

Mutual Exclusion

No deadlock

No lockout

Bounded waiting

Bakery ALGO ticket

Complexity $2n$ R/W

```

ALGO
CHOOSING = TRUE
NUM = max{ $\sum_{i=1}^k$  NUMi, ..., NUMn} + 1
CHOOSING = FALSE
FOR i=0, ..., n-1 DO
    WAIT UNTIL CHOOSING = FALSE
    WAIT UNTIL NUMi > 0 OR NUMi = NUM
    NUMi = 0
    } ENTRY
    } EXIT
  
```

Mutual ex

Lemma 1 $\exists P \in CS \Rightarrow NUM_i > 0$

Lemma 2 $\exists P \in CS, NUM_k \neq 0, k \neq i \Rightarrow NUM_k > NUM_i$

Bounded waiting

no lock

Bounded space 2-processors mutex ALGO

Complexity 2 boolean R/W vars: w[0], w[1]

P_1 : case	$w[0]=1$
P_1 : case	$w[0]=0$
P_2 : case	$w[1]=0$
P_2 : case	$w[1]=1$

Mutual ex

no deadlock

no lock

Mutual ex

no deadlock

no lock

ALGO with Priority.

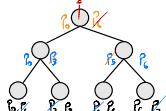
Complexity 3 boolean R/W: w[01], w[1], priority

```

P's case
1. w[0]=0
2. w[0]=1 or Priority>
3. (Priority>1)
4. (Priority>1) & w[1]=0
5. (Priority>1) & w[1]=1
6. End
7. (w[0]=0 & w[1]=1)
8. Priority>1
9. w[1]=0
  
```

Tournament tree
 $n=2^k$

$P_{i \in CS}$



Bounded space n-processor mutex ALGO
Complexity $3(n-1)$ boolean R/W

