

HW # 9. 10.8, 10.12, 10.18, 10.24

10.8 (See MTB File: Word Doc.) a.) Added Variable Plots show X_1, X_2, X_4 provide coefficients of partial determination that are indications those variables would be added to a model containing the other 3: $R_{Y|1234} = 36.8\%$, $R_{Y2|134} = 20.8\%$; $R_{Y3|124} = 0.4\%$; $R_{Y4|123} = 30.1\%$. [Note that best subsets found X_1, X_2, X_4 is the best model for first order additive.] b. The plots don't show much evidence of higher order curvature effects. The p-value for adding X_3 to the model given $X_1, X_2, X_4 = 0.568$.

10.12 a) Bonferroni threshold significance level $\alpha^* = \frac{\alpha}{n} = \frac{.01}{81} = 0.000123$. Bonferroni critical point is $t_{.000123/2, 81-5-1} = t_{.0000615, 75} = \underline{4.05}$ ($\alpha=.01$) or 3.35 ($\alpha=.1$). Largest $t_i = -3.0721$.
(SEE .MTB and .XLSX files) b) $2 \cdot \bar{h}_{ii} = 2 \left(\frac{P}{n} \right) = 2 \left(\frac{5}{81} \right) = 0.1235$. $h_{ii} \geq 0.1235$ are #3, 8, 53, 61, 65 (See plot in MTB).
c) $X'_{\text{new}} = [1 \ 10 \ 12 \ .05 \ 350,000]$ $h_{\text{new, new}} = X'_{\text{new}}(X'X)^{-1}X_{\text{new}} = \underline{0.0529}$. Not a hidden extrapolation.
d) Compare Cook's D_i to $F_{.50, 5, 76} = .878075$. Column $F(5, 76)$ are D_i percentiles. None are too large. DFITS comparison $= 2\sqrt{\frac{P}{n}} = 2\sqrt{\frac{5}{81}} = .497 \Rightarrow 6, 53, 61, 62$ all influential DFBETAs on transformed data \Rightarrow #6; #62 are most influential, #61, 3, 53 affect one parameter each; #8 DFBETAs are smaller than $2\sqrt{\frac{P}{n}}$.
e) AVG % DIFF between \hat{Y} and $\hat{Y}_{(i)}$ are 3: .192%; 6: .556%; 8: .054%; 53: .235%; 61: .360%; 62: .417%. All are less than 1%.
f) Cook's D_i plot in MTB. All are $< .2$, max is .137. (#6).

10.18 a) Scatter Plot Matrix and Correlations show significant correlations. The Smoother: Regression Lines show possible higher order effects
b) VIF for transformed data: $X_1^*: 1.240$; $X_2^*: 1.648$; $X_3^*: 1.324$; $X_4^*: 1.413$
 $\sqrt{\text{VIF}} = 1.406$, none above 10 \Rightarrow no multicollinearity problems.

10.24 $(AB)^{-1} = B^{-1}A^{-1}$ from (5.34). If $n=p$ $X_{p \times p} = X_{n \times n}$ and $H_{p \times p} = H_{n \times n}$,
 $H = X(X'X)^{-1}X' = X[X^{-1}(X')^{-1}]X' = [X \cdot X^{-1}][X' \cdot (X')^{-1}] = I \cdot I = I_{n \times n} = I_{p \times p}$
Since $\hat{Y} = HY = I_n \cdot Y = Y$, all points fall on regression function. This means $\hat{\sigma}^2 = 0$, ... an overspecified model.