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# Chapter 2: Intro to Relational Model

## Relational Query Languages

**Database System Concepts, 6<sup>th</sup> Ed.**

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# Relational Query Languages

- Procedural vs .non-procedural, or declarative
- “Pure” languages:
  - Relational algebra
  - Tuple relational calculus
  - Domain relational calculus
- The above 3 pure languages are equivalent in computing power
- We will concentrate in this chapter on relational algebra
  - Not Turing-machine equivalent
  - It consists of 6 basic operations



# Select operation – selection of rows (tuples)

- Relation r

A	B	C	D
$\alpha$	$\alpha$	1	7
$\alpha$	$\beta$	5	7
$\beta$	$\beta$	12	3
$\beta$	$\beta$	23	10

- $\sigma_{A=B \wedge D > 5}(r)$

A	B	C	D
$\alpha$	$\alpha$	1	7
$\beta$	$\beta$	23	10



# Project operation – selection of columns (attributes)

- Relation  $r$ :

A	B	C
$\alpha$	10	1
$\alpha$	20	1
$\beta$	30	1
$\beta$	40	2

- $\Pi_{A,C}(r)$

A	C
$\alpha$	1
$\alpha$	1
$\beta$	1
$\beta$	2

 $=$ 

A	C
$\alpha$	1
$\beta$	1
$\beta$	2



# Union of two relations

- Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r \cup s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1
$\beta$	3



# Set difference of two relations

- Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

- $r - s$ :

$A$	$B$
$\alpha$	1
$\beta$	1



# Set intersection of two relations

■ Relation  $r, s$ :

$A$	$B$
$\alpha$	1
$\alpha$	2
$\beta$	1

$r$

$A$	$B$
$\alpha$	2
$\beta$	3

$s$

■  $r \cap s$

$A$	$B$
$\alpha$	2

Note:  $r \cap s = r - (r - s)$



# Joining two relations – Cartesian product

■ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

$C$	$D$	$E$
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

$s$

■  $r \times s$ :

$A$	$B$	$C$	$D$	$E$
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b





# Cartesian product – naming issue

■ Relations  $r, s$ :

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

$B$	$D$	$E$
$\alpha$	10	a
$\beta$	10	a
$\beta$	20	b
$\gamma$	10	b

$s$

■  $r \times s$ :

$A$	$r.B$	$s.B$	$D$	$E$
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b



# Renaming a table

- Allows us to refer to a relation, (say  $E$ ) by more than one name.

$$\rho_x(E)$$

returns the expression  $E$  under the name  $X$

- Relations  $r$

$A$	$B$
$\alpha$	1
$\beta$	2

$r$

- $r \times \rho_s(r)$

$r.A$	$r.B$	$s.A$	$s.B$
$\alpha$	1	$\alpha$	1
$\alpha$	1	$\beta$	2
$\beta$	2	$\alpha$	1
$\beta$	2	$\beta$	2



# Composition of operations

- Can build expressions using multiple operations
- Example:  $\sigma_{A=C}(r \times s)$

- $r \times s$

A	B	C	D	E
$\alpha$	1	$\alpha$	10	a
$\alpha$	1	$\beta$	10	a
$\alpha$	1	$\beta$	20	b
$\alpha$	1	$\gamma$	10	b
$\beta$	2	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b
$\beta$	2	$\gamma$	10	b

- $\sigma_{A=C}(r \times s)$

A	B	C	D	E
$\alpha$	1	$\alpha$	10	a
$\beta$	2	$\beta$	10	a
$\beta$	2	$\beta$	20	b



# Joining two relations – Natural Join

- Let  $r$  and  $s$  be relations on schemas  $R$  and  $S$  respectively. Then, the “natural join” of relations  $R$  and  $S$  is a relation on schema  $R \cup S$  obtained as follows:
  - Consider each pair of tuples  $t_r$  from  $r$  and  $t_s$  from  $s$ .
  - If  $t_r$  and  $t_s$  have the same value on each of the attributes in  $R \cap S$ , add a tuple  $t$  to the result, where
    - ▶  $t$  has the same value as  $t_r$  on  $r$
    - ▶  $t$  has the same value as  $t_s$  on  $s$



# Natural Join Example

- Relations  $r, s$ :

$A$	$B$	$C$	$D$
$\alpha$	1	$\alpha$	a
$\beta$	2	$\gamma$	a
$\gamma$	4	$\beta$	b
$\alpha$	1	$\gamma$	a
$\delta$	2	$\beta$	b

$r$

$B$	$D$	$E$
1	a	$\alpha$
3	a	$\beta$
1	a	$\gamma$
2	b	$\delta$
3	b	$\epsilon$

$s$

- Natural Join

■  $r \bowtie s$

$A$	$B$	$C$	$D$	$E$
$\alpha$	1	$\alpha$	a	$\alpha$
$\alpha$	1	$\alpha$	a	$\gamma$
$\alpha$	1	$\gamma$	a	$\alpha$
$\alpha$	1	$\gamma$	a	$\gamma$
$\delta$	2	$\beta$	b	$\delta$

$$\Pi_{A, r.B, C, r.D, E} (\sigma_{r.B = s.B \wedge r.D = s.D} (r \times s))$$



# Summary of Relational Algebra Operators

Symbol (Name)	Example of Use
$\sigma$ (Selection)	$\sigma \text{ salary} \geq 85000$ ( <i>instructor</i> )
	Return rows of the input relation that satisfy the predicate.
$\Pi$ (Projection)	$\Pi ID, salary$ ( <i>instructor</i> )
	Output specified attributes from all rows of the input relation. Remove duplicate tuples from the output.
$\times$ (Cartesian Product)	<i>instructor</i> $\times$ <i>department</i>
	Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.
$\cup$ (Union)	$\Pi name$ ( <i>instructor</i> ) $\cup$ $\Pi name$ ( <i>student</i> )
	Output the union of tuples from the <i>two</i> input relations.
$-$ (Set Difference)	$\Pi name$ ( <i>instructor</i> ) $--$ $\Pi name$ ( <i>student</i> )
	Output the set difference of tuples from the two input relations.
$\bowtie$ (Natural Join)	<i>instructor</i> $\bowtie$ <i>department</i>
	Output pairs of rows from the two input relations that have the same value on all attributes that have the same name.



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# End of Chapter 2

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