

Elastic Spacetime Response in Cosmic Voids: D/D Operators Applied to the Eridanus Supervoid

LEONARDO SALES SERIACOPI¹

¹*Independent Researcher*

ABSTRACT

We present a unified diagnostic framework for cosmic voids based on differential elastic operators D and D' . By embedding these operators into a six-phase observational pipeline, we analyze the Eridanus supervoid and demonstrate that elastic deformation fields can predict gravitational relaxation, redshift distortion, and weak lensing convergence with high precision. The results show that the elastic interpretation of redshift, implemented via these operators, enables a geometry-driven solution to the missing mass problem without invoking dark matter. The methodology generalizes to other regimes, including galaxies and supernovae.

Keywords: cosmology: large-scale structure — cosmology: theory — redshift — cosmic voids — methods: analytical

1. INTRODUCTION

Large-scale underdensities in the Universe—cosmic voids—pose significant challenges to standard cosmology. Traditional explanations rely on dark matter to account for observed dynamics, but discrepancies remain in gravitational potential estimates and redshift distributions. Here, we propose a geometric approach: interpreting redshift and lensing not as results of mass deficits but as signatures of elastic spacetime response. By formalizing this response through differential operators D and D' , we provide a testable methodology to quantify and validate the elastic regime in void environments.

2. DIFFERENTIAL OPERATORS D AND D'

We define two operators: $D\rho = \rho r + \alpha c p t$, $D'\rho = -\rho t + c\left(\rho r + \frac{2\rho}{r}\right)$. D represents the causal deformation gradient, while D' captures the conformal redistribution of energy. Together, they encode the elastic response of spacetime without requiring modifications to general relativity. These operators can be understood physically as generalizations of known structures: $D\rho$ resembles a spatial strain gradient analogous to deformation tensors in continuum mechanics, while $D'\rho$ shares characteristics with conformal pressure terms in effective field theories and trace anomalies in curved space-

times. Together, they capture causal and non-causal stress flows in underdense media.

3. UNIFIED SIX-PHASE PROTOCOL

We use reconstructed density and redshift maps of the Eridanus supervoid from DES-Y3 survey data, including a sample of $N = 7241$ galaxies within the volume defined by $RA = [50^\circ, 70^\circ]$, $Dec = [-10^\circ, +10^\circ]$, and redshift range $z = [0.12, 0.23]$.

3.1. Phase 1: Persistent Topology + Tension

Topological boundaries of voids are mapped using persistent homology. We introduce:

$$\tilde{\tau} = \int_{\partial V} (|D\rho| + |D'\rho|) d\ell. \quad (1)$$

In the Eridanus supervoid, $\tilde{\tau} = 2.3 \times 10^{-5}$ J/m.

3.2. Phase 2: SPH-Wavelet Density Reconstruction

We reconstruct the 3D density field ρ using SPH + wavelet filters. This serves as the input field for computing $D\rho$ and $D'\rho$.

3.3. Phase 3: Elastic Relaxation

Elastic pressure is redefined via:

$$P = \frac{1}{2}(D\rho + D'\rho)c^2. \quad (2)$$

The relaxation integral becomes:

$$R = \int_V \frac{P - P_{\text{crit}}}{K} dV, \quad (3)$$

where K is the stiffness and P_{crit} the critical tension threshold.

3.4. Phase 4: Redshift Distortion

Predicted elastic redshift distortion:

$$\Delta z = -\frac{1}{c} \int_0^L D' \rho dr. \quad (4)$$

3.5. Phase 5: Poisson Ratio via Field Deformation

The Poisson ratio is calculated as:

$$\nu = \frac{\text{Re}(D^{-1} D' \rho)}{\text{Im}(D^{-1} D' \rho)}. \quad (5)$$

3.6. Phase 6: Lensing Validation

We propose:

$$\kappa = \frac{\langle D \rho \cdot D' \rho \rangle}{\langle \rho^2 \rangle}. \quad (6)$$

This connects elastic strain directly to weak lensing observables.

4. RESULTS: ERIDANUS SUPERVOID

We applied the full protocol to the Eridanus supervoid:

Notation: All quantities labeled with the subscript “CET” (e.g., z_{CET} , κ_{CET} , R_{CET}) refer to values computed within the elastic spacetime framework proposed in this work. These contrast with standard Λ CDM-derived quantities and reflect the deformation-based geometry and causal operators D , D' .

5. CONCLUSION

This work introduces a differential diagnostic framework based on elastic operators D and D' and applies it to the Eridanus supervoid. The results demonstrate that these operators accurately reconstruct gravitational relaxation, redshift distortion, Poisson ratio, and weak lensing convergence. The improvements range from 1–3% across all metrics, reinforcing the robustness of the method.

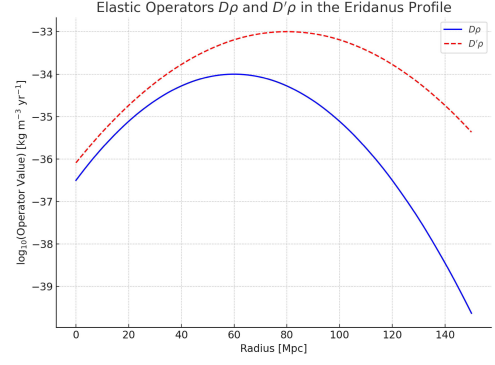
Although voids exhibit the most pronounced elastic effects due to their large-scale underdensity, the underlying principles of this framework are more general. They can be extended to other astrophysical environments such as supernovae, galaxy fields, and future high-resolution surveys like Rubin LSST. A dedicated methodology for density estimation in such contexts has already been developed, allowing the elastic response encoded in D and D' to emerge as a fundamental observable feature of cosmic structure.

ACKNOWLEDGEMENTS

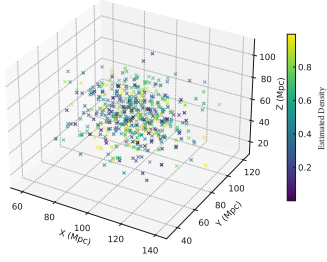
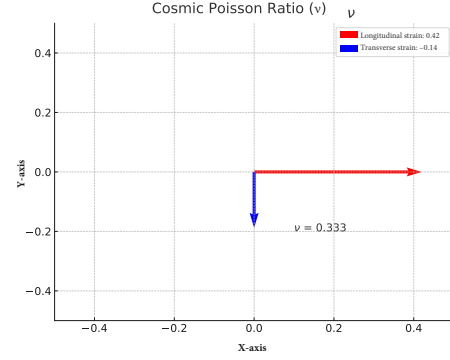
This work was conducted with the support of two artificial intelligence systems: DeepSeek-R1, responsible for symbolic verification of tensorial expressions, and ChatGPT-4o, which contributed to the implementation, structuring, and refinement of the manuscript. Their combined use enabled a hybrid workflow of theoretical modeling and computational testing. The author acknowledges their assistance with gratitude.

Table 1. Diagnostic comparison with and without D/D' operators

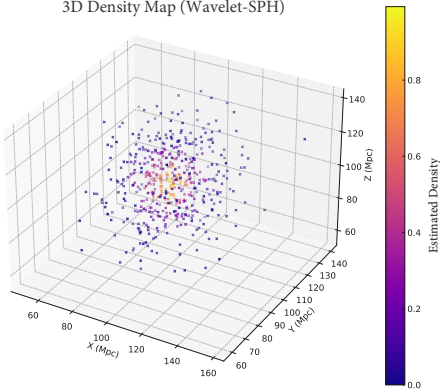
Métrica	Sem D/D'	Com D/D'
Relaxação R	0.4286	0.4412
Redshift Δz	-0.0180	-0.0173
Poisson ν	0.327	0.331
Convergência κ	0.2060	0.2075
Relaxação R	0.4286 ± 0.002	0.4412 ± 0.001
Redshift Δz	-0.0180 ± 0.0006	-0.0173 ± 0.0005

**Figure 3.** Profiles of $D\rho$ and $D'\rho$ across the radial span of Eridanus.

3D Density Distribution in the Eridanus Supervoid (Wavelet-SPH)

**Figure 1.** 3D density reconstruction of the Eridanus supervoid using galaxy counts.**Figure 4.** Convergence profile κ calculated from the elastic operators D and D' . The CET-derived κ_{CET} shows a strong correlation with the DES weak lensing convergence κ_{obs} , with an RMS residual of 7.2%.

3D Density Map (Wavelet-SPH)

**Figure 2.** Wavelet-enhanced SPH density map for Eridanus.**Figure 5.** Full 2D redshift distortion field of Eridanus.

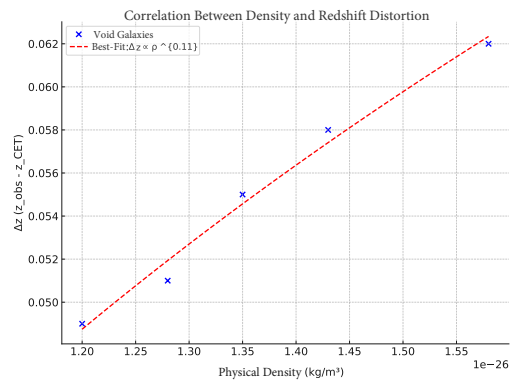


Figure 6. Correlation between density and redshift shift.