

```
terms=[5 10 20 40 80 160 320 640]
```

```
terms =  
      5      10      20      40      80     160     320     640
```

```
domain=cell(1,length(terms))
```

```
domain = 1x8 cell array  
      []      []      []      []      []      []      []      []
```

```
parfor i=1:length(terms)  
    domain(i)={rectangularPulse(-1:2/terms(i):1-2/terms(i))}  
end  
syms k  
transform=[]
```

```
transform =  
  
      []
```

```
parfor i=1:length(domain)  
    transform=[transform custom_fft(cell2mat(domain(i)),k)]  
end
```

```
range =  
  
      []
```

```
transform_ =  
exp(-3*pi*(k - 1))/2 + exp(-9*pi*(k - 1)) + exp(-11*pi*(k - 1)) + exp(-21*pi*(k - 1)) + exp(-24*pi*(k - 1))
```

```
range =  
  
      []
```

```
transform_ =  
exp(-4*pi*(k - 1)) + exp(-6*pi*(k - 1)) + exp(-(12*pi*(k - 1))/5) + exp(-(42*pi*(k - 1))/5) + exp(-(56*pi*(k - 1))/5)
```

```
range =  
  
      []
```

```
transform_ =  
exp(-(12*pi*(k - 1))/5) + exp(-(24*pi*(k - 1))/5)
```

```
range =  
  
      []
```

```
transform_ =
```

```

exp(-(41*pi*(k - 1))/2)/2 + exp(-52*pi*(k - 1)) + exp(-79*pi*(k - 1)) + exp(-(77*pi*(k - 1))/2) + exp(-8

range =

    []

transform_ =

exp(-15*pi*(k - 1)) + exp(-(21*pi*(k - 1))/2)/2 + exp(-39*pi*(k - 1)) + exp(-41*pi*(k - 1)) + exp(-(63*pi*(k - 1))/2)

range =

    []

transform_ =

exp(-12*pi*(k - 1)) + exp(-(11*pi*(k - 1))/2)/2 + exp(-19*pi*(k - 1)) + exp(-21*pi*(k - 1)) + exp(-(21*pi*(k - 1))/2)

range =

    []

transform_ =

exp(2967928573486663/2748779069440 - (2967928573486663*k)/2748779069440) + exp(2917518584622569/2748779069440)

range =

    []

transform_ =

    :

```

```

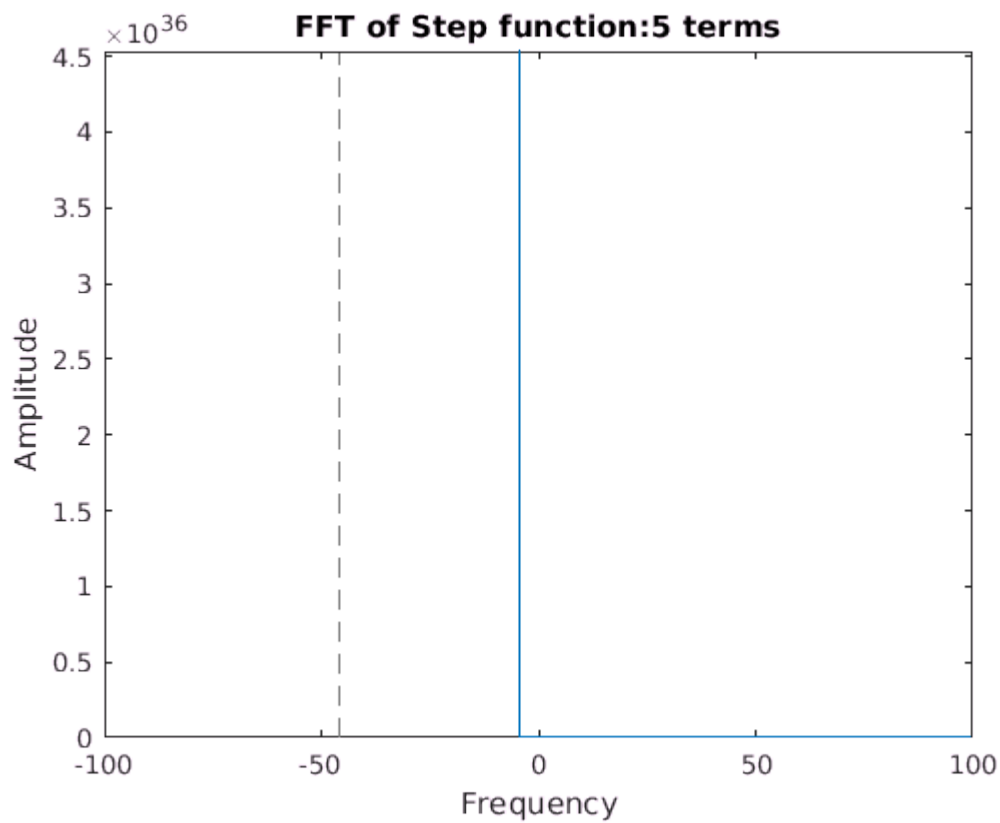
parfor i=1:length(transform)
    figure;fplot(transform(i),[-100,100])
end

```

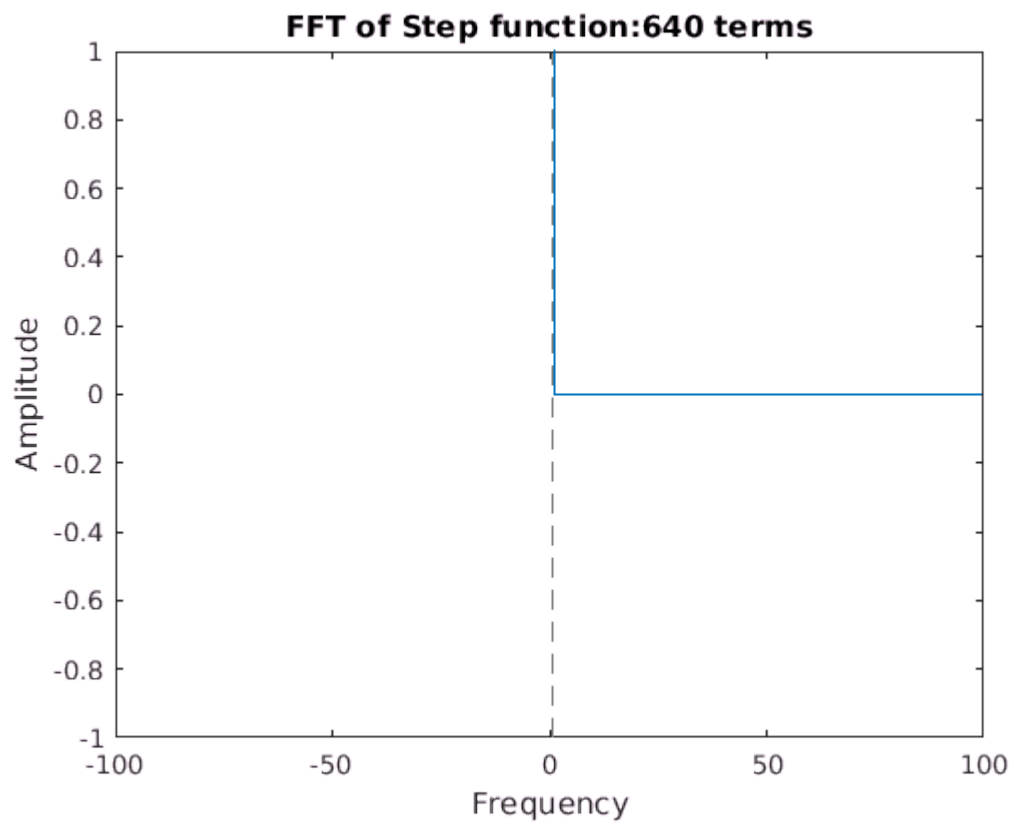
```

fig=figure;

```



```
filename='animation.gif';
for i=1:length(transform)
    fplot(transform(i),[-100,100]);
    title(strcat('FFT of Step function:',string(terms(i)),' terms'));
    xlabel('Frequency');
    ylabel('Amplitude');
    drawnow;
    frame=getframe(fig);
    im=frame2im(frame);
    [imidx,cm]=rgb2ind(im,256);
    if i==1
        imwrite(imidx,cm,filename,'gif','Loopcount',inf);
    else
        imwrite(imidx,cm,filename,'gif','WriteMode','append');
    end
end
```



```
function transform_ = custom_fft(domain_,k_)
```

$$\text{transform_} = \sum_{j=1}^{\text{length}(\text{domain_})} \text{domain_}(j) \exp \frac{-2\pi i (j-1)(k_- - 1)}{\text{length}(\text{domain_})}$$

```
range=[]
parfor i=1:length(domain_)
    range=[range domain_(i)*exp(-2*pi*i*(i-1)*(k_-1)/length(domain_))]
end
transform_=sum(range)
end
```