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Calculates the position of a ball at $t = 1$ sec, given the initial velocity of the ball.

```
v0 = 5;
theta = 45;
g = 9.81;
t = 1;
x = v0*cosd(theta)*t;
y = v0*sind(theta)*t-g*t^2/2;
```

Calculates the positions of the ball described in the last section at $t = 0, 0.2, 0.4, 0.6, 0.8$, and 1.0 seconds.

```
v0 = 5;
theta = 45;
g = 9.81;
t = 0:0.2:1
x= v0*cosd(theta)*t
y= v0*sind(theta)*t-g*t.^2/2
```

$t =$

0	0.2000	0.4000	0.6000	0.8000	1.0000
---	--------	--------	--------	--------	--------

$x =$

0 0.7071 1.4142 2.1213 2.8284 3.5355

$y =$

0 0.5109 0.6294 0.3555 -0.3108 -1.3695

Plots a trajectory curve of the ball described before.

```
v0 = 5; theta = 45; g = 9.81;  
t = 0:0.02:1  
x= v0*cosd(theta)*t  
y= v0*sind(theta)*t-g*t.^2/2  
plot(x,y,'b'); grid;  
title('Trajectory of a Ball')  
xlabel('Distance (m)')  
ylabel('Height (m)')
```

$t =$

Columns 1 through 7

0 0.0200 0.0400 0.0600 0.0800 0.1000 0.1200

Columns 8 through 14

0.1400 0.1600 0.1800 0.2000 0.2200 0.2400 0.2600

Columns 15 through 21

0.2800 0.3000 0.3200 0.3400 0.3600 0.3800 0.4000

Columns 22 through 28

0.4200 0.4400 0.4600 0.4800 0.5000 0.5200 0.5400

Columns 29 through 35

0.5600 0.5800 0.6000 0.6200 0.6400 0.6600 0.6800

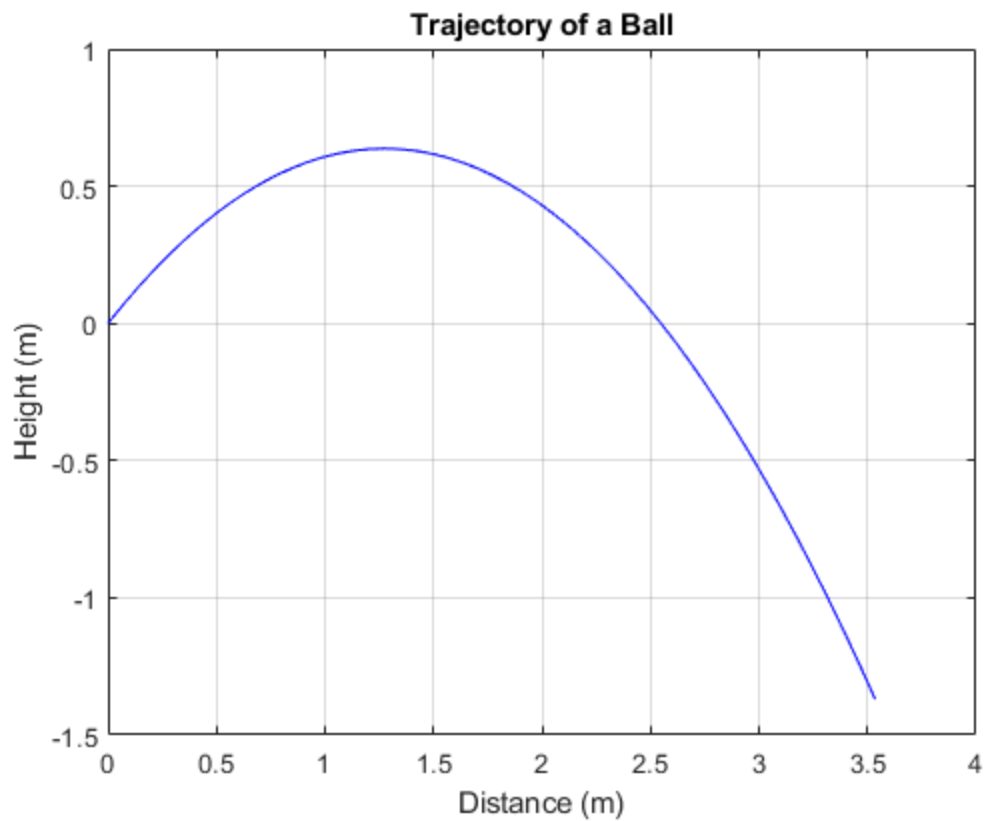
Columns 36 through 42

0.7000 0.7200 0.7400 0.7600 0.7800 0.8000 0.8200

Columns 43 through 49

	0.8400	0.8600	0.8800	0.9000	0.9200	0.9400	0.9600
Columns 50 through 51							
	0.9800	1.0000					
x =							
Columns 1 through 7							
	0	0.0707	0.1414	0.2121	0.2828	0.3536	0.4243
Columns 8 through 14							
	0.4950	0.5657	0.6364	0.7071	0.7778	0.8485	0.9192
Columns 15 through 21							
	0.9899	1.0607	1.1314	1.2021	1.2728	1.3435	1.4142
Columns 22 through 28							
	1.4849	1.5556	1.6263	1.6971	1.7678	1.8385	1.9092
Columns 29 through 35							
	1.9799	2.0506	2.1213	2.1920	2.2627	2.3335	2.4042
Columns 36 through 42							
	2.4749	2.5456	2.6163	2.6870	2.7577	2.8284	2.8991
Columns 43 through 49							
	2.9698	3.0406	3.1113	3.1820	3.2527	3.3234	3.3941
Columns 50 through 51							
	3.4648	3.5355					
y =							
Columns 1 through 7							
	0	0.0687	0.1336	0.1945	0.2515	0.3045	0.3536
Columns 8 through 14							
	0.3988	0.4401	0.4775	0.5109	0.5404	0.5660	0.5877
Columns 15 through 21							

0.6054	0.6192	0.6291	0.6351	0.6371	0.6352	0.6294
Columns 22 through 28						
0.6197	0.6060	0.5884	0.5669	0.5415	0.5122	0.4789
Columns 29 through 35						
0.4417	0.4006	0.3555	0.3065	0.2537	0.1968	0.1361
Columns 36 through 42						
0.0714	0.0028	-0.0697	-0.1461	-0.2265	-0.3108	-0.3990
Columns 43 through 49						
-0.4911	-0.5872	-0.6872	-0.7911	-0.8989	-1.0107	-1.1263
Columns 50 through 51						
-1.2459	-1.3695					



Plots a spiral curve described by the equations $x = \cos(\#)$, $y = \sin(\#)$, and $z = \#/8$, where $\#$ runs from 0 to 8π .

```
theta = 0:5:360*4;
x= cosd(theta)
y= sind(theta);
z = theta/(pi);
plot3(x,y,z, 'r')
```

x =

Columns 1 through 7

1.0000	0.9962	0.9848	0.9659	0.9397	0.9063	0.8660
--------	--------	--------	--------	--------	--------	--------

Columns 8 through 14

0.8192	0.7660	0.7071	0.6428	0.5736	0.5000	0.4226
--------	--------	--------	--------	--------	--------	--------

Columns 15 through 21

0.3420	0.2588	0.1736	0.0872	0	-0.0872	-0.1736
--------	--------	--------	--------	---	---------	---------

Columns 22 through 28

-0.2588	-0.3420	-0.4226	-0.5000	-0.5736	-0.6428	-0.7071
---------	---------	---------	---------	---------	---------	---------

Columns 29 through 35

-0.7660	-0.8192	-0.8660	-0.9063	-0.9397	-0.9659	-0.9848
---------	---------	---------	---------	---------	---------	---------

Columns 36 through 42

-0.9962	-1.0000	-0.9962	-0.9848	-0.9659	-0.9397	-0.9063
---------	---------	---------	---------	---------	---------	---------

Columns 43 through 49

-0.8660	-0.8192	-0.7660	-0.7071	-0.6428	-0.5736	-0.5000
---------	---------	---------	---------	---------	---------	---------

Columns 50 through 56

-0.4226	-0.3420	-0.2588	-0.1736	-0.0872	0	0.0872
---------	---------	---------	---------	---------	---	--------

Columns 57 through 63

0.1736	0.2588	0.3420	0.4226	0.5000	0.5736	0.6428
--------	--------	--------	--------	--------	--------	--------

Columns 64 through 70

0.7071	0.7660	0.8192	0.8660	0.9063	0.9397	0.9659
Columns 71 through 77						
0.9848	0.9962	1.0000	0.9962	0.9848	0.9659	0.9397
Columns 78 through 84						
0.9063	0.8660	0.8192	0.7660	0.7071	0.6428	0.5736
Columns 85 through 91						
0.5000	0.4226	0.3420	0.2588	0.1736	0.0872	0
Columns 92 through 98						
-0.0872	-0.1736	-0.2588	-0.3420	-0.4226	-0.5000	-0.5736
Columns 99 through 105						
-0.6428	-0.7071	-0.7660	-0.8192	-0.8660	-0.9063	-0.9397
Columns 106 through 112						
-0.9659	-0.9848	-0.9962	-1.0000	-0.9962	-0.9848	-0.9659
Columns 113 through 119						
-0.9397	-0.9063	-0.8660	-0.8192	-0.7660	-0.7071	-0.6428
Columns 120 through 126						
-0.5736	-0.5000	-0.4226	-0.3420	-0.2588	-0.1736	-0.0872
Columns 127 through 133						
0	0.0872	0.1736	0.2588	0.3420	0.4226	0.5000
Columns 134 through 140						
0.5736	0.6428	0.7071	0.7660	0.8192	0.8660	0.9063
Columns 141 through 147						
0.9397	0.9659	0.9848	0.9962	1.0000	0.9962	0.9848
Columns 148 through 154						
0.9659	0.9397	0.9063	0.8660	0.8192	0.7660	0.7071
Columns 155 through 161						
0.6428	0.5736	0.5000	0.4226	0.3420	0.2588	0.1736

Columns 162 through 168

0.0872	0	-0.0872	-0.1736	-0.2588	-0.3420	-0.4226
--------	---	---------	---------	---------	---------	---------

Columns 169 through 175

-0.5000	-0.5736	-0.6428	-0.7071	-0.7660	-0.8192	-0.8660
---------	---------	---------	---------	---------	---------	---------

Columns 176 through 182

-0.9063	-0.9397	-0.9659	-0.9848	-0.9962	-1.0000	-0.9962
---------	---------	---------	---------	---------	---------	---------

Columns 183 through 189

-0.9848	-0.9659	-0.9397	-0.9063	-0.8660	-0.8192	-0.7660
---------	---------	---------	---------	---------	---------	---------

Columns 190 through 196

-0.7071	-0.6428	-0.5736	-0.5000	-0.4226	-0.3420	-0.2588
---------	---------	---------	---------	---------	---------	---------

Columns 197 through 203

-0.1736	-0.0872	0	0.0872	0.1736	0.2588	0.3420
---------	---------	---	--------	--------	--------	--------

Columns 204 through 210

0.4226	0.5000	0.5736	0.6428	0.7071	0.7660	0.8192
--------	--------	--------	--------	--------	--------	--------

Columns 211 through 217

0.8660	0.9063	0.9397	0.9659	0.9848	0.9962	1.0000
--------	--------	--------	--------	--------	--------	--------

Columns 218 through 224

0.9962	0.9848	0.9659	0.9397	0.9063	0.8660	0.8192
--------	--------	--------	--------	--------	--------	--------

Columns 225 through 231

0.7660	0.7071	0.6428	0.5736	0.5000	0.4226	0.3420
--------	--------	--------	--------	--------	--------	--------

Columns 232 through 238

0.2588	0.1736	0.0872	0	-0.0872	-0.1736	-0.2588
--------	--------	--------	---	---------	---------	---------

Columns 239 through 245

-0.3420	-0.4226	-0.5000	-0.5736	-0.6428	-0.7071	-0.7660
---------	---------	---------	---------	---------	---------	---------

Columns 246 through 252

-0.8192	-0.8660	-0.9063	-0.9397	-0.9659	-0.9848	-0.9962
---------	---------	---------	---------	---------	---------	---------

Columns 253 through 259

-1.0000	-0.9962	-0.9848	-0.9659	-0.9397	-0.9063	-0.8660
---------	---------	---------	---------	---------	---------	---------

Columns 260 through 266

-0.8192	-0.7660	-0.7071	-0.6428	-0.5736	-0.5000	-0.4226
---------	---------	---------	---------	---------	---------	---------

Columns 267 through 273

-0.3420	-0.2588	-0.1736	-0.0872	0	0.0872	0.1736
---------	---------	---------	---------	---	--------	--------

Columns 274 through 280

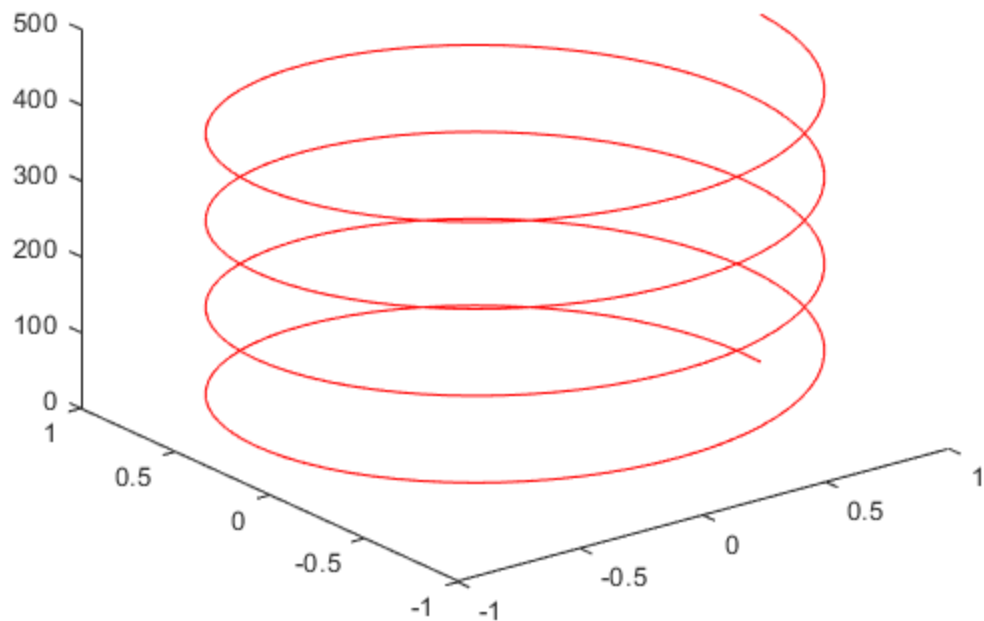
0.2588	0.3420	0.4226	0.5000	0.5736	0.6428	0.7071
--------	--------	--------	--------	--------	--------	--------

Columns 281 through 287

0.7660	0.8192	0.8660	0.9063	0.9397	0.9659	0.9848
--------	--------	--------	--------	--------	--------	--------

Columns 288 through 289

0.9962	1.0000
--------	--------



Runs the commands in the last section as a script file.

```
v0=5; theta = 360/4; g =9.81
t = 0:0.02:1
x = v0*cosd(theta)*t;
y = v0*sind(theta)*t-g*t.^2/2;
disp(x)
disp(y)
plot(x,y)
title('Trajectory of a Ball')
xlabel('Distance (m)')
ylabel('Height (m)')
```

g =

9.8100

t =

Columns 1 through 7

0	0.0200	0.0400	0.0600	0.0800	0.1000	0.1200
---	--------	--------	--------	--------	--------	--------

Columns 8 through 14

0.1400	0.1600	0.1800	0.2000	0.2200	0.2400	0.2600
--------	--------	--------	--------	--------	--------	--------

Columns 15 through 21

0.2800	0.3000	0.3200	0.3400	0.3600	0.3800	0.4000
--------	--------	--------	--------	--------	--------	--------

Columns 22 through 28

0.4200	0.4400	0.4600	0.4800	0.5000	0.5200	0.5400
--------	--------	--------	--------	--------	--------	--------

Columns 29 through 35

0.5600	0.5800	0.6000	0.6200	0.6400	0.6600	0.6800
--------	--------	--------	--------	--------	--------	--------

Columns 36 through 42

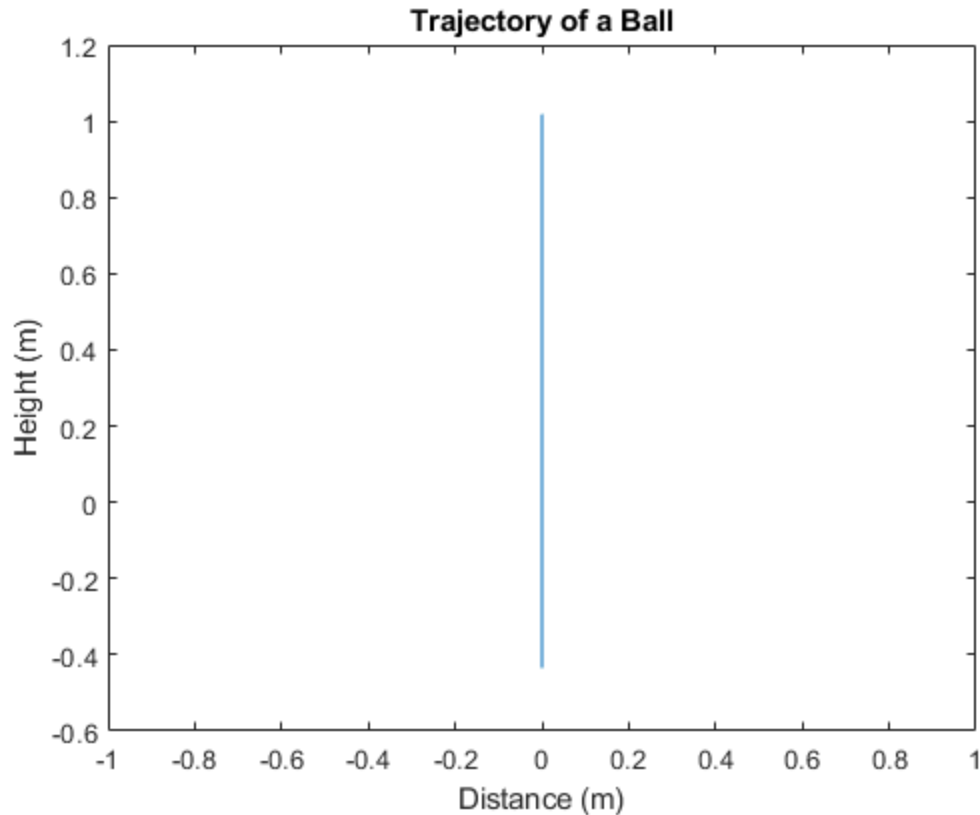
0.7000	0.7200	0.7400	0.7600	0.7800	0.8000	0.8200
--------	--------	--------	--------	--------	--------	--------

Columns 43 through 49

0.8400	0.8600	0.8800	0.9000	0.9200	0.9400	0.9600
--------	--------	--------	--------	--------	--------	--------

Columns 50 through 51

0.9800	1.0000										
Columns 1 through 13											
0	0	0	0	0	0	0	0	0	0	0	0
0	0										
Columns 14 through 26											
0	0	0	0	0	0	0	0	0	0	0	0
0	0										
Columns 27 through 39											
0	0	0	0	0	0	0	0	0	0	0	0
0	0										
Columns 40 through 51											
0	0	0	0	0	0	0	0	0	0	0	0
0											
Columns 1 through 7											
	0	0.0874	0.1710	0.2505	0.3262	0.3979	0.4658				
Columns 8 through 14											
	0.5297	0.5896	0.6457	0.6978	0.7460	0.7903	0.8306				
Columns 15 through 21											
	0.8670	0.8995	0.9281	0.9528	0.9735	0.9903	1.0032				
Columns 22 through 28											
	1.0122	1.0172	1.0183	1.0155	1.0087	0.9981	0.9835				
Columns 29 through 35											
	0.9650	0.9425	0.9162	0.8859	0.8517	0.8136	0.7715				
Columns 36 through 42											
	0.7255	0.6756	0.6218	0.5641	0.5024	0.4368	0.3673				
Columns 43 through 49											
	0.2938	0.2164	0.1352	0.0499	-0.0392	-0.1323	-0.2293				
Columns 50 through 51											
	-0.3302	-0.4350									



Plots the trajectory curves of the ball for elevation angles # varying from # 8to 3# 8. The collection of the curves form a surface in the height-distance-# space.

```
v0=5; g =9.81;
time = 0:0.01:1; n = length(time);
theta = 45:1.8:135
m = length(theta);
time_arr = repmat(time,m,1);
theta_arr = repmat(theta',1,n);
X = v0*cosd(theta_arr).*time_arr;
Z = v0*sind(theta_arr).*time_arr-g*time_arr.^2/2;
surf(X,theta_arr,Z) % #####

hold on % #####
Z = zeros(m,n); %##51X101#matrix
mesh(X,theta_arr,Z)
xlabel('Distance (m)')
ylabel('Angle (radian)')
zlabel('Height (m)')
colorbar % #####
```

axis vis3d %#####

theta =

Columns 1 through 7

45.0000 46.8000 48.6000 50.4000 52.2000 54.0000 55.8000

Columns 8 through 14

57.6000 59.4000 61.2000 63.0000 64.8000 66.6000 68.4000

Columns 15 through 21

70.2000 72.0000 73.8000 75.6000 77.4000 79.2000 81.0000

Columns 22 through 28

82.8000 84.6000 86.4000 88.2000 90.0000 91.8000 93.6000

Columns 29 through 35

95.4000 97.2000 99.0000 100.8000 102.6000 104.4000 106.2000

Columns 36 through 42

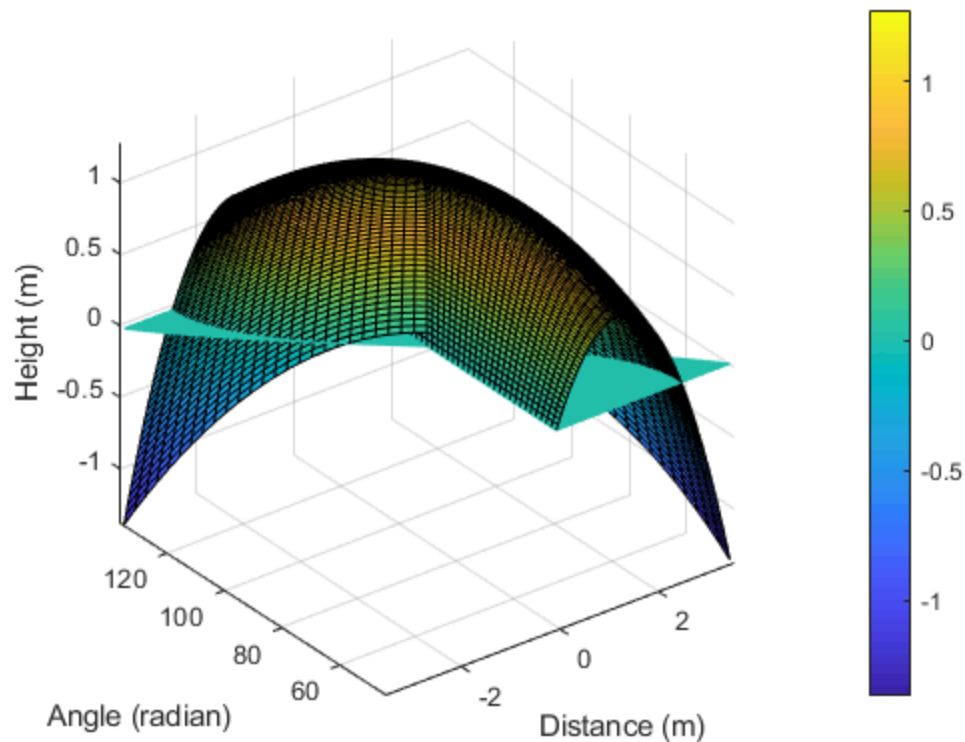
108.0000 109.8000 111.6000 113.4000 115.2000 117.0000 118.8000

Columns 43 through 49

120.6000 122.4000 124.2000 126.0000 127.8000 129.6000 131.4000

Columns 50 through 51

133.2000 135.0000



Derives an expression for the range of the ball as a function of the elevation angle and plots a range-versus-angle curve. (a)

```

clc % ##command window
clear all % ##WorkSpace##
close all % #####

syms v0 theta g t % syms #####
x = v0*cosd(theta)*t
y = v0*sind(theta)*t-g*t^2/2
solutions = solve(y,t) % solve #####
t0 = solutions(2) % solutions(index) ##index####
range = subs(x,t,t0) % subs(S,OLD,NEW) #####S#####OLD#####NEW#
range = simplify(range) % #####
range = subs(range,[v0,g],[5,9.81]);
fplot(range,[360/8,360*3/8]) % fplot : #####
title('Range as Function of Angle (a)')
xlabel('Elevation angle ')
ylabel('Range (m)')

```

x =

$$t*v0*\cos((\pi*\theta)/180)$$

$$y =$$

$$t*v0*\sin((\pi*\theta)/180) - (g*t^2)/2$$

$$\text{solutions} =$$

$$(2*v0*\sin((\pi*\theta)/180))^0/g$$

$$t0 =$$

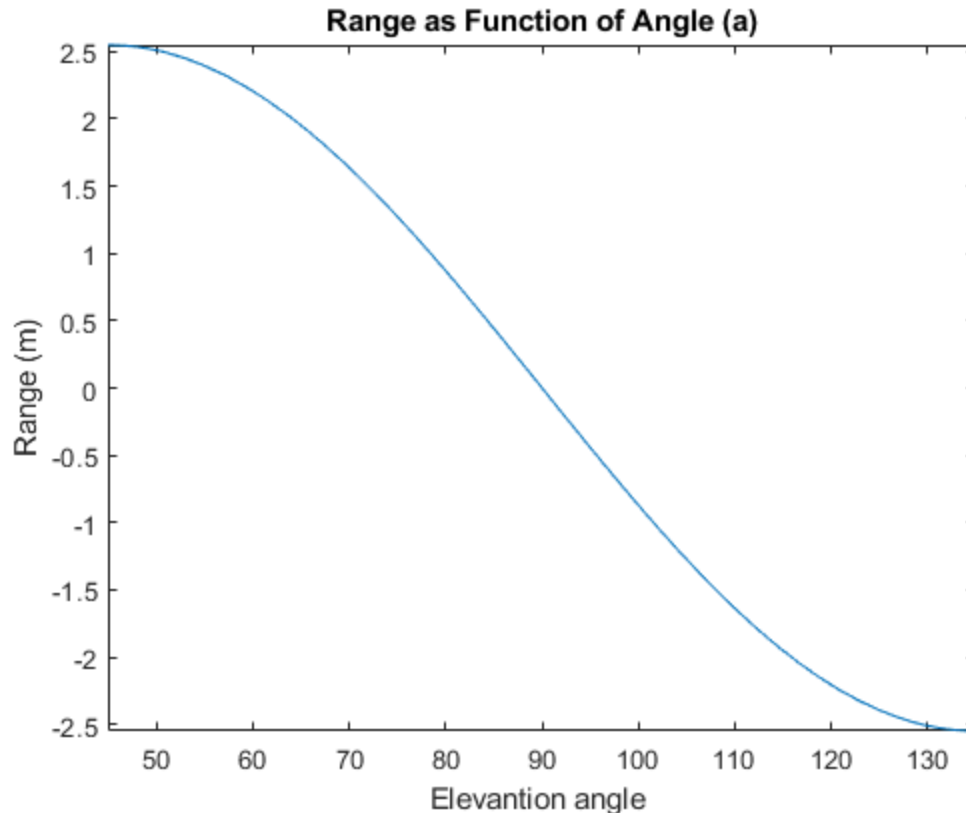
$$(2*v0*\sin((\pi*\theta)/180))/g$$

$$\text{range} =$$

$$(2*v0^2*\cos((\pi*\theta)/180)*\sin((\pi*\theta)/180))/g$$

$$\text{range} =$$

$$(v0^2*\sin((\pi*\theta)/90))/g$$



Derives an expression for the range of the ball as a function of the elevation angle and plots a range-versus-angle curve. (b)

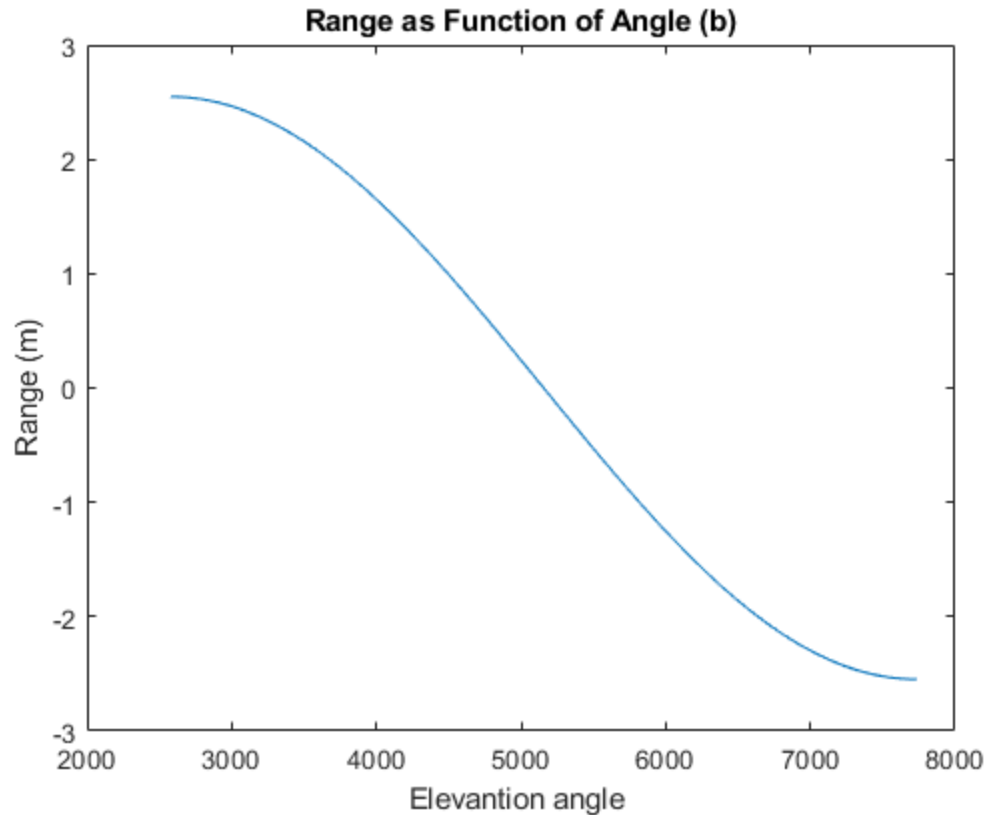
```

clc % ##command window
clear all % ##WorkSpace##
close all % #####

syms v0 theta g t % syms #####
x = v0*cosd(theta)*t
y = v0*sind(theta)*t-g*t^2/2
solutions = solve(y,t) % solve #####
t0 = solutions(2) % solutions(index) ##index####
range = subs(x,t,t0) % subs(S,OLD,NEW) #####S#####OLD#####NEW#
range = simplify(range) % #####
range = subs(range,[v0,g],[5,9.81])
func = matlabFunction(range)
theta = [360/8:360/200:360*(3/8)];
range = func(theta);
plot(theta*180/pi,range)
title('Range as Function of Angle (b)')
xlabel('Elevation angle ')
ylabel('Range (m)')

```

```
x =  
  
t*v0*cos((pi*theta)/180)  
  
y =  
  
t*v0*sin((pi*theta)/180) - (g*t^2)/2  
  
solutions =  
  
      0  
(2*v0*sin((pi*theta)/180))/g  
  
t0 =  
  
(2*v0*sin((pi*theta)/180))/g  
  
range =  
  
(2*v0^2*cos((pi*theta)/180)*sin((pi*theta)/180))/g  
  
range =  
  
(v0^2*sin((pi*theta)/90))/g  
  
range =  
  
(2500*sin((pi*theta)/90))/981  
  
func =  
  
function_handle with value:  
  
@(theta)sin(theta.*pi.*(1.0./9.0e1)).*2.54841997961264
```

Calculates and tabulates the positions of the ball at $t = 0, 0.1, 0.2, \dots, 1$ sec, allowing the input of an initial speed and an elevation angle.

```
disp('Enter initial speed (m/s): ');
v0 = 5
disp('Enter elevation angle: ');
theta = 45
g = 9.81; t = 0:0.1:1;
x = v0*cosd(theta)*t;
y = v0*sind(theta)*t-g*t.^2/2;
Table = [t',x',y'];
fprintf('\n time (s)    x (m)    y (m)\n')
fprintf('%10.1f %9.3f %9.3f\n',Table')
```

Enter initial speed (m/s):

v0 =

5

Enter elevation angle:

theta =

<i>time (s)</i>	<i>x (m)</i>	<i>y (m)</i>
0.0	0.000	0.000
0.1	0.354	0.305
0.2	0.707	0.511
0.3	1.061	0.619
0.4	1.414	0.629
0.5	1.768	0.542
0.6	2.121	0.356
0.7	2.475	0.071
0.8	2.828	-0.311
0.9	3.182	-0.791
1.0	3.536	-1.369

Creates a trajectory table, write the table to a text file, reads the table from the text file, and prints the table on the screen.

```

v0 = 5; theta = 45; g = 9.81;
t = 0:0.1:1;
x = v0*cosd(theta)*t;
y = v0*sind(theta)*t-g*t.^2/2;
Table = [t ; x ; y];
% Write to a file
file = fopen('#####/Ch1/dat/Datafile01_10.dat','w');
fprintf(file, '   Time (s)    x (m)   y (m)\n');
fprintf(file, '%10.1f %9.3f %9.3f\n',Table');
fclose(file);
% Read from the file
file = fopen('#####/Ch1/dat/Datafile01_10.dat','r');
fscanf(file, '   Time (s)    x (m)   y (m)\n');
Table = fscanf(file, '   %f %f %f\n',[3,11]);
fclose(file);
% Print on the screen
fprintf( '   Time (s)    x (m)   y (m)\n');
fprintf('%10.1f %9.3f %9.3f\n',Table')

```

<i>Time (s)</i>	<i>x (m)</i>	<i>y (m)</i>
0.0	0.300	0.600
0.9	0.400	1.400
2.5	3.500	0.500
0.5	-0.300	0.100
0.4	0.700	1.000
0.7	1.768	2.828
0.0	0.619	0.356
-0.8	0.200	0.500
0.8	0.000	1.061
2.1	3.182	0.305

0.6 0.071 -1.369

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