

FORMULÁRIO

Considerando que u é uma função real de variável real x e que $a, \alpha, \beta \in \mathbb{R}$,

$$\frac{d}{dx} u^\alpha = \alpha u^{\alpha-1} \frac{du}{dx} \quad (\alpha \neq 0)$$

$$\frac{d}{dx} \log_a u = \frac{\log_a e}{u} \frac{du}{dx}$$

$$\frac{d}{dx} \left(\frac{a^u}{\ln a} \right) = a^u \frac{du}{dx}$$

$$\frac{d}{dx} e^u = e^u \frac{du}{dx}$$

$$\frac{d}{dx} u^v = \frac{d}{dx} e^{v \ln u} = e^{v \ln u} \frac{d}{dx} (v \ln u)$$

$$\frac{d}{dx} \cos u = -\operatorname{sen} u \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{sen} u = \cos u \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{tg} u = \sec^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{cotg} u = -\operatorname{cosec}^2 u \frac{du}{dx}$$

$$\frac{d}{dx} \sec u = \sec u \operatorname{tg} u \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{cosec} u = -\operatorname{cosec} u \operatorname{cotg} u \frac{du}{dx}$$

$$\frac{d}{dx} (\arccos u) = -\frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$$

$$\frac{d}{dx} (\operatorname{arcsen} u) = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$$

$$\frac{d}{dx} (\operatorname{arctg} u) = \frac{1}{1+u^2} \frac{du}{dx}$$

$$\frac{d}{dx} (\operatorname{arccotg} u) = -\frac{1}{1+u^2} \frac{du}{dx}$$

$$\frac{d}{dx} (\operatorname{arcsec} u) = \frac{1}{|u| \sqrt{u^2-1}} \frac{du}{dx}$$

$$\frac{d}{dx} (\operatorname{arccosec} u) = -\frac{1}{|u| \sqrt{u^2-1}} \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{ch} u = \operatorname{sh} u \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{sh} u = \operatorname{ch} u \frac{du}{dx}$$

$$\frac{d}{dx} \operatorname{th} u = \operatorname{sech}^2 u \frac{du}{dx}$$

Algumas fórmulas trigonométricas:

$$\sec \alpha = \frac{1}{\cos \alpha}$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \operatorname{sen} \alpha \operatorname{sen} \beta$$

$$\cos \frac{\alpha}{2} = \pm \sqrt{\frac{1 + \cos \alpha}{2}}$$

$$\operatorname{cosec} \alpha = \frac{1}{\operatorname{sen} \alpha}$$

$$\operatorname{sen}(\alpha \pm \beta) = \operatorname{sen} \alpha \cos \beta \pm \operatorname{sen} \beta \cos \alpha$$

$$\operatorname{sen} \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{2}}$$

$$\cos^2 \alpha + \operatorname{sen}^2 \alpha = 1$$

$$\operatorname{tg}(\alpha \pm \beta) = \frac{\operatorname{tg} \alpha \pm \operatorname{tg} \beta}{1 \mp \operatorname{tg} \alpha \operatorname{tg} \beta}$$

$$\operatorname{tg} \frac{\alpha}{2} = \pm \sqrt{\frac{1 - \cos \alpha}{1 + \cos \alpha}} = \frac{1 - \cos \alpha}{\operatorname{sen} \alpha}$$

Algumas fórmulas relevantes

$$\operatorname{ch} u = \frac{e^u + e^{-u}}{2}$$

$$\operatorname{ch} \frac{u}{2} = \pm \sqrt{\frac{\operatorname{ch} u + 1}{2}}$$

$$\operatorname{ch}(u \pm v) = \operatorname{ch} u \operatorname{ch} v \pm \operatorname{sh} u \operatorname{sh} v$$

$$\operatorname{sh} u = \frac{e^u - e^{-u}}{2}$$

$$\operatorname{sh} \frac{u}{2} = \pm \sqrt{\frac{\operatorname{ch} u - 1}{2}}$$

$$\operatorname{sh}(u \pm v) = \operatorname{sh} u \operatorname{ch} v \pm \operatorname{sh} v \operatorname{ch} u$$

$$\operatorname{th} u = \frac{\operatorname{sh} u}{\operatorname{ch} u}$$

$$\operatorname{coth} u = \frac{1}{\operatorname{th} u}$$

$$\operatorname{th} \frac{u}{2} = \pm \sqrt{\frac{\operatorname{ch} u - 1}{\operatorname{ch} u + 1}} = \frac{\operatorname{sh} u}{\operatorname{ch} u + 1}$$

$$\operatorname{th}(u \pm v) = \frac{\operatorname{th} u \pm \operatorname{th} v}{1 \pm \operatorname{th} u \operatorname{th} v}$$

$$\operatorname{ch}^2 u - \operatorname{sh}^2 u = 1$$