

Getting in Between People and Their Measurement

Psychometric Evaluation of (Intensive) Longitudinal Data



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👉 Introduction to ILD

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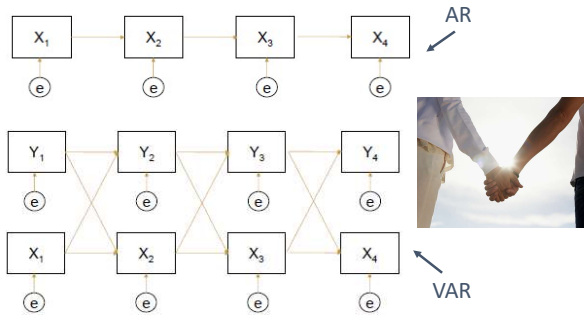
Experience Sampling

- Experience Sampling Methodology (ESM)
 - (or Ambulatory Assessment, Ecological Momentary Assessment)
- Many subjects
- Repeatedly fill in questionnaires (> 50 x)
- Investigate dynamics of psychological constructs/factors in daily life
- May be used, e.g., for personalized therapy



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Experience Sampling



→ The use of ESM designs tremendously increased in the last years...

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Experience Sampling

- Psychological constructs are usually latent (unobserved)
- Assessment via self-report measures in the form of questionnaires



- We have to worry about the same things we always have to worry about with questionnaires, and it is more challenging.
- Generally, measurement models can be evaluated with (different types of) factor analysis

$$y_i = \tau + \Lambda \eta_i + \epsilon_i$$
- The measurement model(s) for an ESM study at hand can differ compared to cross-sectional studies and other ESM studies!

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Experience Sampling

- Chapter 4 from the "Free ESM Handbook" gives guidelines on how to construct questionnaires for ESM studies (think of **questionnaire length**, **wording**, **response scale**, **order of questions**...).



- In this lecture, we'll focus on **how to evaluate your measurements** after the data has been collected.
- Per topic, we'll start by recapping some of the basics of proper measurement in **cross-sectional** and **panel data**.
- We'll then extend the insights from "traditional" data types to **ILD** and will highlight what additional steps and checks you need to do with this new type of data.

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Outline

Part 1 ~14:05-14:50

- Introduction to Different Data Types
- Factor Models
- Invariance

Break ~14:50-15:00

Part 2 ~15:00-15:50

- Discussion
- Reliability

Break~15:50-16:00

Part 3 ~16:00-17:00

- Lab
- If there is time: Exploring Non-Invariance for ILD + Discussion

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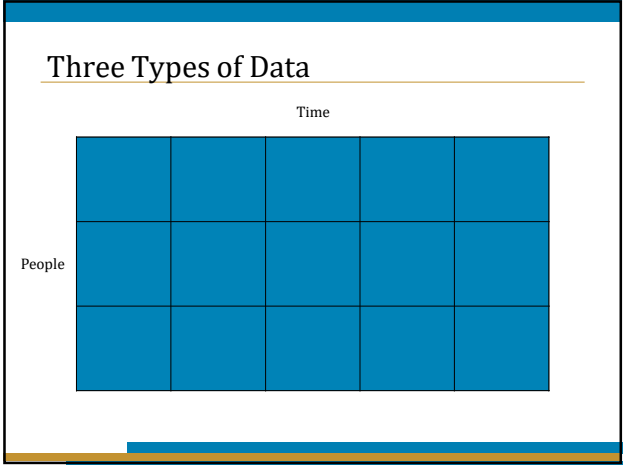
Introduction to Different Data Types

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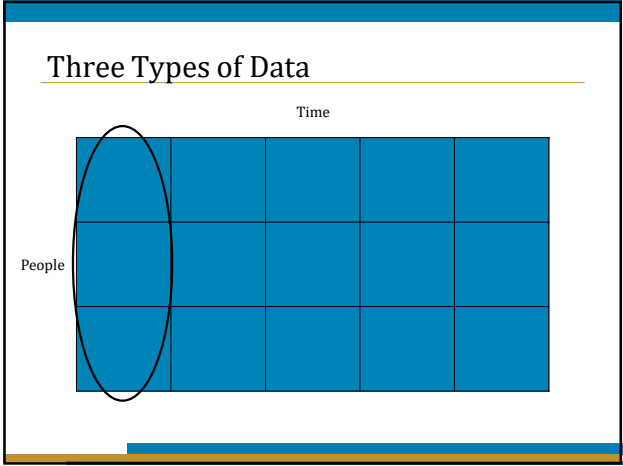
Introduction to Different Data Types

- Questionnaires applied to three types of data (mainly)
 - Cross-sectional
 - Panel
 - Intensive Longitudinal

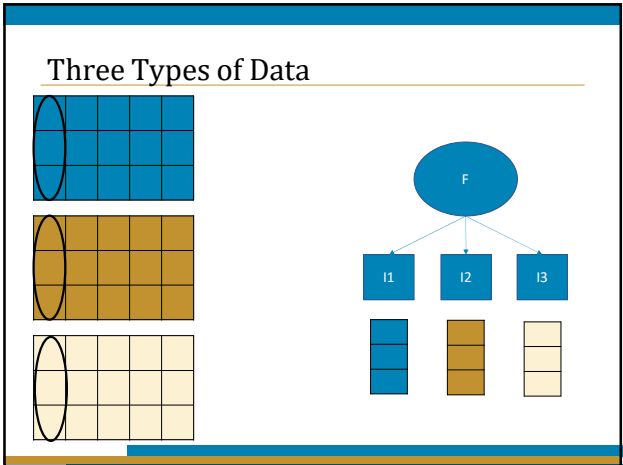
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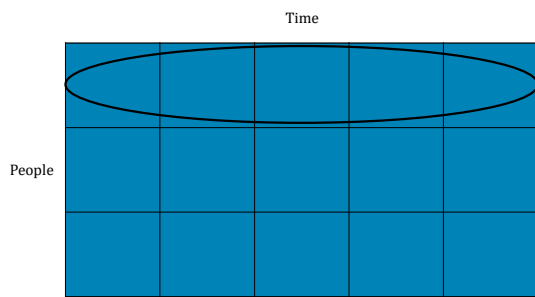


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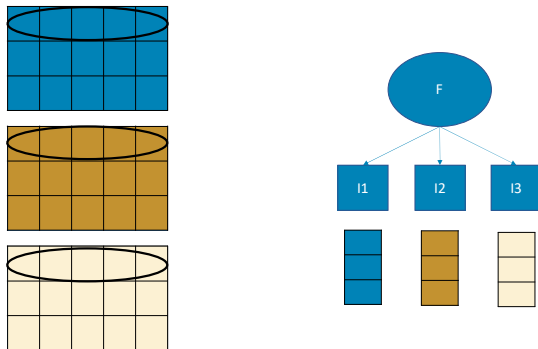
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Three Types of Data



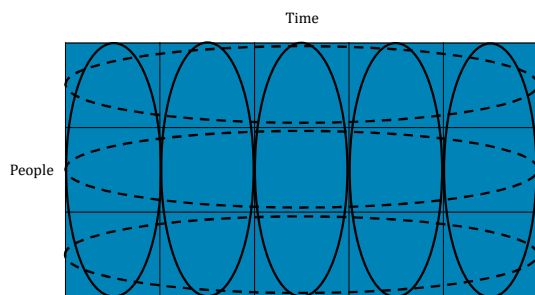
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Three Types of Data



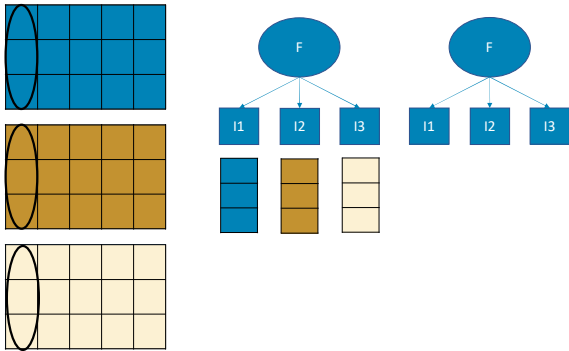
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Three Types of Data



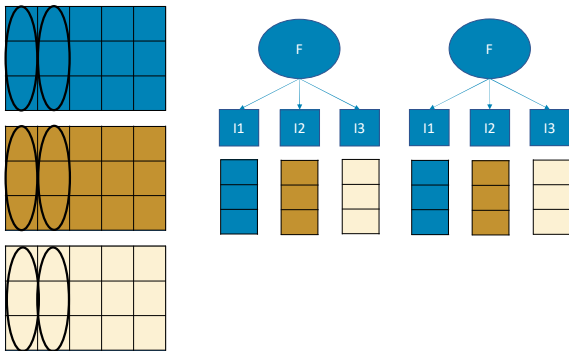
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Three Types of Data



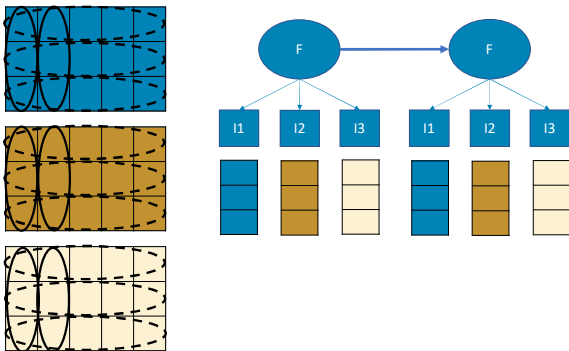
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Three Types of Data



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Three Types of Data



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Introduce Cross-Sectional & Panel Data

To what extent do the following statements apply to you?	1-7
I often check the location of security cameras.	
I count the number of security guards.	
I sense whether someone is an easy target.	
I enjoy getting others in trouble.	
I enjoy other people's pain.	
I dream about stealing money.	
I do not sympathize with others.	
I root for the bad guy in movies.	
I have been told that I am not a good roommate.	
I am more important than others.	
I am bored by other people.	
I often walk around naked outside.	
I often bully/bullied my siblings.	
I don't have many friends.	
Money is more important than relationships.	
I would hurt others to get what I want.	



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Introduce ILD

Question	0-100
How much does the following apply to you: I can do anything	
How much does the following apply to you: I don't fail	
How much does the following apply to you: If something bad happens, it's someone else's fault	
How much does the following apply to you: I'm smarter than other people	
How much does the following apply to you: I avoid making the mistakes other people make	
How much does the following apply to you: I would definitely hire myself	
How much does the following apply to you: I'm better looking than others	



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Psychometrics

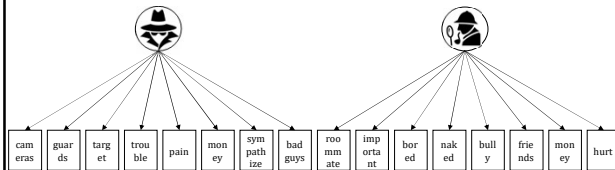
- Factor model
 - Do items measure what they are expected to measure?
 - It allows distinguishing the amount of variance in each item that is due to the common factor and the remaining error variance.
- Invariance
 - Is all systematic variability in item scores attributable to the psychological construct of interest?
 - Or is there variability due to group membership?
 - Does the factor model differ across groups?
- Reliability
 - Determining the reliability of assessing between-person differences.
 - When we have multiple items that measure the same underlying construct, internal consistency can be used as a measure of reliability.

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Factor Model

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Factor Model



- Allows to investigate whether items that are expected to measure a factor indeed measure the factor.
- Allows distinction between item variance that is due to the **common factor** and **unique item variance**.
- You can think of factor analysis as regressing item scores on the latent factors. Regression weights are called loadings.

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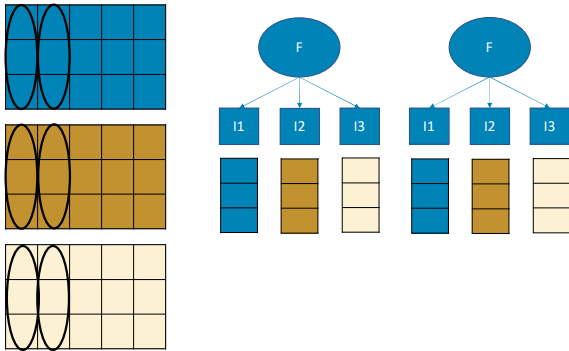
Factor Model Cross-Sectional Data

Regression notation:

$$y_i = \tau + \Lambda \eta_i + \epsilon_i$$

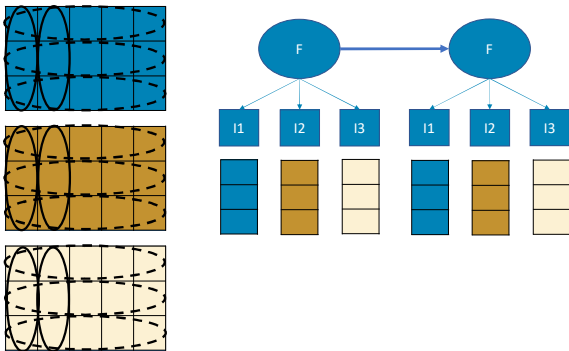
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Factor Model for Panel Data



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Factor Model for Panel Data



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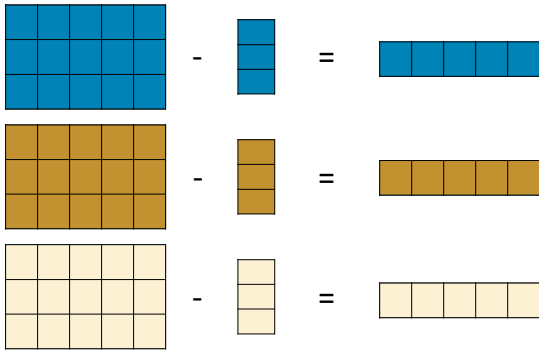
Factor Model Panel Data

Regression notation:

$$y_{i,t} = \tau + \Lambda \eta_{i,t} + \epsilon_{i,t}$$

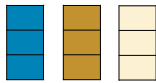
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Multilevel



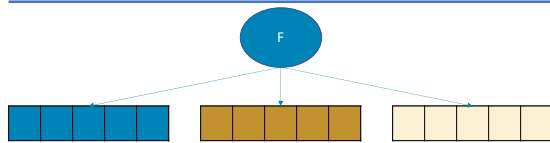
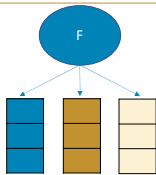
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Multilevel



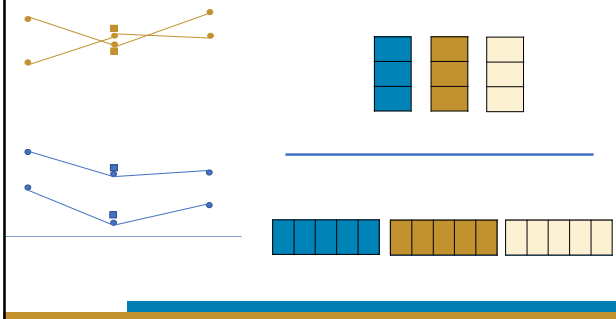
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Multilevel



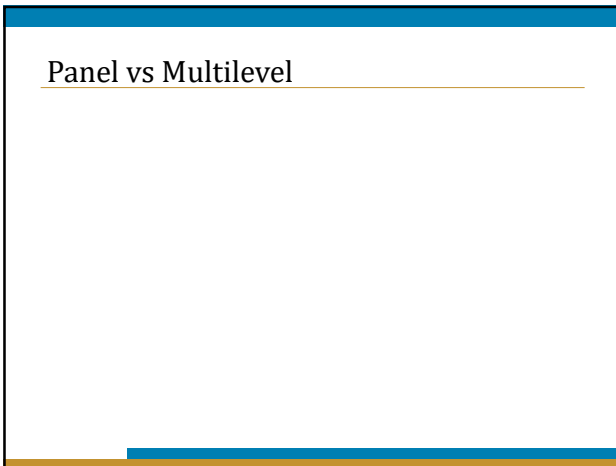
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Multilevel



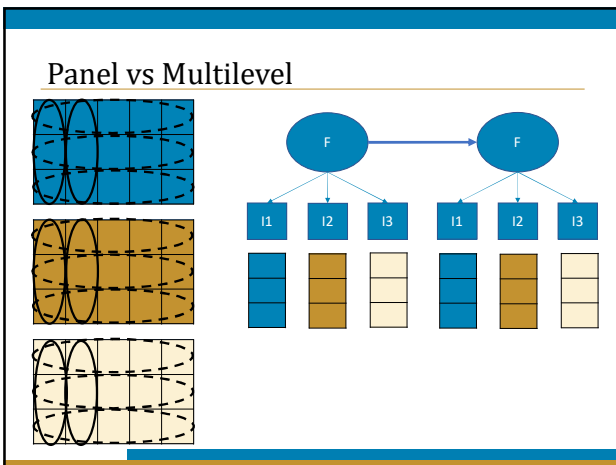
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Panel vs Multilevel



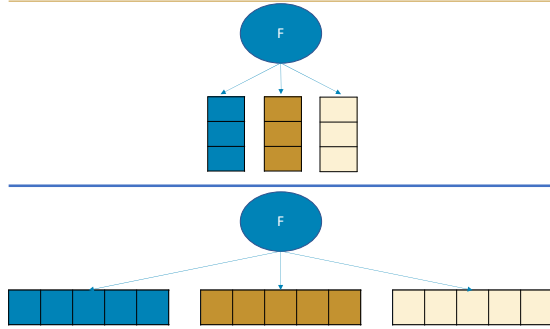
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Panel vs Multilevel



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Panel vs Multilevel



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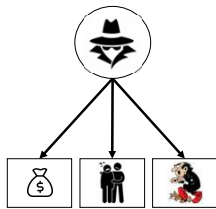


Measurement Invariance

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Measurement Invariance

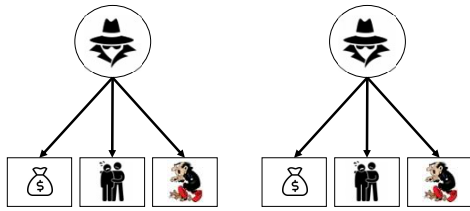
Different **levels** of invariance (that build up on each other) need to hold for valid between-group comparisons of the latent factor.



I dream about stealing money.
I do not sympathize with others.
I root for the bad guy in movies.

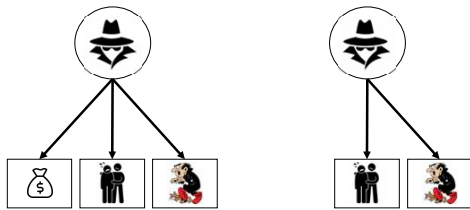
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Configural/Pattern Invariance



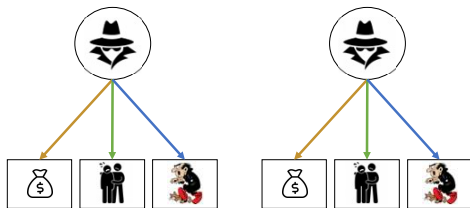
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Configural/Pattern Invariance



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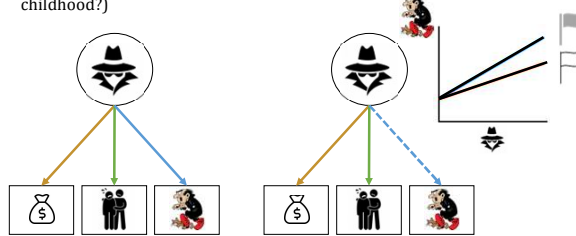
Loading Invariance



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Metric invariance

- Identifying with the bad guy is a worse indicator of *criminal-mindedness* in the white country; more other reasons for that (empathy for bad childhood?)

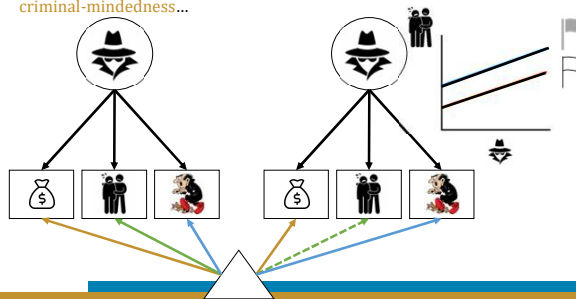


- If we ignore this, then we might misinterpret differences in *item scores* as differences in *criminal-mindedness*, although they are at least partly induced by differences in the regression weights.

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Scalar invariance

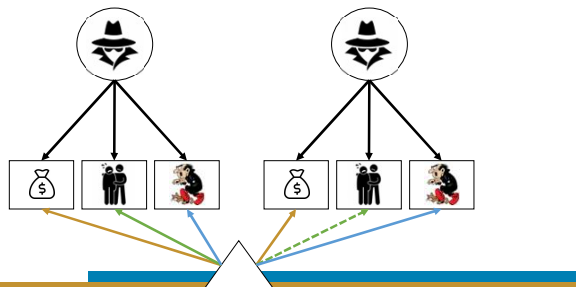
- One (perhaps very individualistic) country scores generally lower on *sympathizing with others*, regardless of the *criminal-mindedness*.
- Again: differences in item scores would be misinterpreted as differences in *criminal-mindedness*...



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Partial invariance

- You can allow for small differences in loadings and intercepts across groups!
- You will see that in the lab session.



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Regression Notation

- For cross-sectional data

$$y_{i,g} = \tau_g + \Lambda_g \eta_{i,g} + \epsilon_{i,g}$$

- For (intensive) longitudinal data

$$y_{i,t} = \tau_{i,t} + \Lambda_{i,t} \eta_{i,t} + \epsilon_{i,t}$$

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Invariance for longitudinal data

		Person	
		No restrictions	Invariance constraints on the measurement model
Time	No restrictions	$y_{i,t} = \tau_{i,t} + \Lambda_{i,t} \eta_{i,t} + \epsilon_{i,t}$ No invariance over time and subjects	$y_{i,t} = \tau_i + \Lambda_i \eta_{i,t} + \epsilon_{i,t}$ No invariance over time Measurement invariance over subjects
	Invariance constraints on the measurement model	$y_{i,t} = \tau_i + \Lambda_i \eta_{i,t} + \epsilon_{i,t}$ No invariance over subjects Measurement invariance over time	$y_{i,t} = \tau + \Lambda \eta_{i,t} + \epsilon_{i,t}$ Measurement invariance over time and subjects

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Invariance for longitudinal data

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Invariance for longitudinal data

		Person	
		No restrictions	Invariance constraints on the measurement model
Time	No restrictions	$y_{Li} = \tau_{Li} + \Lambda_{Li} \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over time and subjects</p>	$y_{Li} = \tau_i + \Lambda_i \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over time Measurement invariance over subjects</p>
	Invariance constraints on the measurement model	$y_{Li} = \tau_i + \Lambda_i \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over subjects Measurement invariance over time</p>	$y_{Li} = \tau + \Lambda \eta_{Li} + \varepsilon_{Li}$ <p>Measurement invariance over time and subjects</p>

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Invariance for longitudinal data

		Person	
		No restrictions	Invariance constraints on the measurement model
Time	No restrictions	$y_{Li} = \tau_{Li} + \Lambda_{Li} \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over time and subjects</p>	$y_{Li} = \tau_i + \Lambda_i \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over time Measurement invariance over subjects</p>
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Invariance for longitudinal data

This model is not identified.
We can't use this as a baseline.

		Person	
		No restrictions	Invariance constraints on the measurement model
Time	No restrictions	$y_{Li} = \tau_{Li} + \Lambda_{Li} \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over time and subjects</p>	$y_{Li} = \tau_i + \Lambda_i \eta_{Li} + \varepsilon_{Li}$ <p>No invariance over time Measurement invariance over subjects</p>
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Invariance for longitudinal data

		Person	
		No restrictions	Invariance constraints on the measurement model
Time	No restrictions	$y_{i,t} = \tau_{i,t} + A_{i,t} \eta_{i,t} + \varepsilon_{i,t}$ <p>No invariance over time and subjects</p>	$y_{i,t} = \tau_i + A_{i,t} \eta_{i,t} + \varepsilon_{i,t}$ <p>No invariance over time Measurement invariance over subjects</p>
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We could start by assuming invariance over time and compare a model with and without restrictions across persons.

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Invariance for longitudinal data

		Person	
		No restrictions	Invariance constraints on the measurement model
Time	No restrictions	$y_{i,t} = \tau_{i,t} + A_{i,t} \eta_{i,t} + \varepsilon_{i,t}$ <p>No invariance over time and subjects</p>	$y_{i,t} = \tau_i + A_{i,t} \eta_{i,t} + \varepsilon_{i,t}$ <p>No invariance over time Measurement invariance over subjects</p>
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We could start by assuming invariance over persons and compare a model with and without restrictions across time.

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Invariance for longitudinal data

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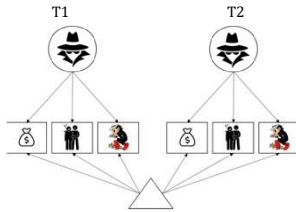
Often unrealistic.

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Invariance for longitudinal data

- For Panel Data: You can still simply run pairwise comparisons.
- For ILD: This becomes too much!!



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Invariance for ILD

- Alternative to testing: Consider intensive longitudinal data as **cross-classified** (McNeish et al. 2020).
- He builds up on multilevel analysis but now lets observations be nested in both individuals and time, resulting in two variance terms.

	ID = 1	ID = 2	ID = 3
T = 1	Y_{11}	Y_{12}	Y_{13}
T = 2	Y_{21}	Y_{22}	Y_{23}
T = 3	Y_{31}	Y_{32}	Y_{33}

- What is high variance?

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Invariance for ILD

- There is variance/non-invariance across time/subjects. And then?
 - You may try to explain the variance by adding covariates
 - In DSEM (Mplus),
 - it is possible to have
 - random **intercepts** and **slopes** to capture **between-person** differences
 - random **intercepts** for differences across **time**
 - it is NOT possible to have
 - **loadings** vary across **time**
 - But do we even want that? Are constructs at all comparable?
 - Should we not rather **embrace** measurement model changes and differences?
 - What if even the number and nature of factors differ?

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Break 

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 Discussion

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 Reliability

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The Many Reliabilities of Affective Dynamics

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¹University of California, Davis
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³California State University, Sacramento

Abstract

Reliability is a key concept in psychology that has been broadly studied since the introduction of Cronbach's alpha, which is a measure of the internal consistency of a test. Despite its importance, this is a topic that is relatively understudied when dealing with intensive longitudinal data. In particular, when studying the psychological dynamics of affective states, there is no warranty that intensive longitudinal measurements are reliable. Given this, empirical researchers need tools to study and report the reliability of the scales used in intensive longitudinal research. In recent years, different approaches to estimate the reliability of the scales and the items used when studying psychological dynamics have been proposed. However, the advantages and disadvantages of each of these methods are unclear, making it difficult to determine when a certain approach would be preferred over the others. Specifically, these diverse approaches estimate reliability indices based on statistical models such as linear multilevel analysis, vector autoregressive models and dynamic factor models. Furthermore, while some methods suggest estimating one reliability index for the scale that applies to the whole sample, others estimate specific reliability indices for each individual in the sample. This wide variety of approaches can provoke some confusion for empirical researchers. Therefore, we aim to highlight the advantages and disadvantages of each of the available methods used to estimate the reliability of intensive longitudinal data. We also showcase their use with empirical data.

Keywords: reliability, dynamic factor analysis, experience sampling methods

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MITNB consortium on improving validity of time-series measurement in social sciences

MITNB

Measurement is the new black

<https://osf.io/m2v38/>

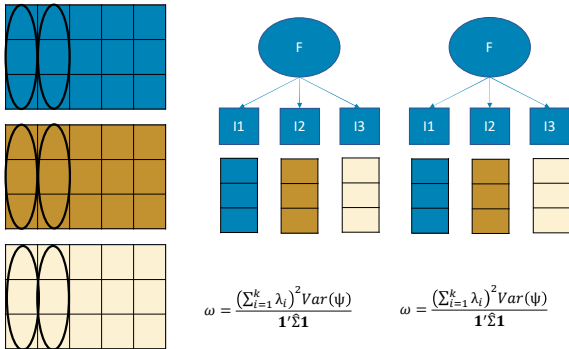
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Reliability (assuming invariance)

- Several statistics developed in 1930s-1950s as short cut estimates of reliability, for instance, Cronbach's alpha.
 - Developed before technological advances to find factor structures of scales.
 - Now we can use **model-based** estimates for reliability that do consider factor structure of scales.
 - This is important in case not all items measure the factors equally well.
 - We will use omega:
- $\omega = \frac{(\sum_{i=1}^k \lambda_i)^2}{\mathbf{1}' \Sigma \mathbf{1}}$
 - with Σ as the observed covariance matrix,
 - k as the number of items
 - $Var(\psi)$ as the variance of the factor scores
 - $\mathbf{1}$ as a k -dimensional row-vector used to sum elements in the matrix.

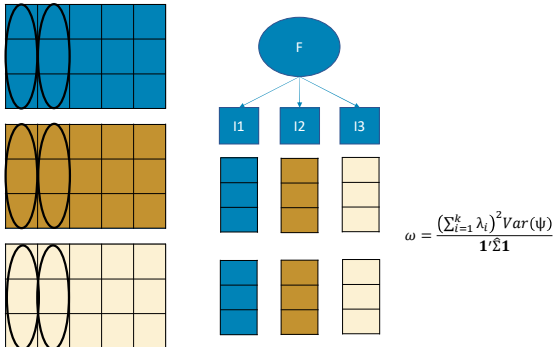
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Reliability for Panel Data



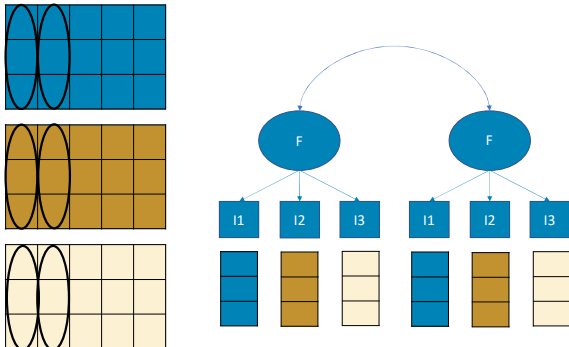
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Reliability for Panel Data



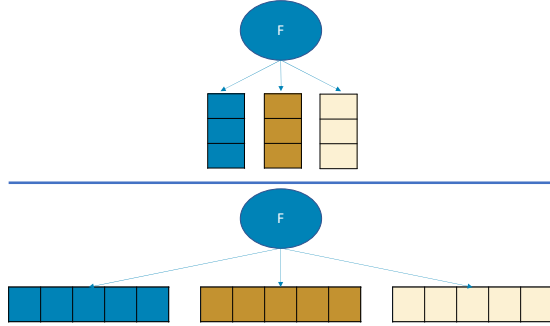
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Reliability for Panel Data



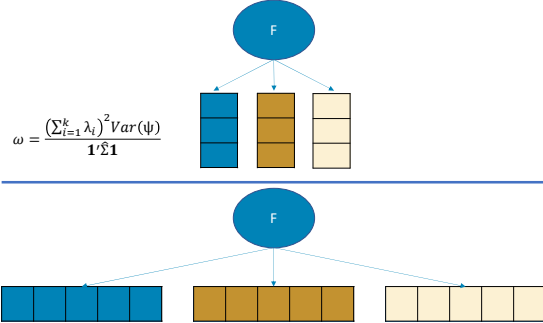
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Multilevel Reliability



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Multilevel Reliability



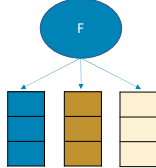
$$\omega = \frac{(\sum_{i=1}^k \lambda_i)^2 \text{Var}(\psi)}{\mathbf{1}' \hat{\Sigma} \mathbf{1}}$$

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Multilevel Reliability

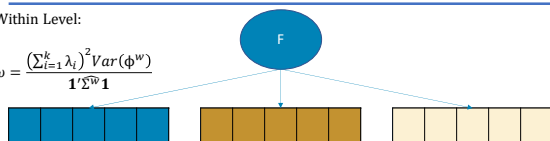
Between Level:

$$\omega = \frac{(\sum_{i=1}^k \lambda_i)^2 \text{Var}(\phi^b)}{\mathbf{1}' \hat{\Sigma}^b \mathbf{1}}$$



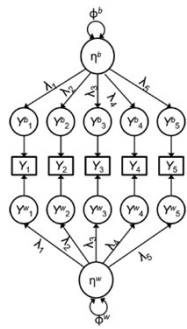
Within Level:

$$\omega = \frac{(\sum_{i=1}^k \lambda_i)^2 \text{Var}(\phi^w)}{\mathbf{1}' \hat{\Sigma}^w \mathbf{1}}$$



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Reliability for Panel Data & ILD



Assume invariance between the within- and between factor model and use

$$\omega = \frac{(\sum_{i=1}^k \lambda_i)^2 \text{Var}(\psi)}{\mathbf{1}' \Sigma \mathbf{1}}$$

$$ICC = \frac{\eta^b}{(\eta^b + \eta^w)}$$

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Reliability for Panel Data & ILD

- Previous slide shows that there are different ways to get reliabilities with multilevel analysis for the same basic model.
- But there is even more flexibility, and so, even more ways to calculate reliability with the exact same data.
- Above we split variance in between-person variance and within-person variance, but is that the only important distinction?
 - Do different items behave differently?
 - Do we need to distinguish between specific time-points?

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Reliability for Panel Data & ILD

- Different partitionings lead to different “true” variances (that we care about) and total variances.

$$\omega = \frac{(\sum_{i=1}^k \lambda_i)^2 \text{Var}(\psi)}{\mathbf{1}' \Sigma \mathbf{1}}$$

$$R_{1F} = \frac{\sigma_{\text{PERSON}}^2 + [\sigma_{\text{PERSON-ITEM}/m}^2]}{\sigma_{\text{PERSON}}^2 + [\sigma_{\text{PERSON-ITEM}/m}^2] + [\sigma_{\text{ERROR}/m}^2]}$$

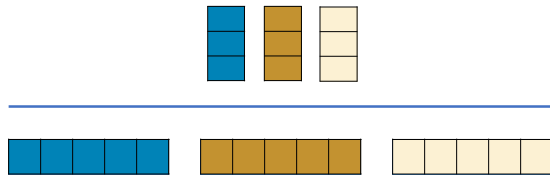
$$R_{1B} = \frac{\sigma_{\text{PERSON}}^2 + [\sigma_{\text{PERSON-ITEM}/m}^2]}{\sigma_{\text{PERSON}}^2 + [\sigma_{\text{PERSON-ITEM}/m}^2] + \sigma_{\text{DAY}}^2 + \sigma_{\text{PERSON-DAY}}^2 + [\sigma_{\text{ERROR}/m}^2]}$$

$$R_{KF} = \frac{\sigma_{\text{PERSON}}^2 + [\sigma_{\text{PERSON-ITEM}/m}^2]}{\sigma_{\text{PERSON}}^2 + [\sigma_{\text{PERSON-ITEM}/m}^2] + [\sigma_{\text{ERROR}/Km}^2]}$$

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Reliability for Panel Data & ILD

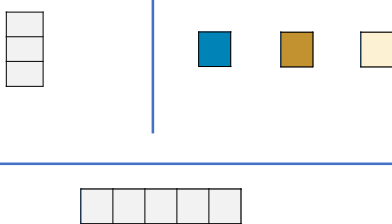
$$Y_{tj} = \mu + Person_j + e_{tj}$$



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Reliability for Panel Data & ILD

$$Y_{itj} = \mu + Item_i + Person_j + e_{itj}$$



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Reliability for Panel Data & ILD

$$Y_{tj} = \mu + Person_j + e_{tj}$$

$$Y_{itj} = \mu + Item_i + Person_j + e_{itj}$$

$$Y_{itj} = \mu + Item_i + Day_t + Person_j + e_{itj}$$

$$Y_{itj} = \mu + Item_i + Day_t + Person_j + (ID)_{it} + (IP)_{ij} + (DP)_{tj} + (IDP)_{itj} + e_{itj}$$

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Reliability for Panel Data & ILD

- Lai (2021): "Reliability is a characteristic of an observed composite"
 - So doesn't like using latent variables, should use actual composites you can calculate from the data (e.g., sum-scores).

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Reliability for Panel Data & ILD

- Overall composite of p items (Y) for person i in cluster j is simply the sum of the p item scores:

$$Z_{ij} = \sum_{k=1}^p Y_{ijk}$$

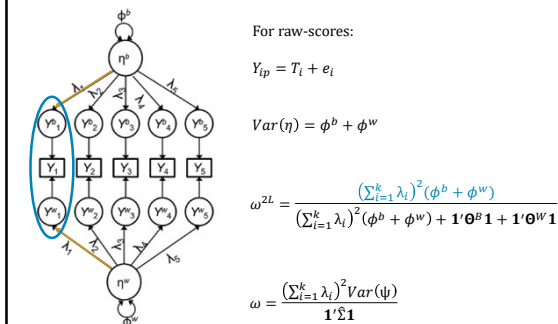
- The between-level observed composite score is:

$$Z_i^b = \sum_{j=1}^{n_j} \frac{Z_{ij}}{n_j}$$

- Within composite score is $Z_{ij} - Z_i^b$

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Reliability for Panel Data & ILD



True score variance in Y1

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Reliability for Panel Data & ILD

- Always compare **true score** variance to **total variance**.
- Different methods only differ in what they consider true- and total variance, and in terms of possible constraints on the multilevel factor-model.
 - In **factor models**, true-score variance is the variance of the factors
 - For **composites**, true-score variance can be determined based on the factor-model.

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Break 

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Lab

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Exploring Non-Invariance for Intensive Longitudinal Data

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Exploring Longitudinal Invariance

- Pairwise comparisons to detect all types of differences and changes are almost impossible.
- No method, then...

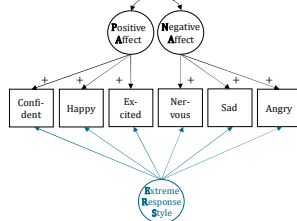


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Response Styles

Changes in the factor models (the measurement models) are even more likely than in panel or cross-sectional data.

- Distracting situations
- Getting demotivated



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Substantive differences

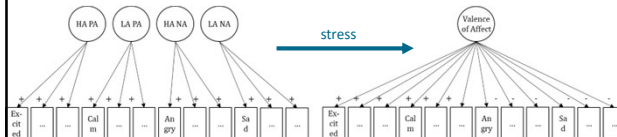
- Ability to differentiate between emotions
 - High differentiators: Label in a differentiated and context dependent way
 - Low differentiators: Less specific emotional experiences



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Substantive differences

- Ability to differentiate between emotions
 - High differentiators: Label in a differentiated and context dependent way
 - Low differentiators: Less specific emotional experiences



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Existing Approaches Were Limited

- Only tested if invariance across subjects OR if invariance across time was violated
- Assumed that the number and nature of factors are the same



- No pinpointing for which subjects and time-points the MM differs
- No insights into what the MM differences look like

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Latent Markov Factor Analysis

• Vogelsmeier et al. 2019

• Latent Markov model:

- Latent class model that allows for transitions
- Initial state probabilities
- Transition probabilities
- Probabilities may depend on individual- or time-point-specific covariates

• Exploratory factor analysis per state

- State-specific intercepts, loadings, and unique variances
- States may differ regarding all levels of invariance, thus, also regarding number of factors !!
- For observations within the same state, invariance holds

$$y_{itk} = \tau_k + \Lambda_k \eta_{it} + \epsilon_{itk},$$

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Estimation

- Can be estimated with a FIML or three-step approach

LATENT
GOLD



```
install.packages("devtools")
library("devtools")
install_github("LeonieVm/lmfa@0.1.3")
library("lmfa")
```

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Step 1: Investigating measurement models

- Step 1a: Selecting the number of states and factors**
- run `step1()` with the model selection option and store the results (e.g., into the object "modelselection")
 - inspect the models using `summary(modelselection)` and return non-converged models using `step1()` without the model selection option
 - choose best model(s) based on the BIC and Chull using `plot(modelselection)` and `chull_lmfa(modelselection)`
 - store the best model(s) (e.g., into the object "measurementmodel")

- Step 1b: Interpreting the measurement models**
- use `summary(measurementmodel)` to obtain the measurement model parameters from the chosen model(s)
 - investigate state-specific (initially rotated and standardized) loadings
 - investigate state-specific intercepts
 - investigate state-specific unique variances

- Step 1c: Attach factor scores to the dataset**
- store the outcome of `factor_scores_lmfa(ESEM, measurementmodel)` into a new dataset

Step 2: Obtaining state assignments & classification errors

- run `step2()` to calculate classification errors, posterior state-membership probabilities, and model state assignments and store the results (e.g., into the object "classification")
- obtain the results with `summary(classification)`
- if desired, attach posterior state-membership probabilities and the model state assignments to the dataset by storing `classification` into a new dataset

Step 3: Investigating transition model

- Step 3a: Selecting the covariates for the transition model**
- run `step3()` using the posterior state-membership probabilities of the `classification` object from `step2()` and all covariates of interest and store the results (e.g., into the object "transitionmodel")
 - inspect Wald test results with `summary(transitionmodel)` and look at the p-values to decide which covariates should be included in the final transition model

- Step 3b: Interpreting the transition model**
- use `summary(transitionmodel)` to obtain the transition model parameters and probabilities for covariates being equal to their sample means
 - use `probabilities(transitionmodel)` to obtain initial state and transition probabilities for any covariate value (and interval length) of interest

- Step 3c: Updating state assignments & investigating state memberships**
- if desired, attach posterior state-membership probabilities and the model state assignments to the dataset by storing `transitionmodel` into a new dataset
 - use `invariance(transitionmodel)` to investigate for which subjects within- and between-person invariance holds
 - use `plot(transitionmodel)` to investigate subjects' individual transitions

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Data (simulated for the *lmfa* package)

- Long format
- Column indicating time between previous and current observation
- Columns with indicator items
- Explanatory variables

	id	deltaT	negativeEvent	intervention	Interested	Joyful	Determined	Calm
1	1	0.00	53	0	45	16	8	75
2	1	0.56	37	0	52	42	35	50
3	1	1.04	55	0	71	80	70	78
4	1	1.81	59	0	62	77	75	94
5	1	0.80	73	0	27	40	46	17
6	1	2.45	49	0	55	53	18	45

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Step 1: Investigating Measurement Models

- The state-specific MMs are estimated ...
- ...while disregarding the transitions and the covariate effects on these transitions.
- What is the best model in terms of the number of factors and states?
 - Model selection

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Step 1: Investigating Measurement Models

```
modelselection <- step1(data = ESM,
  indicators = c(
    "Interested", "Joyful", "Determined", "Calm",
    "Lively", "Enthusiastic", "Relaxed", "Cheerful",
    "Content", "Energetic", "Upset", "Gloomy",
    "Sluggish", "Anxious", "Bored", "Irritated",
    "Nervous", "Listless"),
  modelselection = TRUE,
  n_state_range = 1:4,
  n_fact_range = 2:3)
```

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Step 1: Investigating Measurement Models

```
summary(modelselection)
##          LL          BIC convergence n par
## [323] -353166.8 708485.3          1    254
## [333] -353149.0 708602.3          1    272
## [3232] -353085.0 708940.1          1    327
## [3233] -353067.8 709058.2          0    345
## [3333] -353047.8 709170.6          0    363
## [3222] -353316.0 709249.7          1    309
## [322]  -353855.3 709709.8          1    236
## [33]   -354421.0 710375.3          1    181
## [2222] -353976.8 710418.8          1    291
## [32]   -355010.3 711401.4          1    163
## [222]  -355095.1 712037.0          1    218
## [22]   -356377.4 713983.1          1    145
## [3]    -361759.6 724281.6          1     90
## [2]    -363744.0 728098.0          1     72
```

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Step 1: Investigating Measurement Models

```
## Obliquely rotated standardized loadings:
##
## Interested  0.66  0.04  0.00  0.68  0.01  0.57 -0.01  0.02
## Joyful     0.60  0.02  0.02  0.65 -0.01  0.88  0.01  0.06
## Determined  0.37  0.03  0.53  0.61  0.00  0.84  0.02 -0.01
## Calm       0.37  0.53  0.01  0.59  0.00  0.18 -0.15  0.82
## Lively     0.63  0.03  0.03  0.65  0.00  0.88 -0.01  0.01
## Enthusiastic 0.65 -0.01  0.02  0.64  0.00  0.89  0.02  0.00
## Relaxed    0.64  0.02  0.00  0.64  0.01  0.16 -0.14  0.85
## Cheerful   0.63  0.07  0.01  0.63 -0.01  0.91  0.01  0.02
## Content    0.61  0.00  0.03  0.67  0.02  0.93  0.02  0.01
## Energetic  0.64 -0.01  0.00  0.63 -0.01  0.90  0.05 -0.01
## Upset      0.09  0.67  0.01  0.00  0.53  0.03  0.83 -0.03
## Gloomy     0.24  0.39  0.44  -0.01  0.53  0.02  0.82 -0.01
## Sluggish   0.07 -0.01  0.73  -0.01  0.50  -0.29  0.34  0.77
## Anxious    0.09  0.70 -0.02  0.00  0.52  0.05  0.79 -0.01
## Bored      0.07 -0.01  0.74  -0.01  0.52  0.04  0.47 -0.04
## Irritated  0.06  0.51 -0.05  0.01  0.58  0.04  0.85 -0.02
## Nervous    0.08  0.73 -0.04  0.00  0.51  0.03  0.74  0.01
## Listless   0.06 -0.05  0.73  0.01  0.54  0.02  0.46 -0.03
```

Configural invariance clearly violated!

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Step 1: Investigating Measurement Models

```
## Intercepts:
##
## Interested  49.24  61.46  51.98
## Joyful     48.92  61.12  49.95
## Determined  46.60  61.20  50.35
## Calm       46.25  61.14  54.76
## Lively     49.29  60.85  50.57
## Enthusiastic 48.99  61.16  50.24
## Relaxed    49.00  61.12  54.90
## Cheerful   49.03  61.02  50.42
## Content    49.39  60.84  49.98
## Energetic  49.35  60.90  50.41
## Upset      44.12  26.54  36.42
## Gloomy     45.88  27.09  35.93
## Sluggish   44.95  26.54  33.26
## Anxious    45.81  26.48  35.83
## Bored      44.98  26.75  29.94
## Irritated  43.48  26.69  35.66
## Nervous    46.39  26.50  35.94
## Listless   45.35  26.84  29.67

## Unique variances:
##
## Interested  273.26  53.37  96.43
## Joyful     273.82  48.67  92.81
## Determined  261.86  49.93  92.70
## Calm       265.99  51.75  99.17
## Lively     286.09  48.20  104.04
## Enthusiastic 257.06  50.09  107.07
## Relaxed    270.54  49.55  99.75
## Cheerful   284.69  50.47  83.05
## Content    271.52  41.15  92.38
## Energetic  271.12  53.24  95.55
## Upset      278.71  46.13  92.89
## Gloomy     256.03  46.46  73.85
## Sluggish   245.57  51.70  82.24
## Anxious    276.61  45.65  87.14
## Bored      253.52  47.69  103.11
## Irritated  267.30  44.56  84.99
## Nervous    261.57  49.30  86.21
## Listless   269.07  47.29  92.10
```

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Step 2: Obtaining State Assignments

- Each observation is assigned to the state with the highest state-membership probability.
- The inherent classification uncertainty is calculated.
- Relevant for obtaining unbiased estimates for the transition model

```
classification <- step2(data = ESM_fs, model = measurementmodel323)
```

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Step 3: Investigating Transition Model

- The MMs (i.e., the factor parameters) are kept fixed
- The transitions between the states are estimated (while correcting for step 2's assignment uncertainty)

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Step 3: Investigating Transition Model

```
transitionmodel <- step3(data = ESM,
  identifier = "id",
  n_state = 3,
  postprobs =
    classification$classification_posteriors[, -1],
  timeintervals = "deltaT",
  initialCovariates = NULL,
  transitionCovariates =
    c("intervention", "negativeEvent"))
```

Wald tests:

	Wald	df	p-value
intervention	213.3821	6	0
negativeEvent	55.7629	6	0

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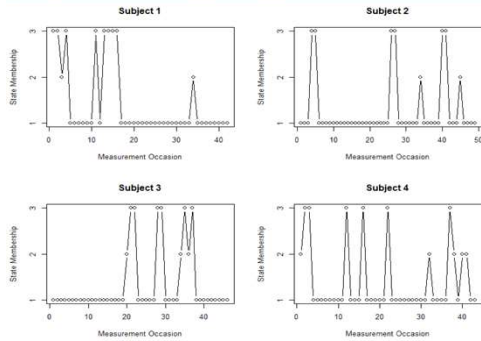
Step 3: Investigating Transition Model

```
probabilities(model = transitionmodel,
             deltaT = 1,
             initialCovariateScores = NULL,
             transitionCovariateScores = c(0, 49.65))

## 1. Initial state probabilities:
## (no covariates defined)
##
##   S1  S2  S3
## 0.42 0.34 0.24
##
## 2. Transition probabilities:
## interval length: 1
## intervention score: 0
## negativeEvent score: 49.65
##
##   S1  S2  S3
## S1 0.84 0.07 0.08
## S2 0.37 0.44 0.19
## S3 0.54 0.08 0.39
```

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Step 3: Investigating Transition Model



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Accounting for Non-Invariance?



- Obtain dataset with state memberships and state-specific factor scores

```
ESM_fs <- factorscores_lmfa(data = ESM, model = measurementmodel323)
ESM_fs_c1 <- classification$data
```

- Continue with one state only
- Accept that invariance does not hold and focus on substantively interesting results:
 - E.g., learning about situations in which emotion differentiation is reduced

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Code online

Latent Markov Factor Analysis

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Discussion

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References

- Adolf, J., Schuurman, N. K., Borkenau, P., Borsboom, D., & Dolan, C. V. (2014). Measurement invariance within and between individuals: a distinct problem in testing the equivalence of intra- and inter-individual model structures. *Frontiers in Psychology*, 5, 1–14. doi:10.3389/fpsyg.2014.00883
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- McNeish, D., Mackinnon, D. P., Marsch, L. A., & Poldrack, R. A. (2021). Measurement in Intensive Longitudinal Data. *Structural Equation Modeling: A Multidisciplinary Journal*, 1–16. doi:10.1080/10705511.2021.1915788
- Vogelsmeier, L. V. D. E., Vermunt, J. K., van Roekel, E., & De Roover, K. (2019). Latent Markov factor analysis for exploring measurement model changes in time-intensive longitudinal studies. *Structural Equation Modeling: A Multidisciplinary Journal*, 26, 557–575. doi:10.1080/10705511.2018.1554445

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