

# Practica 7

KD - Tree

Integrantes: Mita Yagua Lesly Yaneth  
Pinto Medina Brian  
Ccari Quispe José  
Gonza Condori, Gabriel  
Flores Herrera, Jefferson  
Profesor: Msc. Vicente Machaca Arceda

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## 1. Range Query Circle

Se incluyo en el archivo **kdtree.js** la función *range\_query\_circle*. La captura de pantalla del **Código 4** se encuentra en la sección Capturas de pantalla como **Figura 4**.

A continuación se muestra la función implementada en el siguiente código y los resultados de este como visualización web.

Código 1: range\_query\_circle

```
1 function range_query_circle(data , center , radio , queue , depth = 0) {  
2     let neight = [];  
3     let root = buildKDTree(data);  
4  
5     for(let i = 0; i < data.length; ++i) {  
6         let arr = [];  
7         convertKDTreeToArray(root, arr);  
8         let closePoint = closest_point(root, center, depth);  
9         if (distanceSquared( center, closePoint.point.vectorialSpace) < radio){  
10             neight.push(closePoint.point.vectorialSpace);  
11         }  
12         deleteNode(arr, closePoint);  
13         root = buildKDTree(arr);  
14     }  
15     return neight;  
16 }
```

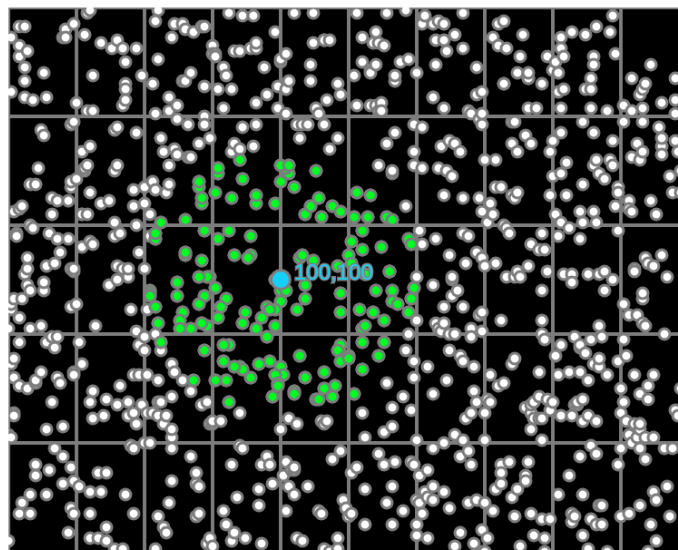


Figura 1: Visualización del navegador Web Circulo

## 2. Range Query Rec

Se incluyo en el archivo **kdtree.js** la función *range\_query\_rec*. La captura de pantalla del **Código 4** se encuentra en la sección Capturas de pantalla como **Figura 4**.

A continuación se muestra la función implementada en el siguiente código y los resultados de este como visualización web.

Código 2: range\_query\_rec

```
1 function range_query_circle(data , center , radio , queue , depth = 0) {  
2     let neight = [];  
3     let root = buildKDTree(data);  
4  
5     for(let i = 0; i < data.length; ++i) {  
6         let arr = [];  
7         convertKDTreeToArray(root, arr);  
8         let closePoint = closest_point(root, center, depth);  
9         if (distanceSquared( center, closePoint.point.vectorialSpace) < radio){  
10             neight.push(closePoint.point.vectorialSpace);  
11         }  
12         deleteNode(arr, closePoint);  
13         root = buildKDTree(arr);  
14     }  
15     return neight;  
16 }
```

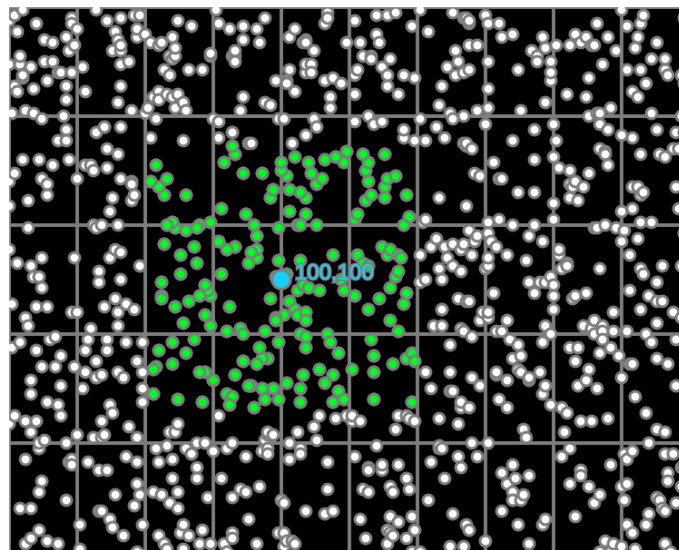


Figura 2: Visualización del navegador Web Rectangulo

### 3. Código fuente

Código 3: main.html

```
1 <html>
2   <head>
3     <title>KD Tree</title>
4     <script src = "p5.min.js"></script>
5     <script src = "kdtree.js"></script>
6     <script src = "sketch.js"></script>
7   </head>
8   <body>
9
10  </body>
11 </html>
```

Código 4: kdtree.js

```
1 k = 2;
2
3 class Node {
4   constructor(point, axis) {
5     this.point = point;
6     this.left = null;
7     this.right = null;
8     this.axis = axis;
9   }
10 };
11
12 class N_Point {
13   constructor(points) {
14     this.vectorialSpace = points;
15   }
16 }
17
18 function distanceSquared ( point1 , point2 ){
19   var distance = 0;
20   for (var i = 0; i < k; i ++){
21     distance += Math.pow(( point1 [i] - point2 [i]) , 2) ;
22   }
23   return Math.sqrt( distance );
24 }
25
26 function closest_point_brute_force ( points , point ) {
27   var closestPoint ;
28   var minDistance;
29   var distance;
30   for(var i= 0; i< points.length ;i++){
31     if(i==0){
32       minDistance = distanceSquared(points[0].vectorialSpace,point);
33       closestPoint = points [0]. vectorialSpace;
```

```

34     }
35     distance = distanceSquared(points[i]. vectorialSpace, point);
36
37     if(minDistance >= distance ){
38         minDistance = distance;
39         closestPoint = points[i]. vectorialSpace;
40     }
41 }
42 return closestPoint ;
43 }
44
45 function naive_closest_point(node , point , depth = 0, best = null ) {
46     if(node != null){
47         if(depth == 0){
48             best = node.point.vectorialSpace;
49         }
50
51         var axisDistance = point[node.axis] - node.point.vectorialSpace[node.axis];
52         let distanceBest = distanceSquared(best, point);
53         let distanceNode = distanceSquared(node.point.vectorialSpace, point);
54
55
56         if ( Math.abs(axisDistance) <= distanceBest ){
57             if(distanceBest > distanceNode){
58                 best = node.point.vectorialSpace;
59             }
60             if(axisDistance > 0){
61                 return naive_closest_point (node.right , point , depth+1, best );
62             }
63             else{
64                 return naive_closest_point (node.left , point , depth+1, best);
65             }
66         }else{
67             return best;
68         }
69     }else{
70         return best;
71     }
72 }
73
74 //////////////////////////////////////////////////Practica-07 //////////////////////////////////////
75
76
77 function range_query_circle(data , center , radio , queue , depth = 0) {
78     let neight = [];
79     let root = buildKDTree(data);
80
81     for(let i = 0; i < data.length; ++i) {
82         let arr = [];
83         convertKDTreeToArray(root, arr);
84         let closePoint = closest_point(root, center, depth);
85         if(distanceSquared( center, closePoint .point. vectorialSpace) < radio){

```

```

86     neight.push(closePoint.point.vectorialSpace);
87   }
88   deleteNode(arr, closePoint);
89   root = buildKDTree(arr);
90 }
91 return neight;
92 }
93
94 function range_query_rec(data , center , diameter , queue , depth = 0) {
95   let neight = [];
96   let root = buildKDTree(data);
97
98   for(let i = 0; i < data.length; ++i) {
99     let arr = [];
100    convertKDTreeToArray(root, arr);
101    let closePoint = closest_point(root, center, depth);
102
103    let dimX = [closePoint.point.vectorialSpace [0],0];
104    let centerX =[center [0],0];
105
106    let dimY = [0,closePoint.point.vectorialSpace [1]];
107    let centerY =[0,center [1]];
108
109    if(distanceSquared(centerX,dimX) < diameter && distanceSquared(centerY,dimY) <
110    ⇨ diameter){
111      neight.push(closePoint.point.vectorialSpace);
112    }
113    deleteNode(arr, closePoint);
114    root = buildKDTree(arr);
115  }
116  return neight;
117 }
118
119
120 function closest_point(node, point, depth = 0) {
121   if(node == null) {
122     return null;
123   }
124
125   if(point[node.axis] < node.point.vectorialSpace [node.axis]) {
126     var nextBranch = node.left;
127     var otherBranch = node.right;
128   } else {
129     var nextBranch = node.right;
130     var otherBranch = node.left;
131   }
132
133   var temp = closest_point(nextBranch, point, depth + 1);
134   var best = closest(temp, node, point);
135
136   var distanceBest = distanceSquared(point, best.point.vectorialSpace);

```

```
137     var distanceAxis = Math.abs(point[node.axis] - node.point.vectorialSpace[node.axis]);
138
139     if(distanceAxis <= distanceBest) {
140         temp = closest_point(otherBranch, point, depth + 1);
141         best = closest(temp, best, point);
142     }
143
144     return best;
145 }
146
147 function closest(node, root, point) {
148     if(node == null)
149         return root;
150     if(root == null)
151         return node;
152
153     let distanceNode = distanceSquared(node.point.vectorialSpace, point);
154     let distanceRoot = distanceSquared(root.point.vectorialSpace, point);
155
156     if(distanceNode < distanceRoot)
157         return node;
158     else
159         return root;
160 }
161
162 function convertKDTreeToArray(node,array){
163     array.push(node.point);
164     if(node.left != null)
165         convertKDTreeToArray(node.left,array);
166     if(node.right != null)
167         convertKDTreeToArray(node.right,array);
168 }
169
170 function KNN(data, n, point) {
171     let neight = [];
172     let root = buildKDTree(data);
173
174     for(let i = 0; i < n; ++i) {
175         let arr = [];
176         convertKDTreeToArray(root, arr);
177         let closePoint = closest_point(root, point);
178         neight.push(closePoint.point.vectorialSpace);
179         deleteNode(arr, closePoint);
180         root = buildKDTree(arr);
181     }
182     return neight;
183 }
184
185 function deleteNode(arr, node) {
186     for(let i = 0; i < arr.length; ++i) {
187         if(arr[i].vectorialSpace == node.point.vectorialSpace)
188             arr.splice(i, 1);
```



```

189     }
190 }
191
192 function getHeight(node) {
193     if (node === null)
194         return 0;
195
196     return Math.max(getHeight(node.left), getHeight(node.right)) + 1;
197 }
198
199 function generateDot(node) {
200     var s = "digraph G{\n";
201     var cola = [];
202     cola.push(node);
203     while (cola.length > 0) {
204         let nodo = (cola.splice(0, 1)) [0];
205         if (nodo.left === null) {
206             continue;
207         }
208         let space = nodo.point.vectorialSpace.length;
209         for (let i = 0; i < space - 1; ++i) {
210             s += "\n";
211             s += nodo.point.vectorialSpace[i];
212             s += ",";
213         }
214         s += nodo.point.vectorialSpace[space - 1];
215         s += "\n -> ";
216         for (let i = 0; i < space - 1; ++i) {
217             s += "\n";
218             s += nodo.left.point.vectorialSpace[i];
219             s += ",";
220         }
221         s += nodo.left.point.vectorialSpace[space - 1];
222         s += "\n,\n";
223         cola.push(nodo.left);
224
225         //RIGHT NODE
226         if (nodo.right === null) {
227             continue;
228         }
229         for (let i = 0; i < space - 1; ++i) {
230             s += "\n";
231             s += nodo.point.vectorialSpace[i];
232             s += ",";
233         }
234         s += nodo.point.vectorialSpace[space - 1];
235         s += "\n -> ";
236         for (let i = 0; i < space - 1; ++i) {
237             s += "\n";
238             s += nodo.right.point.vectorialSpace[i];
239             s += ",";
240         }

```

```
241     s += nodo.right.point.vectorialSpace[space - 1];
242     s += "\\n";
243     cola.push(nodo.right);
244 }
245 s += "}"
246 return s;
247 }
248
249 function buildKDTree(points, depth = 0) {
250     if(points.length === 0) {
251         return;
252     } else {
253         mergeSort(points, 0, points.length - 1, depth % points[0].vectorialSpace.length);
254         let median = Math.floor(points.length / 2);
255         let root = new Node(points[median], depth % points[0].vectorialSpace.length);
256         points.splice(median, 1);
257         let leftBranch = points.slice(0, median);
258         let rightBranch = points.slice(median, points.length);
259
260         root.left = buildKDTree(leftBranch, depth + 1);
261         root.right = buildKDTree(rightBranch, depth + 1);
262
263         return root;
264     }
265 }
266 }
267
268 function mergeSort(points, left, right, dim) {
269     let mid = Math.floor((left + right) / 2);
270
271     if(left < right) {
272         mergeSort(points, left, mid, dim);
273         mergeSort(points, mid + 1, right, dim);
274         merge(points, left, mid, right, dim);
275     }
276 }
277
278 function merge(points, left, mid, right, dim) {
279     let temp = [];
280     let i = left;
281     let j = mid + 1;
282
283     while(i <= mid && j <= right) {
284         if(points[i].vectorialSpace[dim] <= points[j].vectorialSpace[dim])
285             temp.push(points[i++]);
286         else
287             temp.push(points[j++]);
288     }
289
290     while(i <= mid)
291         temp.push(points[i++]);
292     while(j <= right)
```

```
293     temp.push(points[j++]);
294
295     for(let i = left, j = 0; i <= right; ++i, ++j)
296         points[i] = temp[j];
297 }
```

Código 5: sketch.js

```
1 function setup(){
2     var width = 250;
3     var height = 200;
4
5     var canvas = createCanvas(width, height);
6     canvas.parent('sketch_holder');
7     background(0);
8     for( var x = 0; x < width; x += width / 10){
9         for( var y = 0; y < height; y += height / 5){
10             stroke(125, 125, 125);
11             strokeWeight(1);
12             line(x, 0, x, height);
13             line(0, y, width, y);
14         }
15     }
16
17     var data = [];
18     var point = [100,100];
19
20     //random data
21
22     for(let i = 0; i < 1000; i++){
23         var x = Math.floor(Math.random() * width);
24         var y = Math.floor(Math.random() * height);
25         let newPoint = new N_Point([x,y]);
26         data.push(newPoint);
27     }
28
29     //build KD-tree with data
30
31     var dataChange = data.slice(); //variable temporal porque la siguiente linea modifica data !!!!!
32     var root = buildKDTree(dataChange);
33
34     console.log(root);
35
36     // closest point
37     var closestPoint1 = closest_point_brute_force(data, point);
38     var closestPoint2 = naive_closest_point(root, point);
39     var closestPoint3 = closest_point(root, point);
40
41     console.log("CLOSEST POINT BRUTE FORCE : "+ closestPoint1);
42     console.log("NAIVE CLOSEST POINT NAIVE : "+ closestPoint2);
43     console.log("CLOSEST POINT: " + closestPoint3);
44 }
```

```
45 let knnPoints = range_query_rec(data,point, 20, null);
46 console.log(knnPoints);
47
48 //plot points
49 for(let i=0;i<data.length;i++){
50     x = data[i]. vectorialSpace [0];
51     y = data[i]. vectorialSpace [1];
52     fill (255, 255, 255);
53     circle (x, height - y, 4);
54     textSize(8);
55 }
56 x = closestPoint2 [0];
57 y = closestPoint2 [1];
58
59
60 for(let i = 0; i < knnPoints.length; ++i) {
61     x = knnPoints[i][0];
62     y = knnPoints[i][1];
63     fill (57, 255, 20);
64     circle (x, height - y, 4);
65     textSize(8);
66 }
67
68 var x = point [0];
69 var y = point [1];
70
71 fill (81, 209, 246);
72 circle (x, height - y, 7);
73 textSize(8);
74 text(x + ',' + y, x + 5, height - y);
75
76 // plot graph
77 var graph = generateDot(root);
78
79 var options = {
80     format: 'svg'
81 }
82
83 var image = Viz(graph, options);
84 var graph_holder = document.getElementById('graph_holder');
85
86 graph_holder.innerHTML = image; // SVG
87
88 }
```

## 4. Capturas de pantalla

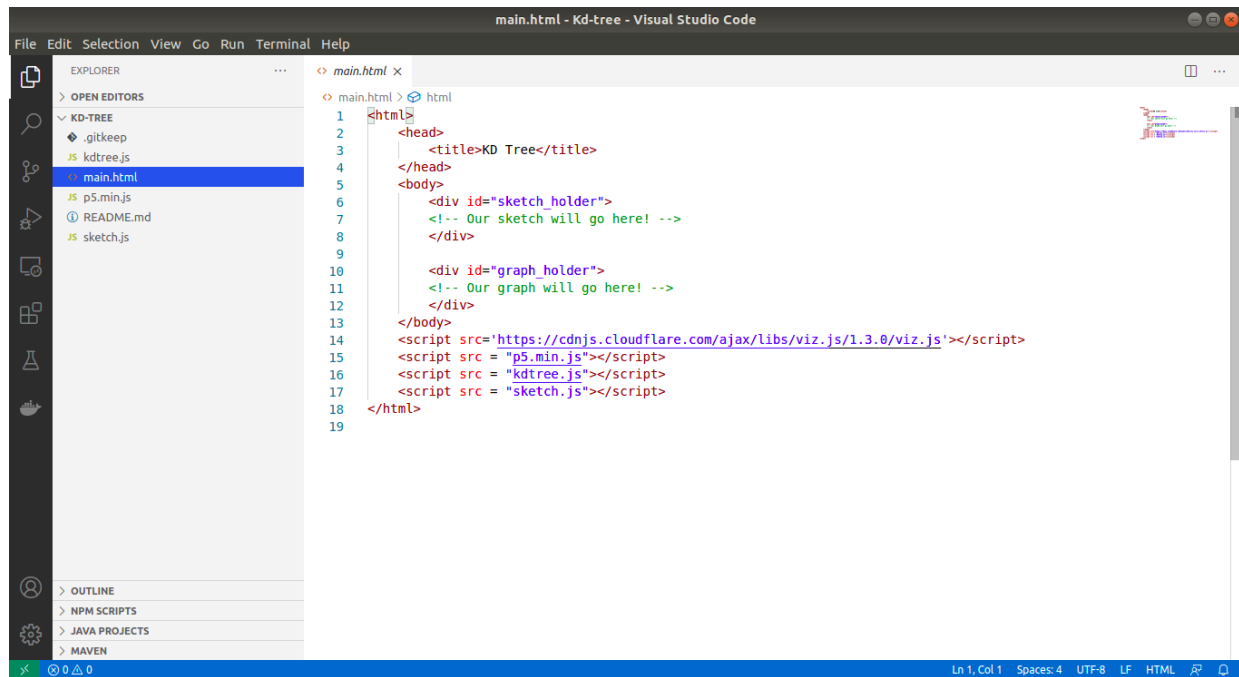


Figura 3: Captura de Pantalla de main.html

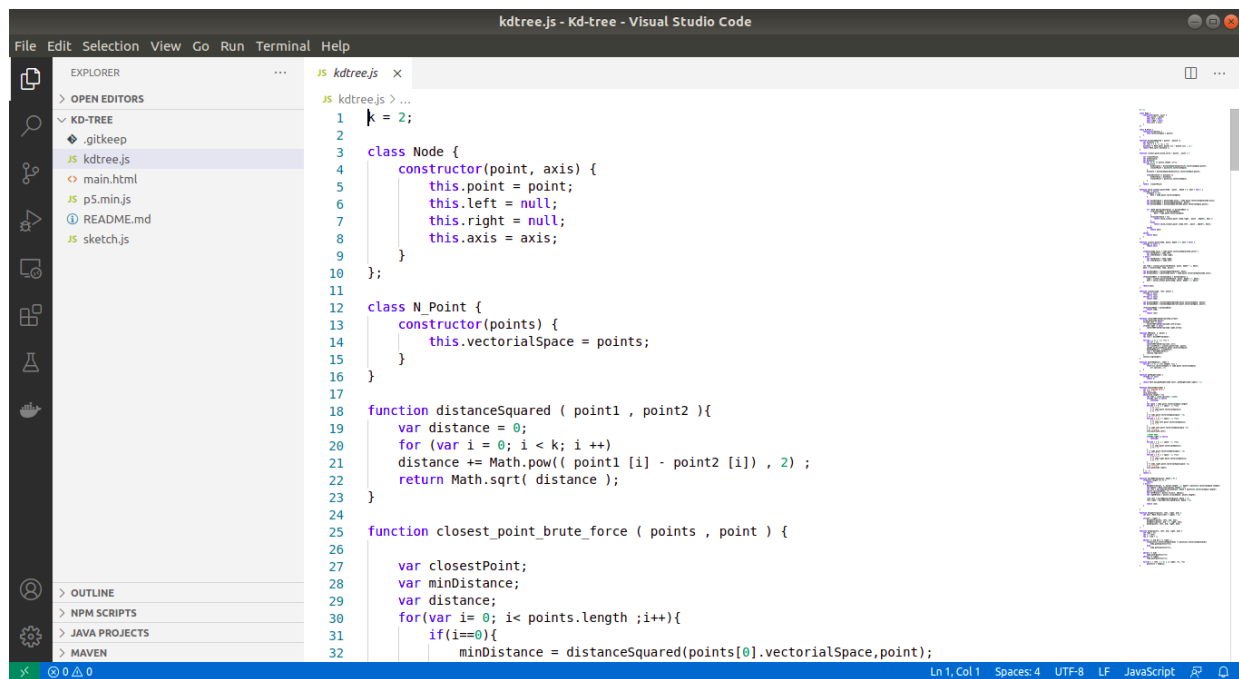


Figura 4: Captura de Pantalla de kdtree.js

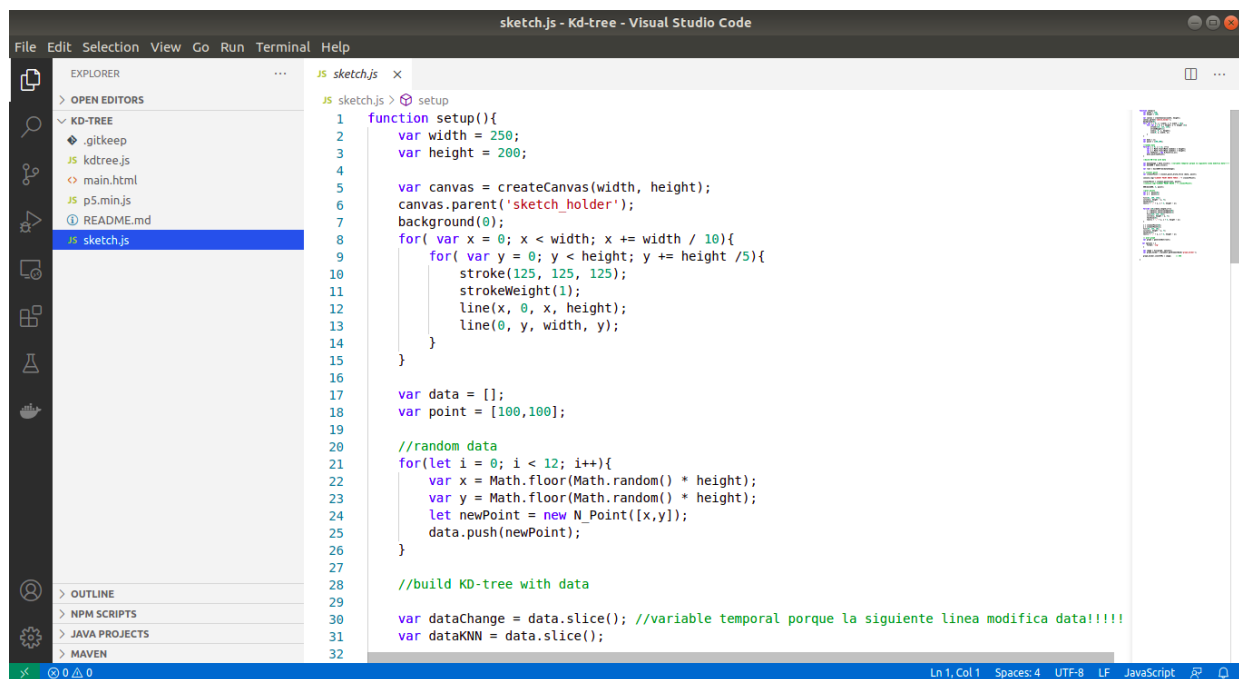


Figura 5: Captura de Pantalla de sketch.js

## 5. Repositorios

Toda la implementación de la estructura KD-Tree, el código, documento, imágenes y un README, se encuentran en los siguientes repositorios

- GitHub: <https://github.com/Leslym03/EDA-Grupo1/tree/master/KDTree>
- GitLab: <https://gitlab.com/pimed/kdtree/-/tree/master>