

Quiz 1: Storage Systems (10 points), 10 minutes

Consider a hard disk with maximum seek time of 15ms, patter speed of 7200RPM, (maximum) bandwidth of 100MB/sec. Assume 4KB per block.

1. [5 points] Compute the completion time and actual bandwidth for sequential access of 100MB of data. Show your work (i.e., how you derive the answer).

$$\text{Average seek time} = T_{seek} = \frac{1}{3} * \text{max seek time} = \frac{1}{3} * 15ms = 5ms$$

$$\text{Time for full rotation is } \frac{60,000ms}{7200rot} = 8.33ms/rotation$$

$$\text{Average rotation latency} = T_{rot} = \frac{1}{2} * 8.33ms = 4.17ms$$

$$\text{Transfer time} = T_{trans} = \frac{100MB}{100MB/sec} = 1000ms$$

$$T = T_{seek} + T_{rot} + T_{trans} = 5ms + 4.17ms + 1000ms = 1009.17ms$$

$$\text{Actual bandwidth} = \frac{100MB}{1009.17ms} = 99.09MB/sec$$

2. [5 points] Compute the completion time and actual bandwidth for random access of 100MB of data. Show your work.

$$\#Blocks = \frac{100MB}{\frac{4KB}{block}} = 25,600blocks$$

$$T' = \#Blocks * (T_{seek} + T_{rot} + T_{trans}') = \frac{100MB}{\frac{4KB}{block}} * \left(5ms + 4.17ms + \frac{4KB}{100MB/sec} \right)$$

$$= 235.75sec$$

$$\text{Actual bandwidth} = \frac{100MB}{235.75sec} = 0.424MB/sec = 434.36KB/sec$$

Quiz 2: Storage Systems (10 points), 10 minutes (afternoon)

Consider a hard disk with maximum seek time of 12ms, patters rotating at 7200RPM, (maximum) transmission bandwidth of 100MB/sec. Assume 4KB per block.

1. [7 points] Compute the completion time and actual bandwidth for **random** access of 100MB of data. Show your work (i.e., how you derive the answer).

$$\# \text{ of blocks} = \frac{100 \text{ MB}}{4 \text{ KB/block}} = 25,600 \text{ blocks} \quad \neq 25000$$

1 K = 1024 !!!!!

$$T_{seek} = \text{Average seek time} = \frac{1}{3} \times \text{maximum seek time} = \frac{1}{3} \times 12\text{ms} = 4\text{ms}$$

$$\text{Since time for a full rotation} = \frac{60000 \text{ ms}}{7200 \text{ rotations}} = 8.33 \text{ ms},$$

$$T_{rotation} = \text{Average rotation latency} = \frac{1}{2} \times 8.33 \text{ ms} = 4.17\text{ms}$$

$$T_{transfer} = \text{Transfer time per block} = \frac{4\text{KB}}{100 \text{ MB/sec}} \times 1000\text{ms} = 0.04\text{ms}$$

$$T = \# \text{ of blocks} \times (T_{seek} + T_{rotation} + T_{transfer}) = 25,600 \times (4\text{ms} + 4.17\text{ms} + 0.04\text{ms}) \\ = 210,176\text{ms} = 210.176\text{sec}$$

$$\text{Actual bandwidth} = \frac{100\text{MB}}{210.176 \text{ sec}} = 0.476\text{MB/sec} = 487.2107\text{KB/sec}$$

2. [3 points] Which of the time: latency or transmission time, dominates the completion time? What if the workload is changed to “**sequential** access of 100MB of data”? Explain your answer.

1. Latency time dominates when we access the data randomly since $8.17\text{ms} > 0.04\text{ms}$ for each block.

2. Transmission time will dominate the completion time when it is changed to sequential access, because it doesn't need to seek and rotate for every block of data.

Quiz 2: Storage Systems (10 points), 10 minutes (morning)

Consider a hard disk with maximum seek time of 12ms, patters rotating at 1000RPM, (maximum) transmission bandwidth of 100MB/sec. Assume 4KB per block.

1. [7 points] Compute the completion time and actual bandwidth for sequential access of 100MB of data. Show your work (i.e., how you derive the answer).

$$\text{Completion Time} = T_{\text{seek}} + T_{\text{rot}} + T_{\text{transfer}}$$

$$\text{Avg. Seek Time} = 1/3 * \text{Max Seek Time} = 1/3 * 12 = 4\text{ms}$$

$$\text{Time for 1 rotation} = 60000 \text{ ms} / 1000 \text{ rotations} = 60 \text{ ms}$$

$$\text{Rotational Latency} = 60/2 = 30\text{ms}$$

$$\text{Transfer Time} = 100 \text{ MB} / 100 \text{ MB} * 1000 = 1000\text{ms}$$

$$\begin{aligned} \text{Therefore, completion time} &= T_{\text{seek}} + T_{\text{rot}} + T_{\text{transfer}} \\ &= 4 + 30 + 1000 \\ &= 1034 \text{ ms} \end{aligned}$$

$$\text{Actual Bandwidth} = |w| / \text{completion time} = 100\text{MB} / 1034\text{ms} = 96.711 \text{ MB/s}$$

2. [3 points] Which of the time: latency or transmission time, dominates the completion time? What if the workload is changed to “random access of 100MB of data”? Explain your answer.

Transfer time dominates the completion time since sequential access of data, thus no rotation/seeking needed once we find start point.

If workload is changed to random access of 100 MB of data:

$$\text{No. of blocks to be transferred} = 100/4 * 1000 = 25000$$

$$\text{Completion time} = 25000 * (4 + 30 + 4/100) = 850000 + 1000 = 851000$$

850000 >> 1000, therefore latency time dominates in this case since multiple seeking/rotation needed.

INF 551 – Spring 2018

Quiz 2: Storage systems (10 points), 10 minutes

Consider a hard drive with the following characteristics:

Number of cylinders	512
Number of heads	8
Number of sectors per track	256
Size of sector	4KB
Number of sectors per block	1
(Maximum) bandwidth	100MB/s
Rotational speed	7,200RPM
Maximum seek time	15ms

a. $512 \times 8 \times 256 \times 4 \text{ KB} = 4 \text{ GB}$

b. rotational latency T_{rot}

$= \frac{1}{2} \times \text{rotational speed}$

$= \frac{1}{2} \times \frac{60000 \text{ ms/min}}{7200 \text{ RPM}} = \frac{25}{6} \text{ ms}$

seek latency T_{seek}

$= \frac{1}{3} \times \text{Maximum seek time} = \frac{1}{3} \times 15 \text{ ms} = 5 \text{ ms}$

Transmission $= \frac{\text{block size}}{\text{bandwidth}}$

$= 1 \times 4 \text{ KB} / 100 \text{ MB/s}$

$= \frac{4 \times 1000 \text{ ms}}{102400} = \frac{1}{25.6} \text{ ms}$

- a) [2 points] What is the capacity of the hard drive?

Capacity = #cylinders * #heads * #sector per track * size of sector

$= 512 * 8 * 256 * 4 \text{ KB} = 2^9 * 2^3 * 2^8 * 2^2 * 2^{10} \text{ Bytes}$

$= 2^{32} \text{ Bytes} = 4 \text{ GB}$

Random

Completion Time

$= \# \text{ blocks } (T_{seek} + T_{rot} + T_{trans})$

- b) [4 points] How much does it take to access 100 blocks **randomly** located on the disk? What

is the actual bandwidth for this workload?

$= 100 \times (\frac{25}{6} \text{ ms} + 5 \text{ ms} + \frac{1}{25.6} \text{ ms}) \approx 921 \text{ ms}$

Random access: For each block

$T_{seek} = \text{Average seek time} = \frac{1}{3} * \text{Maximum seek time} = 5 \text{ ms}$

$T_{rotation} = \frac{1}{2} \text{ rotation} * \text{Full rotation time}$

$= \frac{1}{2} \text{ rotation} * (60000 \text{ ms per minute}) / (7200 \text{ Rotations per minute})$

$= \frac{1}{2} \text{ rotation} * 8.33 \text{ ms / rotation}$

$= 4.17 \text{ ms}$

$T_{transfer} = 4 \text{ KB} / (100 \text{ MB/s}) = 4 \text{ KB} / (100 \text{ KB/ms}) = 0.04 \text{ ms}$

$T = (T_{seek} + T_{rotation} + T_{transfer}) * \# \text{ blocks} = 9.21 * 100 = 921 \text{ ms}$

Actual bandwidth = 100 blocks * 4 KB/sector * 1 sector/block / 921 ms

$= 400 / 921 \text{ KB/ms} = 0.43 \text{ KB/ms} = 0.43 \text{ MB/s}$

Actual Bandwidth $|W| = \frac{\# \text{ blocks} \times \text{block size}}{T_{\text{Completion}}}$

$= \frac{100 \times 1 \times 4 \text{ KB}}{921 \text{ ms}}$

- c) [4 points] How much does it take to access 100 blocks **sequentially** located on the disk?

What is the actual bandwidth for this workload?

Sequential access:

For the full process:

$T_{seek} = 5 \text{ ms}$

$T_{rotation} = 4.17 \text{ ms}$

For each block:

$T_{transfer} = 0.04 \text{ ms}$

$T = T_{seek} + T_{rotation} + T_{transfer} * \# \text{ blocks}$

$= 5 + 4.17 + 0.04 * 100$

$= 13.17 \text{ ms}$

Actual bandwidth = 400 / 13.17 KB/ms = 30.37 KB/ms = 30.37 MB/s

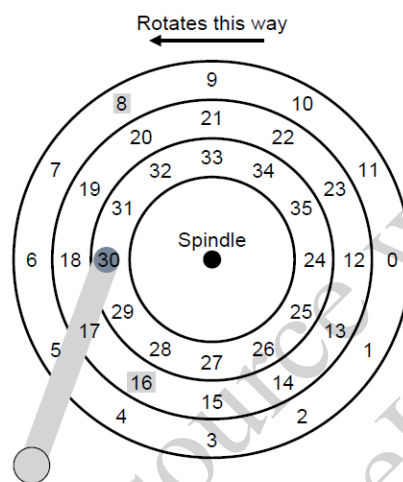
25
50
~~72000~~
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12 6

INF 551 – Spring 2016

Quiz 1: Storage systems (10 points)

10 minutes

Consider the following hard disk. Suppose the head is on sector #30 and the requests in the queue are 16 and 8 (which 16 arrived first). Suppose that the disk rotates at **6,000 RPM** and it takes **1ms** to travel a track. According to the SPTF (shortest positioning time first) algorithm, which request should be served first? Explain your answer by computing the positioning time for each request.



$$10 \text{ ms} \times \frac{10}{12} + 1 = \frac{112}{12} \text{ ms}$$

$$10 \text{ ms} \times \frac{2}{12} + 2 = \frac{44}{12} \text{ ms} < \frac{112}{12} \text{ ms}$$

Answer:

The disk rotates at 6,000 RPM, so

$$T_{\text{rotation}} = \frac{\text{Time (ms)}}{1 \text{ rotation}} = \frac{1 \text{ min}}{6,000 \text{ rot}} \times \frac{60 \text{ sec}}{1 \text{ min}} \times \frac{1000 \text{ msec}}{\text{sec}} = \frac{60,000 \text{ msec}}{6,000 \text{ rot}} = \frac{10 \text{ msec}}{\text{rotation}}$$

Consider 30 → 16: we will need to travel 1 track and rotate over 10 sectors. So

$$\text{The positioning time } T_{30-16} = T_{\text{seek}} + T_{\text{rotation}} = 1 \text{ ms} + \frac{10}{12} * 10 \text{ ms} \approx 9.33 \text{ ms}$$

Consider 30 → 8: we will need to travel 2 tracks and rotate over 2 sectors. So

$$\text{The positioning time } T_{30-8} = T_{\text{seek}} + T_{\text{rotation}} = 2 \text{ ms} + \frac{2}{12} * 10 \text{ ms} \approx 3.67 \text{ ms}$$

Therefore, sector 8 will be served first.