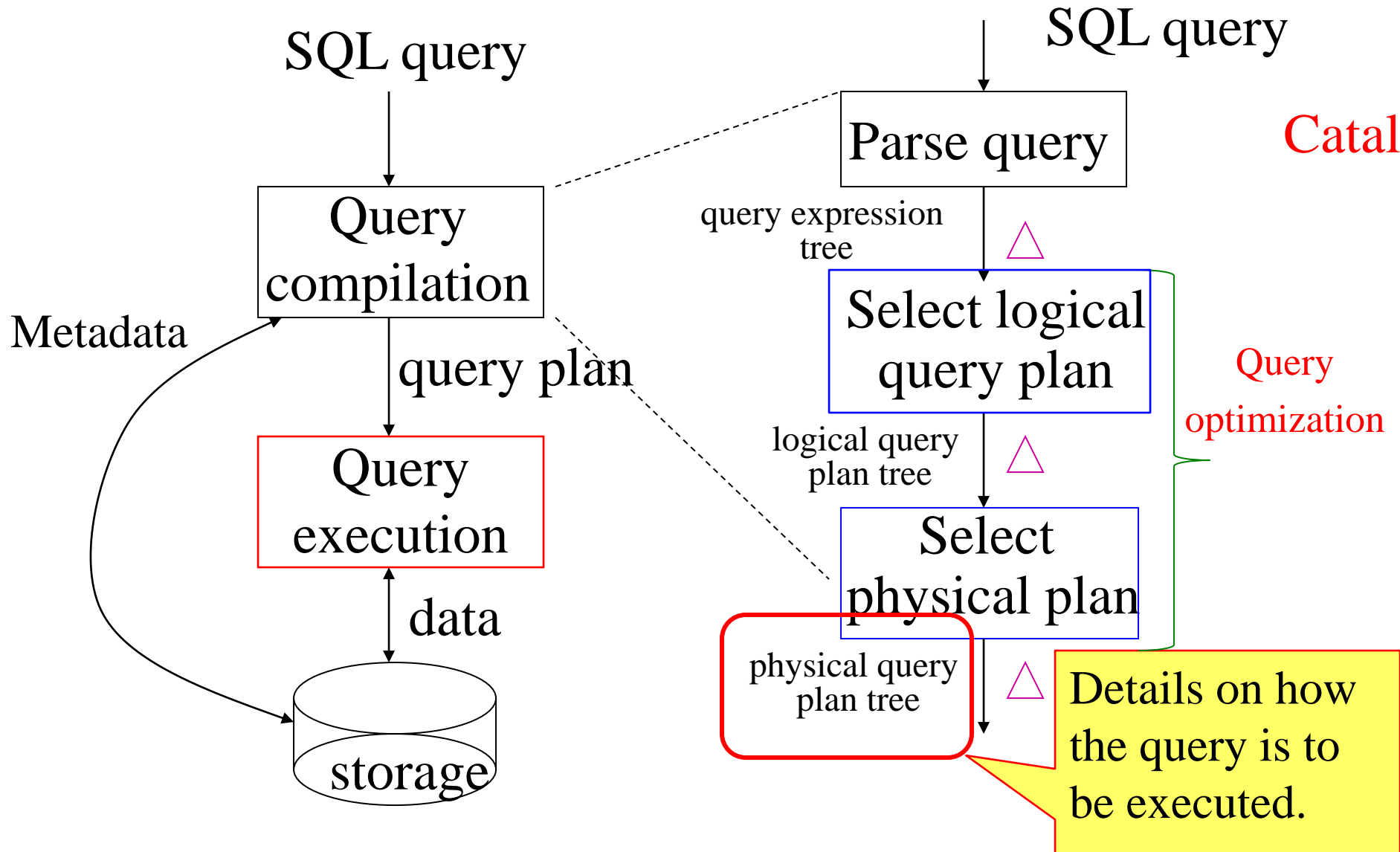


Query Execution

DSCI 551
Wensheng Wu

Components of Query Processor



Converting SQL to Logical Plans

Select a_1, \dots, a_n
From R_1, \dots, R_k
Where C

$$\Pi_{a_1, \dots, a_n}(\sigma_C(R_1 \times R_2 \times \dots \times R_k))$$

Select b_1, \dots, b_m , aggs
From R_1, \dots, R_k
Where C
Group by b_1, \dots, b_m

$$\gamma_{b_1, \dots, b_m, \text{aggs}}(\sigma_C(R_1 \times R_2 \times \dots \times R_k))$$

Logical Query Optimization

- Apply algebraic laws to turn initial query plan into more efficient one
- Use heuristics
 - E.g., do selections & projection as early as possible

Example of Algebraic Law

$$\square \sigma_C (R \bowtie S) = \sigma_C (R) \bowtie S$$

- That is, we can push selection down to R if condition C only contains attributes in R

Physical Query Optimization

- Turn logical query plan into physical ones
 - That is, plan with physical operators
- Pick a physical plan with the lowest cost (I/O's)
 - I.e., cost-based optimization

Outline

- Logical/physical operators
- Cost model
- One-pass algorithms
- Nested-loop joins: 1.x
- Two-pass algorithms
 - Sorting-based
 - Hashing-based
- Index-based algorithms

Logical vs. Physical Operators

- Logical operators
 - what they do
 - e.g., union, selection, projection, join, group-by
- Physical operators
 - how they do it
 - Main methods: scanning, hashing, sorting, and index-based
 - E.g., methods for implementing joins include:
 - nested loop join, sort-merge join, hash join, index join
 - Different methods may have different requirements on the amount of available memory & different costs

Logical Query Plans

```
SELECT  P.buyer
FROM    Purchase P, Person Q
WHERE   P.buyer=Q.name
```

Construct logical
plan...

NLJ (Purchase outer) :
 for p in Purchase:
 for q in Person:
 if (p.buyer = q.name)
NLJ (Person is outer):...

Logical Query Plans

```
SELECT P.buyer
FROM Purchase P, Person Q
WHERE P.buyer=Q.name AND
      Q.city='LA'
```

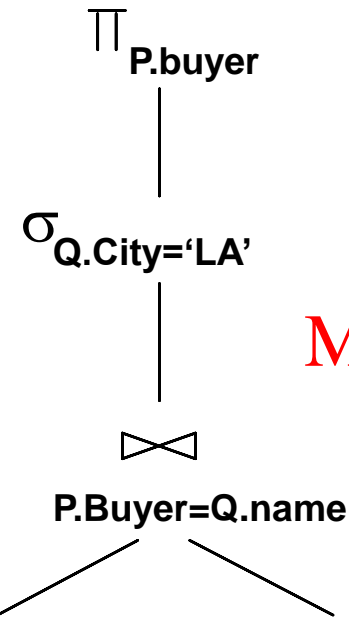
n, john

Query Plan:

- Tree with logical operators
- $h(\text{buyer})$
- $h(\text{name})$
- $h(\text{John}) = 0/1$

100MB
(purchase)

2GB = Part1:
P2: 90
P3: 20



$M(\text{memory}) = 2$

Scenario A:

B:

C:

Purchase (m)

Person (n)

100MB

200MB

100MB

2GB = P1 (1GB),

2GB

2GB

R1: 1GB

P1: 1GB

Notes

$$h(\text{John}) = (74+111+104+110) \\ \% 2 + 1 = 2$$

Example (cont'd)

M = 1GB

	Purchase	Person
A:	100MB	200MB
B:	100MB	2GB
C:	2GB	2GB

R1: 500MB	P1: 500M
-----------	----------

R2: 500M	P2: 500M
----------	----------

R3: 500M	P3: 500M
----------	----------

R4: 500M	P4: 500M
----------	----------

R1 join P1

R1 join P2

R1 join P3

R1 join P4

R2 join P1

...

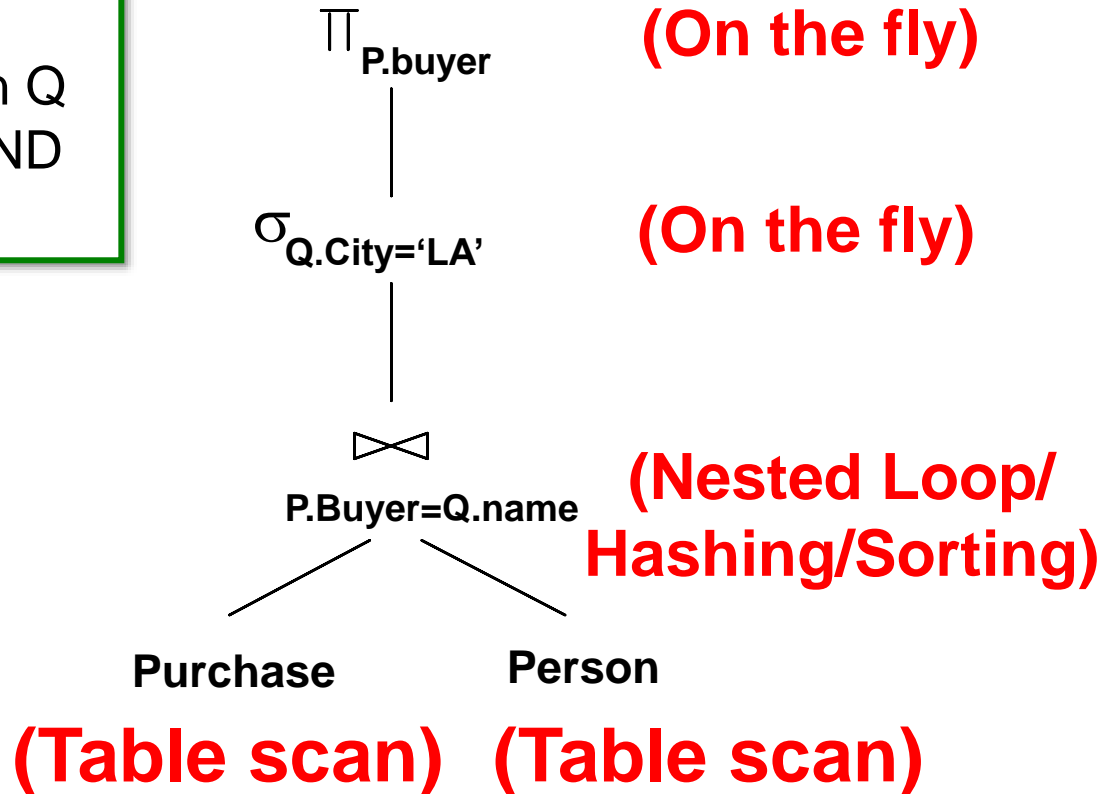
Block-based NLJ algorithm

Physical Query Plans

```
SELECT P.buyer
FROM   Purchase P, Person Q
WHERE  P.buyer=Q.name AND
       Q.city='LA'
```

Query Plan:

- Logical tree plus
- **Implementation**
choice at each node



How do We Combine Operations?

- **The iterator model.** Each operation is implemented by 3 functions:
 - *Open*: sets up the data structures and performs initializations
 - *GetNext*: returns the the next tuple of the result.
 - *Close*: ends the operations. Cleans up the data structures.
- Enables pipelining!
- Contrast with **data-driven materialized model**

```
class C
def c
def m
def c
```

```
class F
def
def
```

```
class F
def
```

```
class J
def
```

Cost Model

- Cost parameters
 - M = number of blocks/pages that are available in main memory
 - $B(R)$ = number of blocks holding R
 - $T(R)$ = number of tuples in R
 - $V(R,a)$ = number of distinct values of the attribute a of R
- Estimating the cost of physical operators:
 - Important in query optimization
 - Here we consider I/O cost only
 - We assume operands are relations stored on disk, but operator results will be left in main memory (e.g., pipelined to next operator in query plan)
 - So we don't include the cost of *writing* the result

Selectivity

- The larger $V(R,a)$, the more selective a is for R
- Employee(ssn, name, age, gender)
 - Which of the above attributes is most/least selective?
 - $V(\text{Employee}, \text{gender}) = 2$
 - $V(\text{Employee}, \text{ssn}) = n$

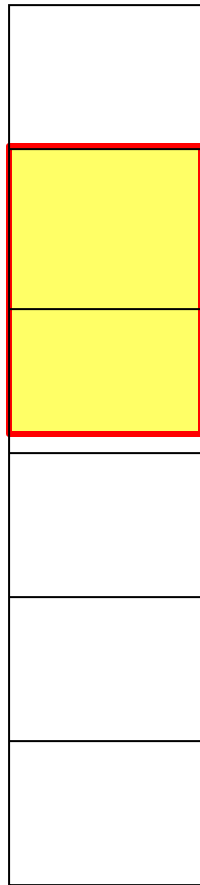
I/O Cost

- # of blocks read from or written to disk
- Recall that disk reads/writes data in the unit of block

Scanning Tables

- Reading every row of tables
- The table is *clustered* (i.e., block consists only of records from this table):
 - # of I/O's = # of blocks
- The table is *unclustered* (e.g. its records are placed in blocks with those of other tables)
 - May need one block read for each record

Scanning Clustered/Unclustered Tables



2 Block Reads
($B(R) = 2$)

Clustered table

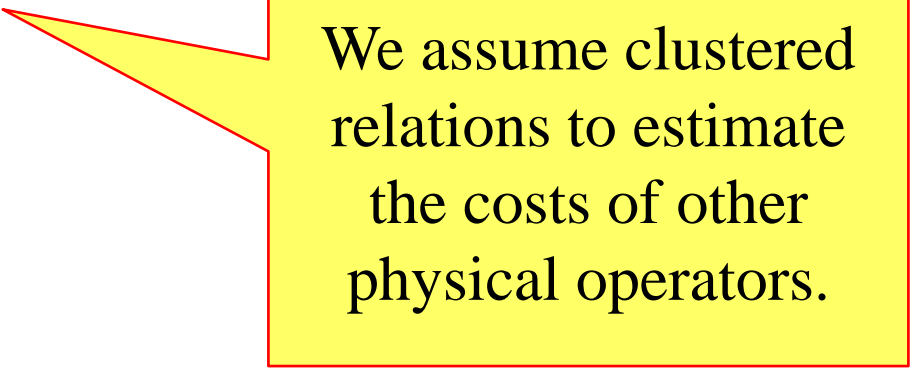


4 Reads
($T(R) = 4$)

Unclustered table

Cost of the Scan Operator

- Clustered relation:
 - Table scan: $B(R)$
- Unclustered relation:
 - $T(R)$



We assume clustered relations to estimate the costs of other physical operators.

Classification of Physical Operators

- One-pass algorithms
 - Read the data only once from disk
 - Usually, require at least one of the input relations fits in main memory
- Nested-Loop Join algorithms (1.x)
 - Read one relation only once, while the other will be read repeatedly from disk
- Two-pass algorithms
 - First pass: read data from disk, process it, write it to the disk
 - Second pass: read the data for further processing

Classification of Physical Operators

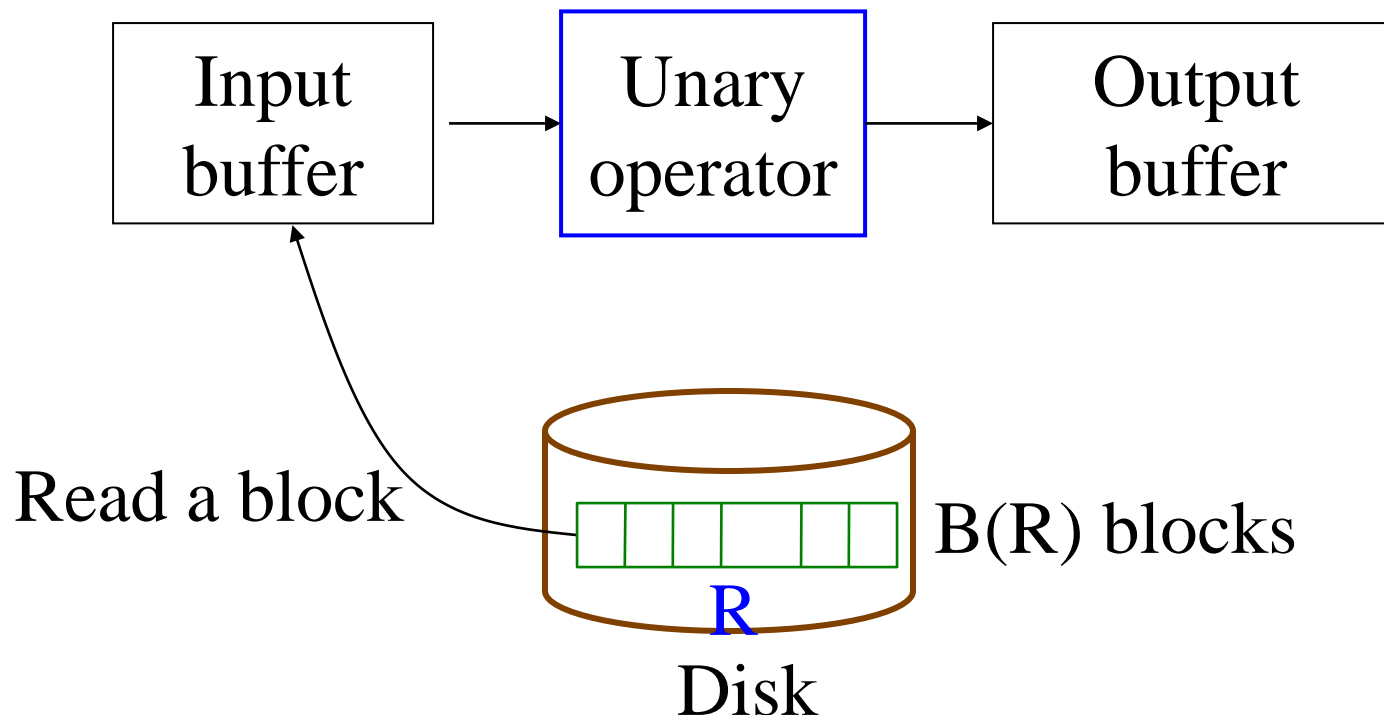
- K-pass algorithms
 - If data are too big or memory is too small, the algorithm may need $k > 2$ passes over the data

One-pass algorithms

One-pass Algorithms

Selection $\sigma(R)$, projection $\Pi(R)$

- Both are tuple-at-a-time algorithms
- Cost: $B(R)$



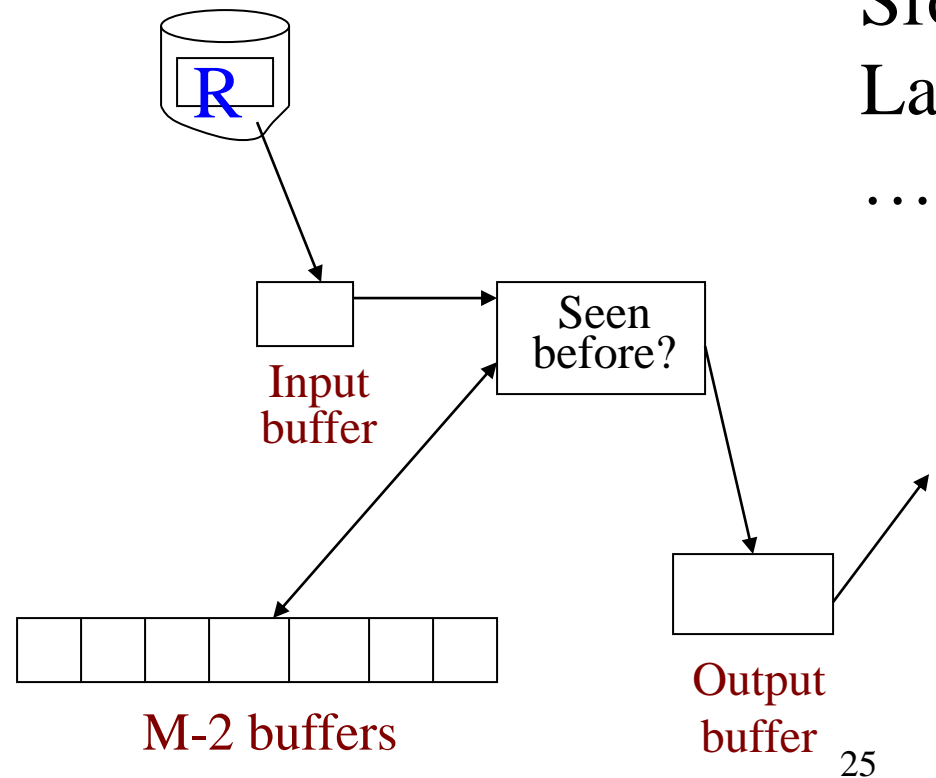
One-pass Algorithms

Duplicate elimination $\delta(R)$

- Need to keep a dictionary in memory:
 - balanced search tree
 - hash table
 - Etc.
- Cost: $B(R)$
- Assumption:

$$B(\delta(R)) \leq M-2$$

or roughly M



One-pass Algorithms

Grouping: $\gamma_{\text{city}, \text{sum}(\text{price})} (R)$

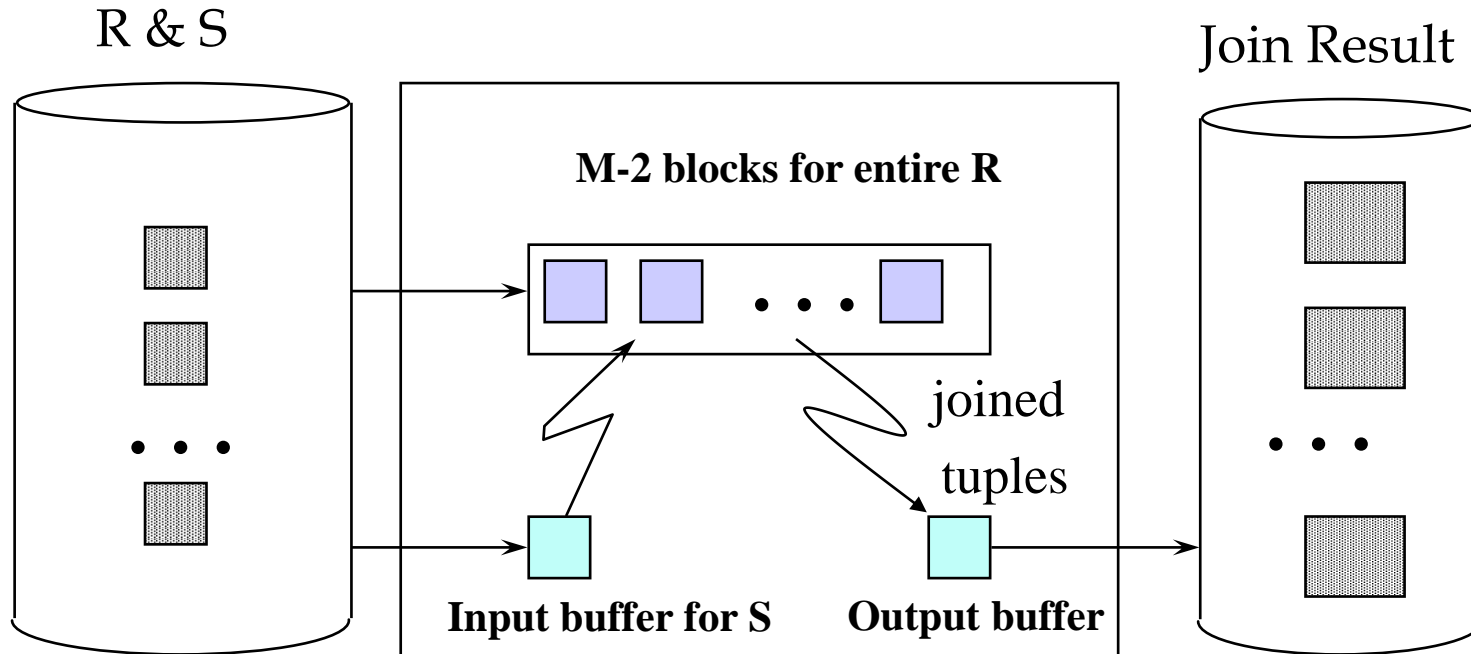
- Need to keep a dictionary in memory
 - Also store the $\text{sum}(\text{price})$ for each city
- Cost: $B(R)$
- Assumption: number of cities and sums fit in memory

One-pass Algorithms

Binary operations: $R \cap S$, $R \cup S$, $R - S$, $R \bowtie S$

- Assumption: $\min(B(R), B(S)) \leq M$ (or $M-2$ to be exact)
- Scan a smaller table of R and S into main memory, then read the other one, block by block
- Cost: $B(R)+B(S)$ (assume both are clustered)
- E.g. $R \cap S$ (assume set-based, no duplicates)
 - Read S into $M-2$ buffers and build a search structure
 - Read each block of R , and for each tuple t of R , see if t is also in S .
 - If so, copy t to the output; if not, ignore t

One-pass join algorithm



$$M = 102$$

$$B(R) \leq 100$$

Nested-loop join
(none of tables fits in memory...)

Tuple-based Nested Loop Joins

- Join $R \bowtie S$
- Assume neither relation is clustered

```
for each tuple r in R do  
  for each tuple s in S do  
    if r and s join then output (r,s)
```

- Cost: $T(R) T(S)$

Block-based Nested Loop Joins

- Assume both relations are clustered

for each $(M-2)$ blocks b_r of R do

for each block b_s of S do

for each tuple r in b_r do

for each tuple s in b_s do

if r and s join then output(r,s)

cost (R is outer): $1 +$

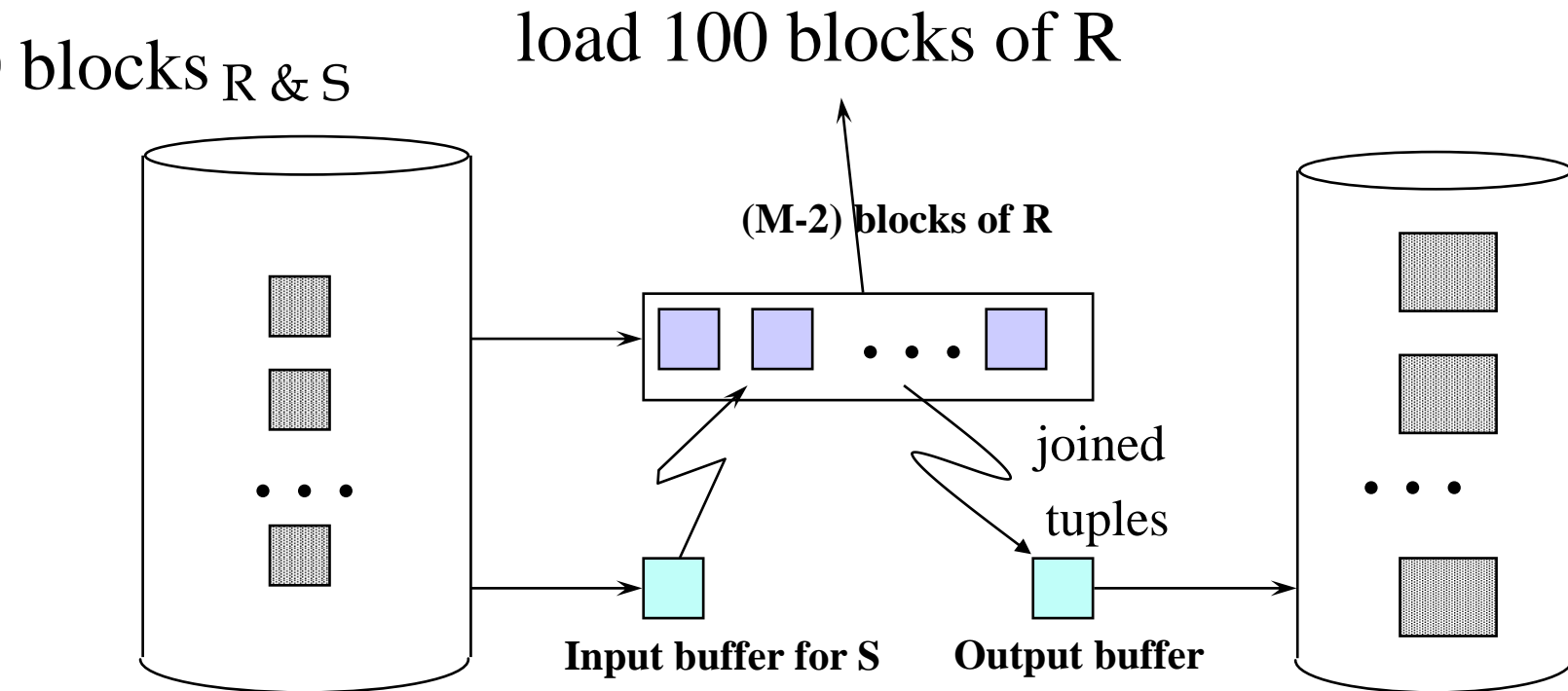
- R: one pass

- S: $B(R)/(M-2) *$

$\Rightarrow B(R) + B(R)/(M-$

- Assume $B(R) \leq B(S)$ & $B(R) > M$

Block-based Nested Loop Joins

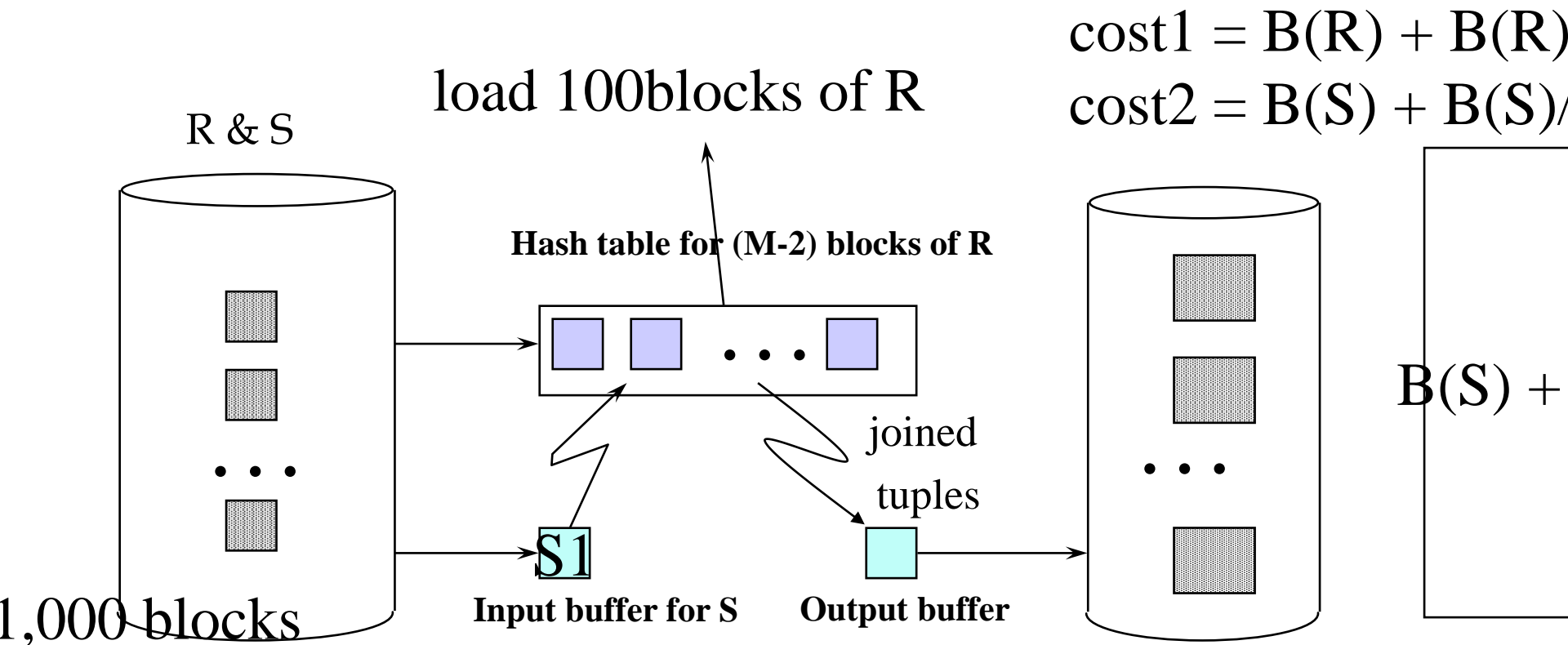


100 blocks

$$\text{cost}(R \text{ is outer}) = B(R) + B(R)/(M-2) * B(S)$$

$$\text{cost}(S \text{ is outer}) = B(S) + B(S)/(M-2) * B(R)$$

Block-based Nested Loop Joins



R outer: $B(R) + B(R)/(M-2) * B(S)$

S outer: $B(S) + B(S)/(M-2) * B(R)$

$M-2 \geq 1 \Rightarrow M \geq 3$

notes

- load 1st 100 blocks of R
 - load one block of S for 5000 times
=> making one pass through S
- load 2nd 100 blocks of R
=> making one pass through S
- ...
- load 10th 100 blocks of R
=> make one pass through S

cost (R is outer):

- R: one pass
 - S: $B(R)/(M-2) * B(S)$
 - 10 passes through S
- => $B(R) + B(R)/(M-2) * B(S)$

cost (S is outer):

- S: one pass
 - R: $B(S)/(M-2) * B(R)$
 - 50 passes through R
- => $B(S) + B(S)/(M-2) * B(R)$

Block-based Nested Loop Joins

- Cost:
 - Read R once: cost $B(R)$
 - Outer loop runs $B(R)/(M-2)$ times, and each time need to read S: costs $B(R)B(S)/(M-2)$
 - Total cost: $B(R) + B(R)B(S)/(M-2)$
- Notice: it is better to iterate over the smaller relation first
- $R \bowtie S$: R=outer relation, S=inner relation
- What is the minimum memory requirement?

Example

- Suppose $M = 102$ blocks (i.e., pages), $B(R) = 1000$ blocks, $B(S) = 5,000$ blocks
 - # of chunks from $R = 10$, chunk size = 100 blocks
- Cost of $R \bowtie S$ using blocked-based nested-loop join algorithm
 - If R is outer relation: one pass R ; 10 passes through S
 - $1000 \text{ blocks} + 1000/(102-2) * 5000 = 51,000$
 - If S is outer relation: one pass S ; 50 passes R
 - $+ 5000/(102-2) * 1000 = 55,000$

select
for
f

$B(R)$
1.x
 $B(S)$
1.x

Two-pass algorithms

Two-pass Algorithms

- If an operation can not be completed in one pass, can we design an algorithm to complete it in two passes?
 - Yes, but with certain restriction on the relation size

Ideas

- Sorting
 - Sort relation(s) into **runs**
 - Perform the needed operation while merging the runs
- Hashing
 - Hash relation(s) into **buckets**
 - Only need to examine a bucket or a pair of buckets at a time

Duplicate Elimination $\delta(R)$

Based on Sorting

- Simple idea: sort first, then eliminate duplicates
- Pass 1: sort runs of size M , write
 - Cost: $2B(R)$
- Pass 2: merge $M-1$ runs, but include each tuple only once
 - Cost: $B(R)$
- Total cost: $3B(R)$, Assumption: $B(R) \leq M^2$
 - since $B/M = \#$ of runs
 - $\#$ of runs has to be $\leq M-1$ to complete the merging in the second pass
 - So $B/M \leq M - 1$

Grouping: $\gamma_{\text{city}, \text{sum}(\text{price})} (R)$ Based on Sorting

- Pass 1: same as before
- Pass 2: same as before, but also compute $\text{sum}(\text{price})$ for group during the merge phase.
- Total cost: $3B(R)$
- Assumption: $B(R) \leq M^2$

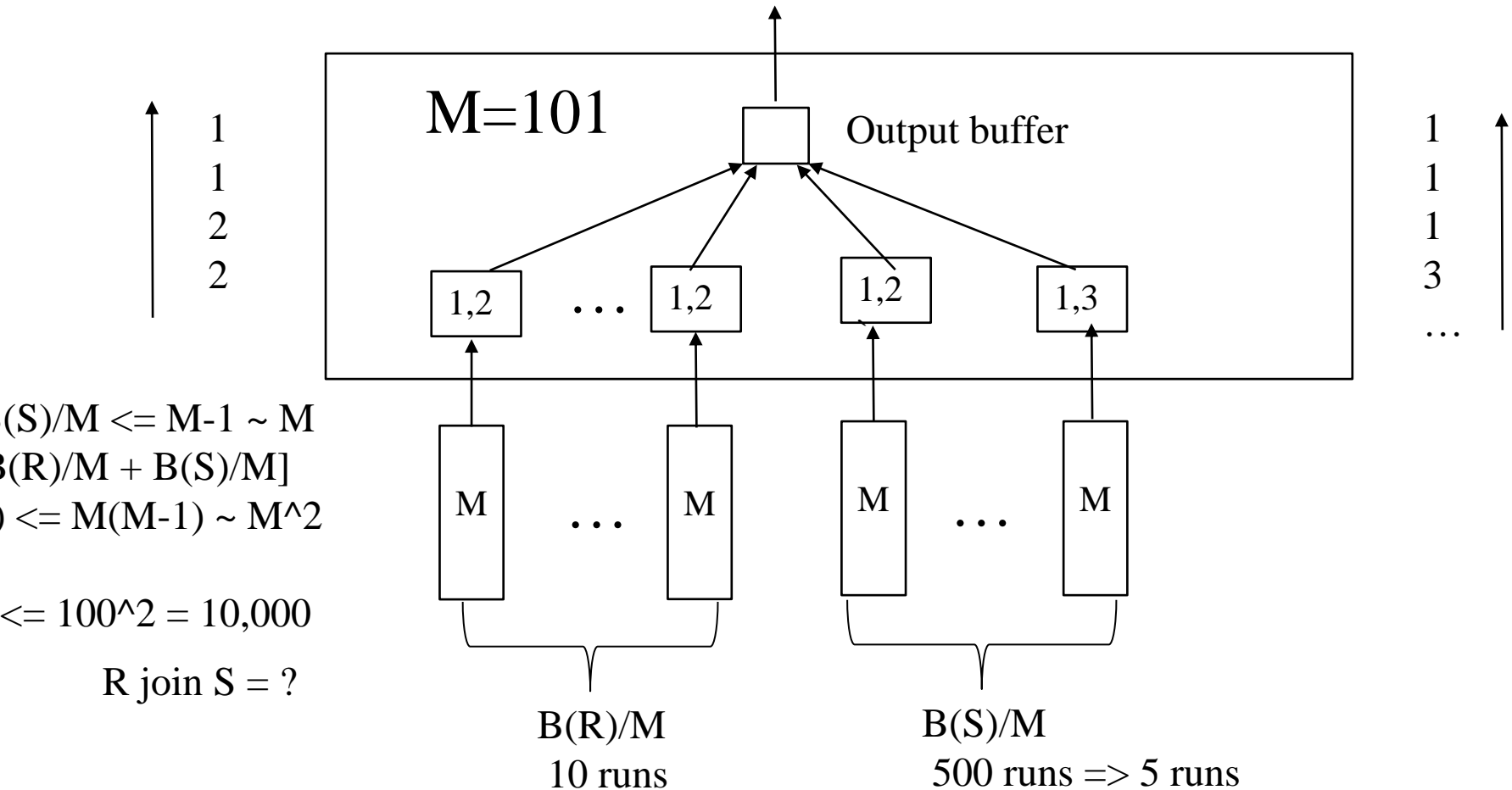
Binary operations: $R \cap S$, $R \cup S$, $R - S$

Based on Sorting

- Idea: sort R , sort S , then do the right thing
- A closer look:
 - Step 1: split R into runs of size M , then split S into runs of size M . Cost: $2B(R) + 2B(S)$
 - Step 2: **merge $M-1$ runs from R and S** ; output a tuple on a case by cases basis
- Total cost: $3B(R) + 3B(S)$
- Assumption: $B(R) + B(S) \leq M^2$

Merging picture

S on R.a=S.a



notes (simple-sort)

1. completely sort R:

- $R(1000) \Rightarrow 10 \text{ runs} \Rightarrow 1 \text{ run}$
- cost: $4B(R)$

2. completely sort S:

- $S(50,000) \Rightarrow 500 \text{ runs} \Rightarrow 5 \text{ runs} \Rightarrow 1 \text{ run}$
- cost: $6B(S)$

3. merge R and S (both sorted)

- cost: $B(R) + B(S)$

Total cost: $5B(R) + 7B(S)$

Notes (sort-merge)

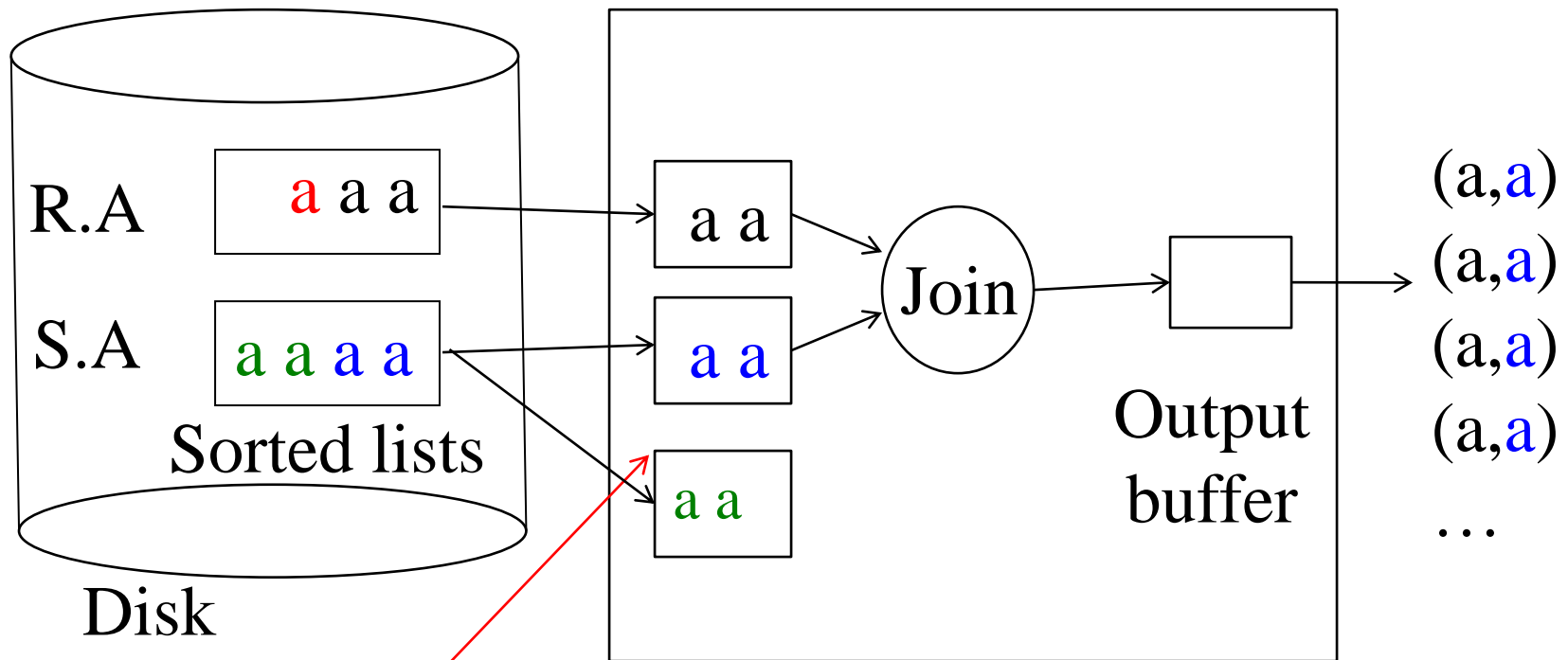
- R (1000 blocks) \Rightarrow 10 runs
 - cost: $2 B(R)$
- S (50,000) \Rightarrow 500 runs \Rightarrow 5 runs
 - cost: $4 B(S)$
- join by merging 10 runs with 5 runs
 - cost: $B(R) + B(S)$
- total: $3B(R) + 5B(S)$

Problem with join

- A large number of tuples with the same value on the join attribute(s)
- But buffer can not hold all joining tuples (with the same value on join attribute) for at least one relation

Problem with join

Many tuples may have the same value on the join attribute



Main memory
buffers

Remember the tuple may
have other attributes than A

Sort-Merge Join

- Assume buffer is enough to hold join tuples for at least one relation
 - Note that buffer also needs to hold a block for each run of the other relation
- Total cost: $3B(R)+3B(S)$
- Assumption: $B(R) + B(S) \leq M^2$

Example

- Suppose $M = 101$ blocks (i.e., pages), $B(R) = 1,000$ blocks, $B(S) = 50,000$ blocks ($R.a = S.a$)
 - Suppose we use 100 blocks in sorting
- Cost of $R \bowtie S$ using sort-merge join algorithm
 - Pass 1: sort $R \Rightarrow 10$ runs, 100 blocks/run
sort $S \Rightarrow 500$ runs, 100 blocks/run
extra step: merging 500 runs from $S \Rightarrow 5$ runs
 - Pass 2 (merge): $B(R) + B(S)$
 - total cost: $3B(R) + 3B(S) \Rightarrow 3B(R) + 5B(S)$

Simple Sort-based Join

- Start by **completely** sorting both R and S on the join attribute (assuming this can be done in 2 passes):
 - Cost: $4B(R)+4B(S)$ (because we need to write result to disk)
- Read both relations in sorted order, match tuples
 - Cost: $B(R)+B(S)$
- Can use as many buffers as possible to load join tuples from one relation (with the same join value), say R
 - Only one buffer is needed for the other relation, say S
- If we still can not fit all join tuples from R
 - Need to use nested loop algorithm, higher cost

Simple Sort-based Join

- Total cost: $5B(R)+5B(S)$
- Assumption: $B(R) \leq M^2$, $B(S) \leq M^2$, and at least one set of the tuples with a common value for the join attributes fit in M (or $M-2$ to be exact)
 - Note that we only need one page buffer for the other relation

Example

- Suppose $M = 101$ blocks (i.e., pages), $B(R) = 1,000$ blocks, $B(S) = 5,000$ blocks
 - Assume that we use 100 blocks in sorting
- Cost of $R \bowtie S$ using simple sort-based join algorithm
 - Sort R (completely): $4B(R) = 4000$
 - Sort S : $4B(S) = 20,000$
- What if $B(S) = 50,000$ blocks?
 - 500 runs \Rightarrow 5 runs \Rightarrow 1 run

Notes

Sorting R (completely):

$B(R) + B(R) // 10 \text{ runs}$

$B(R) + B(R) // 1 \text{ run}$

$= 4B(R)$

Sorting S:

$= 4B(S)$

Merging R and S:

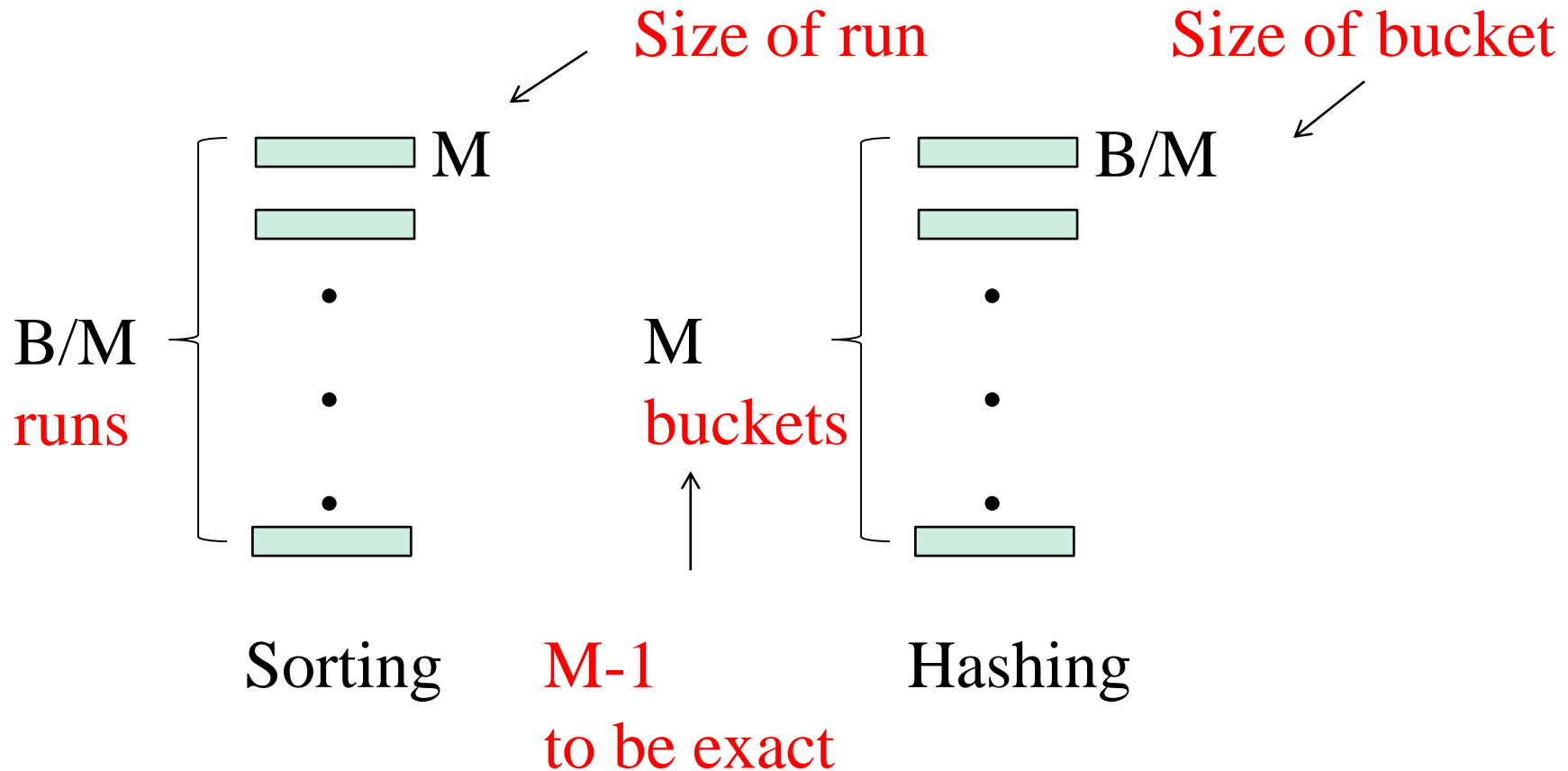
$B(R) + B(S)$

Two-Pass Algorithms Based on Hashing

Hashing-Based Algorithms

- Hash all the tuples of input relations using an appropriate hash key such that:
 - All the tuples that need to be considered together to perform an operation go to the same bucket
- Reduce the size of input relations by a factor of M
- Perform the operation by working on a bucket (or a pair of buckets for binary operations) at a time
 - Apply a one-pass algorithm for the operation

Sorting vs. Hashing



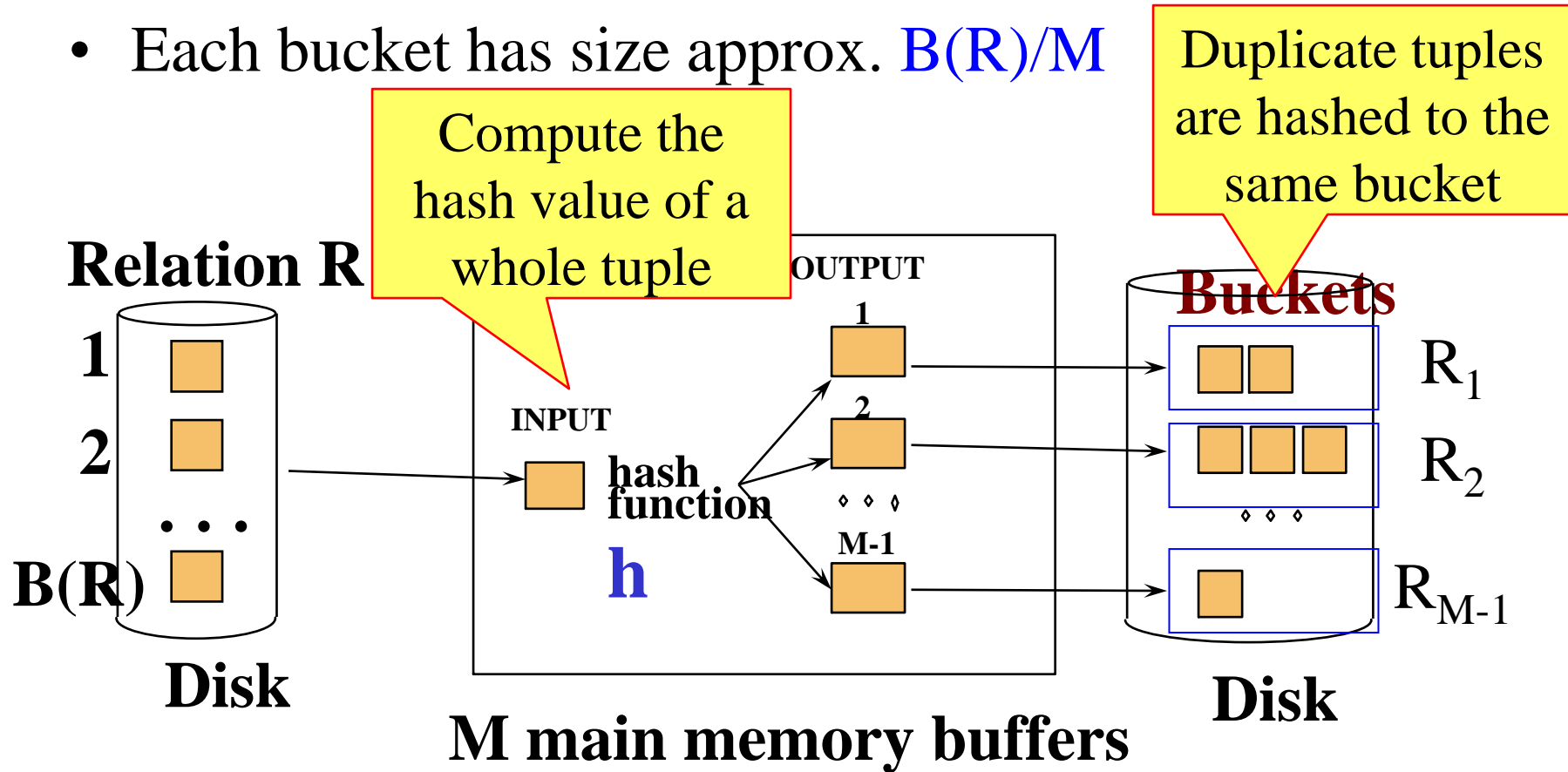
"Partitioning" picture

Hashing-Based Algorithm for δ

- Recall: $\delta(R)$ = duplicate elimination
- Step 1. Partition R into $(M-1)$ buckets
- Step 2. Apply δ to each bucket (must read it into main memory)
- Cost: $3B(R)$
- Assumption: $B(R) \leq M^2$
 - To be more exact: $B(R)/(M-1) \leq M-2$

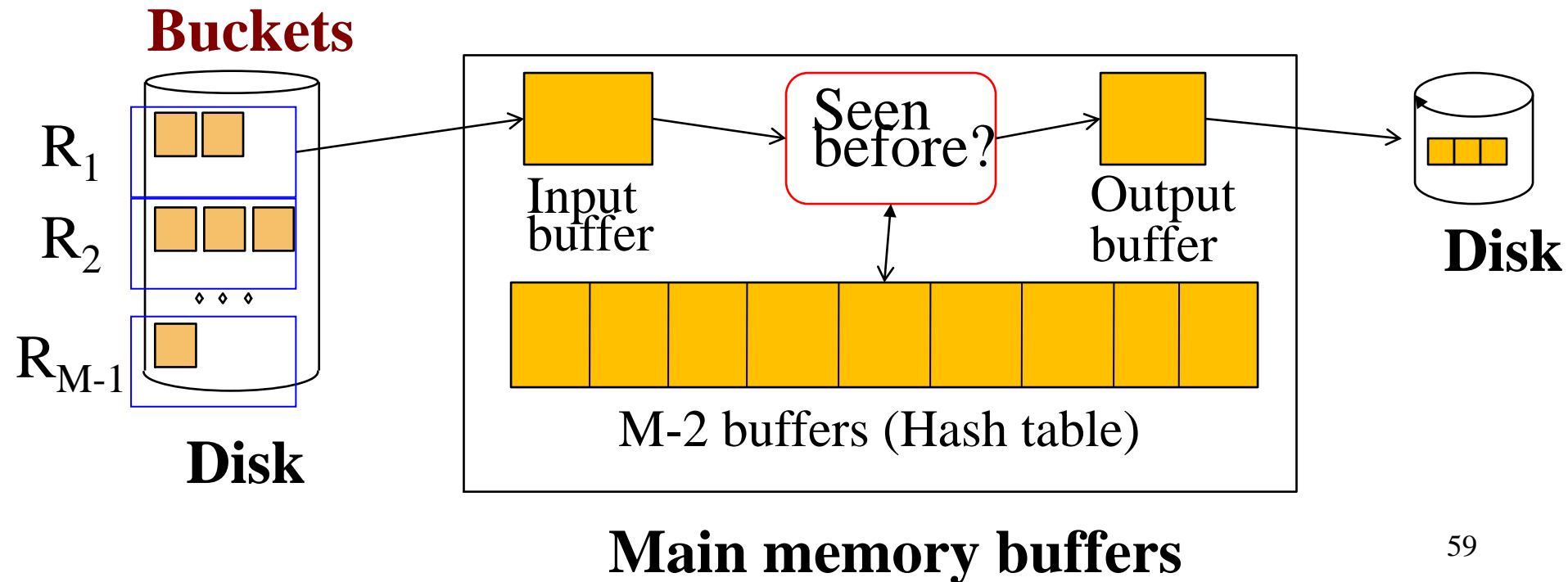
Two-Pass Duplicate Elimination Based on Hashing

- Idea: partition a relation R into buckets, on disk
- Each bucket has size approx. $B(R)/M$



Two Pass Duplicate Elimination Based on Hashing

- Does each bucket fit in main memory ?
 - Yes if $B(R)/(M-1) \leq M-2$ (i.e., approx. $B(R) \leq M^2$)
- Apply the one-pass δ algorithm for each R_i



Partitioned Hash Join

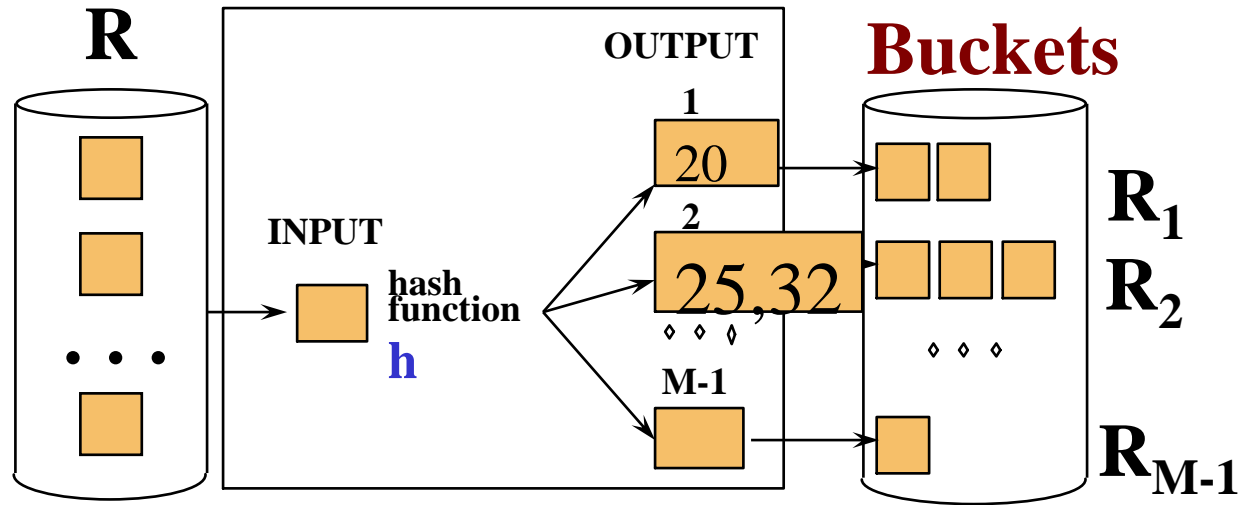
$R \bowtie S$

- Step 1:
 - Hash S into $M - 1$ buckets
 - send all buckets to disk
- Step 2
 - Hash R into $M - 1$ buckets
 - Send all buckets to disk
- Step 3
 - Join every pair of **corresponding** buckets

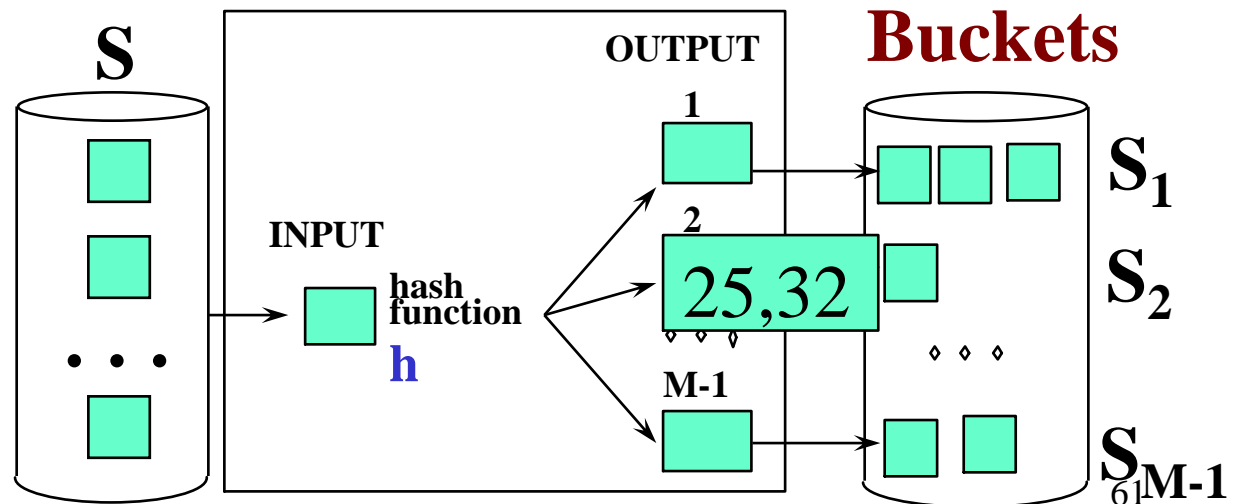
Partitioned Hash-Join

- Partition tuples in R and S using **join attributes** as key for hash
- Tuples in partition R_i only match tuples in partition S_i .
- $R.\text{age} = S.\text{age}$
- $h(r.\text{age}) = h(25) = 2$
- $h(s.\text{age}) = h(25) = ?$

Relation



Relation

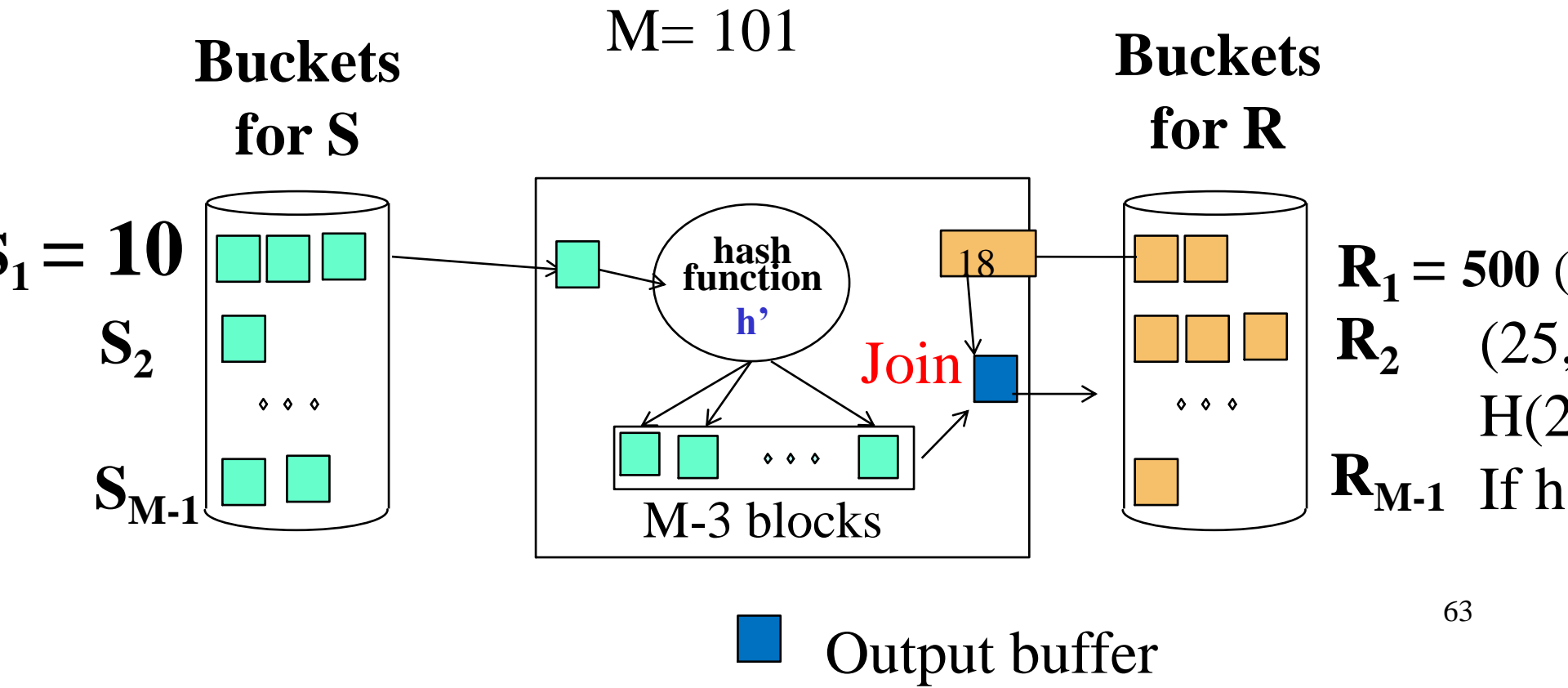


notes

- $h(25) = 1$
- $h(32) = 0$
- $h(a) = a \% 2$
- $h'(a)$
 - $(2+5)\%2 = 1$
 - $(3+2)\%2 = 1$

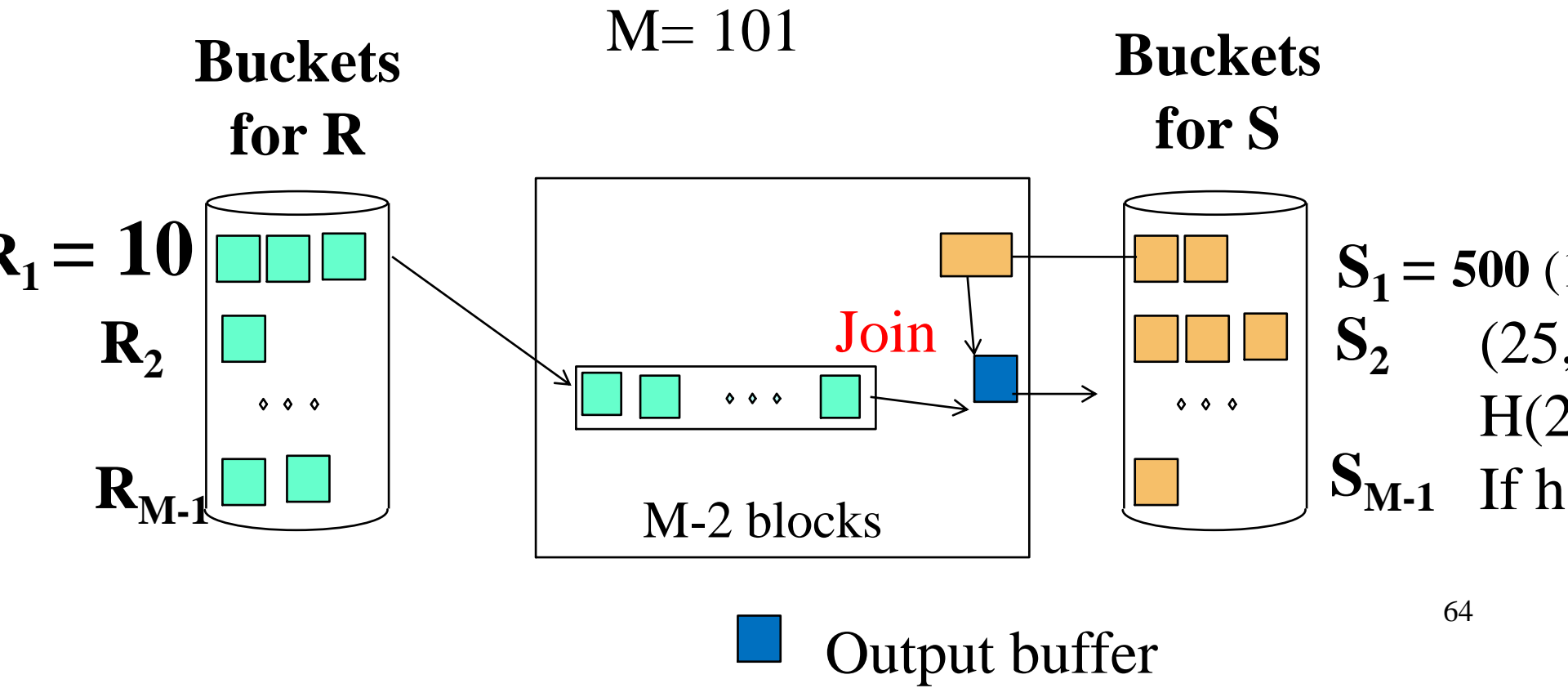
Partitioned Hash-Join: Second Pass

- Read in a partition of S, say S_i , hash it using **another** hash function h'
- Load the matching partition R_i , one block at a time, output joining tuples.



Partitioned Hash-Join: Second Pass

- Read in a partition of S , say S_i , hash it using **another** hash function h'
- Load the matching partition R_i , one block at a time, output joining tuples.



Partitioned Hash Join

- Cost: $3B(R) + 3B(S)$
- Assumption: $\min(B(R), B(S)) \leq M^2$
 - Or to be more exact: $\min(B(R), B(S))/(M-1) \leq M-3$
 - Or $\min(B(R), B(S))/(M-1) \leq M-2$ (if we do not use hash table to speed up the lookup)

Example

- Suppose $M = 101$ blocks (i.e., pages), $B(R) = 1,000$ blocks, $B(S) = 50,000$ blocks ($R.a = S.a$)
- Cost of $R \bowtie S$ using partitioned hash join algorithm
 - Pass 1: hash R into 100 buckets, 10 blocks/bucket (R_1)
hash S into 100 buckets, 500 blocks/bucket (S_1)
cost: $2B(R) + 2B(S)$
 - Pass 2: join R_i with S_i
cost: $B(R) + B(S)$
- What if $B(S) = 50,000$ blocks?

Example

- Suppose $M = 101$ blocks (i.e., pages), $B(R) = 10,000$ blocks, $B(S) = 50,000$ blocks ($R.a = S.a$)
- Cost of $R \bowtie S$ using partitioned hash join algorithm
 - Pass 1: hash R into 100 buckets, 100 blocks/bucket ($R1$)
hash S into 100 buckets, 500 blocks/bucket ($S1$)
cost: $2B(R) + 2B(S)$
 - extra: hash ($R1$) \Rightarrow 100 buckets, 1 block/bucket ($R11$)
hash($S1$) \Rightarrow 100 buckets, 5 blocks/bucket ($S11$)
join $R11$ with $S11$, $R12$ with $S12$, ... $R1,100$ with $S1,100$
 - Pass 2: join R_i with S_i
cost: $B(R) + B(S)$

notes

- size of $R_i = B(R)/(M-1)$
- size of $S_i = B(S)/(M-1)$
- $\min[B(R)/(M-1), B(S)/(M-1)] \leq M - 2$
- $\min[B(R), B(S)] \leq (M-1)(M-2) \sim M^2$
 - $\min(1000, 50000) \leq 10,000$
- recall sorting formula
 - $B(R) + B(S) \leq M^2$
 - $1000 + 50,000 \leq 10,000$

Example

- Suppose $M = 101$ blocks (i.e., pages), $B(R) = 20,000$ blocks, $B(S) = 50,000$ blocks
- Cost of $R \bowtie S$ using partitioned hash join algorithm
 - Pass 1: hash R into 100 buckets, 200 blocks/bucket (R_i)
hash S into 100 buckets, 500 blocks/bucket (S_i)
cost: $2B(R) + 2B(S)$
 - pass 2: join R_1 (200 blocks) with S_1 (500 blocks)
join R_2 with S_2 , ...
 - Pass 3:
cost: ...

Sort-based vs. Hash-based Algorithms

- Hash-based algorithms for binary operations have a size requirement only on the smaller of two input relations
- Sort-based algorithms sometimes allow us to produce a result in sorted order and take advantage of that sort later
- Hash-based algorithm depends on the buckets being of equal size, which may not be true if data are skewed

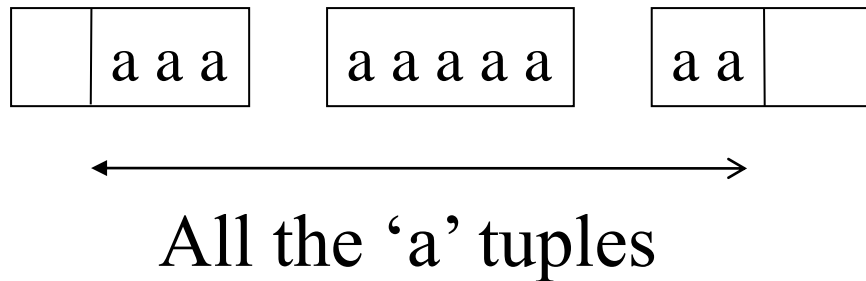
Index-Based Algorithms

Index-based Algorithms

- The existence of an index on one or more attributes of a relation makes available some algorithms that would not be feasible without the index
- Useful for selection operations
- Also, algorithms for join and other binary operations use indexes to good advantage

Clustered indexes

- In a clustered index, all tuples with the same value of the search key appear on roughly as the number of blocks as can hold them
 - That is, they are clustered together

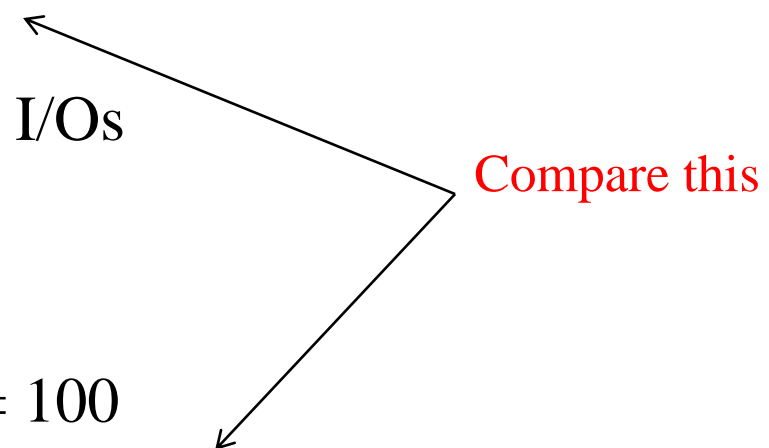


Index Based Selection

- Selection on equality: $\sigma_{a=v}(R)$
- Clustered index on attribute a : $\text{cost} = B(R)/V(R,a)$
- Unclustered index on a : $\text{cost} = T(R)/V(R,a)$

We here ignore the cost of reading index blocks

Index Based Selection

- Example: $B(R) = 2000$, $T(R) = 100,000$, $V(R, a) = 20$, compute the cost of $\sigma_{a=v}(R)$
 - Cost of using table scan:
 - If R is clustered: $B(R) = 2000$ I/Os
 - If R is unclustered: $T(R) = 100,000$ I/Os
 - Cost of index-based selection:
 - If index is clustered: $B(R)/V(R, a) = 100$
 - If index is unclustered: $T(R)/V(R, a) = 5000$
- 
- A diagram consisting of two arrows originating from a single point on the right and pointing towards the left. The top arrow points to the value '2000' in the first bullet point's sub-item. The bottom arrow points to the value '5000' in the third bullet point's sub-item. The text 'Compare this' is written in red to the right of the arrow junction.

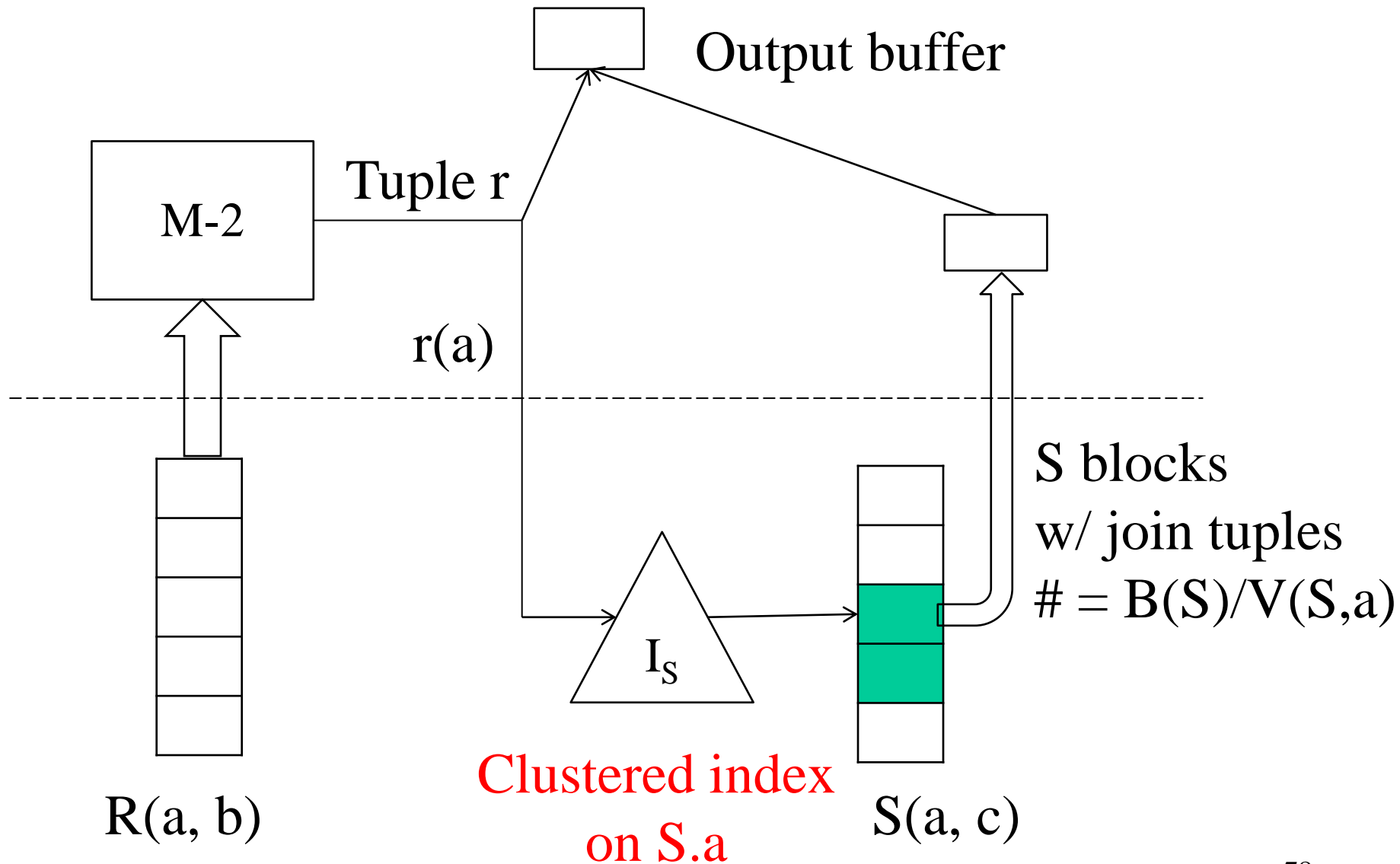
Index-Based Join

- $R \bowtie S$
- Assume S has an index on the join attribute
- Iterate over R , for each tuple, fetch corresponding tuple(s) from S
- Assume R is clustered. Cost:
 - If index is clustered: $B(R) + T(R)B(S)/V(S,a)$
 - If index is unclustered: $B(R) + T(R)T(S)/V(S,a)$
- Compare this to NLJ (both R & S clustered)
 - $B(R) + B(R)/(M-2) * B(S)$

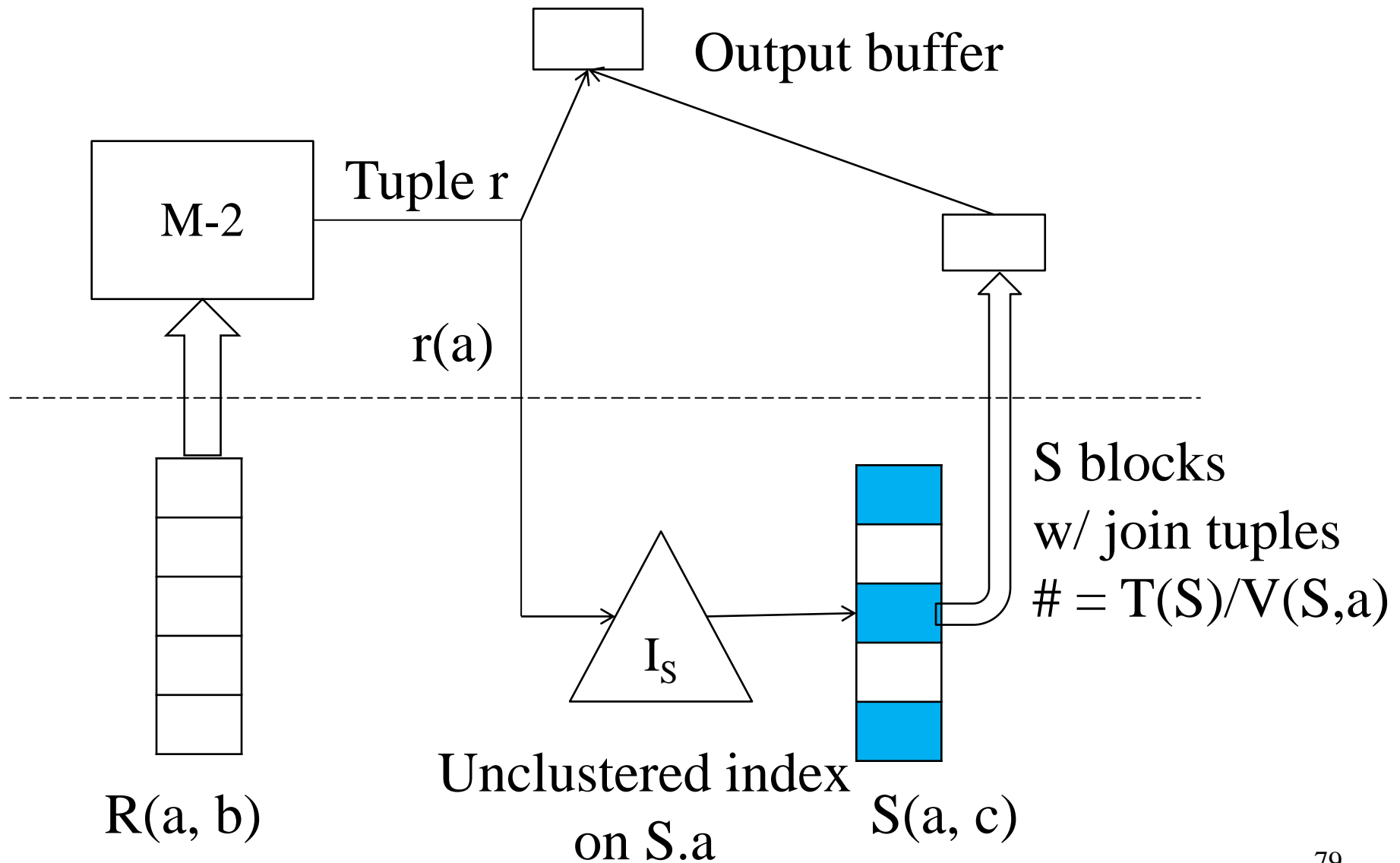
Indexed-Based Join vs. NLJ

- Index-based (R clustered, clustered index S.a)
 - $B(R) + T(R)B(S)/V(S,a)$
- NLJ (R & S clustered)
 - $B(R) + B(R)/(M-2) * B(S)$
- Index-Based wins if:
 - $T(R)/V(S,a) < B(R)/(M-2)$, or
 - $V(S,a) > (M-2) * T(R)/B(R)$

Index-Based Join: Clustered Index



Index-Based Join: Unclustered Index



Example

- Suppose $M = 102$ blocks (i.e., pages)
- $R(a, b) \bowtie S(a, c)$
- S has an index on attribute "a" and $V(S,a) = 100$
- $B(R) = 1,000$ blocks, $B(S) = 5,000$ blocks
- $T(R) = 10,000$ tuples, $T(S) = 50,000$ tuples
- Cost of $R \bowtie S$ using index-based join algorithm
 - Index on $S.a$ is clustered
 - Index on $S.a$ is unclustered

Index-Based Join: Two Indexes

- Assume both R and S have a clustered index (e.g., B+-tree) on the join attribute
- Then can perform a sort-merge join where sorting is already done (for free)
- Cost: $B(R) + B(S)$

