

# **Generative Models for Aircrafts Icing Image Prediction**

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李云艾

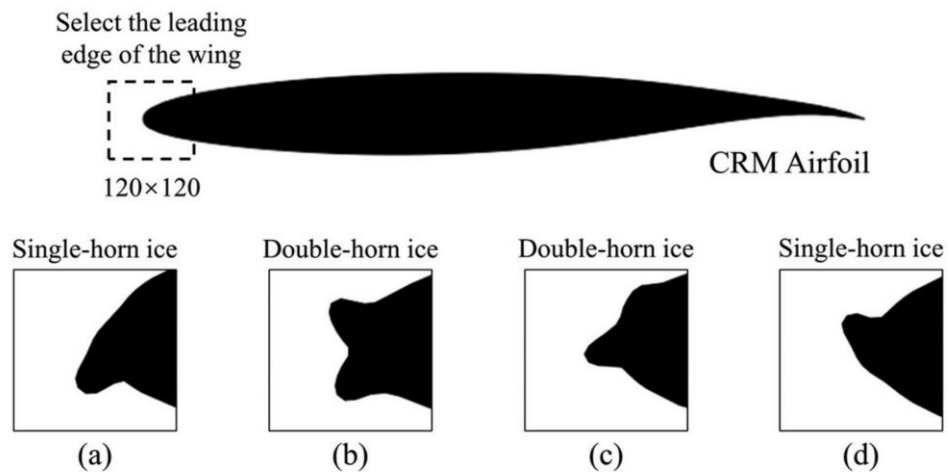
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# Background

- icing image:

wing (fixed shape) + ice (to predict under certain icing conditions)



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Icing condition

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MVD (medium volume diameter)( $\mu\text{m}$ )

LWC (liquid water content)/( $\text{g}/\text{m}^3$ )

Temperature ( $^{\circ}\text{C}$ )

Icing time (s)

Velocity (m/s)

AOA (angle of attack) (deg)

Chord length (inch)

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low dim input (7)  $\rightarrow$  high dim out put ( $142 \times 142$ ) (categories unknown)

# A Common Way to Process the Input Data

- Inspired by Conditional GAN

**icing condition** (dimension increased by NN)

+

**original wing image without ice** (dimension decreased)

to (40\*40)

# Original VAE Model

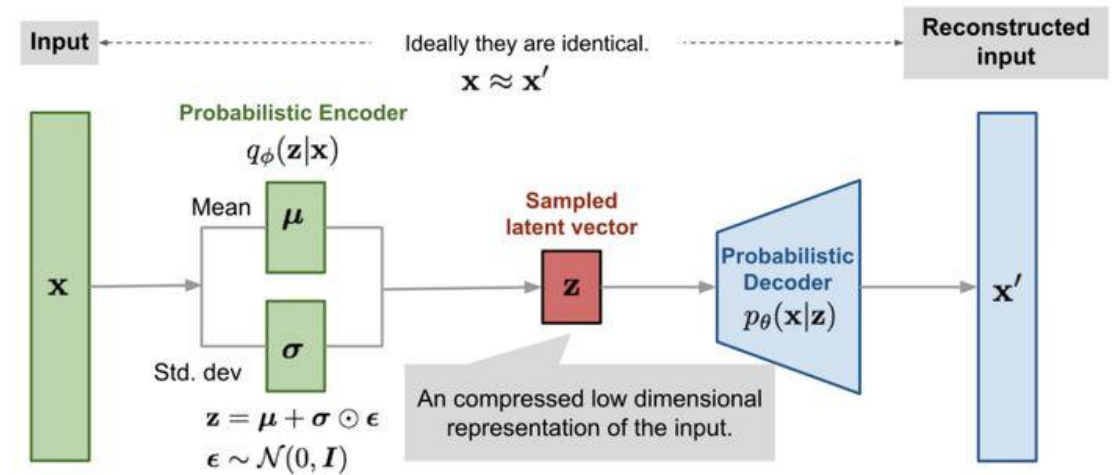
- **basic model structure:**

**parameters:**


input&output: 142\*142 1-channel image

latent dimension: 1024

- **loss**=KL-divergence + WeightedFocal\_loss
- **KL-divergence** (check next slide)
- **WeightedFocal\_loss**=  (reduces the relative loss for well-classified examples ( $p > 0.5$ ), putting more focus on hard, misclassified examples)
- **problem: vanishing KL loss** (Posterior Collapse)



# Modified Model : VAE + BN

- Problems : the KL between  can be computed as:



When the decoder is autoregressive, it can recover the data independent of the latent  $z$  (only by noises). The optimization will encourage the approximate posterior to approach the prior which results to the zero value of the K.

- Solutions: 1. Avoid posterior collapse by **keeping the expectation of the KL's distribution positive**. The batch normalization to the parameters ensure a positive lower bound of this expectation.
- 2. Cost annealing : Gradually increase weight on the KL divergence term

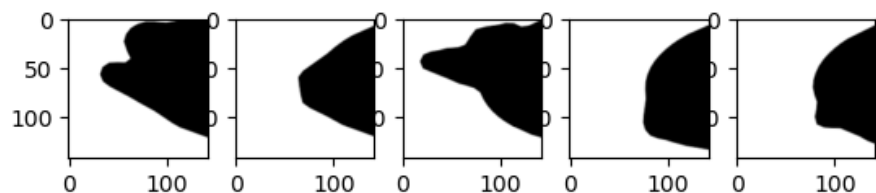
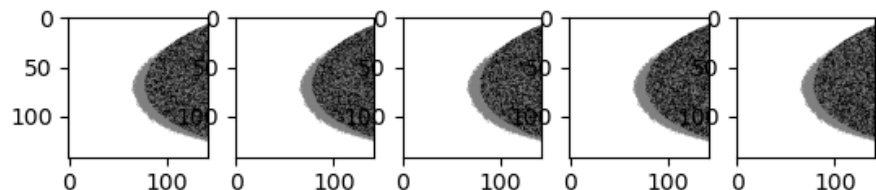
Qile Zhu, Jianlin Su *A Batch Normalized Inference Network Keeps the KL Vanishing Away*

Bowman et al. *Generating sentences from a continuous space*. CONLL 2016.

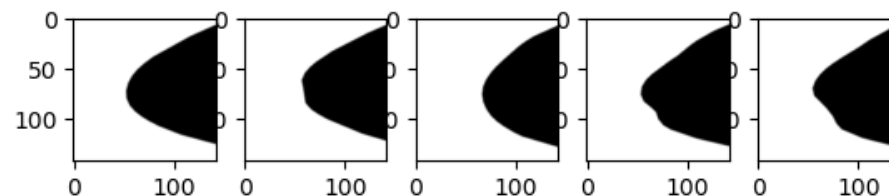
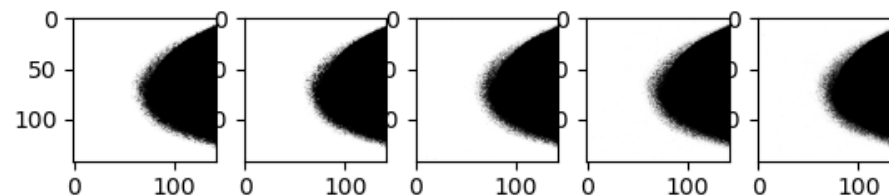
# Results

×No clear differences between generated images

(The model still doesn't work better after putting a weighted mask on the non-wing area ( as below ) )



×Poor performance on predicting irregular icing images



PSNR MSE

14.49 0.035

15.30 0.029

18.34 0.014 Average PSNR :

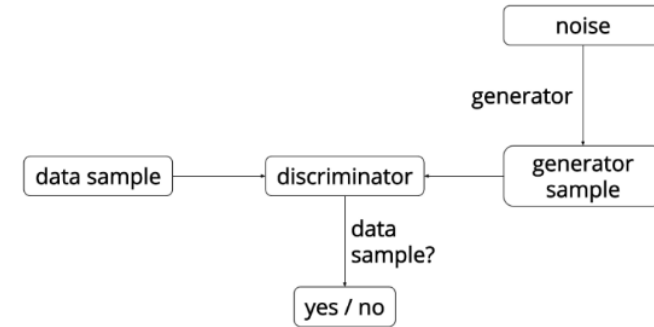
15.42 0.028 14

15.46 0.028 ( batch\_size=64 )

# Generative Adversarial Network

- Basic model structure:
- loss function:

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))]$$



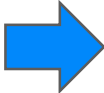
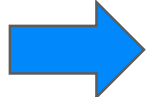
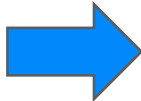
- for fixed generator, , to learn to classify fake images  $D(G(z))=0$  and real images ( $D(x)=0$ )
- for fixed discriminator,  to train generator model that makes D's output 0
- Problem: discriminator\_loss ↓ ( and vanishes ) generator\_loss ↑ (fail to generate images that could be mistaken for real data)

Solutions:

- add Gauss noise to better train the discriminator (failed)
- use [wgan](#)



# Introduction to Wasserstein GAN

- classification(discriminator)  regression("critic")
- **Modifications Details**
  - optimizer** momentum method × Adam  RMSprop (unstable loss gradient )
  - no sigmoid before output ( no longer a 0-1 classifier )
  - a **clip** on parameters to ensure Lipschitz Continuous ( for the convergence )
  - **no log term** in the loss function : (JS divergence  EM/Wasserstein distance)

$$W(P_r, P_g) = \inf_{\gamma \sim \Pi(P_r, P_g)} \mathbb{E}_{(x, y) \sim \gamma} [\|x - y\|]$$

$$K \cdot W(P_r, P_g) \approx \max_{w: |f_w|_L \leq K} \mathbb{E}_{x \sim P_r} [f_w(x)] - \mathbb{E}_{x \sim P_g} [f_w(x)]$$

# Principle behind Wasserstein GAN

- Original Loss:  $-P_r(x) \log D(x) - P_g(x) \log[1 - D(x)]$

- Let its derivative with respect to D be 0:  $D^*(x) = \frac{P_r(x)}{P_r(x) + P_g(x)}$

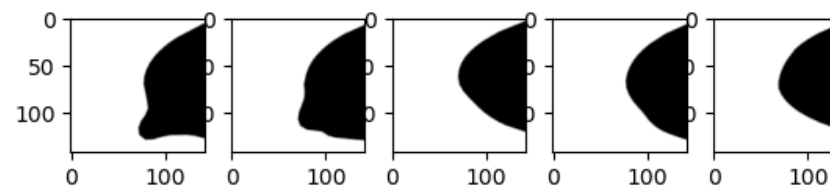
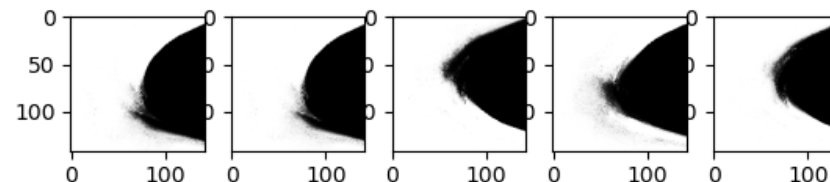
$$\mathbb{E}_{x \sim P_r} \log \frac{P_r(x)}{\frac{1}{2}[P_r(x) + P_g(x)]} + \mathbb{E}_{x \sim P_g} \log \frac{P_g(x)}{\frac{1}{2}[P_r(x) + P_g(x)]} - 2 \log 2$$

- The generator loss defined by the original GAN is equivalent to minimizing the JS divergence between the true distribution and the generated. By simple calculation it is easy to see. If the two distributions have no overlapping parts at all, or their overlapping parts are negligible, the loss is a const.
- When the support set is a low-dimensional manifold in a high-dimensional space, the
- the probability that the overlapping part of the measure is 0 is 1
- This eventually leads to a (approximate) gradient of 0 for the generator and the gradient vanishes.

# Results

Still, it's hard to train a balanced Adversial Model

- ✓ Some details ( horns ) is predicted
- × unsmooth , blur on the boundary
- × low average PSNR



**PSNR MSE**

15.97 0.025

20.56 0.008

14.26 0.037

12.47 0.056

17.74 0.017

average of a batch : 15

## **Some other possible Modifications**

- Classify the dataset
- Icing condition data pre-processing
- Other methods to put weight on the icing area