

Mental Math Techniques

Fast Arithmetic for Trading Interviews

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1 Multiplication Techniques

1. Two-digit \times two-digit: Decompose intelligently

General formula: $(a + b)(c + d) = ac + ad + bc + bd$

But choose b and d to be easy (typically multiples of 10).

Example: 47×63

Rewrite as $47 \times (70 - 7)$:

$$\begin{aligned} 47 \times 70 &= 3290 \\ 47 \times 7 &= 329 \\ 47 \times 63 &= 3290 - 329 = \boxed{2961} \end{aligned}$$

Example: 38×24

Rewrite as $(40 - 2) \times 24$:

$$\begin{aligned} 40 \times 24 &= 960 \\ 2 \times 24 &= 48 \\ 38 \times 24 &= 960 - 48 = \boxed{912} \end{aligned}$$

Example: 56×17

Rewrite as $56 \times (20 - 3)$:

$$\begin{aligned} 56 \times 20 &= 1120 \\ 56 \times 3 &= 168 \\ 56 \times 17 &= 1120 - 168 = \boxed{952} \end{aligned}$$

2. Numbers near 100

Formula: $(100 - x)(100 - y) = 10000 - 100(x + y) + xy$

This is extremely fast because you only work with small numbers x and y .

Example: 97×94

Here $x = 3$, $y = 6$:

$$\begin{aligned} 10000 - 100(3 + 6) + 3 \times 6 &= 10000 - 900 + 18 \\ &= \boxed{9118} \end{aligned}$$

Example: 98×96

Here $x = 2$, $y = 4$:

$$\begin{aligned}10000 - 100(2 + 4) + 2 \times 4 &= 10000 - 600 + 8 \\&= \boxed{9408}\end{aligned}$$

Example: 93×91

Here $x = 7$, $y = 9$:

$$\begin{aligned}10000 - 100(7 + 9) + 7 \times 9 &= 10000 - 1600 + 63 \\&= \boxed{8463}\end{aligned}$$

3. Numbers near 50

Formula: $(50 + x)(50 + y) = 2500 + 50(x + y) + xy$

Example: 53×47

Here $x = 3$, $y = -3$:

$$\begin{aligned}2500 + 50(3 - 3) + 3 \times (-3) &= 2500 + 0 - 9 \\&= \boxed{2491}\end{aligned}$$

Example: 56×54

Here $x = 6$, $y = 4$:

$$\begin{aligned}2500 + 50(6 + 4) + 6 \times 4 &= 2500 + 500 + 24 \\&= \boxed{3024}\end{aligned}$$

Example: 48×52

Here $x = -2$, $y = 2$:

$$\begin{aligned}2500 + 50(-2 + 2) + (-2) \times 2 &= 2500 + 0 - 4 \\&= \boxed{2496}\end{aligned}$$

4. Squaring numbers ending in 5

Formula: $(10a + 5)^2 = 100a(a + 1) + 25$

This is blazing fast.

Example: 35^2

Here $a = 3$:

$$100 \times 3 \times 4 + 25 = 1200 + 25 = \boxed{1225}$$

Example: 65^2

Here $a = 6$:

$$100 \times 6 \times 7 + 25 = 4200 + 25 = \boxed{4225}$$

Example: 85^2

Here $a = 8$:

$$100 \times 8 \times 9 + 25 = 7200 + 25 = \boxed{7225}$$

Example: 125^2

Here $a = 12$:

$$100 \times 12 \times 13 + 25 = 15600 + 25 = \boxed{15625}$$

5. Multiply by 11

Pattern: $\overline{ab} \times 11 = \overline{a(a+b)b}$ (carry if $a+b \geq 10$)

Example: 53×11

Middle digit: $5+3=8$

$$53 \times 11 = \boxed{583}$$

Example: 67×11

Middle digit: $6+7=13$ (carry 1)

$$67 \times 11 = (6+1)37 = \boxed{737}$$

Example: 84×11

Middle digit: $8+4=12$ (carry 1)

$$84 \times 11 = (8+1)24 = \boxed{924}$$

Three-digit: $\overline{abc} \times 11 = \overline{a(a+b)(b+c)c}$

Example: 234×11

$$234 \times 11 = 2(2+3)(3+4)4 = 2574$$

But $3+4=7$, so: $\boxed{2574}$

Example: 578×11

Digits: 5, $(5+7)=12$ (carry), $(7+8)=15$ (carry), 8

$$578 \times 11 = 5(12)(15)8 \rightarrow 5(13)58 \rightarrow 6358 = \boxed{6358}$$

6. Multiply by 5, 25, 125

Multiply by 5: $\times 10 \div 2$

Example: $87 \times 5 = 870 \div 2 = \boxed{435}$

Example: $124 \times 5 = 1240 \div 2 = \boxed{620}$

Multiply by 25: $\times 100 \div 4$

Example: $36 \times 25 = 3600 \div 4 = \boxed{900}$

Example: $84 \times 25 = 8400 \div 4 = \boxed{2100}$

Multiply by 125: $\times 1000 \div 8$

Example: $16 \times 125 = 16000 \div 8 = \boxed{2000}$

Example: $72 \times 125 = 72000 \div 8 = \boxed{9000}$

7. Divide by 5, 25

Divide by 5: $\times 2 \div 10$

This is huge! Dividing by 5 is hard; multiplying by 2 is trivial.

Example: $347 \div 5 = 694 \div 10 = \boxed{69.4}$

Example: $825 \div 5 = 1650 \div 10 = \boxed{165}$

Divide by 25: $\times 4 \div 100$

Example: $675 \div 25 = 2700 \div 100 = \boxed{27}$

Example: $1250 \div 25 = 5000 \div 100 = \boxed{50}$

8. Approximation + correction

Strategy: Compute via an easy nearby number, then adjust.

This is safer than direct multiplication under pressure.

Example: 79×46

Use 80×46 :

$$80 \times 46 = 3680$$

$$\text{subtract 46: } 79 \times 46 = 3680 - 46 = \boxed{3634}$$

Example: 68×29

Use 68×30 :

$$68 \times 30 = 2040$$

$$\text{subtract 68: } 68 \times 29 = 2040 - 68 = \boxed{1972}$$

Example: 103×52

Use 100×52 :

$$100 \times 52 = 5200$$

add 3×52 : $103 \times 52 = 5200 + 156 = \boxed{5356}$

2 Subtraction: Difference Method

Never borrow! Instead, count up from the smaller number to the larger.

Example: $10000 - 5873$

Ask: $5873 + ? = 10000$

Count up:

$$\begin{aligned} 5873 &\rightarrow 6000 \quad (+127) \\ 6000 &\rightarrow 10000 \quad (+4000) \\ \text{Total: } &\boxed{4127} \end{aligned}$$

Example: $8000 - 3456$

Count up:

$$\begin{aligned} 3456 &\rightarrow 3500 \quad (+44) \\ 3500 &\rightarrow 8000 \quad (+4500) \\ \text{Total: } &\boxed{4544} \end{aligned}$$

Example: $5000 - 2738$

Count up:

$$\begin{aligned} 2738 &\rightarrow 2800 \quad (+62) \\ 2800 &\rightarrow 5000 \quad (+2200) \\ \text{Total: } &\boxed{2262} \end{aligned}$$

Example: $1000 - 647$

Count up:

$$\begin{aligned} 647 &\rightarrow 650 \quad (+3) \\ 650 &\rightarrow 1000 \quad (+350) \\ \text{Total: } &\boxed{353} \end{aligned}$$

This is **faster and more accurate** under pressure than borrowing.

3 Addition: Chunking Strategy

Always scan for complements to 10, 100, 1000 before adding left-to-right.

Example: $487 + 596 + 213 + 404$

Pair to 1000s:

$$\begin{aligned}(487 + 513) &= 1000 \quad \text{but we have 596, so:} \\ 487 + 596 &= 1083 \\ 213 + 404 &= 617 \\ \text{Total: } 1083 + 617 &= \boxed{1700}\end{aligned}$$

Better approach:

$$\begin{aligned}(596 + 404) &= 1000 \\ (487 + 213) &= 700 \\ \text{Total: } &= \boxed{1700}\end{aligned}$$

Example: $38 + 67 + 62 + 33$

Pair to 100:

$$\begin{aligned}(38 + 62) &= 100 \\ (67 + 33) &= 100 \\ \text{Total: } &= \boxed{200}\end{aligned}$$

Example: $145 + 387 + 255 + 613$

Pair smartly:

$$\begin{aligned}(145 + 255) &= 400 \\ (387 + 613) &= 1000 \\ \text{Total: } &= \boxed{1400}\end{aligned}$$

Example: $19 + 47 + 81 + 53$

Pair to even 100s:

$$\begin{aligned}(19 + 81) &= 100 \\ (47 + 53) &= 100 \\ \text{Total: } &= \boxed{200}\end{aligned}$$

4 Powers and Roots

Powers of 2 (memorize these!)

| Power | Value |
|----------|------------------------|
| 2^5 | 32 |
| 2^6 | 64 |
| 2^7 | 128 |
| 2^8 | 256 |
| 2^9 | 512 |
| 2^{10} | 1024 |
| 2^{11} | 2048 |
| 2^{12} | 4096 |
| 2^{15} | 32768 |
| 2^{16} | 65536 |
| 2^{20} | $1048576 \approx 10^6$ |

Square roots via Newton's method (one iteration)

Formula: $\sqrt{n} \approx \frac{1}{2} \left(x + \frac{n}{x} \right)$ where x is initial guess

Example: $\sqrt{50}$

Guess $x = 7$ (since $7^2 = 49$):

$$\sqrt{50} \approx \frac{1}{2} \left(7 + \frac{50}{7} \right) = \frac{1}{2}(7 + 7.14) = \boxed{7.07}$$

True value: 7.071...

Example: $\sqrt{80}$

Guess $x = 9$ (since $9^2 = 81$):

$$\sqrt{80} \approx \frac{1}{2} \left(9 + \frac{80}{9} \right) = \frac{1}{2}(9 + 8.89) = \boxed{8.94}$$

True value: 8.944...