R Workshop 4

July 12, 2017

Review from Workshop 3

Continuous Random Variables

We squeezed in continous random variables just before running out of time in the last workshop. Let's summarize some of the concepts.

Calculus provides us a convenient two-way relationship between the CDF and the density function for a random variable.

$$f_X(x) = \frac{dF_X}{dx}$$

$$F_X(b) - F_X(a) = \int_a^b f_X(x)dx$$

Expectation is the natural analog to summation for discrete random variables.

$$E[X] = \int_{-\infty}^{\infty} x f_X(x) dx$$

Finally, the moment generating function is also analogous to the discrete case.

$$m_X(t) = E[e^{xt}] = \int_{-\infty}^{\infty} e^{xt} f_X(x) dx$$

Normal Random Variables

The granddaddy of all the distributions is the *normal distribution*. It is also known as the *Gaussian distribution*. It has the symmetric "bell-shape" that most people recognize. It has two parameters.

- \bullet μ the mean of the distribution
- σ^2 the variance of the distribution

The probability density function is

$$f_X(x;\mu,\sigma^2) = \frac{1}{\sqrt{2\pi}\sigma} e^{\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2} \ x \in (-\infty,\infty)$$

Sometimes a normal random variable with mean μ and variance σ^2 is written $\mathcal{N}(\mu, \sigma^2)$. The "standard normal" is $\mathcal{N}(0, 1)$.

The first thing different about this distribution than past ones we've discussed is that it is a *continuous* distribution. Its domain is not a countable discrete set. In the case of the normal distribution, the domain is the entire real number line.

You might think that with parameter names like "mean" and "variance" you would be off the hook to verify what they are. Alas, here are some verifications for you to make during your boring meetings over the next two weeks.

- 1. Show the area under f_X is 1 with $\mu=0$ and $\sigma=1$. The integral is not obvious. The trick is to compute its square: $\int_0^\infty f_X(x)dx \int_0^\infty f_X(y)dy$. Convert the x and y to polar coordinates r and θ and integrate in two dimensions.
- 2. Show that the moment generating function for $\mathcal{N}(\mu, \sigma^2)$ is $\exp\left[t\mu + \left(\frac{t\sigma}{2}\right)^2\right]$. The trick is completing the square in the exponent.
- 3. Use the moment generating function for $\mathcal{N}(\mu, \sigma^2)$ to verify the mean and variance.

The moment generating function for $\mathcal{N}(\mu, \sigma^2)$ comes in handy for more than simply calculating moments. We'll refer back to this when determining if a function of random variables is normal through comparing the moment generating functions.

Dates and Times

In this section we'll address several classes and functions that address dates and times.

Date

Dates are represented by the **Date** class. Internally, it's the number of days since January 1, 1970. Create an instance of Date with the as.Date() function.

```
In [13]: x <- as.Date('2017-03-15')
x
2017-03-15
```

The second parameter allows you to specify a different date format.

```
In [14]: as.Date(c('3/15/17', '2/21/17'), '%m/%d/%y')
as.Date('20170315', '%Y%m%d')
as.Date('March 15, 2017', '%B %d, %Y')

2017-03-15
2017-03-15
```

In the examples above, we see that the format string uses a percent sign to indicate a special field.

- %d day of the month
- %m number of the month
- %y two digit year
- %Y four digit year
- %B full name of the month (in English).

A full list of the abbreviations can be found from the R help for the strptime function which we'll be covering below.

```
?strptime
```

Note how the first example supplies a vector for the first argument. A column of a dataframe is often the first argument.

To retieve the current date, use Sys.Date().

```
In [15]: Sys.Date()
2017-07-10
```

Times

Times are represented by two nice classes with ugly names: POSIXct and POSIXIt.

- POSIXct is just a large integer under the hood. It's good for dataframe calculations.
- POSIX1t is a list that maintains info about day of the week, day of the year, day of the month, and lots of other things. It's good for presenting date-times in human readable form.

POSIXct

The as.POSIXct function creates a POSIXct object from another object such as a string or Date.

```
In [16]: as.POSIXct(Sys.Date())
    as.POSIXct(Sys.time())
    as.POSIXct("2017-02-25 13:30")
    as.POSIXct("2017-02-25 13:30 PDT")

[1] "2017-07-09 17:00:00 PDT"

[1] "2017-07-10 15:50:47 PDT"

[1] "2017-02-25 13:30:00 PST"

[1] "2017-02-25 13:30:00 PST"
```

Be wary of the timezone settings. In my R console, the last two entries returned PDT instead of PST.

The print method converts POSIXct instances into a human-friendly string. But at its heart, it's an integer suitable for calculation.

```
In [17]: ctime <- as.POSIXct("2017-07-12 15:20:30")
    ctime
    unclass(ctime)
[1] "2017-07-12 15:20:30 PDT"
1499898030</pre>
```

POSIXIt

The as.POSIX1t function creates a POSIX1t instance. From the way it is constructed and printed, the POSIX1t doesn't seem any different than POSIXct. Indeed, they can be converted back and forth. But the POSIX1t stores various attributes of a time.

```
In [18]: ltime <- as.POSIXlt("2017-04-05 12:30:00")</pre>
          ltime
          unclass(ltime)
          [1] "2017-04-05 12:30:00 PDT"
          $sec
          0
          $min
          30
          $hour
          12
          $mday
          5
          $mon
          $year
          117
          $wday
          $yday
          94
          $isdst
          1
          $zone
          'PDT'
          $gmtoff
          <NA>
In [19]: paste("Number of seconds is", ltime$sec, "and hours are", ltime$hour)
          'Number of seconds is 0 and hours are 12'
```

The paste function "pastes" strings together.

Parsing and Formating

Our dates and time objects are easily constructed from strings are formatted in a reasonable way. But often we need to parse exotic date and time formats. Or we may need to present them in exotic ways. R provides the following functions for this.

- strptime parse a date and/or time string.
- strftime format a string from a date or time object.

The parsing function strptime always returns a POSIX1t. This may be converted to either a Date or POSIXct through their respective as functions: as.Date() and as.POSIXct. The **conversion specification** used by the parse and format function is documented in the help for strptime.

```
In [20]: strptime('06/13/2017 14:20', "%m/%d/%Y")
    strptime('Oct 20, 2014 at 16:15', "%b %d, %Y at %H:%M")

[1] "2017-06-13 PDT"

[1] "2014-10-20 16:15:00 PDT"
```

Exercise Parse the following date/times with strptime.

- 1. 170628 3:36 Assume military time.
- 2. 2016136 This is just a date. The first four characters are the year; the last three are the number of days since January 1. Some mainframe systems still use this.
- 3. July 4, 1976 at 15:30 Remember the difference between long month and short month.
- 4. Day 7 of January at 20:00 in the year 2016 Hopefully you don't run into many of these.

Comparisons

The usual comparison operators apply to the date time classes.

```
In [21]: ts <- as.POSIX1t(c("2017-03-01", "2017-04-01", "2017-05-01", "2017-06-01"))
ts > as.POSIX1t("2017-04-15")
FALSE FALSE TRUE TRUE
```

Time Differences

The **difftime** class supports arithmetic based on the difference between two times. A **difftime** can be created implicitly by the subtraction operator.

```
In [22]: td1 <- as.POSIXlt("2017-04-15") - as.POSIXlt("2017-04-07")
td1
Time difference of 8 days</pre>
```

Or it can be created by a direct call to the difftime function with two dates.

```
In [23]: td2 <- difftime("2017-04-15", "2017-04-07")
td2

Time difference of 8 days</pre>
```

Finally, it can be created by specifying the units directly to the as.difftime function.

```
In [24]: td3 <- as.difftime(10, units="days")
td3

Time difference of 10 days</pre>
```

You can compare time differences.

```
In [25]: td1 > td3

FALSE
```

And you can add a difference back to a date or time.

```
In [26]: ts + td3
[1] "2017-03-11 PST" "2017-04-11 PDT" "2017-05-11 PDT" "2017-06-11 PDT"
```

Split (revisited)

In the last workshop we investigated several ways to create factor variables for the purpose of the *split* phase of the *split* apply-combine paradigm. One important technique that was left out was the **cut** function. Its first three parametes are

- 1. a numeric vector to cut
- 2. a specfication for the cuts
- 3. labels for the cuts (optional)

The result is a factor vector with the same length as the first argument. The value of each entry is the cut to which the original entry is placed. A few examples should clear this up. We'll use the InsectSprays dataset on which to demonstrate some cutting techniques.

In [27]: head(InsectSprays)

count	spray
10	Α
7	Α
20	Α
14	Α
14	Α
12	Α

We'll split the dataset based on the "quality" of the spray, which we presume to be proportional to the eradication count. We'll create **quality** factor variable with values of either bad, ok, or good depending on the eradication count in two ways.

- 1. qualityA based on absolute values of the count
- 2. qualityC based on quantiles (college students refer to this as "the curve".

For the absolute case, we simply divide the range of values into equal intervals. In this case, there are three such intervals: bad, ok, and good.

We can see that the intervals are about equal length (no curve). The interval names are informative, but somewhat awkward. We can assign friendlier names with the labels parameter.

```
In [29]: qualityA <- cut(InsectSprays$count, 3, labels=c('bad', 'ok', 'good') )
    table(qualityA)

qualityA
    bad ok good
    37 25 10</pre>
```

Instead of specifying the number of breaks (in which case they are all of equal length), we can specify the actual breakpoints themselves. Since we're "grading on a curve", we'll assign

- bad to the lower third
- ok to the middle third
- good to the upper third

We'll use the quantile function introduced in Workshop 1 to determine these break points.

Then provide these break points to the cut function.

We expect each level to have the same number of entries. This is only approximate due to the different ways quantiles can be computed. (Check the quantile help documentation; there are no fewer than **nine** algorithms from which to choose.) The default is usually fine and only deviates significantly when the sample size is small.

Now we have two factor variables, one absolute and one curved, that split the InsectSprays dataframe into "quality buckets." Let's see how the quality values were divided among the spray brands.

```
In [32]: table(InsectSprays$spray, qualityA)
         table(InsectSprays$spray, qualityC)
            qualityA
            bad ok good
              1 8
                      3
          В
              1
                 8
                       3
          С
                       0
            12
                 0
          D 11
                       0
                 1
                       0
          E 12 0
              0 8
            qualityC
             bad ok good
               0 5
               0
                 4
          С
                 1
                       0
               5 7
                       0
          Е
               8 4
                       0
```

Cutting Dates and Times

Hopefully we haven't completely forgotten dates and times. It turns out we can cut these, too. Remember that we can add a difftime duration to a POSIX1t time instant to get a new instant.

```
In [33]: as.POSIXlt("2017-03-31 12:00") + as.difftime(1, units="days")
        [1] "2017-04-01 12:00:00 PDT"
```

Let's create a sequence of 100 consecutive days.

Like in the numeric case, we can break into equal intervals by specifying the number of breaks.

Since the intervals were equal, it's no surprise that they are evenly distributed in this case.

We can generate break points based on the day of the week.

```
In [36]: mondays <- cut(dtvec, breaks="week")
mondays[1:5]</pre>
```

2017-03-27 2017-03-27 2017-03-27 2017-04-03 2017-04-03

In this example, the times were evenly spaced. The power of the last cut above becomes more apparent when applied to uneven intervals. Some weeks might have many values, some might have few, you just want to sum by week. Your *splitapply-combine* technique would use this operation for the *split* component.

Aggregation

In the last workshop we introduced the *split-apply-combine* paradigm in detail by investigating each step in detail. As a quick review, let's recall the analysis we performed on the InsectSprays dataset.

In [37]: head(InsectSprays)

count	spray
10	Α
7	Α
20	Α
14	Α
14	Α
12	А

- **A** 14.5
- **B** 15.3333333333333
- **C** 2.0833333333333
- **D** 4.9166666666667
- **E** 3.5
- **F** 16.666666666667

The first line is the **split**, which was done based on the value of the spray column. This yielded an insect spray list (isl) where each element of the list was a subset of the original dataset with a particular spray value.

The next line was the **apply**, which applied to the mean function to the count column. It returns a new list (isMeanLst) that has the same number of elements as isl. The value of an element in isMeanLst is the average of the count column of the corresponding subset in isl.

The third line is the **combine**, which converts the list of numbers into a vector of numbers. The last two steps are so common that a function named **sapply** is provided to combine them. The **s** in sapply means "simplify". It's equivalent to lapply followed by unlist.

The aggregate function combines all three steps into a single call.

```
In [40]: aggregate(count ~ spray, data=InsectSprays, mean)
```

spray	count
Α	14.500000
В	15.333333
С	2.083333
D	4.916667
E	3.500000
F	16.666667

Wow! That was easy. Let's break down what we just did.

The first parameter of aggregate is a formula. We saw formulas a few workshops ago when we studied the xtabs function. In general each function that uses a formula interprets it differently. In the case of aggregate we have the following.

- LHS This is the column on which the aggegation function will operate. In the example above it was count. If multiple columns are specified, they are acted upon individually. To operate on all numeric columns, specify a dot on the LHS.
- RHS This is a factor variable that this the basis for the aggregation. It's just like the RHS of the xtabs formula. If you specify multiple factor variables, the result is an interaction.

The second parameter is the name of the data frame. The final parameter is the name of the function to apply to the LHS of the formula.

Exercise: Apply some of these other functions:

```
1. sum
2. sd
3. max
4. min
5. function(x) { max(x) - min(x) }
```

Pivot Tables

Pivot tables are much easier to see than to describe. So let's just do one and you'll get the idea. We'll practice on the ChickWeight dataset.

In [41]: cw <- ChickWeight
head(cw)</pre>

weight	Time	Chick	Diet
42	0	1	1
51	2	1	1
59	4	1	1
64	6	1	1
76	8	1	1
93	10	1	1

This data frame records a bunch of baby chicks divided into four groups according to their diet. Their weight was recorded at several points in time. To determine the affect of the diet, let's aggregate the weight of chicks within a group using the mean function rather than analyzing each chick individually.

In [42]: cwag <- aggregate(weight ~ Time + Diet, data=cw, mean)
head(cwag, n=20)</pre>

Time	Diet	weight	
0	1	41.40000	
2	1	47.25000	
4	1	56.47368	
6	1	66.78947	
8	1	79.68421	
10	1	93.05263	
12	1	108.52632	
14	1	123.38889	
16	1	144.64706	
18	1	158.94118	
20	1	170.41176	
21	1	177.75000	
0	2	40.70000	
2	2	49.40000	
4	2	59.80000	
6	2	75.40000	
8	2	91.70000	
10	2	108.50000	
12	2	131.30000	
14	2	141.90000	

For each combination of Time and Diet we average the weight for all chicks. The cwag data frame shows the weights over time for diet 1 and the beginning of weights of time for diet 2. This organization is awkward if we wish to compare diets. We have to scroll the table up and down to see comparable values in time for each of the diets. It would be better to have a colum for each diet so they appeared next to each other. We should pivot the Diet column into a set of columns.

For this operation we need to another library. There are many libraries out there for this kind of thing and we'll investigate some of them in future workshops. For this workshop we'll use the **reshape2** library. Note that it must be installed since it does not come with a base R installation. The command to install it is

```
install.packages('reshape2')
```

Once its installed, the library is loaded via the library command.

```
In [43]: library(reshape2)
```

The function in reshape2 that performs a pivot is **dcast**. The d in dcast indicates the result is a data frame (the alternative is acast for an array or vector).

Time	1	2	3	4
0	41.40000	40.7	40.8	41.0000
2	47.25000	49.4	50.4	51.8000
4	56.47368	59.8	62.2	64.5000
6	66.78947	75.4	77.9	83.9000
8	79.68421	91.7	98.4	105.6000
10	93.05263	108.5	117.1	126.0000
12	108.52632	131.3	144.4	151.4000
14	123.38889	141.9	164.5	161.8000
16	144.64706	164.7	197.4	182.0000
18	158.94118	187.7	233.1	202.9000
20	170.41176	205.6	258.9	233.8889
21	177.75000	214.7	270.3	238.5556

The dcast function also employs a formula for one of its parameters.

- LHS the variables that will identify a row. In the example above each row is identified by the value of Time.
- RHS the column to be pivoted. In the example above, we pivot on the values of the Diet column.

Each value of the column specified on the RHS becomes a column in the resulting data frame. What determines the values in the new columns? The last parameter to dcast provides the value variable.

To clarify the meaning of the new columns, let's rename them.

Time	diet1	diet2	diet3	diet4
0	41.40000	40.7	40.8	41.0000
2	47.25000	49.4	50.4	51.8000
4	56.47368	59.8	62.2	64.5000
6	66.78947	75.4	77.9	83.9000
8	79.68421	91.7	98.4	105.6000
10	93.05263	108.5	117.1	126.0000
12	108.52632	131.3	144.4	151.4000
14	123.38889	141.9	164.5	161.8000
16	144.64706	164.7	197.4	182.0000
18	158.94118	187.7	233.1	202.9000
20	170.41176	205.6	258.9	233.8889
21	177.75000	214.7	270.3	238.5556

Now it is much easier to compare diets for each time at which the chicks were weighed.

The reverse of the pivot (or dcast) is the **melt** function. That is, we melt all the columns into a single column like we had before.

In [46]: mcwag <- melt(pcwag, id.vars='Time', variable.name='Diet', value.name='weight')
head(mcwag, n=20)</pre>

Time	Diet	weight
0	diet1	41.40000
2	diet1	47.25000
4	diet1	56.47368
6	diet1	66.78947
8	diet1	79.68421
10	diet1	93.05263
12	diet1	108.52632
14	diet1	123.38889
16	diet1	144.64706
18	diet1	158.94118
20	diet1	170.41176
21	diet1	177.75000
0	diet2	40.70000
2	diet2	49.40000
4	diet2	59.80000
6	diet2	75.40000
8	diet2	91.70000
10	diet2	108.50000
12	diet2	131.30000
14	diet2	141.90000

Notice it's the same form as before. The only difference is that the Diet column has values of diet1, diet2, diet3, and diet4 instead of 1, 2, 3, and 4 because we changed the column names before we melted the data frame. This is probably better than the original values because it makes clear these values should be considered categorical instead of quantitative.

Let's review some of the melt parameters.

- id.vars the columns that are **not** going to be melted.
- variable.name the column that will hold the names of the variables that **will** be melted.
- value.name the name of the column that will hold the value of the variables that will be melted.

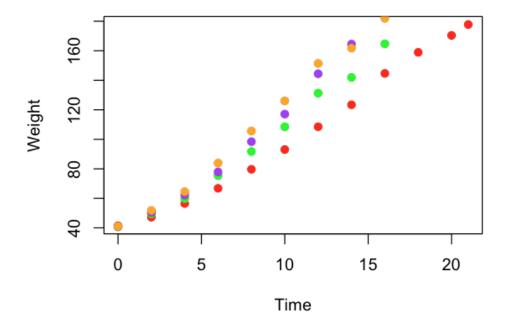
Pivoting is a core skill of any data scientist. There are many tools available for it. It's most important to understand the concept.

Two Variable Plots

We addressed single variable plotting over the last few workshops. Let's apply this aggregated dataset to plot two variables. The function for plotting two variables is plot.

Note: The options command is there to format this Jupyter notebook. It isn't necessary at the R console or RStudio.

Average Chick Weights

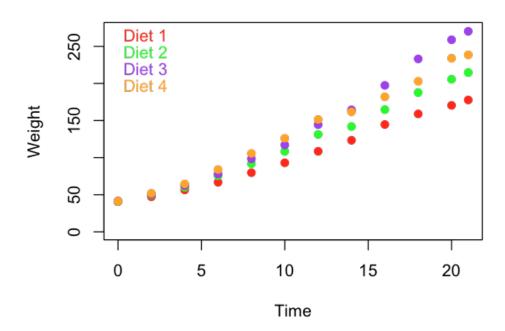


Let's make a few observations.

- The plot function creates a new plot window each time it is called. If you want to plot multiple sets, you have to call something else that does't start a new plot window. In this case, since we're making points, we call the points function.
- We changed the point character from its default (which is a hollow circle) to a solid circle (pch=19).
- Note that the y-axis was optimized for diet1. But the other diets have larger weights that run off the top of the graph. We can fix this by determining the range before hand and setting it with the xlim parametr in the plot command.
- There is no legend indicating which color maps to which diet.

Let's remedy the last two issues.

Average Chick Weights



Exercise Now it's your turn. Make the same plot with lines instead of points. Are the the differences.

- The plot command defaults to points. You override this default with the type parameter. For a line, you want type='1' where the value is the letter 1 for "line". This parameter should replace the pch=19 parameter. You don't a pch parameter for lines.
- Instead of the points command, use the lines command. The line command doesn't need a pch parameter.