# **Project advice**

- EDA: figure types are correct, axes are labelled, units added to the labels if necessary, the figure is informative
- come up with a decent ML question
- correctly identify if the problem is classifiction or regression
- Split your data first!
  - if dataset is i.i.d.: train/val/test or Kfold are good
  - if not i.i.d., follow lecture notes on group-based splitters, time series split, and how to create autoregression features
- Preprocess your dataset next!
  - decide for each feature if it is categorical, ordinal, continuous and preprocess accordingly
  - fit\_transform the training set, transform the validation and test sets!
  - handle missing values in categorical and ordinal features during preprocessing as we discussed in class
  - if you have missing values in continuous features, describe the basic properties of the missing values (e.g., what fraction of the points have missing values, which features, what fraction of the features are missing, etc).
    - o do not impute or drop features/rows!
    - o you will need to apply the advanced missing value techniques we will cover during the second half of the term
- · keep your time! overtime penalty will be applied.

## Mudcard

- Is it a commom practice or must that we choose the sorted values in pred\_prob\_class1 as our threshold?
  - Yes, I actually got this question during a technical interview a few years ago
  - it is common practice and in fact it is the best you can do
  - while it is true that there are infinite numbers between 0 and 1, your dataset is finite
  - so the best thing you can do is to use the sorted pred\_prob\_class1 as p\_crits
  - think of it this way:
    - if two sorted values are p\_crit1 and p\_crit2 where p\_crit1 < p\_crit2, for any p\_crit1 < p\_crit < p\_crit2, the predicted classes will always be the same so why choose any other value in between?
- I am unclear about variance in our Quiz 3 question... how do I calculate it and what is its significance?
  - variance is a pretty standard staticitcal property. if you do not know what it is, definitely read up on it
- What is the variance score? Do we calculate through numpy?
- how should we find out var in the last part?
  - google how to calculate the variance of an array in numpy
- What is the unit of the MSE if it's different from the target variable?
  - whatever the unit of the target variable's unit is squred
  - if y is in years, MSE will be years^2
  - if y is in seconds, MSE will be seconds^2
  - if y is miles, MSE will be miles^2
- Does a negative R2 score in non-iid regression model still indicate a bad model? Or should we use a different regression metric?
  - it indicated a model that's even worse than the baseline
  - doesn't matter what metric you use, the conclusion will be the same
  - all metrics will be worse than the baseline

# Supervised ML algorithms, part 1

By the end of this lecture, you will be able to

- · describe the main components of any ML algorithm
- · describe how linear regression works
- describe how logistic regression works

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## The supervised ML pipeline

The goal: Use the training data (X and y) to develop a model which can accurately predict the target variable (y\_new') for previously unseen data (X\_new).

- 1. Exploratory Data Analysis (EDA): you need to understand your data and verify that it doesn't contain errors
- do as much EDA as you can!
- 2. Split the data into different sets: most often the sets are train, validation, and test (or holdout)
  - practitioners often make errors in this step!
- you can split the data randomly, based on groups, based on time, or any other non-standard way if necessary to answer your ML question
- 3. Preprocess the data: ML models only work if X and Y are numbers! Some ML models additionally require each feature to have 0 mean and 1 standard deviation (standardized features)
- often the original features you get contain strings (for example a gender feature would contain 'male', 'female', 'non-binary', 'unknown') which needs to transformed into numbers
- often the features are not standardized (e.g., age is between 0 and 100) but it needs to be standardized
- 4. Choose an evaluation metric: depends on the priorities of the stakeholders
- often requires quite a bit of thinking and ethical considerations

#### 5. Choose one or more ML techniques: it is highly recommended that you try multiple models

- start with simple models like linear or logistic regression
- try also more complex models like nearest neighbors, support vector machines, random forest, etc.

#### 6. Tune the hyperparameters of your ML models (aka cross-validation)

- ML techniques have hyperparameters that you need to optimize to achieve best performance
- for each ML model, decide which parameters to tune and what values to try
- loop through each parameter combination
  - train one model for each parameter combination
  - evaluate how well the model performs on the validation set
- take the parameter combo that gives the best validation score
- · evaluate that model on the test set to report how well the model is expected to perform on previously unseen data

#### 7. Interpret your model: black boxes are often not useful

- check if your model uses features that make sense (excellent tool for debugging)
- often model predictions are not enough, you need to be able to explain how the model arrived to a particular prediction (e.g., in health care)

# Supervised ML algorithms: three parts

ullet 1. a mathematical model (f) is used to convert the feature values into a prediction

 $f(X_i) = y_i'$ , where i is the ith data point in our sample.  $X_i$  is a vector and  $y_i'$  is a number. - f is your supervised ML algorithm - it usually has a number of intrinsic parameters

- . 2. an optimization algorithm is used to determine the intrinsic parameter values given the training set
  - there are various algorithms
  - e.g., analytical solutions, brute force, gradient descent, backpropagation
- 3. the optimization algorithm minimizes a metric called **the cost function** 
  - the cost function is used to determine the best intrinsic parameters of one model based on the training data
  - it is not the same as the evaluation metric
    - o you use the evlaution metric to compare various models
    - o the model uses the cost function to find the best values of its intrinsic parameters

• keep in mind though that the same metric can be used as the cost function and the evaluation metric (e.g., MSE in regression) but that's not necessarily the case (e.g., the cost function is MSE but you use R2 as an evaluation metric).

## Supervised ML algorithms, part 1

By the end of this lecture, you will be able to

- describe the main components of any ML algorithm
- · describe how linear regression works
- describe how logistic regression works

### **Linear Regression**

```
In []: from sklearn.linear_model import LinearRegression # import the model
LinReg = LinearRegression() # initialize a simple linear regression model
LinReg.fit(X_train,y_train) # we will learn now what happens when you issue this line in regression
```

• This is the mathematical model:

$$f(X_i) = y_i' = w_0 + X_{i1}w_1 + X_{i2}w_2 + ... = w_0 + \sum_{j=1}^m w_j X_{ij}$$

where  $y_i^t$  is the prediction of the linear regression model and w are parameters.

- The cost function is MSE
- We will find the best parameter values by brute force first, then simple gradient descent.

### Let's generate some data

```
In [1]: # load packages and generate data
        import numpy as np
        import matplotlib.pyplot as plt
        import pandas as pd
        import matplotlib
        from sklearn.datasets import make_regression
        matplotlib.rcParams.update({'font.size': 11})
        # fix the seed so code is reproducable
        np.random.seed(1)
        # generate n_samples points
        n_samples = 30
        # generate data
        X, y, coef = make\_regression(n\_samples = n\_samples, n\_features = 1, <math>coef = True, noise= 10, bias=0)
        print(coef) # the coefficients of the underlying linear model, the bias is 0.
        print(np.dot(X,coef)[:,0]) # noise is added to the label
        print(y)
        df = pd.DataFrame()
        df['x1'] = X[:,0]
        df['y'] = y
        print(df.head())
        df.to_csv('data/regression_example.csv',index=False)
```

```
28.777533858634875
       [ 9.18115839 -30.87739085 24.90429735 -4.96205858 32.94232532
        14.46054785 -66.23260778 -19.67600162 -11.0521372 -25.26260034 -59.28576902 -31.67310564 -31.65215819 32.62708851 50.21137962
         -3.53647763 -26.92913658 46.7446537 42.07586066 25.94555749
        -21.90565736 \quad 15.2623224 \quad -15.19948048 \quad -7.70915828 \quad 16.77198455
          1.21480753 25.92441258 -7.17626442 -17.60484091 -9.27837201]
       [ 3.08130585 -48.2639338 25.93592732 1.87178372 45.4428258
          6.88380644 -72.44927625 -16.20740827 -12.15967691 -25.0337406
        -66.76530644 -35.83422144 -27.17695128 53.04737598 52.96856006
         10.13384942 -20.19197583 36.16208808 58.99412194 38.42855536
        -32.81240623 6.77988325 -15.82439642 -20.62478531 18.61129032
          9.78715027 31.80735422 -4.11214063 -11.04200012 -15.08634424]
                x1
       0 0.319039 3.081306
       1 -1.072969 -48.263934
       2 0.865408 25.935927
       3 -0.172428
                    1.871784
       4 1.144724 45.442826
In [2]: def predict(X,w):
            if len(np.shape(w)) != 2:
                 w = np.array(w)[np.newaxis,:] # just a numpy trick to make the dot product work
            y_pred = w[0,0] + X.dot(w[0,1:]) # intercept + w_i*x_i
            return y_pred
        def cost_function(X,y_true,w):
            Take in a numpy array X,y_true, w and generate the cost function
            of using w as parameter in a linear regression model
            m = len(y)
            w = np.array(w)[np.newaxis,:] # just a numpy trick to make the dot product work in predict
            y_pred = predict(X, w)
             cost = (1/m) * np.sum(np.square(y_true-y_pred)) # this is MSE
            return cost
```

$$y_i' = w_0 + x_{i1}w_1$$

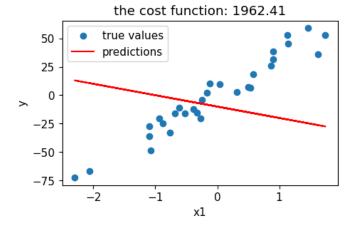
- ullet  $w_0$  is the intercept
- $w_1$  is the slope

#### We are looking for the best fit line!

For a given w vector, the cost function returns the MSE.

```
In [3]: w = [-10,-10] # intercept is w[0], the slope is w[1]

plt.figure(figsize=(5,3))
plt.scatter(df['x1'],df['y'],label='true values')
plt.plot(df['x1'],predict(df['x1'].values[:,np.newaxis],w),label='predictions',color='r')
plt.title('the cost function: '+str(np.around(cost_function(df['x1'].values[:,np.newaxis],df['y'],w),2)))
plt.xlabel('x1')
plt.ylabel('y')
plt.legend()
plt.savefig('figures/line_fit.png',dpi=300)
plt.show()
```



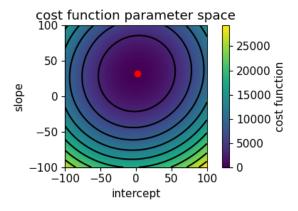
#### What we want:

- Find the w vector that minimizes the cost function!
  - that's our best fit model

#### How we do it:

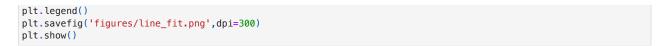
- brute force
  - create a grid of w[0] and w[1] values
  - loop through all w vectors on the grid
  - find the w vector that comes with the smallest cost

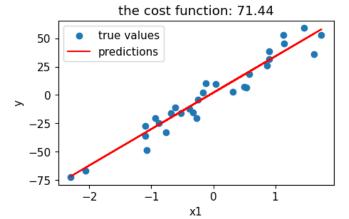
```
In [4]: n_vals = 101
        w0 = np.linspace(-100,100,n_vals) # the intercept values to explore
        w1 = np.linspace(-100,100,n_vals) # the slope values to explore
        cost = np.zeros([len(w0), len(w1)]) # the cost function's value for each w
        # loop through all intercept—slope combinations and calculate the cost function
        for i in range(n_vals):
            for j in range(n_vals):
                w = [w0[i], w1[j]]
                cost[i,j] = cost_function(df['x1'].values[:,np.newaxis],df['y'],w)
        print('min(cost):',np.min(cost))
        min_coords = np.unravel_index(cost.argmin(),np.shape(cost))
        print('best intercept:',w0[min_coords[0]])
        print('best slope:',w1[min_coords[1]])
       min(cost): 71.43643291686587
       best intercept: 2.0
       best slope: 32.0
In [5]: plt.figure(figsize=(5,3))
        ax = plt.gca()
        extent = (np.min(w0), np.max(w0), np.min(w1), np.max(w1))
        fig = ax.imshow(cost.T,origin='lower',extent=extent,vmin=0)
        plt.colorbar(fig,label='cost function')
        ax.contour(w0,w1,cost.T,levels=10,colors='black')
        plt.scatter(w0[min_coords[0]],w1[min_coords[1]],c='r')
        ax.xaxis.set_ticks_position("bottom")
        plt.xlabel('intercept')
        plt.ylabel('slope')
        plt.title('cost function parameter space')
        plt.tight_layout()
        plt.savefig('figures/cost_function.png',dpi=300)
        plt.show()
```



```
In [6]: w = [2,32] # intercept is w[0], the slope is w[1]

plt.figure(figsize=(5,3))
plt.scatter(df['x1'],df['y'],label='true values')
plt.plot(df['x1'],predict(df['x1'].values[:,np.newaxis],w),label='predictions',color='r')
plt.title('the cost function: '+str(np.around(cost_function(df['x1'].values[:,np.newaxis],df['y'],w),2)))
plt.xlabel('x1')
plt.ylabel('y')
```





### Quiz 1

#### The brute force approach works but...

- the number of w vectors to loop through explodes with the number of features we have
  - with n features, we would need to loop through  $\sim 100^n$  w vectors.
  - no guarantee that the best w vector is within our grid.
- We need to use a smarter numerical method to find the best w!
  - gradient descent to the rescue!

#### How do we find the best w values?

- ullet start with arbitrary initial w values and the cost function L
- repeat until convergence:

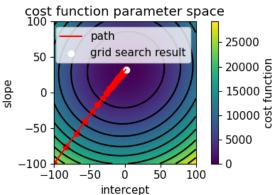
$$w_j := w_j - l rac{\partial L(w)}{\partial w_j}$$
 ,

where  $rac{\partial L(w)}{\partial w_j}$  is the gradient of the cost function at the current w location and l is the learning rate.

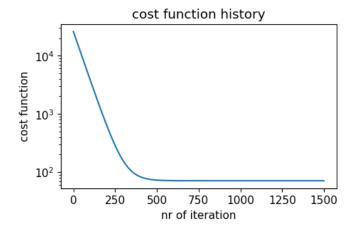
- the gradient tells us which way the cost function is the steepest
- the learning rate tells us how big of a step we take in that direction

```
In [7]: def gradient_descent(X,y_true,w,learning_rate=0.01,iterations=100):
            Χ
                = Matrix of X
                = Vector of Y
            w = Vector of ws
            learning_rate
            iterations = no of iterations
            Returns the final w vector and array of cost history over no of iterations
            m = len(y_true)
            w = np.array(w)[np.newaxis,:]
            cost_history = np.zeros(iterations)
            w_history = np.zeros([iterations+1,np.shape(w)[1]])
            w_history[0] = w
            for it in range(iterations):
                y_pred = predict(X,w)
                delta_w = np.zeros(np.shape(w)) # the step we take
                # the derivative of the cost function with respect to the intercept
                delta_w[0,0] = (1/m) * sum(y_pred - y_true)
                # the derivative of the cost function with respect to the slopes * learning_rate
                delta_w[0,1:] = (1/m)*(X.T.dot((y_pred - y_true)))
                w = w - learning_rate * delta_w # update w so we move down the gradient
                w_history[it+1] = w[0]
                cost_history[it] = cost_function(X,y_true,w[0])
```

```
return w[0], cost_history, w_history
In [8]: w,cost_history,w_hist = gradient_descent(df['x1'].values[:,np.newaxis],df['y'],[-100,-100],0.01,1500)
        print(w)
        print(w_hist)
       [ 1.14458074 32.24849231]
       [[-100.
                       -100.
        [ -99.06782181 -98.70917181]
        [ -98.14419169 -97.43097591]
            1.14457933
        Γ
                         32.24849104]
            1.14458004
                         32.24849168]
            1.14458074
                         32.24849231]]
In [9]: plt.figure(figsize=(5,3))
        ax = plt.gca()
        extent = (np.min(w0), np.max(w0), np.min(w1), np.max(w1))
        fig = ax.imshow(cost.T,origin='lower',extent=extent,vmin=0)
        plt.colorbar(fig, label='cost function')
        ax.contour(w0,w1,cost.T,levels=10,colors='black')
        plt.plot(w_hist[::20,0],w_hist[::20,1],color='r',label='path')
        plt.scatter(w_hist[::20,0],w_hist[::20,1],c='r')
        plt.scatter(w0[min_coords[0]],w1[min_coords[1]],c='w',label='grid search result')
        ax.xaxis.set_ticks_position("bottom")
        plt.legend()
        plt.xlabel('intercept')
        plt.ylabel('slope')
        plt.title('cost function parameter space')
        plt.tight_layout()
        plt.savefig('figures/cost_function_with_path.png',dpi=300)
        plt.show()
```



```
In [10]: plt.figure(figsize=(5,3))
   plt.plot(cost_history)
   plt.semilogy()
   plt.ylabel('cost function')
   plt.xlabel('nr of iteration')
   plt.title('cost function history')
   plt.savefig('figures/cost_hist.png',dpi=300)
   plt.show()
```



### DO NOT USE MY gradient\_descent FUNCTION!

- it is for illustration purposes only
- it is much slower than the sklearn implemementation!

### Quiz 2

### Supervised ML algorithms, part 1

By the end of this lecture, you will be able to

- describe the main components of any ML algorithm
- describe how linear regression works
- · describe how logistic regression works

# Logistic regression

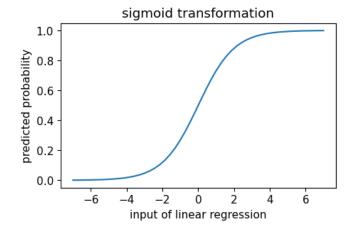
```
In []: from sklearn.linear_model import LogisticRegression
LogReg = LogisticRegression() # initialize a simple logistic regression model
LogReg.fit(X_train,y_train) # we will learn what happens when you issue this line in classification
```

- name is misleading, logistic regression is for classification problems!
- the model:

$$y_i' = rac{1}{1+e^{-z}}$$
 , where  $z = w_0 + \sum_{j=1}^m w_j x_{ij}$ 

 $f(z) = \frac{1}{1+e^{-z}}$  is the sigmoid function.

• it is linear regression model but a sigmoid function is applied to its output



### The cost function

• the logloss metric is used as a cost function in logistic regression

$$L(w) = -rac{1}{m} \sum_{i=1}^m [y_i \ln(y_i') + (1-y_i) \ln(1-y_i')] \ L(w) = -rac{1}{m} \sum_{i=1}^m [y_i \ln(rac{1}{1+e^{-w_0+\sum_{j=1}^m w_j x_{ij}}}) + (1-y_i) \ln(1-rac{1}{1+e^{-w_0+\sum_{j=1}^m w_j x_{ij}}})]$$

## **Gradient descent**

- the basic algorithm works but the <code>gradient\_descent</code> function needs to be updated because the cost function changed!
- repeat until convergence:

$$w_j := w_j - l rac{\partial L(w)}{\partial w_j}$$
 ,

where  $rac{\partial L(w)}{\partial w_j}$  is the gradient of the cost function at the current w location and l is the learning rate.

### Mud card