

HT No: 6



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Problema 1

Datos

$A = 7.60 \text{ cm}^2$
 $d = 1.80 \text{ mm}$
 $V = 20 \text{ V}$

a.) $V = Ed$
 $\frac{V}{d} = E \rightarrow \frac{20}{1.80 \times 10^{-3}} = 11.1 \text{ k V/m}$

b.) $\delta = \frac{Q}{A} = \frac{74.5 \times 10^{-12}}{7.60 \times 10^{-4}} = 98.4 \text{ nC/m}^2$

c.) $C = \frac{\epsilon_0 A}{d} = \frac{(8.85 \times 10^{-12})(7.60 \times 10^{-4})}{(1.80 \times 10^{-3})} = 3.74 \text{ pF}$

d.) $C = \frac{Q}{V} \rightarrow Q = CV$
 $3.74 \times 10^{-12} (20) = Q$
 $\hookrightarrow Q = 74.8 \text{ pC}$

a.) 11.1 k V/m
b.) 98.4 n C/m²
c.) 3.74 pF
d.) 74.8 pC

Problema 2.

Dados:

$$A = 10 \text{ cm}^2$$

$$d = 3 \text{ mm}$$

$$V = 200 \text{ volt}$$

$$a.) q = \frac{\epsilon_0 A V}{d} = \frac{(8.85 \times 10^{-12})(10 \times 10^{-4})(200)}{(3 \times 10^{-3})} = 590 \text{ pF}$$

$$b.) q' = \frac{k \epsilon_0 A V}{d} = \frac{5(8.85 \times 10^{-12})(10 \times 10^{-4})(200)}{(3 \times 10^{-3})} = 2.95 \times 10^{-9}$$

$$q' - q = 2.95 \text{ n} - 590 \text{ p} = 2.36 \text{ nC}$$

d.)

$$\text{Antes. } C = \frac{Q}{V}$$

$$C = Q$$

$$\text{Después. } C' = \frac{Q}{V'} \rightarrow C = \frac{k \epsilon_0 A}{d}$$

$$C = Q \cdot \frac{Q}{k} = \frac{\epsilon_0 A}{d}$$

$$Q = Q$$

$$C = \frac{Q}{V}$$

$$C = \frac{Q}{V'}$$

$$kV = V'$$

$$V' = (200)(5)$$

$$V' = 1000$$

$$V_T = V' - V$$

$$V_T = 1000 - 200$$

$$V_T = 800$$

$$a.) 590 \text{ pF}$$

$$b.) 2.36 \text{ nC}$$

$$d.) 800 \text{ volt}$$

Problema 3

Datos

$$d = 1.50 \text{ cm}$$

$$A = 25 \text{ cm}^2$$

$$\Delta V = 250 \text{ V}$$

$$K = 80$$

$$C = \frac{K \epsilon_0 A}{d} = \frac{(80)(8.85 \times 10^{-12})(25 \times 10^{-4})}{(0.0150)}$$

$$C = 116 \text{ pF}$$

a.) 1.475×10^{-12} (Sin dieléctrico)
 $\rightarrow Q = C \Delta V = (1.475 \times 10^{-12})(250)$
 $Q = 369 \times 10^{-12} \text{ C}$

b.) (con dieléctrico)

$$C = \frac{Q}{\Delta V} \rightarrow \Delta V = \frac{Q}{C} \rightarrow \frac{369 \times 10^{-12}}{116 \times 10^{-12}} = 3.12 \text{ Volt}$$

c.) $U = \frac{1}{2} Q \Delta V = \frac{1}{2} (369 \times 10^{-12})(3.12 - 250)$

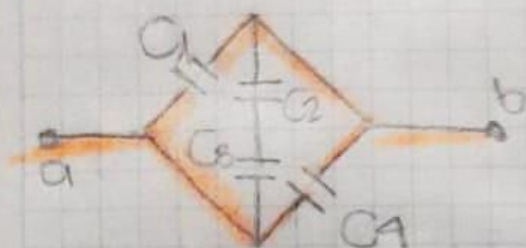
$$U = -4.55 \times 10^{-8} \text{ J} \approx -45.5 \text{ nJ}$$

a.) 369 pC

b.) 116 pF, 3.12 Volt

c.) -45.5 nJ

Problema 4.



$$C_1 = 4 \mu F$$

$$V_{ab} = 100 \text{ V}$$

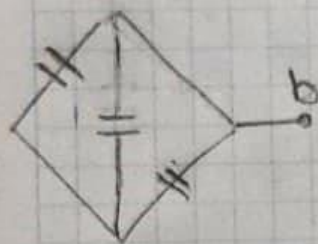
$$C_2 = 7 \mu F$$

$$C_3 = 5 \mu F$$

$$C_4 = 6 \mu F$$

→ En serie C_2 y C_3

$$C_{23} = \left[\frac{1}{C_2} + \frac{1}{C_3} \right]^{-1} \rightarrow \left[\frac{1}{7 \times 10^{-6}} + \frac{1}{5 \times 10^{-6}} \right]^{-1} = 2.92 \mu F$$



→ En paralelo

$$C_{eq} = C_1 + C_{23} + C_4$$

$$C_{eq} = 4 \mu + 2.92 \mu + 6 \mu$$

$$C_{eq} = 12.92 \mu F$$

$$U_{eq} = \frac{1}{2} C \Delta V^2$$

$$U_{eq} = \frac{1}{2} (12.92 \mu)(100)^2$$

$$U_{eq} = 64.6 \text{ mJ}$$

* $C_1 // C_{23} // C_4 \rightarrow$ el voltaje es el mismo

$$V_1 = V_{23} = V_4 = 100 \text{ Voltios}$$

$$C_{23} = \frac{Q}{V} = C_{23} V = Q_{23} \rightarrow Q_{23} = 292 \mu C$$

$$C_1 = \frac{1}{2} C \Delta V^2 = \frac{1}{2} (4 \mu)(100)^2 = 20 \text{ mJ}$$

$$C_2 = \frac{1}{2} C \Delta V^2 = \frac{1}{2} (7 \mu)(41.7)^2 = 6.09 \text{ mJ}$$

$$C_3 = \frac{1}{2} C \Delta V^2 = \frac{1}{2} (5 \mu)(58.4)^2 = 8.52 \text{ mJ}$$

$$C_4 = \frac{1}{2} C \Delta V^2 = \frac{1}{2} (6 \mu)(100)^2 = 30 \text{ mJ}$$

* Como C_2 y C_3 son en serie

$$Q_{23} = Q_2 = Q_3 = 292 \mu C$$

$$C_2 = \frac{Q}{V} \rightarrow V_2 = \frac{Q_2}{C_2}$$

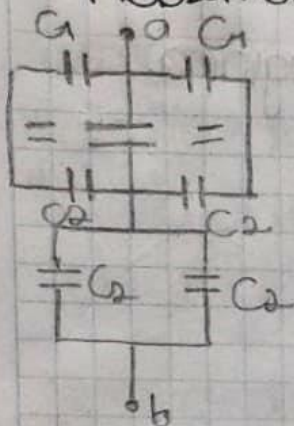
$$V_2 = 41.71 \text{ V}$$

$$C_3 = \frac{Q}{V} \rightarrow V_3 = \frac{Q_3}{C_3}$$

$$V_3 = 58.4 \text{ V}$$

- a.) $C_{eq} = 12.92 \mu F$
- b.) $V_2 = 41.71 \text{ V}$, $V_3 = 58.4 \text{ V}$
- c.) $U_1 = 20 \text{ mJ}$, $U_2 = 6.09 \text{ mJ}$
- ☒ $U_3 = 8.52 \text{ mJ}$, $U_4 = 30 \text{ mJ}$
- $U_{eq} = 64.6 \text{ mJ}$

Problema 5



$$\begin{aligned} C_1 &= 5 \text{ MF} \\ C_2 &= 10 \text{ MF} \\ C_3 &= 2 \text{ MF} \end{aligned}$$

Paralelo C_2 y C_4

$$\begin{aligned} C_2 &= C_2 + C_4 \rightarrow (10 \text{ MF} + 10 \text{ MF}) \\ C_2 &= 20 \text{ MF} = V = 13.92 \text{ V} \\ Q &= 278.4 \text{ C} \end{aligned}$$

En Serie C_1 y C_2

$$\begin{aligned} C_{12} &= \left(\frac{1}{C_1} + \frac{1}{C_2} \right)^{-1} = \left(\frac{1}{5 \text{ MF}} + \frac{1}{20 \text{ MF}} \right)^{-1} \\ C_{12} &= 3.33 \text{ MF} \end{aligned}$$

En Paralelo C_{12} y C_3

$$\begin{aligned} C_{123} &= C_{12} + C_3 \\ C_{123} &= 5.66 \text{ MF} \end{aligned}$$

En Serie C_{123} y C_5

$$C_{eq} = \left(\frac{1}{C_{123}} + \frac{1}{C_5} \right)^{-1}$$

$$C_{eq} = \left(\frac{1}{5.66 \text{ MF}} + \frac{1}{20 \text{ MF}} \right)^{-1}$$

Carga en $C_3 = 83.6 \text{ MC}$

$$C_3 = Q/V_3$$

$$V_3 = \frac{Q_3}{C_3} = \frac{(83.6 \times 10^{-6})}{2 \times 10^{-6}}$$

$$V_3 = 41.8 \text{ V}$$

$$U = \frac{1}{2} \cdot C \cdot V^2$$

$$U = \frac{1}{2} (6.04) (60)^2$$

$$U = 10.9 \text{ mJ}$$

C_{12} y C_3 en Paralelo

$$\begin{aligned} V_{12} &= V_3 = V_{123} = 41.8 \text{ V} \\ C_{123} &= \frac{Q_{123}}{V_{123}} \end{aligned}$$

$$\begin{aligned} C_{123} &= V_{123} = \frac{Q_{123}}{V_{123}} \\ Q_{123} &= (2.66 \times 10^{-6}) (41.8) \\ &= 3.62 \times 10^{-6} \text{ C} \end{aligned}$$

C_{123} y C_5 en Serie

$$Q_{123} = Q_5 = 3.62 \times 10^{-6}$$

$$C_{eq} = \frac{Q_{eq}}{V_{eq}} \rightarrow V_{eq} = \frac{Q_{eq}}{C_{eq}} = \frac{3.62}{6.04}$$

$$V = 59.93 \text{ V} \approx 60 \text{ V}$$

a.) $C = 6.04 \text{ MF}$

b.) $V = 60 \text{ V}$

c.) $U = 10.9 \text{ mJ}$