

# IMD0033 - Probabilidade

## Aula 07 - Introdução a Numpy

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# Agenda

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- Numpy - Overview
- Understanding NumPy ndarrays
- Selecting and slicing
- Arithmetic operations
- Adding rows and columns
- Sorting



nyc\_taxis.csv



# Atualizar o repositório

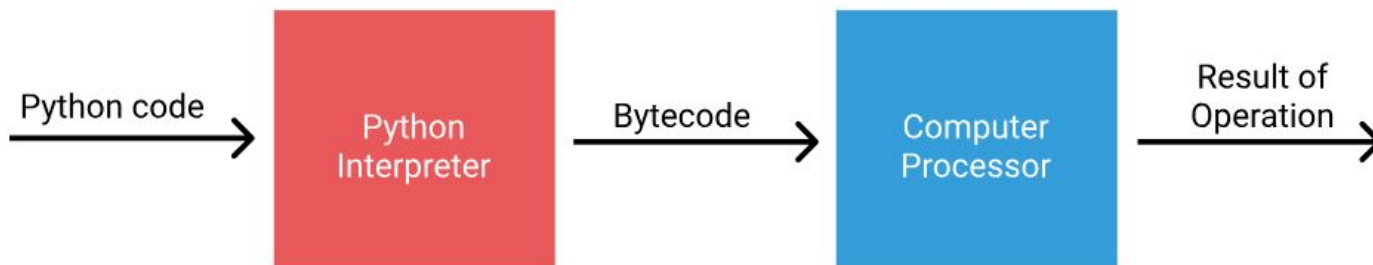
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```
git clone https://github.com/ivanovitchm/imd0033_2018_2.git
```

Ou ....

```
git pull
```

# Understanding Vectorization



Language Type	Example	Time taken to write program	Control over program performance
High-Level	Python	Low	Low
Low-Level	C	High	High

How can Python be so efficient?

# Unvectorized code using list of lists

---

6	5
1	3
5	6
1	4
3	7
5	8
3	5
8	4

Two columns of numbers

```
my_numbers = [  
    [6, 5],  
    [1, 3],  
    [5, 6],  
    [1, 4],  
    [3, 7],  
    [5, 8],  
    [3, 5],  
    [8, 4]  
]
```

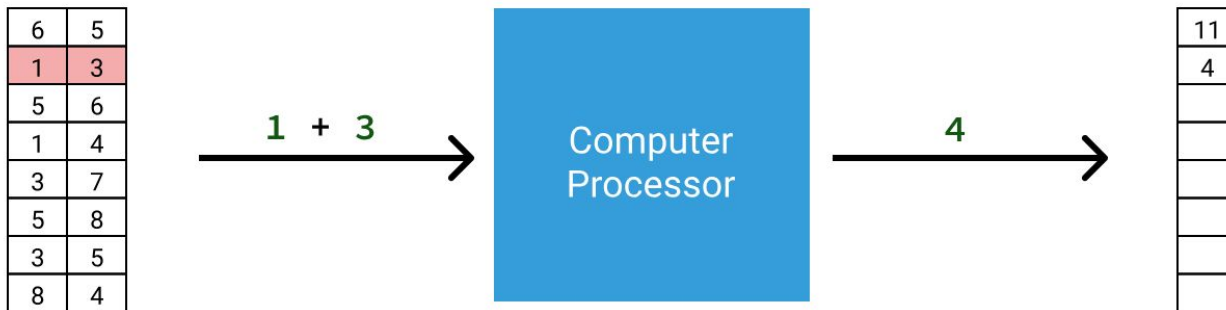
List of lists representation

```
sums = []  
  
for row in my_numbers:  
    row_sum = row[0] + row[1]  
    sums.append(row_sum)
```

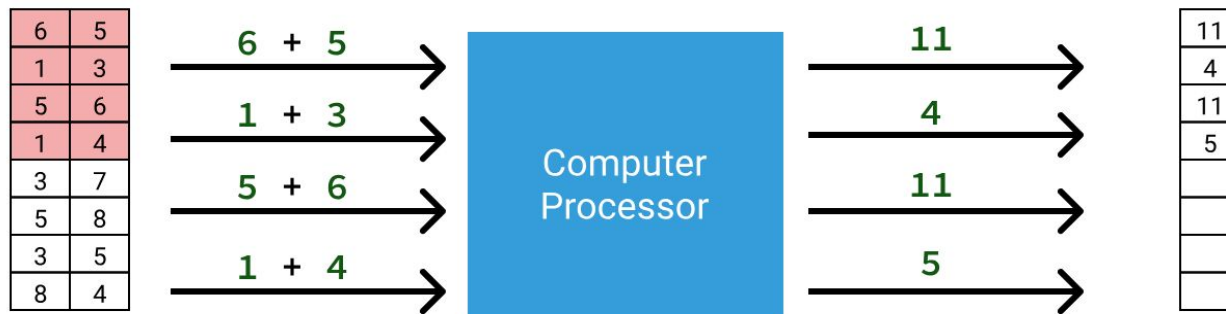
Python code to sum each row

# How Vectorization Makes Code Faster

Single Instruction Multiple Data (SIMD)



Numpy



# NYC Taxi-Airport Data

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There is data on over **1.3 trillion** individual trips, reaching back as far as 2009 and is regularly updated

`nyc_taxis.csv`

# NYC Taxi-Airport Data

---

pickup_year	pickup_month	pickup_day	pickup_dayofweek	pickup_time	pickup_location_code	dropoff_location_code	trip_distance	trip_length	fare_amount	total_amount
2016	1	1	5	0	2	4	21.00	2037	52.0	69.99
2016	1	1	5	0	2	1	16.29	1520	45.0	54.30
2016	1	1	5	0	2	6	12.70	1462	36.5	37.80
2016	1	1	5	0	2	6	8.70	1210	26.0	32.76
2016	1	1	5	0	2	6	5.56	759	17.5	18.80
2016	1	1	5	0	4	2	21.45	2004	52.0	105.60
2016	1	1	5	0	2	6	8.45	927	24.5	32.25
2016	1	1	5	0	2	6	7.30	731	21.5	22.80
2016	1	1	5	0	2	5	36.30	2562	109.5	131.38
2016	1	1	5	0	6	2	12.46	1351	36.0	37.30

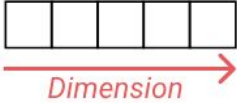
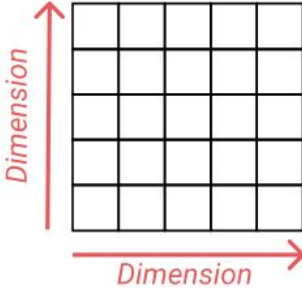
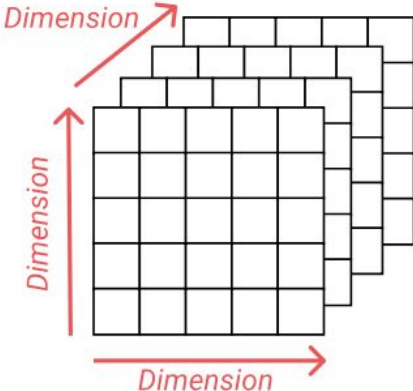


```
1 import csv
2 import numpy as np
3
4 # import nyc_taxi.csv as a list of lists
5 # remove the header row
6 # convert each element to float
7
8 taxi = np.array(
9     [[float(item) for item in row]
10      for row in list(csv.reader(open("nyc_taxis.csv", "r")))[1:]]
11 )
12 print(type(taxi))
13 taxi[:,2:]
14
15
```

<class 'numpy.ndarray'>

```
array([[2.016e+03, 1.000e+00, 1.000e+00, 5.000e+00, 0.000e+00, 2.000e+00,
        4.000e+00, 2.100e+01, 2.037e+03, 5.200e+01, 8.000e-01, 5.540e+00,
        1.165e+01, 6.999e+01, 1.000e+00],
       [2.016e+03, 1.000e+00, 1.000e+00, 5.000e+00, 0.000e+00, 2.000e+00,
        1.000e+00, 1.629e+01, 1.520e+03, 4.500e+01, 1.300e+00, 0.000e+00,
        8.000e+00, 5.430e+01, 1.000e+00]])
```

# Understanding Numpy ndarray

	Number of Dimensions	Known As
	One	One-dimensional array, array, list, vector, sequence
	Two	Two-dimensional array, matrix, table, list of lists, spreadsheet
	Three	Three-dimensional array, multi-dimensional array, panel

# Introduction to Numpy

---

```
>>> print(taxi)
```

```
[[ 2016.  1.  1. ..., 11.65  69.99  1. ]
 [ 2016.  1.  1. ...,  8.    54.3   1. ]
 [ 2016.  1.  1. ...,  0.    37.8   2. ]
 ...,
 [ 2016.  6. 30. ...,  5.    63.34  1. ]
 [ 2016.  6. 30. ...,  8.95  44.75  1. ]
 [ 2016.  6. 30. ...,  0.    54.84  2. ]]
```

```
>>> taxi.shape
(89560, 15)
```

*List of lists method**NumPy method***Selecting a single row**

	0	1	2	3	4
row					
0					
1					
2					
3					
4					

```
sel_lol = data_lol[1]
```

```
sel_np = data_np[1]
```

*Same syntax as list of lists.  
Produces a 1D ndarray.*

**Selecting multiple rows**

	0	1	2	3	4
rows					
0					
1					
2					
3					
4					

```
sel_lol = data_lol[2:]
```

```
sel_np = data_np[2:]
```

*Same syntax as list of lists.  
Produces a 2D ndarray.*

## List of lists method

Selecting a single  
item

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = data_lol[1][3]
```

## NumPy method

```
sel_np = data_np[1,3]
```

*Comma separated row/column  
locations. Produces a single  
Python object.*

## List of lists method

## NumPy method

## Selecting a single column

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = []

for row in data_lol:
    col4 = row[3]
    sel_lol.append(col4)
```

```
sel_np = data_np[:,3]
```

*Comma separated row wildcard and column location. Produces a 1D ndarray*

## Selecting multiple columns

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = []

for row in data_lol:
    col23 = row[1:3]
    sel_lol.append(col23)
```

```
sel_np = data_np[:,1:3]
```

*Comma separated row wildcard and column slice location. Produces a 2D ndarray*

## Selecting multiple, specific columns

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = []

for row in data_lol:
    cols = [row[1],
            row[3],row[4]]
    sel_lol.append(cols)
```

```
cols = [1,3,4]
sel_np = data_np[:,cols]
```

*Comma separated row wildcard and list of column locations. Produces a 2D ndarray*

## List of lists method

## NumPy method

Selecting a 1D  
slice (row)

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = data_lol[2][1:4]
```

```
sel_np = data_np[2,1:4]
```

*Comma separated row location  
and column slice. Produces a  
1D ndarray*

Selecting a 1D  
slice (column)

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = []
```

```
rows = data_lol[1:]
for r in rows:
    col5 = r[4]
    sel_lol.append(col5)
```

```
sel_np = data_np[1:,4]
```

*Comma separated row slice  
and column location. Produces  
a 1D ndarray*

### List of lists method

Selecting a 2D slice

	0	1	2	3	4
0					
1					
2					
3					
4					

```
sel_lol = []  
  
rows = data_lol[1:4]  
for r in rows:  
    new_row = r[:3]  
    sel_lol.append(new_row)
```

### NumPy method

```
sel_np = data_np[1:4,:3]
```

*Comma separated row/column slice locations. Returns a 2D ndarray*



# Lesson\_07\_Introduction\_to\_numpy.ipynb

## Up to Section 1.5



# Vector Math (list of lists vs numpy)

---

```
import numpy as np

# create random (500,5) numpy arrays and list of lists
np_array = np.random.rand(500,5)
list_array = np_array.tolist()

def python_subset():
    filtered_cols = []
    for row in list_array:
        filtered_cols.append([row[1],row[2]])
    return filtered_cols

def numpy_subset():
    return np_array[:,1:3]
```

# Vector Math (list of lists vs numpy)

---

```
%%timeit -r 1 -n 1  
list_of_list = python_subset()
```

1 loop, best of 1: 182  $\mu$ s per loop

```
%%timeit -r 1 -n 1  
numpy_array = numpy_subset()
```

1 loop, best of 1: 9.06  $\mu$ s per loop

# Vector Math (numpy)

---

6	5
1	3
5	6
1	4
3	7
5	8
3	5
8	4

2D array



6	5
1	3
5	6
1	4
3	7
5	8
3	5
8	4

Two 1D arrays



6	+	5
1	+	3
5	+	6
1	+	4
3	+	7
5	+	8
3	+	5
8	+	4

Vectorized addition



11
4
11
5
10
13
8
12

Result

# Calculating Statistics for 1D ndarrays

---

Calculation	Function Representation	Method Representation
Calculate the minimum value of <b>trip_mph</b>	<code>np.min(trip_mph)</code>	<code>trip_mph.min()</code>
Calculate the maximum value of <b>trip_mph</b>	<code>np.max(trip_mph)</code>	<code>trip_mph.max()</code>
Calculate the mean average value of <b>trip_mph</b>	<code>np.mean(trip_mph)</code>	<code>trip_mph.mean()</code>
Calculate the median average value of <b>trip_mph</b>	<code>np.median(trip_mph)</code>	There is no ndarray median method

# Calculating Statistics for 2D ndarrays

2D ndarray

1	0	1	1
0	1	4	3
0	1	0	2
3	0	1	3

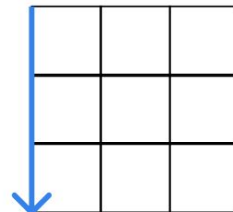
`ndarray.max(axis=0)`

1	0	1	1
0	1	4	3
0	1	0	2
3	0	1	3

3	1	4	3
---	---	---	---

Result

`ndarray.method(axis=0)`  
Calculates along the **row** axis



Results

Calculates result for  
each **column**.

2D ndarray

1	0	1	1
0	1	4	3
0	1	0	2
3	0	1	3

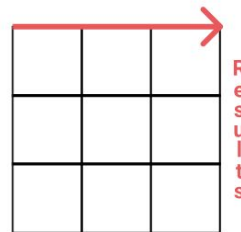
`ndarray.max(axis=1)`

1	0	1	1
0	1	4	3
0	1	0	2
3	0	1	3

Result

1
4
2
3

`ndarray.method(axis=1)`  
Calculates along the **column** axis



Results

Calculates result for  
each **row**.

# Adding Rows and Columns to ndarrays (concatenate)

---

```
>>> print(ones)
```

```
[[ 1  1  1]
 [ 1  1  1]]
```

```
>>> print(zeros)
```

```
[ 0  0  0]
```

```
>>> print(ones.shape)
```

```
(2, 3)
```

```
>>> print(zeros.shape)
```

```
(3,)
```

## Adding Rows and Columns to ndarrays (concatenate)

---

```
>>> zeros_2d = np.expand_dims(zeros,axis=0)
```

```
>>> print(zeros_2d)
```

```
[[ 0  0  0]]
```

```
>>> print(zeros_2d.shape)
```

```
(1, 3)
```



## Adding Rows and Columns to ndarrays (concatenate)

---

```
>>> combined = np.concatenate([ones,zeros_2d],axis=0)
```

```
>>> print(combined)
```

```
[[ 1  1  1]
 [ 1  1  1]
 [ 0  0  0]]
```

# Sorting ndarrays

```
fruit = np.array(['orange', 'banana',  
                 'apple', 'grape',  
                 'cherry'])
```



```
sorted_order = np.argsort(fruit)
```

orange	0
banana	1
apple	2
grape	3
cherry	4

```
sorted_fruit = fruit[sorted_order]
```



apple
banana
cherry
grape
orange

2	1	4	3	0
---	---	---	---	---

# Lesson\_07\_Introduction\_to\_numpy.ipynb

## Up to Section 1.11

