P8106 Midterm Project

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Load Data

```
load("data/dat1.RData")
train data = dat1 |>
  janitor::clean_names() |>
  mutate(
    gender = as.factor(gender),
    diabetes = as.factor(diabetes),
    hypertension = as.factor(hypertension),
    race = fct_recode(race,
                  White = "1",
                  Asian = "2",
                  Black = "3",
                  Hispanic = "4"),
    gender = fct_recode(gender,
                        Male = "1",
                        Female = "0"),
    smoking = fct_recode(smoking,
                         "Never smoked" = "0",
                         "Former smoker" = "1",
                          "Current smoker" = "2"))
load("data/dat2.RData")
test_data = dat2 |>
  janitor::clean_names() |>
  mutate(
    gender = as.factor(gender),
    diabetes = as.factor(diabetes),
    hypertension = as.factor(hypertension),
    race = fct_recode(race,
                  White = "1",
                  Asian = "2",
                  Black = "3",
                  Hispanic = "4"),
    gender = fct_recode(gender,
                        Male = "1",
                        Female = "0"),
    smoking = fct_recode(smoking,
                         "Never smoked" = "0",
                          "Former smoker" = "1",
```

```
"Current smoker" = "2")
```

Modify Data

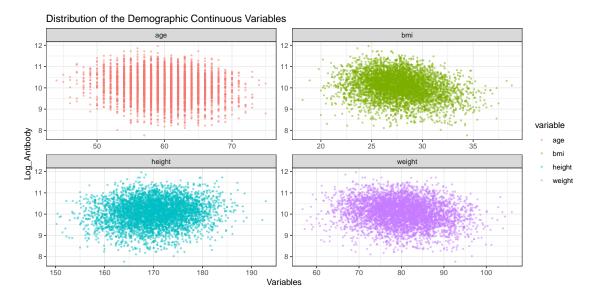
```
train_data1 =
   train_data %>%
   select(-id, -height, -weight, -hypertension)

x_train = model.matrix(log_antibody ~ ., train_data1)[, -1]
colnames(x_train) = make.names(colnames(x_train), unique = TRUE)

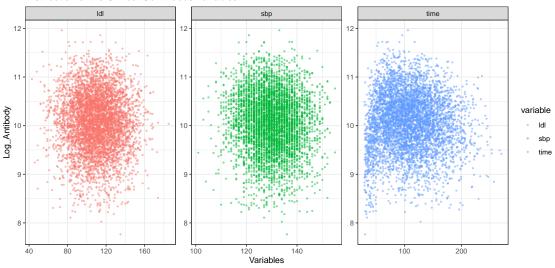
y_train = train_data1[, "log_antibody"]
ctrl1 = trainControl(method = "cv", number = 10)
```

Descriptive Analysis

Numeric Variables



Distribution of the Clinical Continuous Variables

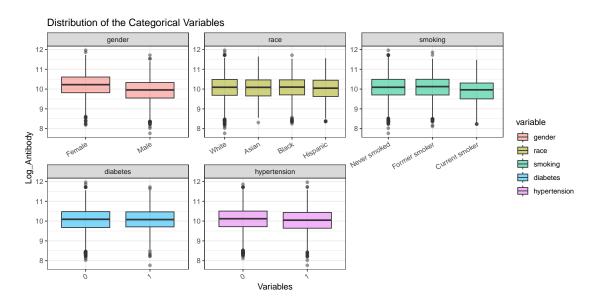


```
train_data %>%
 pivot_longer(
   cols = c(age, height, weight, bmi, sbp, ldl, time, log_antibody),
   names_to = "variable_name",
   values_to = "value"
  ) %>%
  group_by(variable_name) %>%
  summarize(
   mean = mean(value),
   median = median(value),
   min = min(value),
   first_quantile = quantile(value, probs = 0.25),
   third_quantile = quantile(value, probs = 0.75),
   max = max(value)
  ) %>%
  ungroup() %>%
  arrange(desc(variable_name == "log_antibody"), variable_name) %>%
  knitr::kable(digits = 3, caption = "Descriptive Statistics")
```

Table 1: Descriptive Statistics

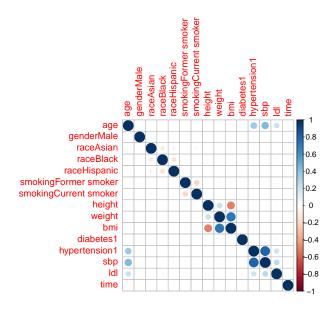
variable_name	mean	median	min	first_quantile	third_quantile	max
log_antibody	10.064	10.089	7.765	9.682	10.478	11.961
age	59.968	60.000	44.000	57.000	63.000	75.000
bmi	27.740	27.600	18.200	25.800	29.500	38.800
height	170.126	170.100	150.200	166.100	174.225	192.900
ldl	109.909	110.000	43.000	96.000	124.000	185.000
sbp	129.900	130.000	101.000	124.000	135.000	155.000
time	108.863	106.000	30.000	76.000	138.000	270.000
weight	80.109	80.100	56.700	75.400	84.900	106.000

Categorical Variables



Correlation Plot

```
x_corr = model.matrix(log_antibody ~ ., train_data[, -1])[, -1]
corrplot(cor(x_corr), method = "circle", type = "full")
```



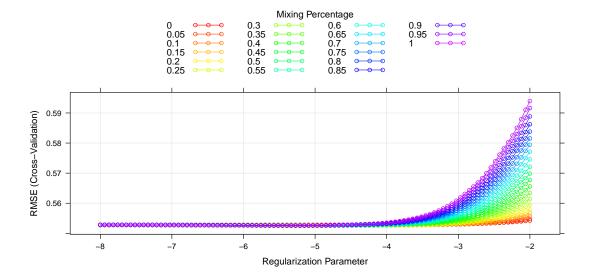
Regression

Elastic Net

Elastic Net

```
set.seed(37)
enet_fit = train(log_antibody ~ .,
                 data = train_data1,
                 method = "glmnet",
                 tuneGrid = expand.grid(alpha = seq(0, 1, length = 21),
                                         lambda = exp(seq(-2, -8, length = 100))),
                 trControl = ctrl1)
enet_fit$bestTune
                   lambda
##
        alpha
## 2044
            1 0.004544037
coef(enet_fit$finalModel, enet_fit$bestTune$lambda)
## 13 x 1 sparse Matrix of class "dgCMatrix"
                                    s1
## (Intercept)
                         1.272351e+01
## age
                         -1.914947e-02
## genderMale
                         -2.859704e-01
```

```
## raceAsian
## raceBlack
## raceHispanic
                         -2.469963e-02
## smokingFormer smoker
                          1.592525e-02
## smokingCurrent smoker -1.770936e-01
## bmi
                         -4.820177e-02
## diabetes1
                          4.263422e-05
## sbp
## ldl
## time
                         -1.850422e-04
mycol = rainbow(25)
mypar = list(superpose.symbol = list(col = mycol),
superpose.line = list(col = mycol))
plot(enet_fit, par.settings = mypar, xTrans = log)
```

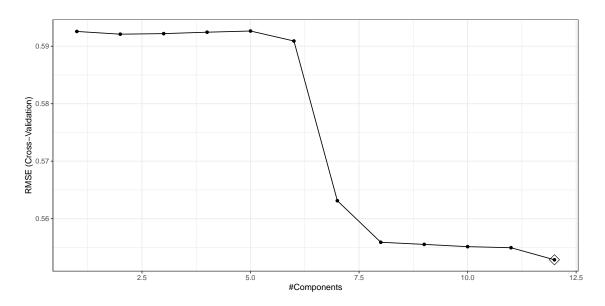


PCR

Fit method: svdpc

```
##
           1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps
            13.522 23.760 33.489
                                    42.534
## X
                                              51.17
                                                     59.563
                                                               67.70
           1.296
                    1.493
                            1.512
                                     1.512
                                               1.54
                                                       2.032
                                                               13.44
## .outcome
##
           8 comps 9 comps 10 comps 11 comps 12 comps
                                        95.36
                                                 100.0
## X
             75.76
                      82.63
                               89.32
## .outcome
             13.48
                      13.68
                               13.78
                                        13.84
                                                  14.5
```

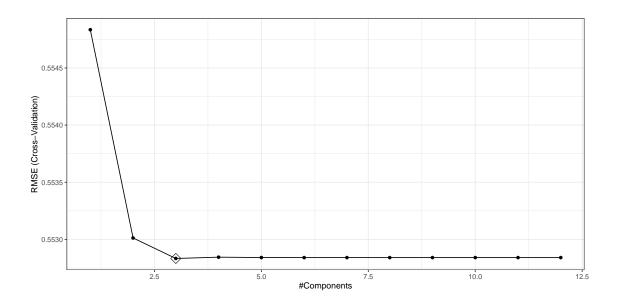
```
ggplot(pcr_fit, highlight = TRUE)
```



PLS

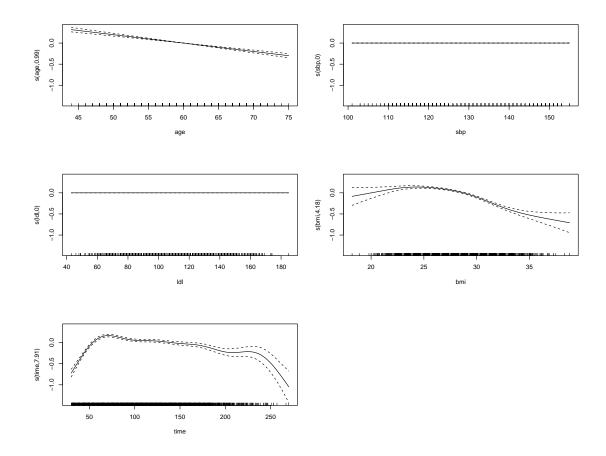
```
set.seed(37)
pls_fit = train(x_train, y_train,
                method = "pls",
                tuneGrid = data.frame(ncomp = 1:12),
                trControl = ctrl1,
                preProcess = c("center", "scale"))
summary(pls_fit)
## Data:
           X dimension: 5000 12
## Y dimension: 5000 1
## Fit method: oscorespls
## Number of components considered: 3
## TRAINING: % variance explained
##
             1 comps 2 comps 3 comps
## X
               9.295
                        21.21
                                 26.88
## .outcome 13.885
                        14.45
                                 14.50
```

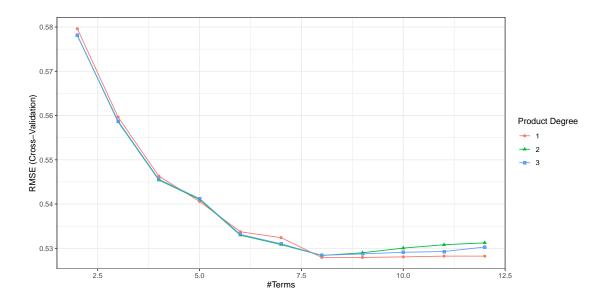
```
ggplot(pls_fit, highlight = TRUE)
```



GAM and MARS

```
set.seed(37)
gam.fit = train(x_train, y_train,
                 method = "gam",
                 trControl = ctrl1)
gam.fit$bestTune
     select method
##
## 2
       TRUE GCV.Cp
gam.fit$finalModel
##
## Family: gaussian
## Link function: identity
##
## Formula:
## .outcome ~ genderMale + raceAsian + raceBlack + raceHispanic +
       smokingFormer.smoker + smokingCurrent.smoker + diabetes1 +
##
       s(age) + s(sbp) + s(ldl) + s(bmi) + s(time)
## Estimated degrees of freedom:
## 0.992 0.000 0.000 4.179 7.915 total = 21.09
##
## GCV score: 0.2786375
par(mfrow = c(3, 2))
plot(gam.fit$finalModel)
par(mfrow = c(1, 1))
```





mars.fit\$bestTune

```
## nprune degree
## 8 9 1
```

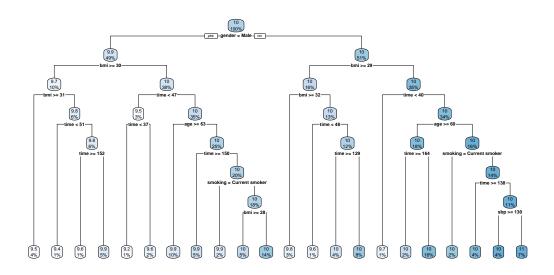
coef(mars.fit\$finalModel)

##	(Intercept)	h(27.8-bmi)	h(time-57)
##	10.847446930	-0.061997354	-0.002254182
##	h(57-time)	${\tt genderMale}$	h(age-59)
##	-0.033529326	-0.296290451	-0.022957648
##	h(59-age)	<pre>smokingCurrent.smoker</pre>	h(bmi-23.7)
##	0.016138468	-0.205126851	-0.084380175

Regression Trees

size of tree

```
## Find the cp that yields the minimum cross-validation error
minErr = which.min(cpTable[,4])
tree_final = rpart::prune(tree_full, cp = cpTable[minErr, 1])
rpart.plot(tree_final)
```



summary(tree_final)

```
## Call:
## rpart(formula = log_antibody ~ ., data = train_data1, control = rpart.control(cp = 0))
    n = 5000
##
##
               CP nsplit rel error
##
                                      xerror
                       0 1.0000000 1.0007146 0.02004169
## 1
     0.057918182
                       1 0.9420818 0.9432020 0.01870086
## 2
     0.027293800
## 3 0.025172140
                       2 0.9147880 0.9295966 0.01846651
                       3 0.8896159 0.9042136 0.01812179
## 4 0.020759383
```

```
## 5 0.010560350
                       4 0.8688565 0.8829836 0.01767741
## 6
    0.007928454
                       5 0.8582961 0.8761783 0.01736189
## 7
     0.007483148
                       6 0.8503677 0.8729469 0.01732773
## 8 0.006830408
                       7 0.8428845 0.8657230 0.01716499
## 9
     0.006412912
                       8 0.8360541 0.8604904 0.01704889
## 10 0.006407846
                       9 0.8296412 0.8572604 0.01697315
## 11 0.004852623
                      10 0.8232334 0.8485364 0.01678947
## 12 0.003284421
                      11 0.8183808 0.8465873 0.01664462
## 13 0.003033803
                      12 0.8150963 0.8465219 0.01667932
## 14 0.002914817
                      13 0.8120625 0.8466921 0.01669623
## 15 0.002790737
                      14 0.8091477 0.8452142 0.01665712
## 16 0.002730117
                      15 0.8063570 0.8450512 0.01661721
## 17 0.002560197
                      16 0.8036269 0.8476923 0.01669101
## 18 0.002327749
                      17 0.8010667 0.8483089 0.01668839
## 19 0.002223936
                      19 0.7964112 0.8451645 0.01661475
## 20 0.002164228
                      21 0.7919633 0.8447269 0.01660173
##
  Variable importance
##
              time gender
                                                        ldl
       bmi
                               age smoking
                                                sbp
##
        31
                28
                                 7
                                         3
                                                  3
                                                          1
##
  Node number 1: 5000 observations,
                                        complexity param=0.05791818
     mean=10.06434, MSE=0.355722
##
     left son=2 (2427 obs) right son=3 (2573 obs)
##
##
     Primary splits:
##
         gender splits as RL,
                                       improve=0.057918180, (0 missing)
##
                 < 29.65 to the right, improve=0.049512600, (0 missing)
         bmi
                                       improve=0.041303690, (0 missing)
##
         time
                 < 46.5 to the left,
##
                 < 60.5 to the right, improve=0.018144830, (0 missing)
##
         smoking splits as RRL,
                                       improve=0.008813525, (0 missing)
##
     Surrogate splits:
##
         sbp < 119.5 to the left, agree=0.518, adj=0.007, (0 split)
##
         time < 37.5 to the left, agree=0.518, adj=0.006, (0 split)
##
         ldl < 140.5 to the right, agree=0.517, adj=0.005, (0 split)
##
         age < 66.5 to the right, agree=0.516, adj=0.003, (0 split)
##
         bmi < 20.75 to the left, agree=0.515, adj=0.002, (0 split)
## Node number 2: 2427 observations,
                                        complexity param=0.02517214
     mean=9.91655, MSE=0.3395789
##
     left son=4 (524 obs) right son=5 (1903 obs)
##
##
     Primary splits:
##
                 < 29.85 to the right, improve=0.054323820, (0 missing)
         bmi
                 < 46.5 to the left, improve=0.049666810, (0 missing)
##
         time
                 < 60.5 to the right, improve=0.017649280, (0 missing)
##
                                       improve=0.009762305, (0 missing)
##
         smoking splits as RRL,
                 < 141.5 to the right, improve=0.004210017, (0 missing)
##
         ldl
   Node number 3: 2573 observations,
                                        complexity param=0.0272938
##
     mean=10.20375, MSE=0.3309125
##
     left son=6 (820 obs) right son=7 (1753 obs)
##
     Primary splits:
                 < 28.95 to the right, improve=0.057015340, (0 missing)
##
         bmi
##
                 < 46.5 to the left, improve=0.036007110, (0 missing)
         time
                 < 59.5 to the right, improve=0.023746020, (0 missing)
##
         age
```

```
##
                                       improve=0.010252650, (0 missing)
         smoking splits as RRL,
##
                 < 128.5 to the right, improve=0.006713466, (0 missing)
         sbp
##
     Surrogate splits:
##
         ldl < 164.5 to the right, agree=0.683, adj=0.005, (0 split)
##
         sbp < 108.5 to the left, agree=0.682, adj=0.002, (0 split)
##
## Node number 4: 524 observations,
                                       complexity param=0.004852623
     mean=9.657717, MSE=0.3166048
##
##
     left son=8 (207 obs) right son=9 (317 obs)
##
     Primary splits:
##
         bmi
                 < 31.45 to the right, improve=0.05202457, (0 missing)
                 < 50.5 to the left, improve=0.04364456, (0 missing)
##
##
         smoking splits as RRL,
                                       improve=0.01948327, (0 missing)
                 < 120.5 to the right, improve=0.01676732, (0 missing)
##
##
                 < 59.5 to the right, improve=0.01274723, (0 missing)
         age
##
     Surrogate splits:
##
                     to the right, agree=0.615, adj=0.024, (0 split)
         ldl < 152
##
         time < 31.5 to the left, agree=0.609, adj=0.010, (0 split)
##
                     to the left, agree=0.607, adj=0.005, (0 split)
         sbp < 109
##
## Node number 5: 1903 observations,
                                        complexity param=0.02075938
     mean=9.987821, MSE=0.3223782
##
     left son=10 (137 obs) right son=11 (1766 obs)
##
##
     Primary splits:
                 < 46.5 to the left, improve=0.060185330, (0 missing)
##
         time
##
         age
                 < 62.5 to the right, improve=0.023530880, (0 missing)
##
                 < 141.5 to the right, improve=0.008688514, (0 missing)
         ldl
                 < 28.35 to the right, improve=0.008031965, (0 missing)
         bmi
##
                                       improve=0.007860098, (0 missing)
         smoking splits as RRL,
##
## Node number 6: 820 observations,
                                       complexity param=0.006830408
##
     mean=10.00291, MSE=0.3091452
##
     left son=12 (162 obs) right son=13 (658 obs)
##
     Primary splits:
##
             < 32.25 to the right, improve=0.047923770, (0 missing)
##
         time < 47.5 to the left, improve=0.047697360, (0 missing)
##
         age < 60.5 to the right, improve=0.021396790, (0 missing)
##
         ldl < 73.5 to the right, improve=0.011921340, (0 missing)
         sbp < 137.5 to the right, improve=0.008408437, (0 missing)
##
##
## Node number 7: 1753 observations,
                                        complexity param=0.01056035
##
     mean=10.29769, MSE=0.313402
     left son=14 (53 obs) right son=15 (1700 obs)
##
##
     Primary splits:
                 < 39.5 to the left, improve=0.034188120, (0 missing)
##
         time
                 < 59.5 to the right, improve=0.028638110, (0 missing)
##
         age
##
         smoking splits as RRL,
                                       improve=0.017123260, (0 missing)
                 < 128.5 to the right, improve=0.009433160, (0 missing)
##
##
         bmi
                 < 26.75 to the right, improve=0.005238462, (0 missing)
##
## Node number 8: 207 observations
     mean=9.498897, MSE=0.2980599
##
##
## Node number 9: 317 observations,
                                       complexity param=0.002223936
```

```
##
     mean=9.761427, MSE=0.3014877
##
     left son=18 (27 obs) right son=19 (290 obs)
##
     Primary splits:
                         to the left, improve=0.03944451, (0 missing)
##
                 < 51
         time
##
         smoking splits as RRL,
                                       improve=0.03307206, (0 missing)
                 < 58.5 to the right, improve=0.02350311, (0 missing)
##
                 < 121.5 to the right, improve=0.02005357, (0 missing)
##
         sbp
                 < 80.5 to the right, improve=0.01272572, (0 missing)
##
         ldl
##
## Node number 10: 137 observations,
                                        complexity param=0.003033803
     mean=9.487714, MSE=0.3536406
     left son=20 (46 obs) right son=21 (91 obs)
##
##
     Primary splits:
         time < 36.5 to the left, improve=0.11137440, (0 missing)
##
##
         sbp < 118.5 to the right, improve=0.05219794, (0 missing)
##
             < 26.65 to the right, improve=0.04629031, (0 missing)
##
         age < 65.5 to the right, improve=0.04068284, (0 missing)
##
         ldl < 88.5 to the left, improve=0.02321797, (0 missing)
##
## Node number 11: 1766 observations,
                                         complexity param=0.007483148
##
    mean=10.02662, MSE=0.2990454
     left son=22 (508 obs) right son=23 (1258 obs)
##
##
     Primary splits:
                 < 62.5 to the right, improve=0.025202130, (0 missing)
##
         age
##
         time
                 < 97.5 to the right, improve=0.015378130, (0 missing)
                 < 142.5 to the right, improve=0.012513270, (0 missing)
##
##
         smoking splits as RRL,
                                       improve=0.009228690, (0 missing)
                 < 28.35 to the right, improve=0.008363651, (0 missing)
##
         bmi
##
     Surrogate splits:
         sbp < 140.5 to the right, agree=0.737, adj=0.085, (0 split)
##
##
         ldl < 159.5 to the right, agree=0.715, adj=0.008, (0 split)
##
## Node number 12: 162 observations
     mean=9.757604, MSE=0.2946382
##
##
## Node number 13: 658 observations,
                                        complexity param=0.006407846
     mean=10.06331, MSE=0.2942538
##
     left son=26 (51 obs) right son=27 (607 obs)
##
    Primary splits:
##
         time < 47.5 to the left, improve=0.058863320, (0 missing)
         age < 61.5 to the right, improve=0.018077840, (0 missing)
##
         bmi < 31.35 to the right, improve=0.011334980, (0 missing)
##
         ldl < 73.5 to the right, improve=0.009520452, (0 missing)
##
##
         sbp < 137.5 to the right, improve=0.009235878, (0 missing)
## Node number 14: 53 observations
     mean=9.71145, MSE=0.4536552
##
##
## Node number 15: 1700 observations,
                                         complexity param=0.007928454
     mean=10.31597, MSE=0.2979808
##
##
     left son=30 (914 obs) right son=31 (786 obs)
##
     Primary splits:
##
         age
                 < 59.5 to the right, improve=0.027837610, (0 missing)
                                       improve=0.016679170, (0 missing)
##
         smoking splits as RRL,
```

```
##
                 < 159.5 to the right, improve=0.014116890, (0 missing)
##
                 < 128.5 to the right, improve=0.009671418, (0 missing)
         sbp
##
         bmi
                 < 26.75 to the right, improve=0.004398652, (0 missing)
##
     Surrogate splits:
##
         sbp < 126.5 to the right, agree=0.645, adj=0.232, (0 split)
         ldl < 91.5 to the right, agree=0.569, adj=0.069, (0 split)
##
         time < 176.5 to the left, agree=0.545, adj=0.017, (0 split)
##
         bmi < 21.35 to the right, agree=0.540, adj=0.005, (0 split)
##
##
## Node number 18: 27 observations
     mean=9.404035, MSE=0.2771699
##
## Node number 19: 290 observations,
                                         complexity param=0.002223936
     mean=9.794701, MSE=0.2907525
##
##
     left son=38 (62 obs) right son=39 (228 obs)
##
     Primary splits:
##
                 < 151.5 to the right, improve=0.04911456, (0 missing)
         time
         smoking splits as RRL,
##
                                       improve=0.04214043, (0 missing)
##
                 < 121.5 to the right, improve=0.02250072, (0 missing)
         sbp
                 < 58.5 to the right, improve=0.02190715, (0 missing)
##
         age
##
         ldl
                 < 80.5 to the right, improve=0.01055996, (0 missing)
##
## Node number 20: 46 observations
     mean=9.208578, MSE=0.2594872
##
##
## Node number 21: 91 observations
##
     mean=9.628815, MSE=0.3419384
## Node number 22: 508 observations
     mean=9.890003, MSE=0.3020677
##
##
## Node number 23: 1258 observations,
                                         complexity param=0.006412912
##
     mean=10.08178, MSE=0.287245
##
     left son=46 (250 obs) right son=47 (1008 obs)
##
     Primary splits:
##
                 < 149.5 to the right, improve=0.031564790, (0 missing)
         time
##
         age
                 < 54.5 to the right, improve=0.011762700, (0 missing)
##
         ldl
                 < 126.5 to the right, improve=0.011752420, (0 missing)
##
         smoking splits as RRL,
                                        improve=0.010707140, (0 missing)
##
                 < 109.5 to the left, improve=0.007957896, (0 missing)
         sbp
##
     Surrogate splits:
##
         ldl < 162.5 to the right, agree=0.802, adj=0.004, (0 split)
##
## Node number 26: 51 observations
     mean=9.609269, MSE=0.2289111
##
## Node number 27: 607 observations,
                                         complexity param=0.002730117
     mean=10.10146, MSE=0.2809679
##
##
     left son=54 (225 obs) right son=55 (382 obs)
##
     Primary splits:
##
         time < 128.5 to the right, improve=0.02847191, (0 missing)
         age < 61.5 to the right, improve=0.02293396, (0 missing)
##
##
         bmi < 31.35 to the right, improve=0.01993356, (0 missing)
         ldl < 111.5 to the right, improve=0.01092987, (0 missing)
##
```

```
##
         sbp < 137.5 to the right, improve=0.01007648, (0 missing)
##
     Surrogate splits:
##
         sbp < 114.5 to the left, agree=0.636, adj=0.018, (0 split)
         age < 52.5 to the left, agree=0.631, adj=0.004, (0 split)
##
         bmi < 32.15 to the right, agree=0.631, adj=0.004, (0 split)
##
##
## Node number 30: 914 observations,
                                         complexity param=0.002914817
     mean=10.23151, MSE=0.2886223
##
##
     left son=60 (101 obs) right son=61 (813 obs)
##
     Primary splits:
##
         time
                 < 163.5 to the right, improve=0.019652420, (0 missing)
                                        improve=0.012542120, (0 missing)
##
         smoking splits as RRL,
##
                 < 24.85 to the right, improve=0.010077130, (0 missing)
                 < 70.5 to the right, improve=0.004980359, (0 missing)
##
         age
##
                 < 79.5 to the right, improve=0.004331232, (0 missing)
         ldl
##
## Node number 31: 786 observations,
                                         complexity param=0.002790737
##
     mean=10.41418, MSE=0.2909223
     left son=62 (78 obs) right son=63 (708 obs)
##
##
     Primary splits:
##
         smoking splits as RRL,
                                        improve=0.021707010, (0 missing)
                 < 184.5 to the right, improve=0.020284770, (0 missing)
##
##
                 < 129.5 to the right, improve=0.013958710, (0 missing)
         sbp
                                        improve=0.008200332, (0 missing)
##
         race
                 splits as LRLL,
                 < 54.5 to the right, improve=0.007226599, (0 missing)
##
##
     Surrogate splits:
##
         sbp < 149
                     to the right, agree=0.903, adj=0.026, (0 split)
##
## Node number 38: 62 observations
     mean=9.565542, MSE=0.2656172
##
##
## Node number 39: 228 observations
##
     mean=9.857017, MSE=0.2794241
##
## Node number 46: 250 observations
     mean=9.890584, MSE=0.2961252
##
##
## Node number 47: 1008 observations,
                                          complexity param=0.003284421
     mean=10.12921, MSE=0.273727
##
     left son=94 (87 obs) right son=95 (921 obs)
##
##
     Primary splits:
##
                                        improve=0.021171970, (0 missing)
         smoking splits as RRL,
                 < 28.25 to the right, improve=0.016615490, (0 missing)
##
         bmi
##
         ldl
                 < 126.5 to the right, improve=0.013732310, (0 missing)
                 < 52.5 to the right, improve=0.009102790, (0 missing)
##
         age
                 < 109.5 to the left, improve=0.008120837, (0 missing)
##
         sbp
##
## Node number 54: 225 observations
##
     mean=9.984915, MSE=0.2376411
##
## Node number 55: 382 observations
     mean=10.1701, MSE=0.293776
##
##
## Node number 60: 101 observations
```

```
##
     mean=10.01783, MSE=0.30527
##
## Node number 61: 813 observations
     mean=10.25805, MSE=0.2801773
##
##
## Node number 62: 78 observations
     mean=10.17476, MSE=0.3236525
##
##
## Node number 63: 708 observations,
                                        complexity param=0.002327749
##
     mean=10.44056, MSE=0.2803057
##
     left son=126 (182 obs) right son=127 (526 obs)
##
     Primary splits:
         time < 137.5 to the right, improve=0.019352530, (0 missing)
##
##
         sbp < 133.5 to the right, improve=0.014196050, (0 missing)
##
         age < 55.5 to the right, improve=0.009180245, (0 missing)
##
         race splits as LRLL,
                                    improve=0.008380573, (0 missing)
##
         bmi < 28.45 to the right, improve=0.007482769, (0 missing)
##
     Surrogate splits:
##
         ldl < 154.5 to the right, agree=0.744, adj=0.005, (0 split)
##
## Node number 94: 87 observations
     mean=9.881514, MSE=0.2388818
##
                                        complexity param=0.002560197
## Node number 95: 921 observations,
##
     mean=10.1526, MSE=0.2706758
##
     left son=190 (236 obs) right son=191 (685 obs)
##
     Primary splits:
         bmi < 28.25 to the right, improve=0.018266070, (0 missing)
##
         ldl < 127.5 to the right, improve=0.013821740, (0 missing)
##
         age < 55.5 to the right, improve=0.012300610, (0 missing)
##
##
         sbp < 109.5 to the left, improve=0.011041330, (0 missing)
##
         time < 95.5 to the right, improve=0.007309987, (0 missing)
##
     Surrogate splits:
##
                     to the right, agree=0.746, adj=0.008, (0 split)
         ldl < 164
##
         age < 46.5 to the left, agree=0.745, adj=0.004, (0 split)
##
## Node number 126: 182 observations
##
     mean=10.31535, MSE=0.2119669
##
## Node number 127: 526 observations,
                                         complexity param=0.002327749
     mean=10.48388, MSE=0.2966499
##
     left son=254 (191 obs) right son=255 (335 obs)
##
     Primary splits:
         sbp < 129.5 to the right, improve=0.028452590, (0 missing)
##
                                    improve=0.013522720, (0 missing)
##
         time < 50.5 to the left,
                                    improve=0.012365230, (0 missing)
##
         race splits as LRLL,
         bmi < 28.35 to the right, improve=0.009747016, (0 missing)
##
##
         age < 54.5 to the right, improve=0.007912211, (0 missing)
##
     Surrogate splits:
##
         ldl < 145.5 to the right, agree=0.646, adj=0.026, (0 split)
##
         bmi < 22.7 to the left, agree=0.644, adj=0.021, (0 split)
##
         time < 42.5 to the left, agree=0.641, adj=0.010, (0 split)
##
## Node number 190: 236 observations
```

```
## mean=10.03281, MSE=0.2619733
##
## Node number 191: 685 observations
## mean=10.19387, MSE=0.2670264
##
## Node number 254: 191 observations
## mean=10.36221, MSE=0.2972116
##
## Node number 255: 335 observations
## mean=10.55325, MSE=0.2830768
```

${\bf Comparison}$

