

# Missing data in supervised ML

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[https://github.com/brown-ccv/ODSC\\_West\\_2019](https://github.com/brown-ccv/ODSC_West_2019) ([https://github.com/brown-ccv/ODSC\\_West\\_2019](https://github.com/brown-ccv/ODSC_West_2019))

## About me

- Born and raised in Hungary
- Astrophysics PhD at MPA, Heidelberg, Germany
- Postdoctoral researcher at MIT (still in astrophysics at the time)
- Started at Brown in December 2015 as a Data Scientist
- Promoted to Lead Data Scientist in 2017
- Adjunct Lecturer in Data Science this semester
  - Teaching the course *DATA1030: Hands-on data science* to the DS master students at Brown

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## Data Science at Brown

- Center for Computation and Visualization
- Institutional Data group
  - Data-driven decision support and predictive modeling for Brown's administrative units
  - Academic research on data-intensive projects
- **OPEN POSITION** - more on this later

[https://github.com/brown-ccv/ODSC\\_West\\_2019](https://github.com/brown-ccv/ODSC_West_2019) ([https://github.com/brown-ccv/ODSC\\_West\\_2019](https://github.com/brown-ccv/ODSC_West_2019))

## Learning Objectives

By the end of this workshop, you will be able to

- Describe the three main types of missingness patterns
- Evaluate simple approaches for handling missing values
- Apply XGBoost to a dataset with missing values
- Apply multivariate imputation
- Apply the reduced-features model (also called the pattern submodel approach)
- Decide which approach is best for your dataset

## Before we start, a few words on our dataset: kaggle house price

- good for educational purposes
  - messy data that requires quite a bit of preprocessing
  - a nice mixture of continuous, ordinal, and categorical features, each feature type has missing values
- lots of excellent kernels on kaggle
  - check them out [here \(https://www.kaggle.com/c/house-prices-advanced-regression-techniques\)](https://www.kaggle.com/c/house-prices-advanced-regression-techniques)
- dataset and description available in repo
  - let's take a look!

## Missing values often occur in datasets

- survey data: not everyone answers all the questions
- medical data: not all tests/treatments/etc are performed on all patients
- sensor can be offline or malfunctioning
- customer data: not every user uses all features of an app

## Missing values are an issue for multiple reasons

### Conceptual reason

- missing values can introduce biases
  - bias: the samples (the data points) are not representative of the underlying distribution/population
  - any conclusion drawn from a biased dataset is also biased.
  - rich people tend to not fill out survey questions about their salaries and the mean salary estimated from survey data tend to be lower than true value

## Practical reason

- missing values (NaN, NA, inf) are incompatible with sklearn
  - all values in an array need to be numerical otherwise sklearn will throw a *ValueError*
- there are a few supervised ML techniques that work with missing values (e.g., XGBoost, CatBoost)
  - we will cover those later today

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## Missing data patterns

- **MCAR** - Missing Complete At Random
  - some people skip some survey questions by accident
- **MAR** - Missing At Random
  - males are less likely to fill out a survey on depression
  - this has nothing to do with their level of depression after accounting for maleness
- **MNAR** - Missing Not At Random
  - depressed people are less likely to fill out a survey on depression due to their level of depression

## MCAR test

- MCAR can be diagnosed with a statistical test ([Little, 1988](https://www.tandfonline.com/doi/abs/10.1080/01621459.1988.10478722) (<https://www.tandfonline.com/doi/abs/10.1080/01621459.1988.10478722>))
  - python implementation available in the [pymice](https://github.com/RianneSchouten/pymice) (<https://github.com/RianneSchouten/pymice>) package or in the skipped slide

```

In [1]: # from the pymice package
# https://github.com/RianneSchouten/pymice

import numpy as np
import pandas as pd
import math as ma
import scipy.stats as st

def checks_input_mcar_tests(data):
    """ Checks whether the input parameter of class McarTests is correct
        Parameters
        -----
        data:
            The input of McarTests specified as 'data'
        Returns
        -----
        bool
            True if input is correct
    """

    if not isinstance(data, pd.DataFrame):
        print("Error: Data should be a Pandas DataFrame")
        return False

    if not any(data.dtypes.values == np.float):
        if not any(data.dtypes.values == np.int):
            print("Error: Dataset cannot contain other value types than
floats and/or integers")
            return False

    if not data.isnull().values.any():
        print("Error: No NaN's in given data")
        return False

    return True

def mcar_test(data):
    """ Implementation of Little's MCAR test
        Parameters
        -----
        data: Pandas DataFrame
            An incomplete dataset with samples as index and variables as col
umns
        Returns
        -----
        p_value: Float
            This value is the outcome of a chi-square statistical test, test
ing whether the null hypothesis
            'the missingness mechanism of the incomplete dataset is MCAR' ca
n be rejected.
    """

    if not checks_input_mcar_tests(data):
        raise Exception("Input not correct")

```

```

dataset = data.copy()
vars = dataset.dtypes.index.values
n_var = dataset.shape[1]

# mean and covariance estimates
# ideally, this is done with a maximum likelihood estimator
gmean = dataset.mean()
gcov = dataset.cov()

# set up missing data patterns
r = 1 * dataset.isnull()
mdp = np.dot(r, list(map(lambda x: ma.pow(2, x), range(n_var))))
sorted_mdp = sorted(np.unique(mdp))
n_pat = len(sorted_mdp)
correct_mdp = list(map(lambda x: sorted_mdp.index(x), mdp))
dataset['mdp'] = pd.Series(correct_mdp, index=dataset.index)

# calculate statistic and df
pj = 0
d2 = 0
for i in range(n_pat):
    dataset_temp = dataset.loc[dataset['mdp'] == i, vars]
    select_vars = ~dataset_temp.isnull().any()
    pj += np.sum(select_vars)
    select_vars = vars[select_vars]
    means = dataset_temp[select_vars].mean() - gmean[select_vars]
    select_cov = gcov.loc[select_vars, select_vars]
    mj = len(dataset_temp)
    parta = np.dot(means.T, np.linalg.solve(select_cov, np.identity(
select_cov.shape[1])))
    d2 += mj * (np.dot(parta, means))

df = pj - n_var

# perform test and save output
p_value = 1 - st.chi2.cdf(d2, df)

return p_value

```

## Takeaway

- it can be challenging to infer the missingness pattern from an incomplete dataset
  - There is a statistical test to differentiate MCAR and MAR
  - MNAR is difficult/impossible to diagnose to the best of my knowledge
- multiple patterns can be present in the data
  - even worse, multiple patterns can be present in one feature!
  - missing values in a feature can occur due to a mix of MCAR, MAR, MNAR

# Learning Objectives

By the end of this workshop, you will be able to

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## Simple approaches for handling missing values

- 1) categorical/ordinal features: treat missing values as another category
  - missing values in categorical/ordinal features are not a big deal
- 2) continuous features: this is the tough part
  - sklearn's SimpleImputer
- 3) exclude points or features with missing values
  - might be OK

### 1a) Missing values in a categorical feature

- YAY - this is not an issue at all!
- Categorical feature needs to be one-hot encoded anyway
- Just replace the missing values with 'NA' or 'missing' and treat it as a separate category

### 1b) Missing values in a ordinal feature

- this can be a bit trickier but usually fine
- Ordinal encoder is applied to ordinal features
  - where does 'NA' or 'missing' fit into the order of the categories?
  - usually first or last
- if you can figure this out, you are golden

```
In [2]: # read the data
import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split

# Let's load the data
df = pd.read_csv('data/train.csv')
# drop the ID
df.drop(columns=['Id'],inplace=True)

# the target variable
y = df['SalePrice']
df.drop(columns=['SalePrice'],inplace=True)
# the unprocessed feature matrix
X = df.values
print(X.shape)
# the feature names
ftrs = df.columns
```

(1460, 79)

```
In [3]: # let's split to train, test, and holdout
X_other, X_holdout, y_other, y_holdout = train_test_split(df, y, test_size=0.2, random_state=0)
X_train, X_test, y_train, y_test = train_test_split(X_other, y_other, test_size=0.25, random_state=0)

print(X_train.shape)
print(X_test.shape)
print(X_holdout.shape)
```

(876, 79)

(292, 79)

(292, 79)

```

In [4]: # collect the various features
cat_ftrs = ['MSZoning', 'Street', 'Alley', 'LandContour', 'LotConfig', 'Neighborhood', 'Condition1', 'Condition2', \
            'BldgType', 'HouseStyle', 'RoofStyle', 'RoofMatl', 'Exterior1st', 'Exterior2nd', 'MasVnrType', 'Foundation', \
            'Heating', 'CentralAir', 'Electrical', 'GarageType', 'PavedDrive', 'MiscFeature', 'SaleType', 'SaleCondition']
ordinal_ftrs = ['LotShape', 'Utilities', 'LandSlope', 'ExterQual', 'ExterCond', 'BsmtQual', 'BsmtCond', 'BsmtExposure', \
               'BsmtFinType1', 'BsmtFinType2', 'HeatingQC', 'KitchenQual', 'Functional', 'FireplaceQu', 'GarageFinish', \
               'GarageQual', 'GarageCond', 'PoolQC', 'Fence']
ordinal_cats = [['Reg', 'IR1', 'IR2', 'IR3'], ['AllPub', 'NoSewr', 'NoSeWa', 'ELO'], ['Gtl', 'Mod', 'Sev'], \
               ['Po', 'Fa', 'TA', 'Gd', 'Ex'], ['Po', 'Fa', 'TA', 'Gd', 'Ex'], ['NA', 'Po', 'Fa', 'TA', 'Gd', 'Ex'], \
               ['NA', 'Po', 'Fa', 'TA', 'Gd', 'Ex'], ['NA', 'No', 'Mn', 'Av', 'Gd'], ['NA', 'Unf', 'LwQ', 'Rec', 'BLQ', 'ALQ', 'GLQ'], \
               ['NA', 'Unf', 'LwQ', 'Rec', 'BLQ', 'ALQ', 'GLQ'], ['Po', 'Fa', 'TA', 'Gd', 'Ex'], ['Po', 'Fa', 'TA', 'Gd', 'Ex'], \
               ['Sal', 'Sev', 'Maj2', 'Maj1', 'Mod', 'Min2', 'Min1', 'Typ'], ['NA', 'Po', 'Fa', 'TA', 'Gd', 'Ex'], \
               ['NA', 'Unf', 'RFn', 'Fin'], ['NA', 'Po', 'Fa', 'TA', 'Gd', 'Ex'], ['NA', 'Po', 'Fa', 'TA', 'Gd', 'Ex'], \
               ['NA', 'Fa', 'TA', 'Gd', 'Ex'], ['NA', 'MnWw', 'GdWo', 'MnPrv', 'GdPrv']]
num_ftrs = ['MSSubClass', 'LotFrontage', 'LotArea', 'OverallQual', 'OverallCond', 'YearBuilt', 'YearRemodAdd', \
            'MasVnrArea', 'BsmtFinSF1', 'BsmtFinSF2', 'BsmtUnfSF', 'TotalBsmntSF', '1stFlrSF', '2ndFlrSF', \
            'LowQualFinSF', 'GrLivArea', 'BsmtFullBath', 'BsmtHalfBath', 'FullBath', 'HalfBath', 'BedroomAbvGr', \
            'KitchenAbvGr', 'TotRmsAbvGrd', 'Fireplaces', 'GarageYrBlt', 'GarageCars', 'GarageArea', 'WoodDeckSF', \
            'OpenPorchSF', 'EnclosedPorch', '3SsnPorch', 'ScreenPorch', 'PoolArea', 'MiscVal', 'MoSold', 'YrSold']

```



```

In [5]: # preprocess with pipeline and columntransformer
from sklearn.compose import ColumnTransformer
from sklearn.pipeline import Pipeline
from sklearn.preprocessing import OneHotEncoder
from sklearn.preprocessing import OrdinalEncoder
from sklearn.preprocessing import StandardScaler
from sklearn.impute import SimpleImputer

# one-hot encoder
categorical_transformer = Pipeline(steps=[
    ('imputer', SimpleImputer(strategy='constant', fill_value='missing')),
    ('onehot', OneHotEncoder(sparse=False, handle_unknown='ignore'))])

# ordinal encoder
ordinal_transformer = Pipeline(steps=[
    ('imputer2', SimpleImputer(strategy='constant', fill_value='NA')),
    ('ordinal', OrdinalEncoder(categories = ordinal_cats))])

# standard scaler
numeric_transformer = Pipeline(steps=[
    ('scaler', StandardScaler())])

# collect the transformers
preprocessor = ColumnTransformer(
    transformers=[
        ('num', numeric_transformer, num_ftrs),
        ('cat', categorical_transformer, cat_ftrs),
        ('ord', ordinal_transformer, ordinal_ftrs)])

```

```

In [6]: # fit_transform the training set
X_prep = preprocessor.fit_transform(X_train)
# little hacky, but collect feature names
feature_names = preprocessor.transformers_[0][-1] + \
    list(preprocessor.named_transformers_['cat'][1].get_feature_names(cat_ftrs)) + \
    preprocessor.transformers_[2][-1]

df_train = pd.DataFrame(data=X_prep, columns=feature_names)
print(df_train.shape)

# transform the test
df_test = preprocessor.transform(X_test)
df_test = pd.DataFrame(data=df_test, columns = feature_names)
print(df_test.shape)

# transform the holdout
df_holdout = preprocessor.transform(X_holdout)
df_holdout = pd.DataFrame(data=df_holdout, columns = feature_names)
print(df_holdout.shape)

(876, 221)
(292, 221)
(292, 221)

```

## 2) Continuous features: mean or median imputation

- Imputation means you infer the missing values from the known part of the data
- sklearn's SimpleImputer can do mean and median imputation
- USUALLY A BAD IDEA!
  - MCAR: mean/median of non-missing values is the same as the mean/median of the true underlying distribution, but the variances are different
  - not MCAR: the mean/median and the variance of the completed dataset will be off
  - supervised ML model is too confident (MCAR) or systematically off (not MCAR)

## 3) Exclude points or features with missing values

- easy to do with pandas
- it is an ACCEPTABLE approach under two conditions:
  - Little's test supports MCAR ( $p > 0.05$ )
  - only small fraction of points contain missing values (maybe a few percent?)
  - the missing values are limited to one or a few features and a large fraction of points are missing from those features (maybe up to 90%?)
- if the MCAR assumption is justified, dropping points will not introduce biases to your model
- due to the smaller sample size, the confidence of your model might suffer.
- what will you do with missing values when you deploy the model?

```
In [7]: print('data dimensions:',df_train.shape)
print('the p value of the mcar test:',mcar_test(df_train))
perc_missing_per_ftr = df_train.isnull().sum(axis=0)/df_train.shape[0]
print('fraction of missing values in features:')
print(perc_missing_per_ftr[perc_missing_per_ftr > 0])
frac_missing = sum(df_train.isnull().sum(axis=1)!=0)/df_train.shape[0]
print('fraction of points with missing values:',frac_missing)
```

```
data dimensions: (876, 221)
the p value of the mcar test: 0.029160269814447304
fraction of missing values in features:
LotFrontage      0.173516
MasVnrArea       0.004566
GarageYrBlt      0.050228
dtype: float64
fraction of points with missing values: 0.2237442922374429
```

```
In [8]: print(df_train.shape)
        # by default, rows/points are dropped
        df_r = df_train.dropna()
        print(df_r.shape)
        # drop features with missing values
        df_c = df_train.dropna(axis=1)
        print(df_c.shape)
```

```
(876, 221)
```

```
(680, 221)
```

```
(876, 218)
```

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## XGBoost and missing values

- sklearn raises an error if the feature matrix (X) contains nans.
- XGBoost doesn't!
- If a feature with missing values is split:
  - XGBoost tries to put the points with missing values to the left and right
  - calculates the impurity measure for both options
  - puts the points with missing values to the side with the lower impurity
- if missingness correlates with the target variable, XGBoost extracts this info!

```
In [9]: import xgboost
from sklearn.model_selection import ParameterGrid
from sklearn.metrics import mean_squared_error

param_grid = {"learning_rate": [0.03],
              "n_estimators": [2000],
              "seed": [0],
              #"n_jobs": [6],
              #"reg_alpha": [0e0,0.1,0.31622777,1.,3.16227766,10.],
              #"reg_lambda": [0e0,0.1,0.31622777,1.,3.16227766,10.],
              "missing": [np.nan],
              #"max_depth": [1,2,3,4,5],
              "colsample_bytree": [0.9],
              "subsample": [0.66]}

XGB = xgboost.XGBRegressor()
XGB.set_params(**ParameterGrid(param_grid)[0])
XGB.fit(df_train,y_train,early_stopping_rounds=50,eval_set=[(df_test, y_
test)], verbose=False)
print('the test RMSE:',XGB.evals_result()['validation_0']['rmse'][-1])
y_holdout_pred = XGB.predict(df_holdout)
print('the holdout RMSE:',np.sqrt(mean_squared_error(y_holdout,y_holdout
_pred)))
```

```
/anaconda3/envs/datasci_v0.0.2_local4.yml/lib/python3.6/site-packages/x
gboost/core.py:587: FutureWarning: Series.base is deprecated and will b
e removed in a future version
```

```
if getattr(data, 'base', None) is not None and \
```

```
the test RMSE: 24356.306641
```

```
the holdout RMSE: 33267.239641714295
```

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## Multivariate Imputation

- models each feature with missing values as a function of other features, and uses that estimate for imputation
  - at each step, a feature column is designated as target variable  $y$  and the other feature columns are treated as feature matrix  $X$
  - a regressor is trained on  $(X, y)$  for known  $y$
  - then, the regressor is used to predict the missing values of  $y$
- in the ML pipeline:
  - create  $n$  imputed datasets
  - run all of them through the ML pipeline
  - generate  $n$  holdout scores
  - the uncertainty in the holdout scores is due to the uncertainty in imputation
- works on MCAR and MAR, fails on MNAR
- paper [here \(https://www.jstatsoft.org/article/view/v045i03\)](https://www.jstatsoft.org/article/view/v045i03)

## sklearn's IterativeImputer

```
In [10]: from sklearn.experimental import enable_iterative_imputer
from sklearn.impute import IterativeImputer
from sklearn.ensemble import RandomForestRegressor

print(df_train[['LotFrontage', 'MasVnrArea', 'GarageYrBlt']].head())

imputer = IterativeImputer(estimator = RandomForestRegressor(n_estimators=10), random_state=0)
X_impute = imputer.fit_transform(df_train)
df_train_imp = pd.DataFrame(data=X_impute, columns = df_train.columns)

print(df_train_imp[['LotFrontage', 'MasVnrArea', 'GarageYrBlt']].head())

df_test_imp = pd.DataFrame(data=imputer.transform(df_test), columns = df_train.columns)
df_holdout_imp = pd.DataFrame(data=imputer.transform(df_holdout), columns = df_train.columns)
```

	LotFrontage	MasVnrArea	GarageYrBlt
0	0.424926	-0.573303	0.979398
1	NaN	0.492835	1.018748
2	NaN	-0.573303	0.192399
3	-0.049970	0.810076	-0.476551
4	-1.474659	-0.022031	0.979398

  

	LotFrontage	MasVnrArea	GarageYrBlt
0	0.424926	-0.573303	0.979398
1	-1.258797	0.492835	1.018748
2	-0.516232	-0.573303	0.192399
3	-0.049970	0.810076	-0.476551
4	-1.474659	-0.022031	0.979398

```
/anaconda3/envs/datasci_v0.0.2_local4.yml/lib/python3.6/site-packages/sklearn/impute/_iterative.py:599: ConvergenceWarning: [IterativeImputer] Early stopping criterion not reached.
" reached.", ConvergenceWarning)
```

```
In [11]: XGB.fit(df_train_imp,y_train,early_stopping_rounds=50,eval_set=[(df_test_imp, y_test)], verbose=False)
print('the test RMSE:',XGB.evals_result()[ 'validation_0' ][ 'rmse' ][-1])
y_holdout_pred = XGB.predict(df_holdout_imp)
print('the holdout RMSE:',np.sqrt(mean_squared_error(y_holdout,y_holdout_pred)))
```

```
/anaconda3/envs/datasci_v0.0.2_local4.yml/lib/python3.6/site-packages/xgboost/core.py:587: FutureWarning: Series.base is deprecated and will be removed in a future version
if getattr(data, 'base', None) is not None and \
```

```
the test RMSE: 24731.107422
the holdout RMSE: 34163.64520140612
```

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## Reduced-features model (or pattern submodel approach)

- first described in 2007 in a [JMLR article \(http://www.jmlr.org/papers/v8/saar-tsechansky07a.html\)](http://www.jmlr.org/papers/v8/saar-tsechansky07a.html) as the reduced features model
- in 2018, "rediscovered" as the pattern submodel approach in [Biostatistics \(https://www.ncbi.nlm.nih.gov/pubmed/30203058\)](https://www.ncbi.nlm.nih.gov/pubmed/30203058)

My holdout set:

index	feature 1	feature 2	feature 3	target var
0	NA	45	NA	0
1	NA	NA	8	1
2	12	6	34	0
3	1	89	NA	0
4	0	NA	47	1
5	687	24	67	1
6	NA	23	NA	1

To predict points 0 and 6, I will use train and test points that are complete in feature 2.

To predict point 1, I will use train and test points that are complete in feature 3.

To predict point 2 and 5, I will use train and test points that are complete in features 1-3.

Etc. We will train as many models as the number of patterns in holdout.

## How to determine the patterns?

```
In [12]: mask = df_holdout[['LotFrontage', 'MasVnrArea', 'GarageYrBlt']].isnull()
unique_rows, counts = np.unique(mask, axis=0, return_counts=True)
print(unique_rows.shape) # 6 patterns, we will train 6 models
for i in range(len(counts)):
    print(unique_rows[i], counts[i])
```

```
(6, 3)
[False False False] 223
[False False  True] 21
[False  True False] 1
[ True False False] 44
[ True False  True] 2
[ True  True False] 1
```



```

In [13]: def xgb_model(X_train, Y_train, X_test, Y_test, X_holdout, Y_holdout, verbose=1):

    # make into row vectors to avoid an obnoxious sklearn/xgb warning
    Y_train = np.reshape(np.array(Y_train), (1, -1)).ravel()
    Y_test = np.reshape(np.array(Y_test), (1, -1)).ravel()
    Y_holdout = np.reshape(np.array(Y_holdout), (1, -1)).ravel()

    XGB = xgboost.XGBRegressor(n_jobs=1)

    # find the best parameter set
    param_grid = {"learning_rate": [0.03],
                  "n_estimators": [2000],
                  "seed": [0],
                  #"n_jobs": [6],
                  #"reg_alpha": [0e0,0.1,0.31622777,1.,3.16227766,10.],
                  #"reg_lambda": [0e0,0.1,0.31622777,1.,3.16227766,10.],
                  "missing": [np.nan],
                  #"max_depth": [1,2,3,4,5],
                  "colsample_bytree": [0.9],
                  "subsample": [0.66]}

    pg = ParameterGrid(param_grid)

    scores = np.zeros(len(pg))

    for i in range(len(pg)):
        if verbose >= 5:
            print("Param set " + str(i + 1) + " / " + str(len(pg)))
        params = pg[i]
        XGB.set_params(**params)
        eval_set = [(X_test, Y_test)]
        XGB.fit(X_train, Y_train,
                early_stopping_rounds=50, eval_set=eval_set, verbose=False)
    # with early stopping
    Y_test_pred = XGB.predict(X_test, ntree_limit=XGB.best_ntree_limit)

    scores[i] = mean_squared_error(Y_test, Y_test_pred)

    best_params = np.array(pg)[scores == np.max(scores)]
    if verbose >= 4:
        print('Test set max score and best parameters are:')
        print(np.max(scores))
        print(best_params)

    # test the model on the holdout set with best parameter set
    XGB.set_params(**best_params[0])
    XGB.fit(X_train, Y_train,
            early_stopping_rounds=50, eval_set=eval_set, verbose=False)
    Y_holdout_pred = XGB.predict(X_holdout, ntree_limit=XGB.best_ntree_limit)

    if verbose >= 1:
        print('The MSE is:', mean_squared_error(Y_holdout, Y_holdout_pred))

    if verbose >= 2:

```

```

        print ('The confusion matrix is:')
        print (cnf_matrix)
    if verbose >= 3:
        print("Feature importances:")
        print(XGB.feature_importances_)

    return (mean_squared_error(Y_holdout,Y_holdout_pred), Y_holdout_pred
, XGB.feature_importances_)

# Function: Reduced-feature XGB model
# all the inputs need to be pandas DataFrame
def reduced_feature_xgb(X_train, Y_train, X_test, Y_test, X_holdout, Y_h
oldout):

    # find all unique patterns of missing value in holdout set
    mask = X_holdout.isnull()
    unique_rows = np.array(np.unique(mask, axis=0))
    all_Y_holdout_pred = pd.DataFrame()

    print('there are', len(unique_rows), 'unique missing value pattern
s.')

    # divide holdout sets into subgroups according to the unique pattern
s
    for i in range(len(unique_rows)):
        print ('working on unique pattern', i)
        ## generate X_holdout subset that matches the unique pattern i
        sub_X_holdout = pd.DataFrame()
        sub_Y_holdout = pd.Series()
        for j in range(len(mask)): # check each row in mask
            row_mask = np.array(mask.iloc[j])
            if np.array_equal(row_mask, unique_rows[i]): # if the patter
n matches the ith unique pattern
                sub_X_holdout = sub_X_holdout.append(X_holdout.iloc[j])#
append the according X_holdout row j to the subset
                sub_Y_holdout = sub_Y_holdout.append(Y_holdout.iloc[[j
]])# append the according Y_holdout row j
                sub_X_holdout = sub_X_holdout[X_holdout.columns[~unique_rows[i
]]]

        ## choose the according reduced features for subgroups
        sub_X_train = pd.DataFrame()
        sub_Y_train = pd.DataFrame()
        sub_X_test = pd.DataFrame()
        sub_Y_test = pd.DataFrame()
        # 1.cut the feature columns that have nans in the according sub_
X_holdout
        sub_X_train = X_train[X_train.columns[~unique_rows[i]]]
        sub_X_test = X_test[X_test.columns[~unique_rows[i]]]
        # 2.cut the rows in the sub_X_train and sub_X_test that have any
nans
        sub_X_train = sub_X_train.dropna()
        sub_X_test = sub_X_test.dropna()
        # 3.cut the sub_Y_train and sub_Y_test accordingly
        sub_Y_train = Y_train.iloc[sub_X_train.index]
        sub_Y_test = Y_test.iloc[sub_X_test.index]

```

```

        # run XGB
        sub_Y_holdout_pred = xgb_model(sub_X_train, sub_Y_train, sub_X_test,
                                       sub_Y_test, sub_X_holdout, sub_Y_holdout, verbose=0)
        sub_Y_holdout_pred = pd.DataFrame(sub_Y_holdout_pred[1], columns=['sub_Y_holdout_pred'],
                                       index=sub_Y_holdout.index)
        print('    RMSE:', np.sqrt(mean_squared_error(sub_Y_holdout, sub_Y_holdout_pred)))
        # collect the holdout predictions
        all_Y_holdout_pred = all_Y_holdout_pred.append(sub_Y_holdout_pred)

    # rank the final Y_holdout_pred according to original Y_holdout index
    all_Y_holdout_pred = all_Y_holdout_pred.sort_index()
    Y_holdout = Y_holdout.sort_index()

    # get global RMSE
    total_RMSE = np.sqrt(mean_squared_error(Y_holdout, all_Y_holdout_pred))

    return total_RMSE

```

## A python implementation is available on the skipped slide

```

In [14]: print('final RMSE:', reduced_feature_xgb(df_train, y_train, df_test, y_test, df_holdout, y_holdout))

```

```

there are 6 unique missing value patterns.
working on unique pattern 0
    RMSE: 36882.33649761256
working on unique pattern 1
    RMSE: 14122.835714181436
working on unique pattern 2
    RMSE: 7912.15625
working on unique pattern 3
    RMSE: 19059.686269128022
working on unique pattern 4
    RMSE: 20818.556654658543
working on unique pattern 5
    RMSE: 55023.453125
final RMSE: 33488.799390845474

```

## Learning Objectives

By the end of this workshop, you will be able to

- Describe the three main types of missingness patterns
- Evaluate simple approaches for handling missing values
- Apply XGBoost to a dataset with missing values
- Apply multivariate imputation
- Apply the reduced-features model (also called the pattern submodel approach)
- **Decide which approach is best for your dataset**

## Which approach is best for my data?

- **XGB**: run  $n$  XGB models with  $n$  different seeds
- **imputation**: prepare  $n$  different imputations and run  $n$  XGB models on them
- **reduced-features**: run  $n$  reduced-features model with  $n$  different seeds
- rank the three methods based on how significantly different the corresponding mean scores are
  - I hope to talk about the results of this experiment at ODSC East next year!

Now you can

- Describe the three main types of missingness patterns
- Evaluate simple approaches for handling missing values
- Apply XGBoost to a dataset with missing values
- Apply multivariate imputation
- Apply the reduced-features model (also called the pattern submodel approach)
- Decide which approach is best for your dataset

## We are hiring!

- If you don't mind the harsh New England winters and you enjoy working in an academic environment, please come and talk to me or send an email (andras\_zsom@brown.edu).
- The successful applicant will collaborate with Brown's Advancement, they will work on academic research projects with faculty members, and they will be encouraged to organize and teach at workshops and supervise interns.
- MSc is required!
- PhD and/or industry experience preferred.
- Earliest starting date: February 1st 2020.

**Thanks for you attention!**

In [ ]: