

Gli iteratori

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aa 2023/24

La classe `iterator`

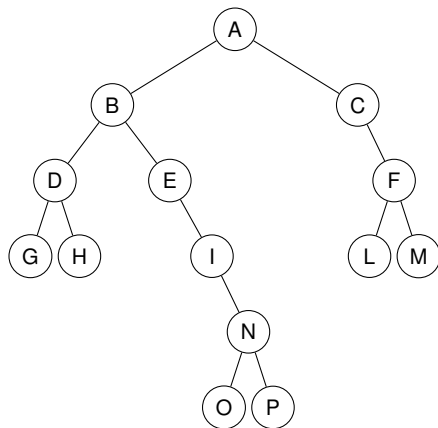
- ▶ Oggetti che a partire da un elemento in un container è in grado di indicare il successivo.
- ▶ Funzioni:
 1. lettura del dato nell'elemento;
 2. controllo di terminazione;
 3. successore (`++`);
 4. ripristinare la radice (ma solo nei `ResettableIterator`)

Visita in ampiezza

- ▶ Serve una **coda** di supporto.
 1. lettura del dato: metodo della classe;
 2. controllo di terminazione: coda vuota;
 3. successore: deque del nodo visitato e enqueue dei due figli del nodo corrente.

Visita in ampiezza

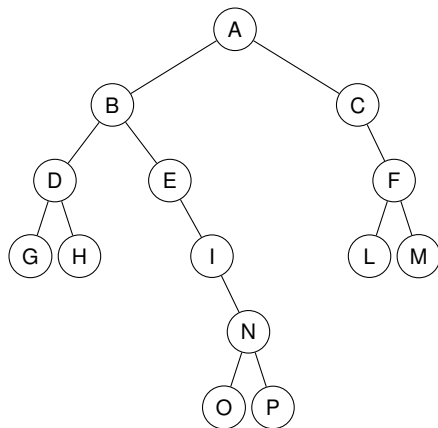
Esempio



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Visita in ampiezza

Esempio

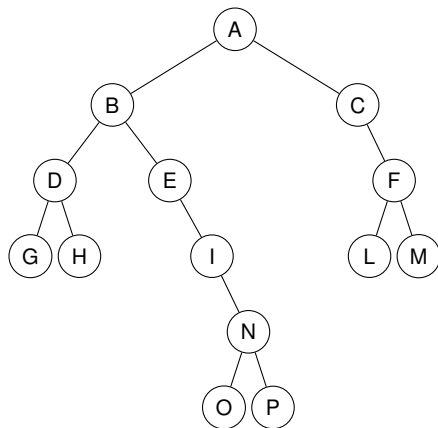


▶ ϵ

▶ $A \rightarrow A$

Visita in ampiezza

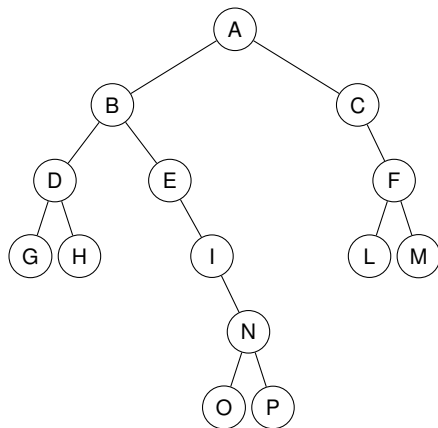
Esempio



- ▶ ϵ
- ▶ $A \rightarrow A$
- ▶ $B, C \rightarrow B$

Visita in ampiezza

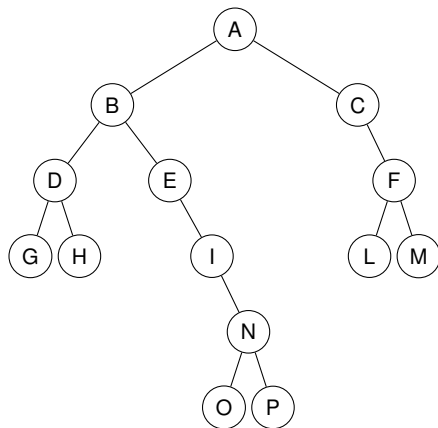
Esempio



- ▶ ϵ
- ▶ $A \rightarrow A$
- ▶ $B, C \rightarrow B$
- ▶ $C, D, E \rightarrow C$

Visita in ampiezza

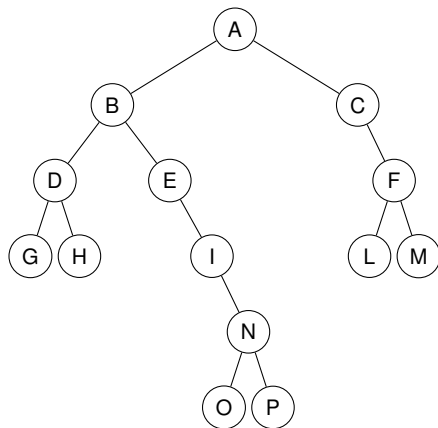
Esempio



- ▶ ϵ
- ▶ $A \rightarrow A$
- ▶ $B, C \rightarrow B$
- ▶ $C, D, E \rightarrow C$
- ▶ ...

Visita in ampiezza

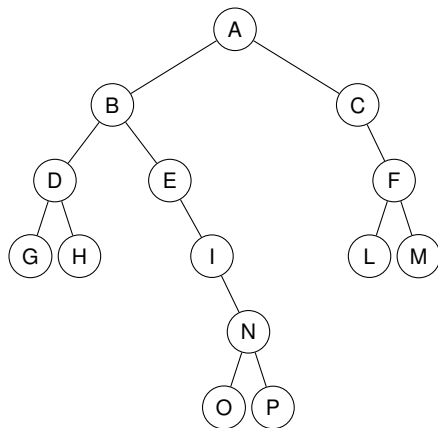
Esempio



- ▶ ϵ
- ▶ $A \rightarrow A$
- ▶ $B, C \rightarrow B$
- ▶ $C, D, E \rightarrow C$
- ▶ ...
- ▶ $P \rightarrow P$

Visita in ampiezza

Esempio



- ▶ ϵ
- ▶ $A \rightarrow A$
- ▶ $B, C \rightarrow B$
- ▶ $C, D, E \rightarrow C$
- ▶ ...
- ▶ $P \rightarrow P$
- ▶ ϵ condizione di terminazione

Visita in ampiezza

Discussione



Visita in profondità

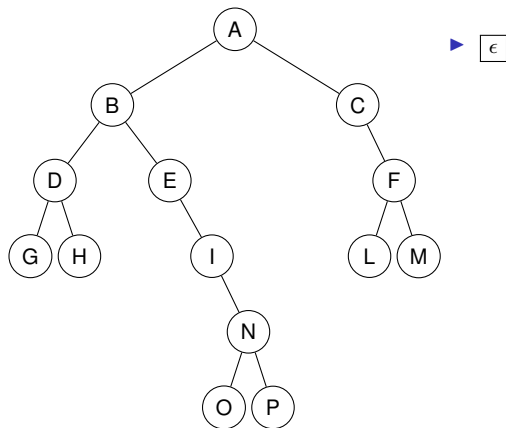
- ▶ Tre strategie:
 - ▶ Preorder
 - ▶ Inorder
 - ▶ Postorder
- ▶ La versione ricorsiva non ci aiuta molto: meglio pensare all'iterativa.

Visita preorder

- ▶ Serve uno **stack** di supporto.
 1. lettura del dato: metodo della classe;
 2. controllo di terminazione: stack vuoto;
 3. successore: pop del nodo visitato e push dei due figli del nodo corrente.

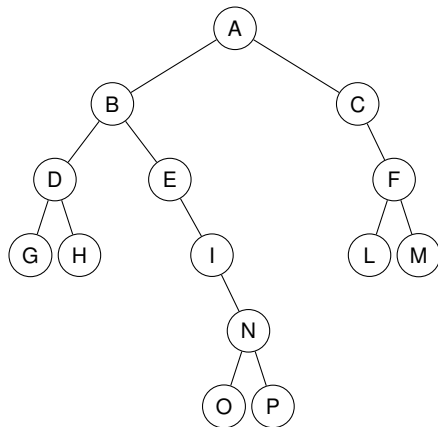
Visita preorder

Esempio



Visita preorder

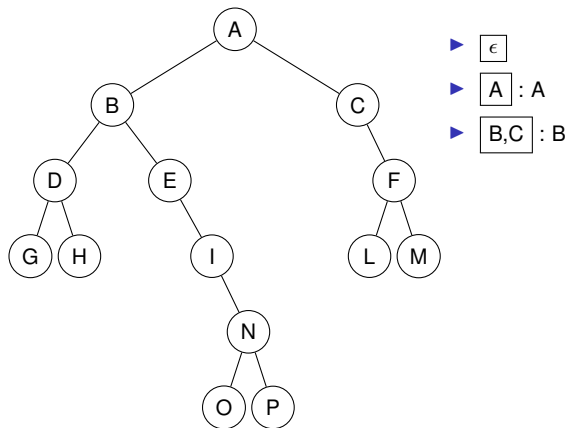
Esempio



► ϵ
► $A : A$

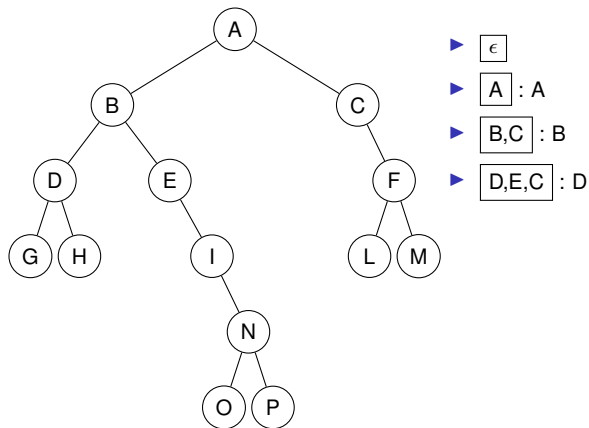
Visita preorder

Esempio



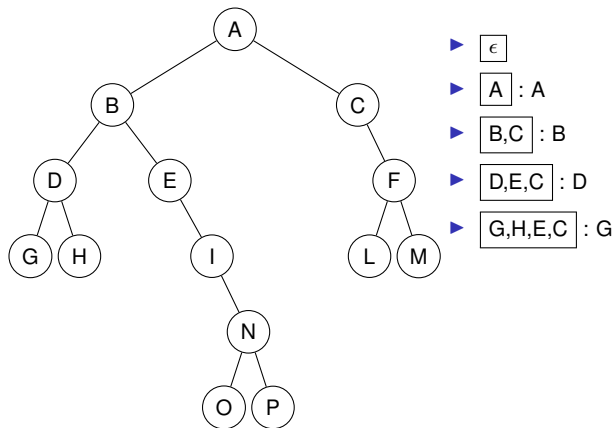
Visita preorder

Esempio



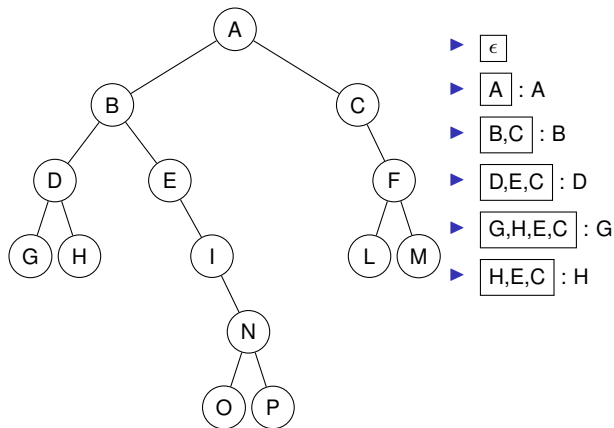
Visita preorder

Esempio



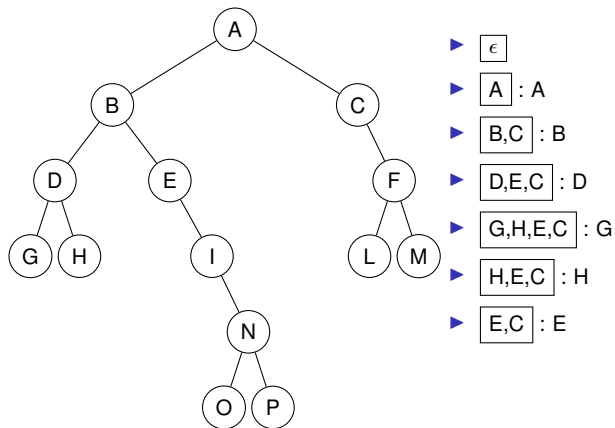
Visita preorder

Esempio



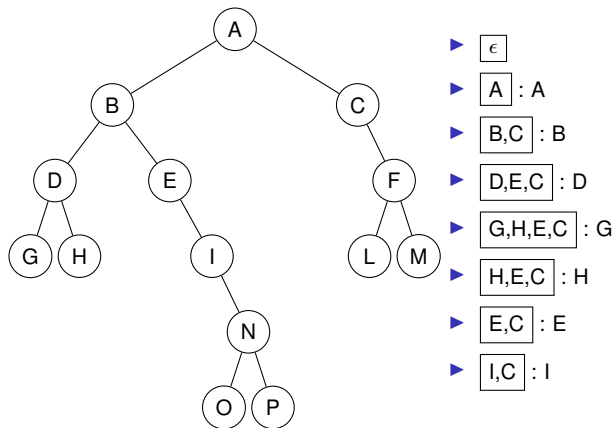
Visita preorder

Esempio



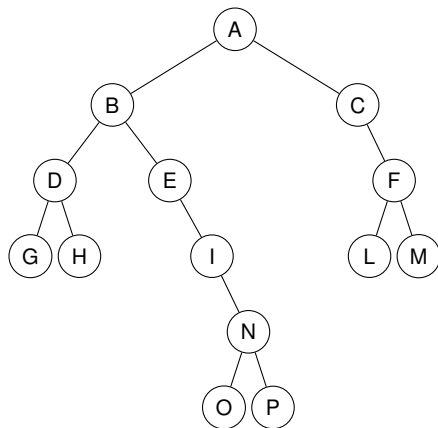
Visita preorder

Esempio



Visita preorder

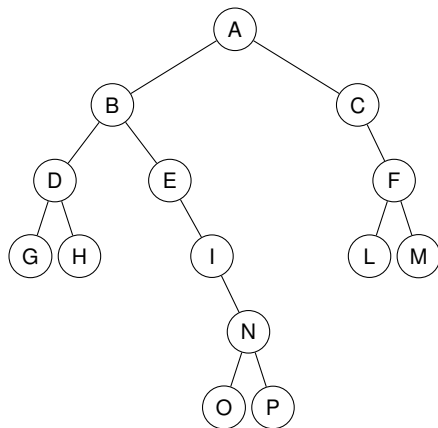
Esempio



- ▶ ϵ
- ▶ $A : A$
- ▶ $B, C : B$
- ▶ $D, E, C : D$
- ▶ $G, H, E, C : G$
- ▶ $H, E, C : H$
- ▶ $E, C : E$
- ▶ $I, C : I$
- ▶ $N, C : N$

Visita preorder

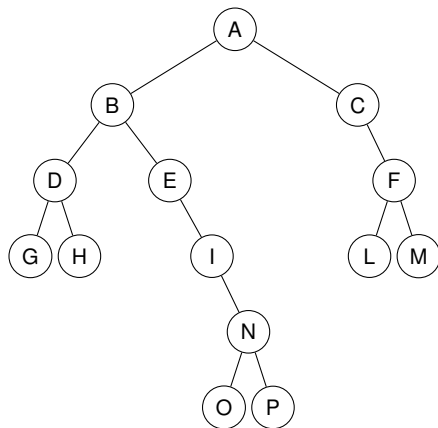
Esempio



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 - ▶ $N, C : N$
- ▶ $O, P, C : O$

Visita preorder

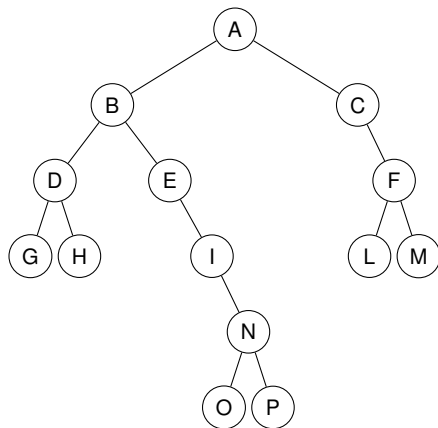
Esempio



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- ▶ $O, P, C : O$
- ▶ $P, C : P$

Visita preorder

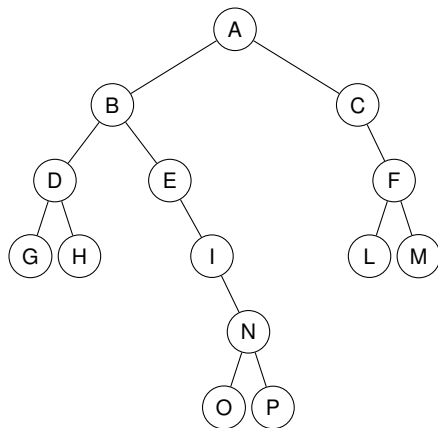
Esempio



- ▶ ϵ
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- ▶ $E, C : E$
- ▶ $I, C : I$
- ▶ $N, C : N$
- ▶ $O, P, C : O$
- ▶ $P, C : P$
- ▶ $C : C$

Visita preorder

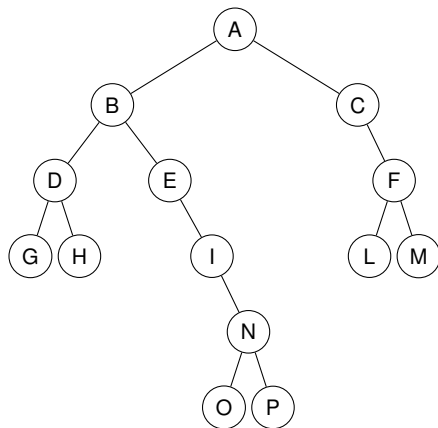
Esempio



- ▶ ϵ
- ▶ $A : A$
- ▶ $B, C : B$
- ▶ $D, E, C : D$
- ▶ $G, H, E, C : G$
- ▶ $H, E, C : H$
- ▶ $E, C : E$
- ▶ $I, C : I$
- ▶ $N, C : N$
- ▶ $O, P, C : O$
- ▶ $P, C : P$
- ▶ $C : C$
- ▶ $F : F$

Visita preorder

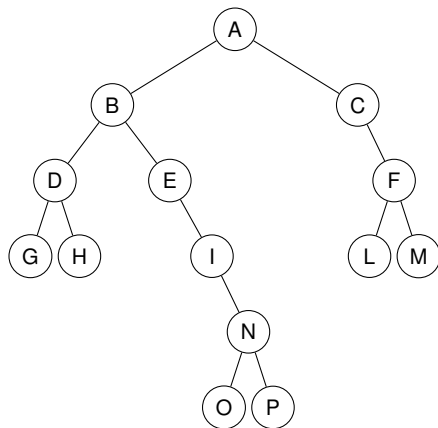
Esempio



- ▶ ϵ
- ▶ $A : A$
- ▶ $B, C : B$
- ▶ $D, E, C : D$
- ▶ $G, H, E, C : G$
- ▶ $H, E, C : H$
- ▶ $E, C : E$
- ▶ $I, C : I$
- ▶ $N, C : N$
- ▶ $O, P, C : O$
- ▶ $P, C : P$
- ▶ $C : C$
- ▶ $F : F$
- ▶ $L, M : L$

Visita preorder

Esempio

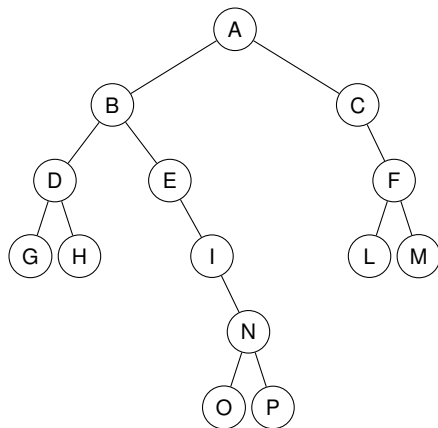


- ▶ ϵ
- ▶ $A : A$
- ▶ $B, C : B$
- ▶ $D, E, C : D$
- ▶ $G, H, E, C : G$
- ▶ $H, E, C : H$
- ▶ $E, C : E$
- ▶ $I, C : I$
- ▶ $N, C : N$

- ▶ $O, P, C : O$
- ▶ $P, C : P$
- ▶ $C : C$
- ▶ $F : F$
- ▶ $L, M : L$
- ▶ $M : M$

Visita preorder

Esempio



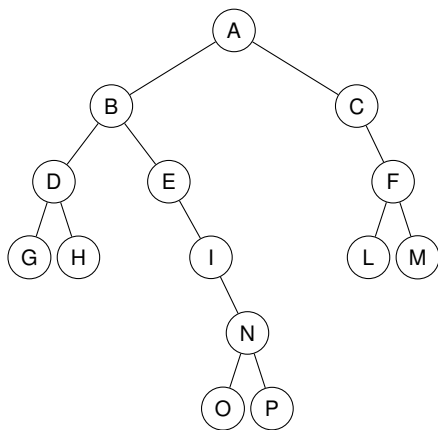
- ▶ ϵ
- ▶ $A : A$
- ▶ $B, C : B$
- ▶ $D, E, C : D$
- ▶ $G, H, E, C : G$
- ▶ $H, E, C : H$
- ▶ $E, C : E$
- ▶ $I, C : I$
- ▶ $N, C : N$
- ▶ $O, P, C : O$
- ▶ $P, C : P$
- ▶ $C : C$
- ▶ $F : F$
- ▶ $L, M : L$
- ▶ $M : M$
- ▶ ϵ condizione di terminazione

Visita inorder

- ▶ In questo caso il nodo corrente viene **scoperto**, ma non ancora **visitato**: prima bisogna visitare il sottoalbero sinistro.
- ▶ Solito **stack** di supporto.
- ▶ `searchLeftMostNode` Ci serve anche una funzione che continua a scendere a sinistra fino a quando possibile inserendo man mano i nodi che incontra nello stack: si ferma al primo nodo il cui figlio sinistro è vuoto.
- ▶ `scopri` Quando scopriamo un nodo, ne facciamo il push nello stack e poi scendiamo a sinistra con `searchLeftMostNode`
 1. lettura del dato: metodo della classe;
 2. controllo di terminazione: stack vuoto;
 3. successore: Pop e restituisco il nodo; visita il suo nodo destro, se c'è.
- ▶ Naturalmente parto dalla radice dell'albero.

Visita inorder

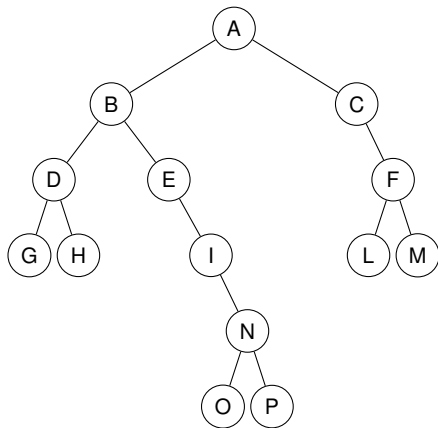
Esempio



Visita inorder

Esempio

► $G, D, B, A : G$



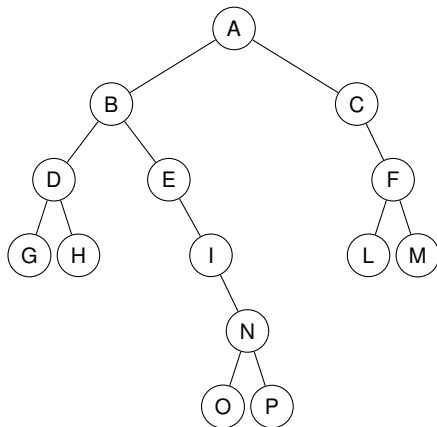
Visita inorder

Esempio

► G, D, B, A : G

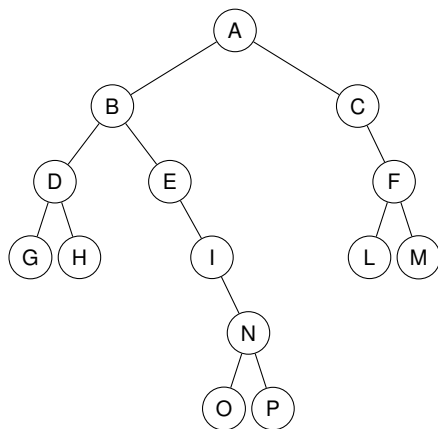
► D, B, A : D

► H, B, A : H



Visita inorder

Esempio



► G, D, B, A : G

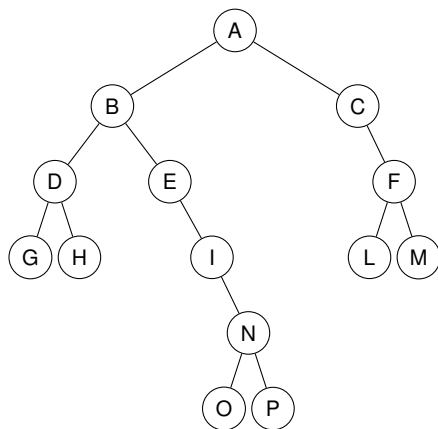
► D, B, A : D

► H, B, A : H

► B, A : B

Visita inorder

Esempio



► G, D, B, A : G

► D, B, A : D

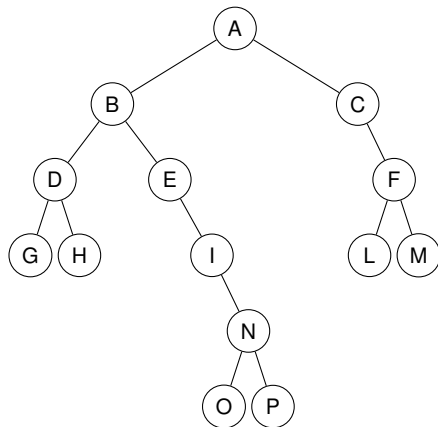
► H, B, A : H

► B, A : B

► E, A : E

Visita inorder

Esempio



▶ G, D, B, A : G

▶ D, B, A : D

▶ H, B, A : H

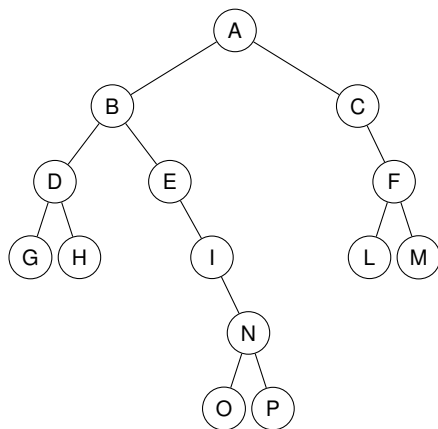
▶ B, A : B

▶ E, A : E

▶ I, A : I

Visita inorder

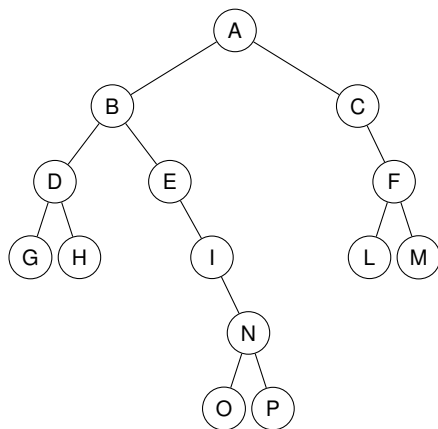
Esempio



- ▶ G, D, B, A : G
- ▶ D, B, A : D
- ▶ H, B, A : H
- ▶ B, A : B
- ▶ E, A : E
- ▶ I, A : I
- ▶ O, N, A : O

Visita inorder

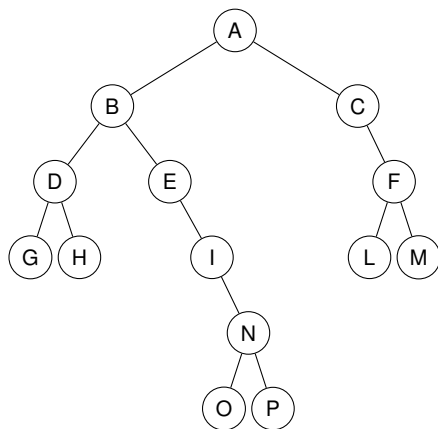
Esempio



- ▶ G, D, B, A : G
- ▶ D, B, A : D
- ▶ H, B, A : H
- ▶ B, A : B
- ▶ E, A : E
- ▶ I, A : I
- ▶ O, N, A : O
- ▶ N, A : N

Visita inorder

Esempio



▶ G, D, B, A : G

▶ D, B, A : D

▶ H, B, A : H

▶ B, A : B

▶ E, A : E

▶ I, A : I

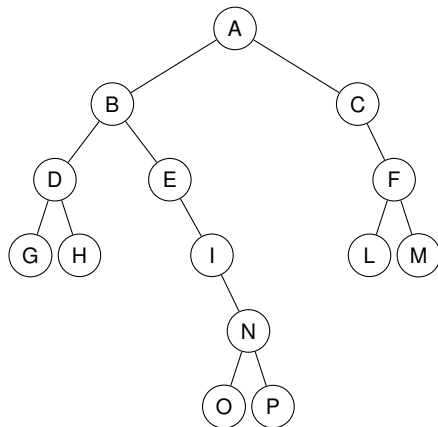
▶ O, N, A : O

▶ N, A : N

▶ P, A : P

Visita inorder

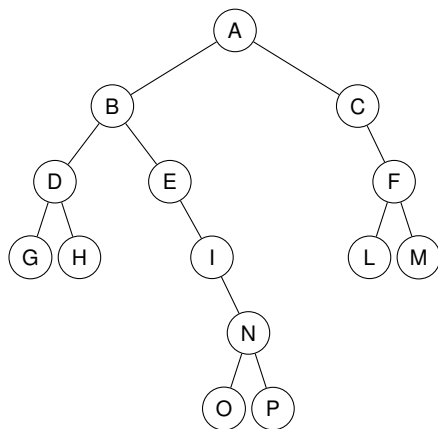
Esempio



- ▶ G, D, B, A : G
- ▶ D, B, A : D
- ▶ H, B, A : H
- ▶ B, A : B
- ▶ E, A : E
- ▶ I, A : I
- ▶ O, N, A : O
- ▶ N, A : N
- ▶ P, A : P
- ▶ A : A

Visita inorder

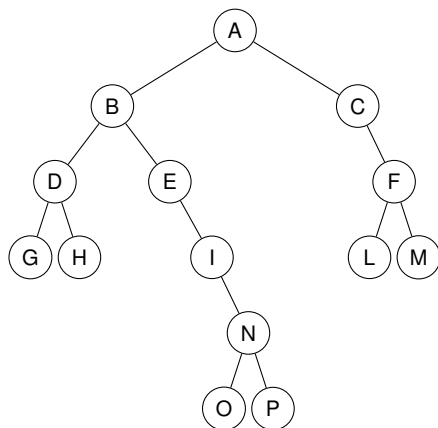
Esempio



- ▶ G, D, B, A : G
- ▶ D, B, A : D
- ▶ H, B, A : H
- ▶ B, A : B
- ▶ E, A : E
- ▶ I, A : I
- ▶ O, N, A : O
- ▶ N, A : N
- ▶ P, A : P
- ▶ A : A
- ▶ C : C

Visita inorder

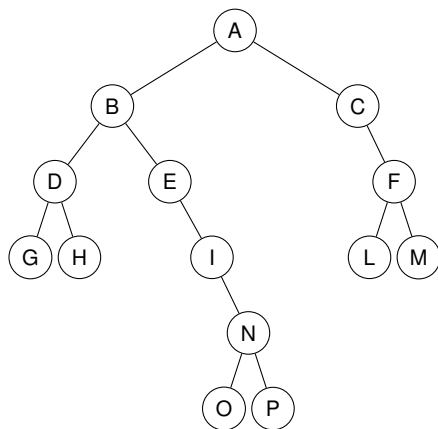
Esempio



- ▶ G, D, B, A : G
- ▶ D, B, A : D
- ▶ H, B, A : H
- ▶ B,A : B
- ▶ E,A : E
- ▶ I,A : I
- ▶ O,N,A : O
- ▶ N,A : N
- ▶ P,A : P
- ▶ A : A
- ▶ C : C
- ▶ L,F : L

Visita inorder

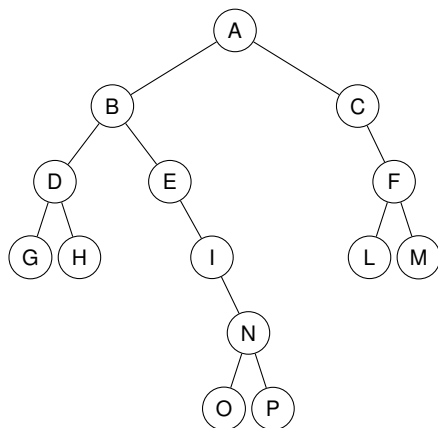
Esempio



- ▶ G, D, B, A : G
- ▶ D, B, A : D
- ▶ H, B, A : H
- ▶ B, A : B
- ▶ E, A : E
- ▶ I, A : I
- ▶ O, N, A : O
- ▶ N, A : N
- ▶ P, A : P
- ▶ A : A
- ▶ C : C
- ▶ L, F : L
- ▶ F : F

Visita inorder

Esempio



▶ G, D, B, A : G

▶ D, B, A : D

▶ H, B, A : H

▶ B, A : B

▶ E, A : E

▶ I, A : I

▶ O, N, A : O

▶ N, A : N

▶ P, A : P

▶ A : A

▶ C : C

▶ L, F : L

▶ F : F

▶ M : M e termino

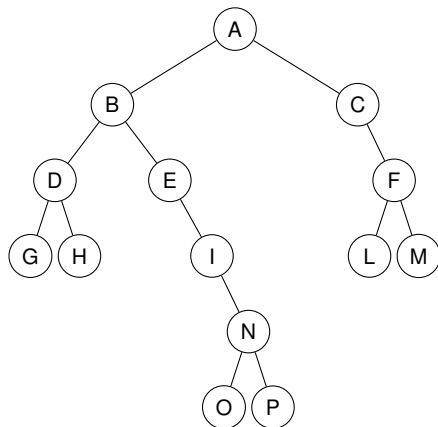
Visita postorder

- ▶ È un po' più complicato, perché la strategia cambia a seconda che stia risalendo l'albero da destra o da sinistra: per capirlo devo tenere l'ultimo nodo restituito, che chiameremo `current`.
- ▶ La visita di un nodo implica fare il pop del nodo e poi scendere a sinistra con `searchLeftMostList`: quando trova un nodo col figlio sinistro vuoto, salta al destro e ricomincia a sinistra, fino a quando non trova una foglia.
- ▶
 1. lettura del dato: metodo della classe;
 2. controllo di terminazione: stack vuoto;
 3. successore: ripeti fino a quando non arrivi ad un pop e restituisci:
 - ▶ se `current ==` figlio sinistro del `top` dello stack, allora scopri il figlio destro;
 - ▶ se `current ==` figlio destro del `top` dello stack, pop e restituisci
 - ▶ altrimenti (foglia), pop e restituisci
- ▶ Naturalmente parto dalla radice dell'albero.

Visita postorder

Esempio

► curr: ϵ ; G, D, B, A : G

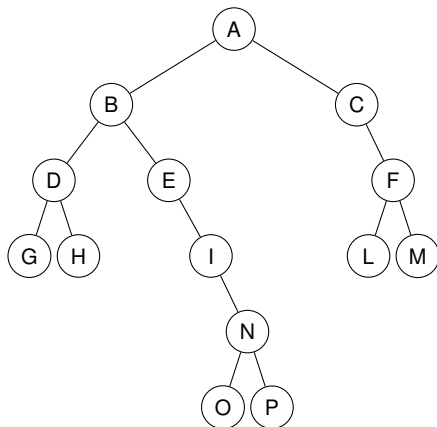


Visita postorder

Esempio

► curr: ϵ ; G, D, B, A : G

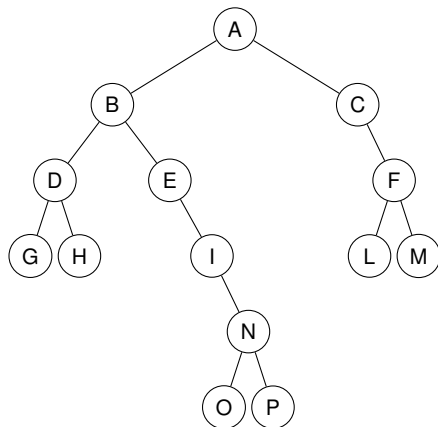
► curr: G; H, D, B, A : H



Visita postorder

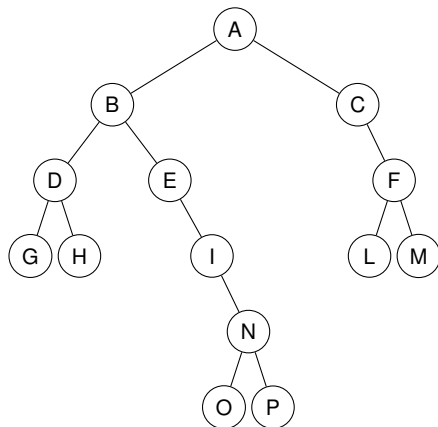
Esempio

- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D



Visita postorder

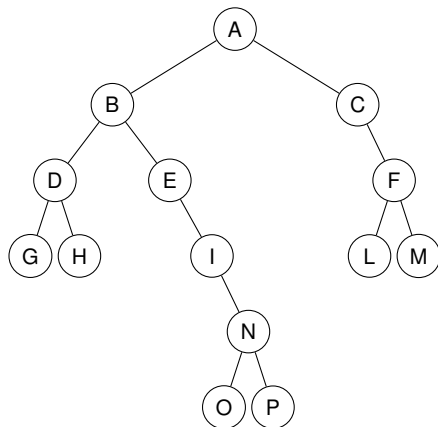
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O

Visita postorder

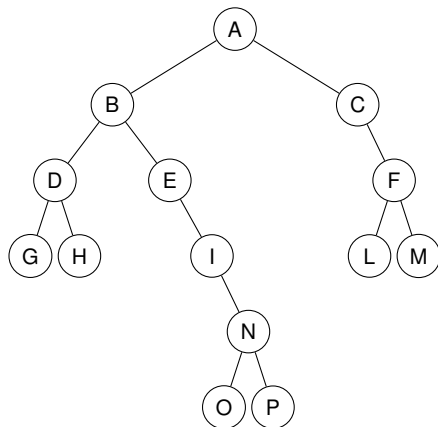
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P

Visita postorder

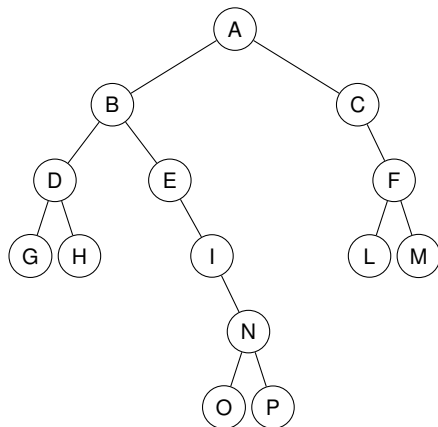
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P
- ▶ curr: P N, I, E, B, A : N

Visita postorder

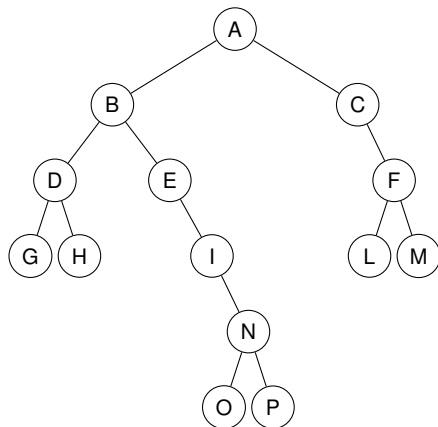
Esempio



- ▶ curr: ϵ ; **G, D, B, A** : G
- ▶ curr: G; **H, D, B, A** : H
- ▶ curr: H; **D, B, A** : D
- ▶ curr: D; **O, N, I, E, B, A** : O
- ▶ curr: O **P, N, I, E, B, A** : P
- ▶ curr: P **N, I, E, B, A** : N
- ▶ curr: N **I, E, B, A** : I

Visita postorder

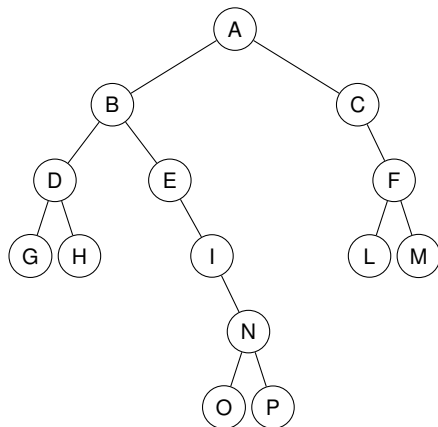
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P
- ▶ curr: P N, I, E, B, A : N
- ▶ curr: N I, E, B, A : I
- ▶ curr: I E, B, A : E

Visita postorder

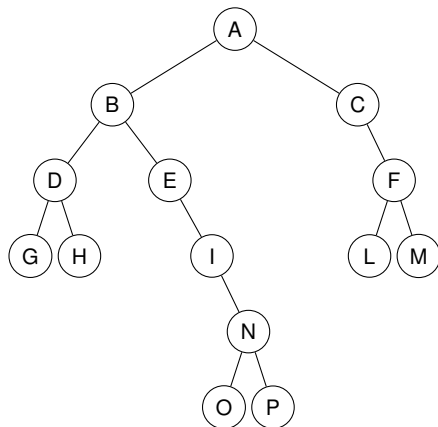
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P
- ▶ curr: P N, I, E, B, A : N
- ▶ curr: N I, E, B, A : I
- ▶ curr: I E, B, A : E
- ▶ curr: E B, A : B

Visita postorder

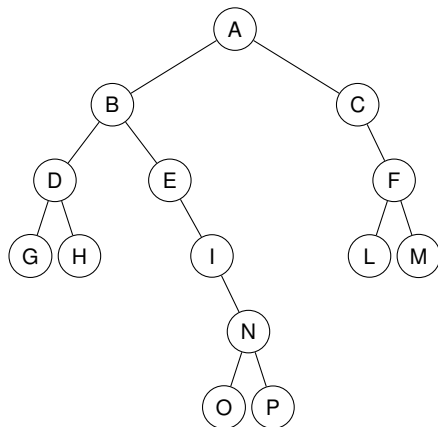
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P
- ▶ curr: P N, I, E, B, A : N
- ▶ curr: N I, E, B, A : I
- ▶ curr: I E, B, A : E
- ▶ curr: E B, A : B
- ▶ curr: B L, F, C, A : L

Visita postorder

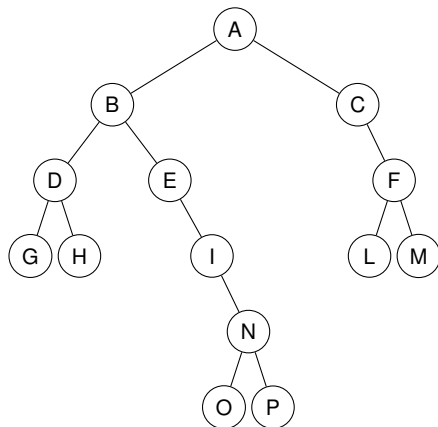
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P
- ▶ curr: P N, I, E, B, A : N
- ▶ curr: N I, E, B, A : I
- ▶ curr: I E, B, A : E
- ▶ curr: E B, A : B
- ▶ curr: B L, F, C, A : L
- ▶ curr: L M, F, C, A : M

Visita postorder

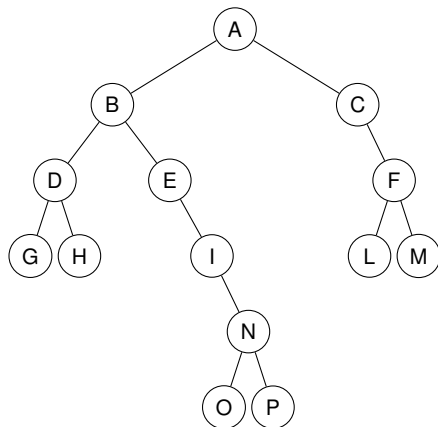
Esempio



- ▶ curr: ϵ ; G, D, B, A : G
- ▶ curr: G; H, D, B, A : H
- ▶ curr: H; D, B, A : D
- ▶ curr: D; O, N, I, E, B, A : O
- ▶ curr: O P, N, I, E, B, A : P
- ▶ curr: P N, I, E, B, A : N
- ▶ curr: N I, E, B, A : I
- ▶ curr: I E, B, A : E
- ▶ curr: E B, A : B
- ▶ curr: B L, F, C, A : L
- ▶ curr: L M, F, C, A : M
- ▶ curr: M F, C, A : F

Visita postorder

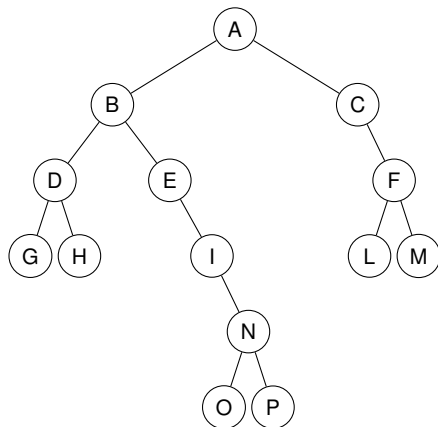
Esempio



- ▶ curr: ϵ ; **G, D, B, A** : G
- ▶ curr: G; **H, D, B, A** : H
- ▶ curr: H; **D, B, A** : D
- ▶ curr: D; **O, N, I, E, B, A** : O
- ▶ curr: O **P, N, I, E, B, A** : P
- ▶ curr: P **N, I, E, B, A** : N
- ▶ curr: N **I, E, B, A** : I
- ▶ curr: I **E, B, A** : E
- ▶ curr: E **B, A** : B
- ▶ curr: B **L, F, C, A** : L
- ▶ curr: L **M, F, C, A** : M
- ▶ curr: M **F, C, A** : F
- ▶ curr: F **C, A** : C

Visita postorder

Esempio



- ▶ curr: ϵ ; **G, D, B, A** : G
- ▶ curr: G; **H, D, B, A** : H
- ▶ curr: H; **D, B, A** : D
- ▶ curr: D; **O, N, I, E, B, A** : O
- ▶ curr: O **P, N, I, E, B, A** : P
- ▶ curr: P **N, I, E, B, A** : N
- ▶ curr: N **I, E, B, A** : I
- ▶ curr: I **E, B, A** : E
- ▶ curr: E **B, A** : B
- ▶ curr: B **L, F, C, A** : L
- ▶ curr: L **M, F, C, A** : M
- ▶ curr: M **F, C, A** : F
- ▶ curr: F **C, A** : C
- ▶ curr: C **A** : A e termino