Tarea 2-U2 1) Encuentre el costo asintótico en terminos de O (ó grande) de la siguiente recurrencia considerando que T(n)=1 si n==0. Puede utilizar cualquier método conocido para encontrarlo. (4p) $T(n)=2T(\frac{n}{2})+\frac{n}{\log^2(n)}$ si n>0T(n)=A $T\left(\frac{\Omega}{2}\right) = 2.T\left(\frac{\Omega}{4}\right) + \frac{\Omega}{2} \cdot \frac{1}{\log^2\left(\frac{\Omega}{2}\right)}$ 10g (6) = 10ge (6) $T\left(\frac{n}{2}\right) = 2 \cdot T\left(\frac{n}{4}\right) + \frac{n}{2} \cdot \frac{1}{\log(n) - \log(2)}^2 = 2 \cdot T\left(\frac{n}{2^2}\right) + \frac{n}{2^2} \cdot \frac{1}{\log(n) - 1 \log(2)}^2$ 10gc (0) T(A)=2.T(A)+ 1 1002(A) $T\left(\frac{n}{4}\right) = 2.T\left(\frac{n}{2^2}\right) + \frac{n}{2^2} \cdot \frac{1}{[\log(n) - \log(2^2)]^2} = 2T\left(\frac{n}{2^3}\right) + \frac{n}{2^2} \cdot \frac{1}{[\log(n) - 2.\log(2)]^2}$ T(8)=27(8)+0,000 $T\left(\frac{0}{8}\right) = 2T \cdot \left(\frac{0}{2^n}\right) + \frac{1}{2^3} \cdot \frac{1}{\lceil \log(n) - \log(2^n) \rceil} = 2T\left(\frac{0}{2^n}\right) + \frac{0}{2^3} \cdot \left\lceil \log(n) - 3 \cdot \log(2) \right\rceil^2$ T(n)=2T(1/2)+f(n) T(n)= 2. [2T(1) + 1 - [log (2)]2]+ 1. [log (2)]2 $T(n) = 2^{2}T\left(\frac{2}{2^{2}}\right) + \Omega \cdot \left[\log\left(\frac{2}{2^{2}}\right)^{-2} + \Omega \cdot$ T(1)=2T(2)+f(1) T(2)=2T(2)+f(2) $\frac{n}{2^{K}} = 1$ $\int_{[0]_{2}(n)=K-1}^{n=2^{K}} |g_{2}(n)| = K-1$ T(n)=2/90/17 (-2001)+n.(2) [109(2)]-2 $\sum_{i=0}^{\log(n)-1} \frac{\log_2(n)-1}{[\log(n)-i\log(2)]^2} = \sum_{i=0}^{\log_2(n)-1} \frac{1}{[L-C,i]^2} \sim \frac{1}{C} \cdot \int_{L-CK}^{L} \frac{1}{x^2} dx$ Aproximerian Integral 1092(0)-1 1 (a-b.i)2 2 1. 50 1 dx

J X a dx = X a+1 ; n = -1 Municiples (22) sem 0,

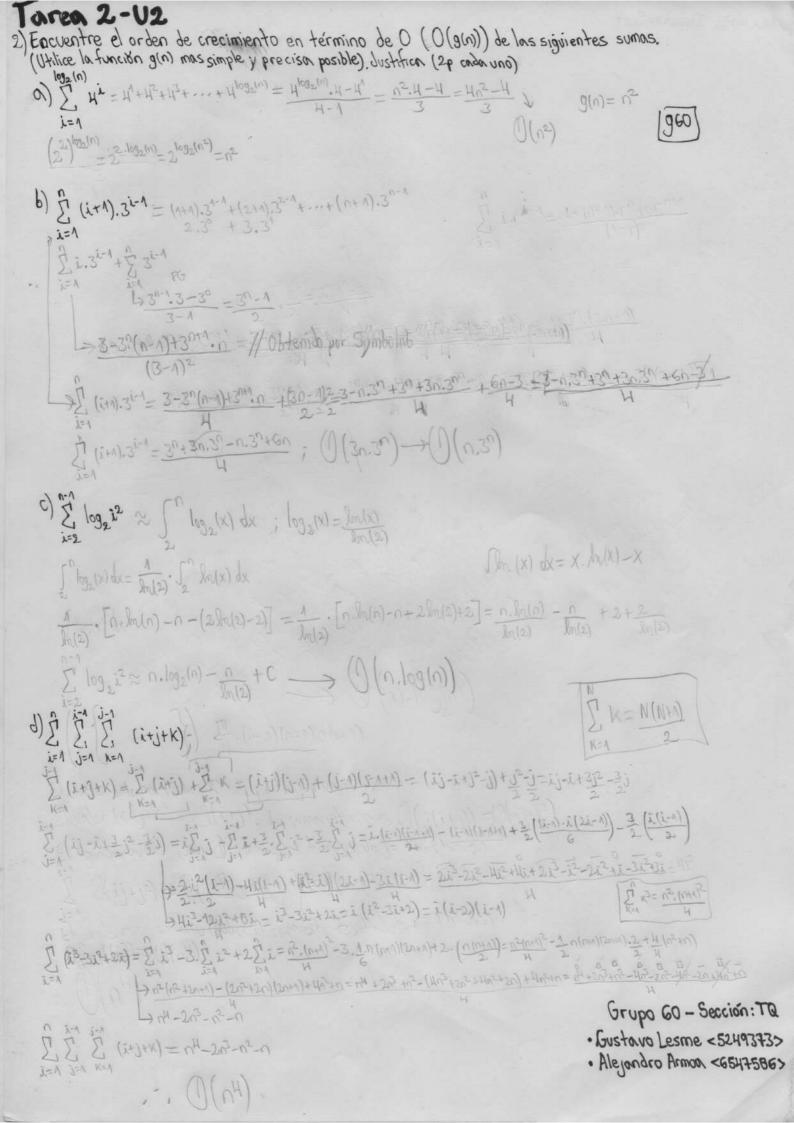
but patric ez numero E>O ; E ez nu unuero unal bedreuso $\int_{-\infty}^{\infty} \frac{1}{x^2} dx = \left[\frac{x^{-2+1}}{2+1} \right]_{\varepsilon}^{\log(n)} = \frac{x^{-1}}{-1} \left| \frac{\log(n)}{\varepsilon} \right| = -\frac{1}{x} \left| \frac{\log(n)}{\varepsilon} \right| - \frac{1}{\log(n)} - \left(\frac{1}{1+\varepsilon} \right) = \frac{1}{\varepsilon} - \frac{1}{\log(n)}$

-> Prevalece ((n); ... El Orden de crecimiento solicitado es ((n)

$$\mathbb{O}(\frac{1}{\log(n)}) < \mathbb{O}(n)$$

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3) Resuelva las siguientes recurrencias, por el método que usted conozca. Justificar las respuestas. Asumir que T(n) es constante para una n suficientemente pequena, por ejemplo T(n)=c, si n==1. (2p cada una) Taren 2-U2 σ) $L(u) = L\left(\frac{\partial u}{\partial u}\right) + u_{5}$ $T(n) = T(\frac{9^2}{10^2}n) + \frac{19}{10}n^2 + n^2$ 960 $T\left(\frac{90}{10}\right) = T\left(\frac{9^2}{10^2}\right) + \frac{9}{10} \cdot 0^2$ T(n)=T(22n)+2n2+n2 T(920)=T(930)+0202 $T(n) = \left[T\left(\frac{92}{10^3}n\right) + \frac{92}{10^2}n^2 + \frac{9}{10}n^2 + n^2\right]$ 10KU= N - N= 10K = (40)K $T(n) = T(\frac{q^3}{10^3}n) + \frac{q^2}{10^2}n^2 + \frac{q}{10}n^2 + n^2$ $\frac{q^{K} \cdot n}{40^{K}} = 1$ $\log_{10}(n) = \log_{10}\left(\left[\frac{40}{9}\right]^{K}\right)$ [(a) = (a) + (a) + (a) + ... + (a) x 1 T(n) = T(ax n) + [a) x 1 (a) x 1 10919(n)=K T(n)= T(10 10 10 1 1 (2) 1/2 (2) 1/2 (2) Suma P.G > an. r-al T(n) = C+[10-10.(9)10300)].12 P.G - (9)x-1 - (90) P.G - (10)x-1 - (10) P.G - (10)x-1 - (10) -10 - 10 (1)(n2) 10-10(10)x T(U)= C+10U2-10(10) -10 N_ - D TO T(n)=T(n-2)+2log_2(n) b) T(n)=T(n-2)+log2(n2) T(n)=[T(n+4)+2log(n-2)]+2log2(n) $T(n) = T(n-2) + 2 \cdot \log_2(n)$ T(n)=T(n-2K)+8 2/09(n-22) T(n-2)=T(n-H)+2.log(n-2) T(n-4) = T(n-6) + 2 log(n-4) n-2K=1 1 K=1/2 1/2 T(n) = 1 2log(n-2i) - 5(09(2)) ~ (12 log(x) dx > n log(2) T(n)=()(n, log(n))

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Tarea 2-U2 T(n)=3T(n-2)+Jn $(3)_{c)T(n)=3T(n-2)+\sqrt{n}}$ TIM=3[3T(N-H)+VN-2]+VN T(n-2)=3T(n-H)+1/n-2 T(n)=32T(n-4)+317-2+1 n-2K=1 T(n)=3[57(n-6)+10-4]+310-2+107 T(n-4)=3T(n-6)+Jn-4 n-1=2K T(n)=32T(n-6)+32/n-47 +34/12 1/n K=n-1 T(1)=C T(n)=3KT(n-2K)+(x) 32.1/n-22) 1-1-12-1-12-1-12 T(n)=32. T(n)#2231. (n-22) 3. V- T(n)=c. \(3^{n-1} + \(3^{0}. \(\sigma - 20' + 3'. \(\sigma - 2.1' + \cdots + 3^{2}. \(\sigma - 2.(\frac{n-2}{2})' \) ()(n-2k) . ((Um) es la cota superior.

 $d)T(n) = \sqrt{n} \cdot T(\sqrt{n}) + n$ $n = 2^{m}$ $m = \log_{2}(n)$ $R(m) = T(2^{m})$ R(m) = S(n)

T(1)=1

 $T(2m) = 2^{m/2} + (2^{m/2}) + 2^{m}$ $S(m) = 2^{m/2} \cdot S(m/2) + 2^{m}$ $S(m) = \frac{S(m/2)}{2^{m/2}} + 1$ $R(m) = \frac{S(m/2)}{2^{m/2}} + 1$ $R(m/2) = \frac{S$

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