

Notes

- Negations of Multiply-Quantified Statements

$$\sim (\forall x \in D, \exists y \in E \text{ s.t. } P(x, y)) \equiv \exists x \in D \text{ s.t. } \forall y \in E, \sim P(x, y)$$

$$\sim (\exists x \in D \text{ s.t. } \forall y \in E, P(x, y)) \equiv \forall x \in D, \exists y \in E \text{ s.t. } \sim P(x, y)$$

Test Yourself

1. a y in E ; y ; $P(x, y)$
2. an x in D ; y in E ; $P(x, y)$
3. $\exists x \text{ s.t. } \forall y, \sim P(x, y)$.
4. $\forall x, \exists y \text{ s.t. } \sim P(x, y)$.
5. may be true or false (c).