CS 32 Week 4 Worksheet Solutions

This worksheet is entirely **optional**, and meant for extra practice. Some problems will be more challenging than others and are designed to have you apply your knowledge beyond the examples presented in lecture, discussion or projects. All exams will be done on paper, so it is in your best interest to practice these problems by hand and not rely on a compiler.

Solutions are written in red. The solutions for **programming** problems are not absolute, it is okay if your code looks different; this is just one way to solve the specific problem.

Concepts

Stacks, Queues

1) Given a string of '(', ')', '[', and ']', write a function to check if the input string is *valid*. Validity is determined by each '(' having a corresponding ')', and each '[' having a corresponding ']', with parentheses being properly nested and brackets being properly nested (JKC)
   Examples: “[()([])[[([][])]]]” → Valid
   “((([(])))“ → Invalid
   “(()))” → Invalid
   “()[]” → Valid

   [Suggested Time: 5 mins]

```
// The idea here is that our stack maintains the sequence of
// opening parentheses and brackets, and removes an opening
// symbol upon seeing the matching closing one. Note that if we
// have a closing symbol, but the stack is empty or the top of
// the stack is not the the matching opening symbol, then we've
// encountered an invalid sequence of parens and brackets.
bool isValid(string symbols) {
     stack<char> openers;
     for (int k = 0; k != symbols.size(); k++) {
          char c = symbols[k];
          switch (c) {
            case '(':
            case '[':
               openers.push(c);
               break;
```

```
                case ')':
                  if (openers.empty() || openers.top()!='(')
                        return false;
                  openers.pop();
                  break;
                case ']':
                  if (openers.empty() || openers.top()!='[')
                        return false;
                  openers.pop();
                  break;
              }
        }
        return openers.empty() ;
}
```

2) Give an algorithm for reversing a queue Q. Only following standard operations are allowed on queue:
   a) Q.push(x) : Add an item x to the back of the queue.
   b) Q.pop() : Remove an item from the front of the queue.
   c) Q.front() : Return the item at the front of the queue
   d) Q.empty() : Check if the queue is empty or not.

   You may use an additional data structure if you wish.

   Example:

   Input: Q = [10, 20, 30, 40, 50, 60, 70, 80, 90, 100]
   Output: Q = [100, 90, 80, 70, 60, 50, 40, 30, 20, 10]

   [Suggested Time: 5 mins]

```
void reverseQueue(queue<int>& Q){
      // use an auxiliary stack
      stack<int> S;
      while (!Q.empty()) {
          S.push(Q.front());
          Q.pop();
      }
      while (!S.empty()) {
          Q.push(S.top());
          S.pop();
      }
}
```

3) Write a function *findNextInts* that takes in two integer arrays of size *n:* *sequence* and *results*. This function assumes that *sequence* already contains a sequence of positive integers. For each position *i* (from 0 to *n*-1) of *sequence*, this function should find the smallest index *j* such that *j* > *i* and *sequence[j]* > *sequence[i]*, and put *sequence[j]* in *results[i]*; if there is no such *j*, put -1 in *sequence[i]*. Try to do this without nested for loops both iterating over the array! (Hint: `#include <stack>`). **Store the nearest value behind the current one that is smaller than it in the result, if no, put -1**

```
void findNextInts(const int sequence[], int results[], int n);
```

Example:

```
int seq[] = {2, 6, 3, 1, 9, 4, 7 }; // Only positive integers!
int res[7];
findNextInts(seq, res, 7);
for (int i = 0; i < 7; i++) { // Should print: 6 9 9 9 -1 7 -1
  cout << res[i] << " ";
}
cout << endl;
```

Notice that the last value in *results* will always be set to -1 since there are no integers in *sequence* after the last one!

[Suggested Time: 10 mins]

```
void findNextInts(const int sequence[], int results[], int n)
{
  if (n <= 0)
    return;

  stack<int> s;

    // push the first index to stack
  s.push(0);

    // iterate for rest of the elements
  for (int i = 1; i < n; i++) {
    int current = sequence[i];

      // Fill in results for preceding unfilled items
      // that are less than current.
    while (!s.empty() && current > sequence[s.top()]) {
     results[s.top()] = current;
     s.pop();
   }
```

```
    s.push(i);
  }

    // Remaining items don't have a later greater value
  while (!s.empty()) {
    results[s.top()] = -1;
    s.pop();
  }
}
```

4) Evaluate the following postfix expression, show your work:
   9 5 * 8 - 6 7 * 5 3 - / *

   [Suggested Time: 5 mins]

```
45 8 - 42 2 / *
37 21 *
777
```

5) Implement a Stack class using only queues as data structures. This class should implement the *empty*, *size*, *top*, *push*, and *pop* member functions, as specified by the standard library's implementation of stack. (The implementation will not be very efficient.)

   [Suggested Time: 10 mins]

```
class Stack {
  //This implementation of Stack accepts only int. See if you
  //can make an implementation with templates!
public:
  bool empty() const;
  size_t size() const;
  int top() const;
  void push(const int& value);
  void pop();
private:
  queue<int> storage;
};d

bool Stack::empty() const {
  return storage.empty();
}
```

```
size_t Stack::size() const {
  return storage.size();
}

int Stack::top() const {
  return storage.back();
}

void Stack::push(const int& value) {
  storage.push(value);
}

void Stack::pop() { //Note that this causes a runtime error if
// storage is empty. This matches how calling pop() on an empty
// C++ STL stack causes a runtime error.
  int limit = storage.size() - 1;
  for (int n = 0; n < limit; n++) {
    storage.push(storage.front());
    storage.pop();
  } //circling the entire queue
  storage.pop(); } //stack is LIFO, queue is LILO,
```

6) Implement a Queue class using only stacks as data structures. This class should implement the *empty*, *size*, *front*, *back*, *push*, and *pop* member functions, as specified by the standard library's implementation of queue. (The implementation will not be very efficient.)
[Suggested Time: 15 mins]

```
class Queue {
  //This implementation of Queue accepts only int. See if you
can
  //make an implementation with templates!
 //pushStorage is a stack that contains items when they're
first
 //pushed. popStorage is another stack, and we move items from
 //pushStorage to popStorage when we want to pop from the queue
public:
  bool empty() const;
  size_t size() const;
  int front() const;
  int back() const;
  void push(const int& value);
  void pop();
```

```
private:
  //move items from pushStorage to popStorage while leaving
back
  //item within pushStorage
  void moveItems();

  //storage for pushing items with one exception: always
includes
  //back item if available
  stack<int> pushStorage;
  //storage for popping items: always includes front item
  stack<int> popStorage;
};

bool Queue::empty() const {
  return pushStorage.empty() && popStorage.empty();
}

size_t Queue::size() const {
  return pushStorage.size() + popStorage.size();
}

int Queue::front() const {
  return popStorage.top();
}

int Queue::back() const {
  if (size() == 1)
    return popStorage.top();
  return pushStorage.top();
}

void Queue::push(const int& value) {
  if (size() > 0)
    pushStorage.push(value);
  else
    popStorage.push(value);
}

void Queue::pop() { //Note that this causes a runtime error if
// popStorage and pushStorage are empty (i.e. the Queue has no
// items in it). This matches how calling pop() on an empty
// C++ STL queue causes a runtime error.
  if (popStorage.size() > 0) {
    popStorage.pop();
```

```
    if (popStorage.size() == 0 && pushStorage.size() > 0)
      moveItems();
  }
  else {
    moveItems();
    popStorage.pop();
  }
}

void Queue::moveItems() {
  int temp = pushStorage.top();
  bool backExists = false;
  if (pushStorage.size() > 1) {
    pushStorage.pop();
    backExists = true;
  }

  while (pushStorage.size() > 0) {
    popStorage.push(pushStorage.top());
    pushStorage.pop();
  }

  if (backExists)
    pushStorage.push(temp);
}
```