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Name: LessTanker

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Problem 0-1.

- (a)  $A = \{1, 6, 12, 13, 9\}, B = \{3, 6, 12, 15\}$  As a result,  $A \cap B = \{6, 12\}$
- (b) Also easy to find that  $A \cup B = \{3, 6, 9, 12, 13, 15\}$ , so answer is 7.
- (c)  $|A - B| = \{1, 9, 13\}$  Answer is 3.

Problem 0-2.

- (a)  $E[X] = \frac{3}{2}$
- (b)  $E[Y] = 12.25$
- (c)  $E[X + Y] = 13.75$

Problem 0-3.

- (a) True
- (b) False
- (c) False

Problem 0-4. Assume that for  $k$ , the cite is true. Then for the  $k+1$  case:

$$\sum_{i=1}^{k+1} i^3 = \sum_{i=1}^k i^3 + (k+1)^3 = \left[\frac{k(k+1)}{2}\right]^2 + (k+1)^3 = \left[\frac{(k+1)(k+2)}{2}\right]^2$$

Therefore we prove that cite.

Problem 0-5. Assume that we have a graph with  $e_0$  edges and  $v_0$  vertices while  $e_0 = v_0 - 1$ . Then we add a vertex to that graph, we can find that we must add two more edges to make this new graph acyclic. As a result, the original graph must be acyclic.

Problem 0-6. Submit your implementation to [alg.mit.edu](http://alg.mit.edu).

```

1 def count_long_subarray(A):
2     '''
3     Input: A      | Python Tuple of positive integers
4     Output: count | number of longest increasing subarrays of A
5     '''
6     count = 1
7     #####
8     # YOUR CODE HERE #
9     #####
10    max_len = 1
11    cur_count = 1
12    for i in range(1, len(A) - 1):
13        if A[i] > A[i - 1] :
14            cur_count += 1
15        else:
16            cur_count = 1
17
18        if cur_count > max_len :
19            max_len = cur_count
20            count = 1
21        elif cur_count == max_len:
22            count += 1
23    return count

```