

# Improving the Estimation of Fingerprint Spatial Relationships via Deep Metric Learning on Continuous Similarities

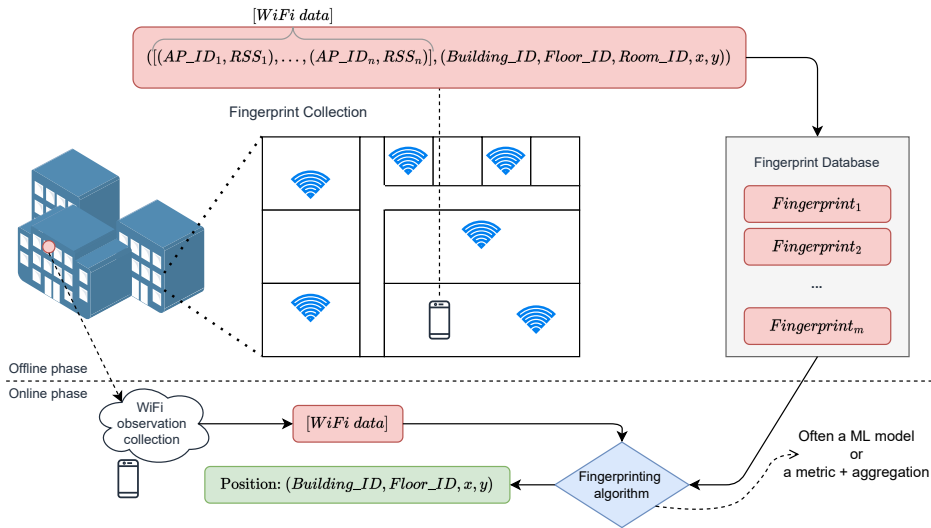
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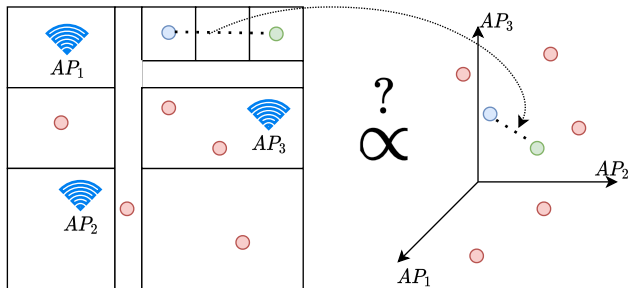
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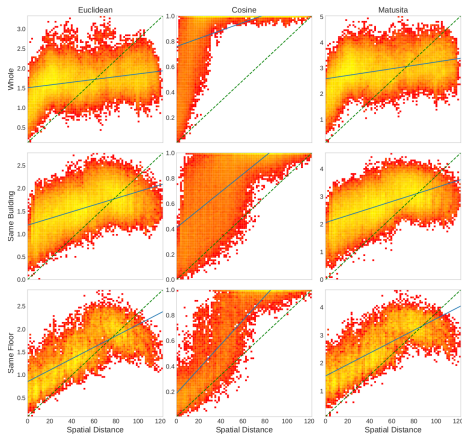
## Main research question

Given a collection of (fingerprint, location) pairs  $\mathcal{P} = \{(\mathbf{x}, \mathbf{y})_i \mid \mathbf{x} \in \mathbb{R}^m, \mathbf{y} \in \mathbb{R}^p\}_{i=1}^N$ , where  $m$  is the number of available APs and  $p$  is the number of dimensions used to represent the locations, is it possible to determine the *spatial relationships* between fingerprints' locations by reasoning directly in the fingerprint space  $\mathbb{R}^m$ ?



## Research question

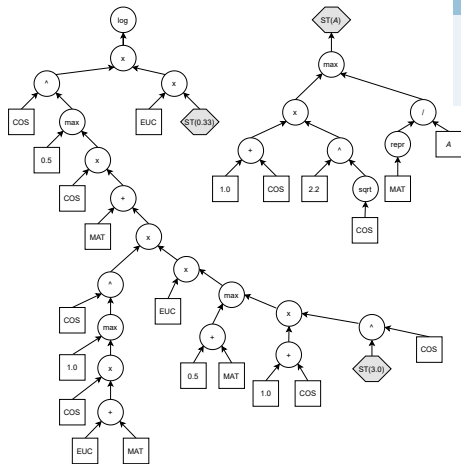
Can *classical* metrics characterise the spatial relationship between fingerprints' positions?



- Large systematic study on multiple metrics, datasets and granularities
- Metrics have rather heterogeneous behaviour, with some outperforming the others (e.g., cosine similarity)
- Variability across different scenarios
- Performance far from the optimal case: **classical metrics fail at characterising the spatial relationship between fingerprints' positions**

## Research question

Could we get better performance by exploiting the heterogeneity of the individual metrics?



- Genetic programming to solve a symbolic regression task → *Learned Meta-metric*
- Good generalisation capabilities on unseen datasets
- Better results, but still not optimal: **likely to be limited from the considered data representation**
- *Bonus*: Correlation maximisation is a good proxy task for positioning: the meta-metric achieves top performance

# Deep Metric Learning in a Nutshell

Deep Metric Learning (DML) aims to learn similarity metrics in an end-to-end fashion with deep neural networks. It consists of learning an embedding function  $\phi_\theta : \mathcal{X} \rightarrow \mathcal{Z}$  from the feature space ( $\mathcal{X}$ ) to a new latent one ( $\mathcal{Z}$ ) in such a way that elements deemed similar according to a given similarity function (often evaluated over  $\mathcal{X}$ 's labels  $\mathcal{Y}$ ) are mapped closer in  $\mathcal{Z}$  than those considered to be dissimilar.

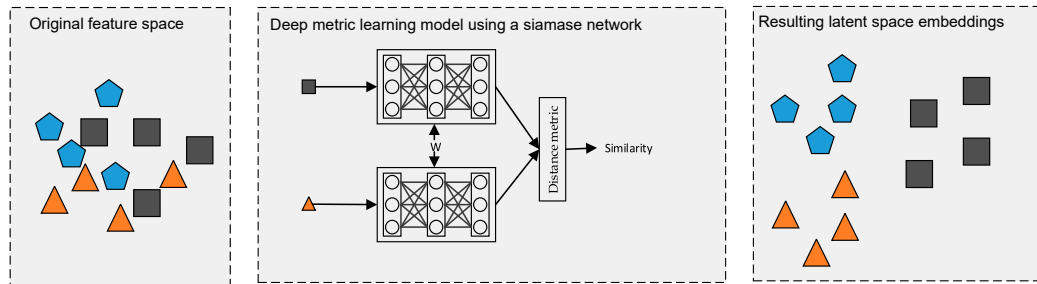


Figure adapted from Kaya M, Bilge HŞ. Deep Metric Learning: A Survey. *Symmetry*. 2019.

# Deep Metric Learning in a Nutshell (cont'd)

- Mainly developed by the computer vision community for tasks like face recognition, person re-identification, zero-shot and self-supervised learning
- Performance largely depends on the loss function and the sampling strategies
  - How to learn comprehensive relationships and leverage all the batch elements?
  - How to implicitly or explicitly mine informative tuples only?

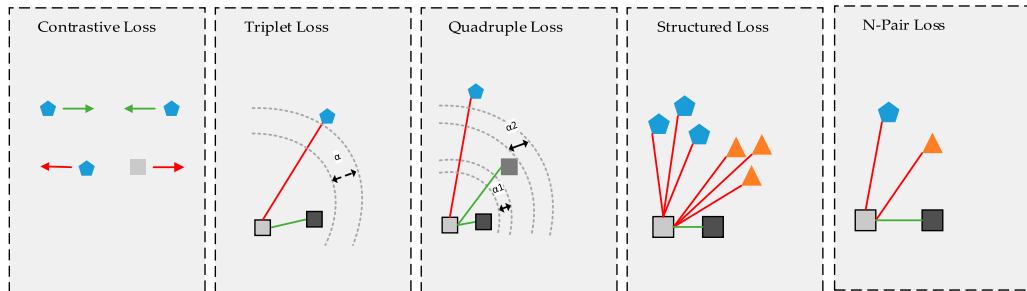


Figure from Kaya M, Bilge HŞ. Deep Metric Learning: A Survey. *Symmetry*. 2019.



## Research question

Can we leverage Deep Metric Learning to obtain an effective similarity function that captures the spatial relationship in the fingerprint space?

Dealing with fingerprints and spatial quantities requires *continuous similarity* assessments

Problem! DML has been defined almost only for binary similarities:

- **Continuous case is more complex** - ranking and proportionality
- Notions of negative and positive elements for tuples construction are not viable anymore
- Defining thresholds for binarization is domain and application dependent and rather ineffective



A possible solution to achieve DML preserving the desired properties is to rely on distance ratios, requiring that:

$$\frac{s(\mathbf{y}_i, \mathbf{y}_j)}{s(\mathbf{y}_k, \mathbf{y}_h)} = c \cdot \frac{\| \phi_{\theta}(\mathbf{x}_i) - \phi_{\theta}(\mathbf{x}_j) \|_2^2}{\| \phi_{\theta}(\mathbf{x}_k) - \phi_{\theta}(\mathbf{x}_h) \|_2^2},$$

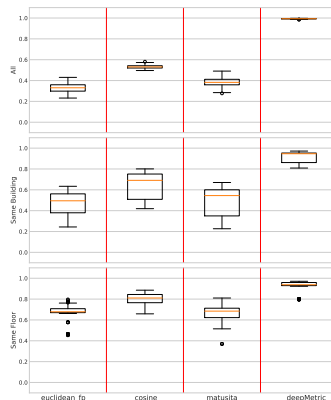
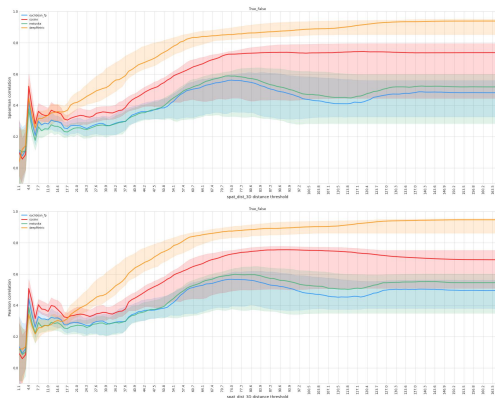
where  $s : \mathbb{R}^p \times \mathbb{R}^p \rightarrow \mathbb{R}$  is a similarity function over the label space (e.g., in fingerprinting, the Euclidean distance),  $c$  is a scaling factor, and  $i, j, k, h \in 1, \dots, N$ .

Note that ratios have some interesting properties in this context:

- The learning task becomes independent from  $s$ , and the scale of the labels
- The choice of the metric used over  $\mathcal{Z}$  becomes (almost) irrelevant
- Preserving proportions grants ranking

Preliminary results are very encouraging but:

- Problems that are solved in binary-supervised DML here might be open
- Specific continuous-related issues, e.g., imbalance in the distances distribution





# DML for Fingerprinting - Why Does it Matter?

- Ease the radio-map creation and maintenance:
  - Having a more reliable metric should allow for a more sparse fingerprint collection
- Promoting the development of semi-supervised localisation solutions:
  - DML is a supervised task, yet it requires knowing only the spatial distances between two fingerprints...
  - ... but such information can be acquired using auxiliary sensors
  - crowdsourcing + a few points labelled with the precise location
- Possible improvement in other downstream tasks
- The approach is rather general and thus may be interesting per se for the ML community, beyond the specific application domain



## Questions?

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Some references:

- Saccomanno, N., Brunello, A., & Montanari, A. (2021). What you sense is not where you are: On the relationships between fingerprints and spatial knowledge in indoor positioning. *IEEE Sensors Journal*
- Brunello, A., Montanari, A., & Saccomanno, N. (2022). A Genetic Programming Approach to WiFi Fingerprint Meta-distance Learning. Under Review
- Kim, S., Seo, M., Laptev, I., Cho, M., & Kwak, S. (2019). Deep metric learning beyond binary supervision. *IEEE/CVF CVPR*