# Multiple Secret Leaders

#### Authors here

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# 1 Some Notation

- 1. We will have n parties
- 2. We will have k leaders elected
- 3. We will have a "bid" published by a user  $i \in [n]$  be denoted as  $b_i$
- 4. We will denote a commitment as  $comm_i$
- 5. We will denote some generic CRHF as h
- 6. We will say Enc<sub>TFHE</sub> and Dec<sub>TFHE</sub> for TFHE encoding and decoding respectively

## 2 Preliminaries

### 2.1 Threshold FHE

[JRS17, BGG<sup>+</sup>18] defines threshold FHE encryption. For the sake of completeness, we will define it here.

**Definition 2.1** (TFHE [JRS17]). Let  $P = \{P_1, ..., P_N\}$  be a set of N parties and S be a class of access structures on P. A TFHE scheme for S is a tuple of PPT algorithms

(TFHE.Setup, TFHE.Encrypt, TFHE.Eval, TFHE.PartDec, TFHE.FinDec)

such that the following specifications are met

- $(pk, sk_1, ..., sk_N) \leftarrow \text{TFHE.Setup}(1^{\lambda}, 1^s, \mathbb{A})$ : Takes as input a security parameter  $\lambda$ , a depth bound on the circuit, and a structure  $\mathbb{A} \in \mathbb{S}$ . Outputs a public key pk and a secret key  $sk_i$  for each party  $P_i$ .
- ct  $\leftarrow$  TFHE.Encrypt $(pk, \mu)$ : Takes as input a public key and a message  $\mu \in \{0, 1\}$  and outputs a ciphertext ct.
- $\hat{\mathsf{ct}} \leftarrow \mathsf{TFHE}.\mathsf{Eval}(C, \mathsf{ct}_1, ..., \mathsf{ct}_k)$ : Takes as input a circuit C of depth at most d and k ciphertexts  $\mathsf{ct}_1, ..., \mathsf{ct}_k$ . Outputs a ciphertext  $\hat{\mathsf{ct}} = C(\mathsf{ct}_1, ..., \mathsf{ct}_k)$ .
- $p_i \leftarrow \text{TFHE.PartDec}(\text{ct}, sk_i)$ : Takes as input a ciphertext ct and a secret key  $sk_i$  and outputs a partial decryption  $p_i$ .

•  $\hat{\mu} \leftarrow \text{TFHE.FinDec}(B)$ : Takes as input a set  $B = \{p_i\}_{i \in S}$  for some  $S \subseteq [N]$  and deterministically outputs a message  $\hat{\mu} \in \{0, 1, \bot\}$ .

Further we remember the definitions of evaluation correctness and simulation security as outlined in, [BEHG20].

**Definition 2.2** (Evaluation Correctness [JRS17]). We have that TFHE scheme is correct if for all  $\lambda$ , depth bounds d, access structure  $\mathbb{A}$ , circuit  $C: \{0,1\}^k \to \{0,1\}$  of depth at most d,  $S \in \mathbb{A}$ , and  $\mu_i \in \{0,1\}$ , we have the following. For  $(pk, sk_1, ..., sk_N) \leftarrow \text{TFHE.Setup}(1^{\lambda}, 1^d, \mathbb{A})$ ,  $\text{ct}_i \leftarrow \text{TFHE.Encrypt}(pk, \mu_i)$  for  $i \in [k]$ ,  $\hat{\text{ct}} \leftarrow \text{TFHE.Eval}(pk, C, \text{ct}_1, ..., \text{ct}_k)$ ,

$$\mathbf{Pr}\left[\mathtt{TFHE.FinDec}(pk, \{\,\mathtt{TFHE.PartDec}(pk, \hat{\mathtt{ct}}, sk_i)\,\}_{i \in S}) = C(\mu_1, ..., \mu_k)\right] = 1 - \mathtt{negl}(\lambda).$$

**Definition 2.3** (Semantic Security [JRS17]). We have that a TFHE scheme satisfies semantic security for for all  $\lambda$ , and depth bound d if the following holds. There is a stateful PPT algorithm  $S = (S_1, S_2)$  such that for any PPT adversary A, the following experiment outputs 1 with negligible probability in  $\lambda$ :

- 1. On input  $1^{\lambda}$  and depth  $1^{d}$ , the adversary outputs  $\mathbb{A} \in \mathbb{S}$
- 2. The challenger runs  $(pk, sk_1, ..., sk_N) \leftarrow \texttt{TFHE.Setup}(1^{\lambda}, 1^d, \mathbb{A})$  and provides pk to A.
- 3. A outputs a set  $S \subseteq \{P_1, ..., P_N\}$  such that  $S \notin A$ .
- 4. The challenger provides  $\{sk_i\}_{i\in S}$  and TFHE.Encrypt $(pk,\mu)$  to  $\mathcal A$  where  $\mu \stackrel{\$}{\leftarrow} \{0,1\}$ .
- 5. A outputs a guess  $\mu'$ . The experiment outputs 1 if  $\mu' = \mu$ .

**Definition 2.4** (Simulation Security [JRS17]). We say that a TFHE scheme is simulation secure if for all  $\lambda$ , depth bound d, and access structure  $\mathbb{A}$  if there exists a stateful PPT simulator,  $\mathcal{S}$ , such that for any PPT adversary  $\mathcal{A}$ , we have that the experiments  $\mathsf{Expt}_{\mathcal{A},\mathsf{Real}}(1^{\lambda},1^{d})$  and  $\mathsf{Expt}_{\mathcal{A},\mathsf{Sim}}(1^{\lambda},1^{d})$  are statistically close as a function of  $\lambda$ . The experiments are defined as follows:

- $\text{Expt}_{\mathcal{A}, \text{Real}}(1^{\lambda}, 1^d)$ :
  - 1. On input the security parameter  $1^{\lambda}$  and depth bound d, the adversary outputs  $\mathbb{A} \in \mathbb{S}$ .
  - 2. Run TFHE.Setup $(1^{\lambda}, 1^d, \mathbb{A})$  to obtain  $(pk, sk_1, ..., sk_N)$ . The adversary is given pk.
  - 3. The adversary outputs a set  $S \subseteq \{P_1, ..., P_N\}$  such that  $S \notin \mathbb{A}$  together with plaintest messages  $\mu_1, ..., \mu_k \in \{0, 1\}$ . The adversary is handed over  $\{sk_i\}_{i \in S}$
  - 4. For each  $\mu_i$ , the adversary is given TFHE. Encrypt $(pk, \mu_i) \to \mathsf{ct}_i$ .
  - 5. The adversary issues a polynomial number of queries,  $(S_i \subseteq \{P_1, ..., P_N\}, C_i)$ . for circuites  $C_i : \{0,1\}^k \to \{0,1\}$ . After each query the adversary receives for  $l \in S_i$  the value

TFHE.PartDec(TFHE.Eval
$$(C_i, \mathsf{ct}_1, ..., \mathsf{ct}_k), sk_l) \to p_l$$

- 6.  $\mathcal{A}$  outputs out, the experiment's output.
- $\operatorname{Expt}_{\mathcal{A}.\operatorname{Sim}}(1^{\lambda},1^{d})$ :
  - 1. On input the security parameter  $1^{\lambda}$  and depth bound d, the adversary outputs  $\mathbb{A} \in \mathbb{S}$ .
  - 2. Run TFHE.Setup $(1^{\lambda}, 1^d, \mathbb{A})$  to obtain  $(pk, sk_1, ..., sk_N)$ . The adversary is given pk.

- 3.  $\mathcal{A}$  outputs a set  $S^* \subseteq \{P_1, ..., P_N\}$  such that  $S \notin \mathbb{A}$  and plaintexts  $\mu_1, ..., \mu_k \in \{0, 1\}$ . The simulator is given  $pk, \mathbb{A}, S^*$  as input and outputs  $\{sk_i\}_{i \in S^*}$  and the state state. The adversary is given  $\{sk_i\}_{i \in S^*}$
- 4. For each  $\mu_i$ , the adversay is given TFHE.Encrypt $(pk, \mu_i) \to \mathsf{ct}_i$ .
- 5.  $\mathcal{A}$  issues a polynomial number of queries of the form  $(S_i \subseteq \{P_1, ..., P_N\}, C_i)$
- 6. for circuits  $C_i: \{0,1\}^k \to \{0,1\}$ . After each query, the simulator computes

$$\mathtt{Sim}_{\mathtt{TFHE}}(C_i, \{\mathtt{ct}_l\}_{l=1}^k, C_i(\mu_1, ..., \mu_k), \mathtt{state}) \rightarrow \{p_l\}_{l \in S_i}$$

and sends  $\{p_l\}_{l \in S_i}$  to the adversary.

7.  $\mathcal{A}$  outputs out, the experiment's output.

## 2.2 Data Independent Priority Queue

In this work, we will use data independent queues as studied in [Tof11, MZ14, MDPB23]. Data independent data structures are unique as their control flow and memory access do not depend on input data ([MZ14]).

**Definition 2.5** (Word RAM model [MZ14]). In the word RAM model, the RAM has a constant number of public and secret registers and can perform arbitrary operations on a constant number of registers in constant time.

**Definition 2.6** (Data Independent Data Structure [MZ14]). In the word RAM model, a data independent data structure is a collection of algorithms where all the algorithms uses RAM such that the RAM can only set its control flow based on registers that are public.

Data independent queues are especially useful as they allow for efficient computation within MPC and FHE as control flow is not dependent on underlying ciphertexts data. We use a data independent queue as outlined in [MDPB23] which allows for

- PQ. Insert: Inserts a tag and value, (p, x) into PQ according to the tag's priority.
- PQ.ExtractFront: Removes and returns the (p, y) with highest tag priority.
- PQ.Front: Returns the (p, y) with highest tag priority without removing the element.

Moreover, we note that the order is stable. I.e. the first inserted among equal tagged elements has a higher priority.

## 2.3 Resevoir Sampling

Resevoir sampling is an online algorithm which allows for randomly selecting k elements from a stream of n elements while using  $\tilde{O}(k)$  space. Algorithm R ([Vit85]) is a simple algorithm which relies on a priority queue with interface:

- Resevoir.Init(k) initialize the resevoir sampling algorithm and data structure
- Resevoir.Insert( $\mu_i, e_i, \text{coin}_i$ ) where  $\mu_i$  is *i*-th item,  $e_i$  is independentally sampled randomness, and  $\text{coin}_i$  is a random coin with probability 1/m of equaling 1.
  - If  $i \leq k$ , insert the item into the queue along with  $e_i$  as its tag via PQ.Insert $(e_i, \mu_i)$ .

- If i > k and  $coin_i = 1$ , replace the smallest labeled item in the queue with the new item if the coin is 1.
- If i > k and  $coin_i = 0$ , do nothing.
- $\mu_{a_1}, \mu_{a_2}, ..., \mu_{a_k} \leftarrow \texttt{Resevoir.Output}()$  where  $a_1, ..., a_k$  are a uniformly random ordered susb-set of [n]
  - Call PQ.ExtractFront k times setting  $\mu_{a_{\ell}}$  to the  $\ell$ -th call to PQ.ExtractFront where  $\ell \in [k]$ .

## 3 TFHE MSLE Protocol

We use a similar notion of ideal functionality for a multi-secret leader election from the ideal functionality of single secret leader election of [CFG22] except that we add a register\_elect phase for each election.

The MSLE functionality  $\mathcal{F}_{\text{MSLE}}$ : Initialize  $E, R \leftarrow \emptyset, b \leftarrow 0$ . Initialize S to denote the set of sets of active participants in each round. Set  $\mathcal{E} \leftarrow \emptyset$  to denote the set of finished elections. Fix some  $k \in \mathbb{N}$  to denote the number of rounds. Upon receiving,

- register from party  $P_i$ , set  $R \leftarrow R \cup \{(i,n)\}$ , broadcast (register, i) to all parties and set  $b \leftarrow b+1$
- register\_elect(eid, w) from party  $P_i$ . If  $eid \in \mathcal{E}$  send  $\bot$  to  $P_i$  and do nothing. If  $(i, w) \notin R$  or  $(i, w) \in S_{eid}$ , send  $\bot$  to  $P_i$  and do nothing. If  $S_{eid}$  is not defined, set  $S_{eid} \leftarrow \{(i, w)\}$ . Otherwise, set  $S_{eid} \leftarrow S_{eid} \cup \{(i, w)\}$ .
- elect(eid) Elect k leaders from  $S_{eid} \subseteq R$  parties. If  $|S| \ge k$  and  $eid \notin \mathcal{E}$ , randomly sample  $W^{eid} \subseteq S_{eid}$  where  $|W^{eid}| = k$ . Then, assign a random ordering to  $W^{eid}$  to get ordered set  $E^{eid}$ . Next, send (outcome, eid, a) to  $P_j$  for all  $E_a^{eid} = (j, \cdot)$  and (outcome, eid,  $\bot$ ) to  $P_i$  if  $(i, \cdot) \notin E^{eid}$ . Store  $E \leftarrow E \bigcup \{E^{eid}\}$ . Set  $\mathcal{E} \leftarrow \mathcal{E} \cup \{eid\}$ .
- reveal from  $P_i$ : for  $E_{eid} \in E$ , if  $i = E_{\ell}^{eid}$ , broadcast (result, eid,  $\ell$ , i). Otherwise, broadcast (rejected, eid,  $\ell$ , i).

Figure 1: Description of the Multi Secret Leader Election functionality

## 3.1 Semi Honest Simulation Security

We can show semi-honest simulation security by showing that the view of each party i in the real protocol can be simulated throughout the course of one election and then that this simulation can be extended for a polynomial number of elections.

We will now show that  $Sim_i$  is indeed a simulator for the view of  $\pi_{MSLE}$  for register\_elect, elect, and reveal.

**Lemma 3.1** (register\_elect is simulation secure). *Proof.* The simulator gets as input party i's secret value,  $s_i$ , party i's TFHE share  $sk_i$ , eid, and ticket number w. We note that if  $eid \in \mathcal{E}$  or  $(i, w) \notin R$ , then the simulator can simply output  $\bot$  and is identical to the real protocol. Otherwise,

The MSLE Protocol  $\pi_{\text{MSLE}}$ : Initialize b = 0. Fix some  $k \in \mathbb{N}$  to denote the number of rounds. Initialize an empty set of tickets, R. Initialize an empty lookup of sets of parties in each election, S. Initialize an empty lookup of reservoir sampling data structures  $\mathcal{R}$  and a set of finished elections  $\mathcal{E}$  Initialize an empty lookup of election results, E.

Initialize  $S \leftarrow \emptyset$  to denote the set of sets of active participants in each round.

#### • initialize

- Set n=0
- Sample a random TFHE secret key, public key pair sk, pk and publish pk.
- Sample some secret  $s_{\text{TFHE}}$  and publish  $\text{Enc}_{\text{TFHE}}(s_{\text{TFHE}})$ . This will be the key to the PRF
- register from party  $P_i$ 
  - If party  $P_i$  does not already have a TFHE share, create a TFHE share,  $sk_i$ , for  $P_i$  and send the share over a secure channel to  $P_i$ .
  - $-R \leftarrow R \cup \{(i,b)\}, \text{ set } b \leftarrow b+1.$
- register\_elect(eid, Enc<sub>TFHE</sub>( $c_i$ ), w) from party  $P_i$  where  $c_i = \text{comm}(s_i)$  for a randomly sampled secret  $s_i$ .
  - If  $eid \in \mathcal{E}$ , then send  $\perp$  to  $P_i$  and do nothing.
  - If  $(i, w) \in S_{eid}$  or  $(i, w) \notin R$ , send  $\perp$  and do nothing.
  - Otherwise, if  $\mathcal{R}_{eid} \notin \mathcal{R}$ ,  $\mathcal{R}_{eid} \leftarrow \texttt{Resevoir.Init}(k)$
  - The CRS will be used to run a PRF to get  $Enc_{TFHE}(e_i), Enc_{TFHE}(coin_i) = Enc_{TFHE}(PRF(c_i, s_{TFHE}))$  for  $i \in S$
  - $\text{Enc}_{\text{TFHE}}(c_i)$  will be fed to the encrypted streaming sampler along with randomness via  $\text{Resevoir}^{eid}$ .  $\text{Insert}(\text{Enc}_{\text{TFHE}}(c_i), \text{Enc}_{\text{TFHE}}(e_i), \text{Enc}_{\text{TFHE}}(\text{coin}_i))$ .

#### • elect(eid)

- If  $eid \in \mathcal{E}$ , then return  $\perp$  and do nothing.
- The encrypted streaming sampler will output a list of k messages via calling Resevoir<sup>eid</sup>.Output() k times:  $\operatorname{Enc}_{\mathrm{TFHE}}(c_{a_1}), \operatorname{Enc}_{\mathrm{TFHE}}(c_{a_2}), ..., \operatorname{Enc}_{\mathrm{TFHE}}(c_{a_k})$ .
- Then, at least t parties will submit decryption shares,  $p_i = \text{TFHE.PartDec}(\text{Enc}_{\text{TFHE}}(c_{a_1}),...,\text{Enc}_{\text{TFHE}}(c_{a_2}))$  to get  $c_{a_1},...,c_{a_k} = \text{TFHE.FinDec}(\{p_i\})$ .
- Add  $E_{eid} = \{c_{a_1}, ..., c_{a_k}\}$  to E.
- reveal $(eid, \ell, \texttt{Enc}_{\texttt{TFHE}}(c_i'))$  from  $P_i$ 
  - $P_i$  submits a proof that they know the opening to  $c_{a_\ell}$ . If this proof verifies, send out (result, eid,  $\ell$ , i) to all parties. Otherwise, send out (rejected, eid,  $\ell$ , i) to all parties.

Figure 2: Description of the MSLE protocol

Simulator for Threshold MSLE  $Sim_i$ : Initialize b = 0. Fix some  $k \in \mathbb{N}$  to denote the number of rounds. Initialize an empty set of tickets, R, an empty lookup of sets of parties in each election, S, a set of finished elections  $\mathcal{E}$ , an empty lookup of election results, E, and a set  $S \leftarrow \emptyset$  to denote the set of sets of active participants in each round. Moreover, set a random tape for the simulator. The simulator knows, input for party  $P_i$ ,  $sk_i$  and  $s_i$ .

- register from party  $P_j$ 
  - $-R \leftarrow R \cup \{(i,b)\}, \text{ set } b \leftarrow b+1.$
  - Simulate the secure channel communication with party  $P_j$  if  $i \neq j$ .
  - Run register honestly if i = j by sending  $sk_i$  to  $P_i$
- register\_elect( $eid, w, s_i, sk_i$ ) from party  $P_j$ .
  - If  $j \neq i$ , the simulator samples a random value  $s'_j$  and follows the protocol directly using  $s'_{\text{TFHE}}$  and  $\text{Enc}_{\text{TFHE}}(c'_j)$  where  $c'_j = \text{comm}(s'_j)$ . Store  $c'_j$  in a lookup table as well as its committed message.
  - If j = i, the simulator will use the commitment  $c_i = \text{comm}(s_i)$ . And run register\_elect as is in the protocol
- elect(eid, out,  $s_i$ ,  $sk_i$ ) where the out is output  $\bot$  or (outcome, eid, q)<sub>i</sub> for all  $i \in [n]$  where  $q \in \{1, ..., k, \bot\}$ .
  - Let  $\overline{n}$  be the total number of successful calls to  $register\_elect(eid,.,.)$  before the election for eid
  - If the output is  $\perp$ , return  $\perp$ .
  - Let  $a_1, ..., a_k$  be the ordered set of parties that won the election. I.e. if  $q_i = \ell$  then  $a_\ell = i$ .
  - The simulator then gives  $\operatorname{Sim}_{\mathsf{TFHE}}(C, \{\operatorname{Enc}_{\mathsf{TFHE}}(c'_j)\}_{j \in [\overline{n}]}, c'_1, ..., c'_{a_\ell}, S, \mathsf{st})$  to the TFHE simulator to get a list of partial decryptions,  $p_1, ..., p_t$  where S is a qualified set and C is the reservoir sampling circuit with PRF seed  $s_{\mathsf{TFHE}}$  hardcoded. Note that this sets the decryption of the output of the TFHE circuit sampling to  $c'_{a_\ell}$  for  $\ell \in [k]$ .
  - Add  $E_{eid} = \{c'_{a_1}, ..., c'_{a_k}\}$  to E.
- reveal $(eid, \ell, \texttt{Enc}_{\texttt{TFHE}}(c'_j))$  from  $P_j$  and output  $\bot$  or  $(\texttt{result}, eid, \ell, j)$ .
  - As the simulator has knowledge of the openings to all of the commitments  $c'_j$  used, the simulator to honestly run  $\mathtt{reveal}(eid, \ell, \mathtt{Enc}_{\mathsf{TFHE}}(c'_j))$  with commitment  $c'_j$  and opening  $s'_j$ .
  - Note that in the semi-honest setting, the output is never  $\perp$

Figure 3: Description of the MSLE protocol

if party  $P_i$  calls register\_elect, then the simulator knows the input of  $P_i$  and can simulate the protocol honestly. If party  $P_j$  call register\_elect for some  $j \neq i$ , then the view of the protocol is that of

 $(\mathtt{Enc}_{\mathtt{TFHE}}(c_i),\mathtt{Enc}_{\mathtt{TFHE}}(e_i,\mathtt{coin}_i),\mathtt{Resevoir}^{eid}.\mathtt{Insert}(\mathtt{Enc}_{\mathtt{TFHE}}(c_j,e_i,\mathtt{coin}_i))).$ 

Note that this view is completely determined by  $\operatorname{Enc}_{\mathrm{TFHE}}(c_j)$ . Also, note that  $c_j$  is drawn from a random distribution and is not in the view of the real protocol. Thus, by semantic security of TFHE (definition 2.3) we have that  $\operatorname{Enc}_{\mathrm{TFHE}}(c_j) \stackrel{\mathrm{C}}{\equiv} \operatorname{Enc}_{\mathrm{TFHE}}(c_j')$  where  $c_j'$  is a commitment to a random value.

**Lemma 3.2** (elect is simulation secure). *Proof.* If the view of the real protocol is  $\bot$  because eid was already called, then the simulator can simply output  $\bot$  and is thus identical to the real protocol. Otherwise, note that the simulator needs to "fix" the output of elect to yield a list of commitments such that, if  $a_{\ell} = j$  if party j wins election  $\ell$ . Thus, the TFHE simulator can simply output the decryption shares,  $p_1, ...p_t$  using  $\mathtt{Sim}_{\mathsf{TFHE}}(C, \{\mathtt{Enc}_{\mathsf{TFHE}}c'_j\}_{j \in [\overline{n}]}, c'_1, ..., c'_{a_{\ell}}, S, \mathsf{st})$ . Note that the reservoir sampling circuit is indeed simulated by  $\mathtt{Sim}_{\mathsf{TFHE}}$  and the decryption shares are simulated as well such that the cipher texts decrypt to  $c'_{a_1}, ..., c'_{a_k} \stackrel{\mathtt{C}}{=} c_{a_1}, ..., c_{a_k}$  by lemma 3.1.

**Lemma 3.3** (reveal is simulation secure). *Proof.* Note that the simulator can simply run reveal honestly as the simulator has knowledge of the openings to all of the commitments  $c'_j$  used and thus has an identical view to that of the real protocol.

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