Problem 10.6

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Each column is one step of QMC1 $\,$

In QMC1 we remove useless literals $\,$

 $(x \wedge T) \vee (x \wedge F)$ is the same as $x \wedge (T \vee F)$

which is the same as x

Therefore we remove any literal that is redundant in such a way.

| Initial | Reduced 1 | Reduced 2 |
|---------|-----------|-----------|
| FFTT | FFTX | XFTX |
| FTFF | XFTF | TFXF |
| TFFF | XTFF | TXFF |
| TFTF | TFXF | |
| TTFF | TFTX | |

The next step removes all the non-essential monomials.

Non-essentials are the monomials whose true statements can all be fulfilled by others.

If this can happen then there existence is useless.

| | | FFTT | FFTF | FTFF | TFFF | TFTF | TFTT | TTFF |
|----------------|------------------|------|------|------|------|------|------|------|
| $\bar{x_2}$ | 3 | Т | Т | F | F | Т | Т | F |
| $x_1\bar{x_2}$ | \overline{c}_4 | F | F | F | Т | Т | F | F |
| $x_1\bar{x_3}$ | \overline{c}_4 | F | F | F | Т | F | F | Τ |

$$(\bar{x_2}x_3)+(x_1\bar{x_2}\bar{x_4})+(x_1\bar{x_3}\bar{x_4})$$