Edge flow regularizations

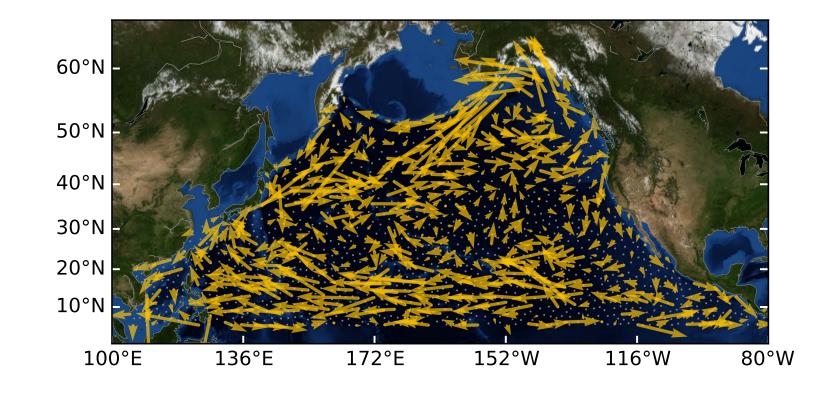
 ℓ_1, ℓ_2 regularization

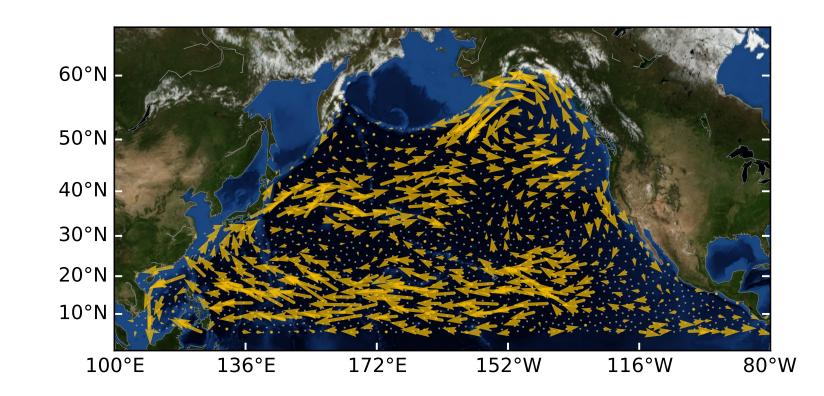
Tikhonov regularization

$$\|\mathbf{y} - \mathbf{f}\|_{2}^{2} + \gamma \cdot \|\text{div/curl}\|_{2}^{2}$$

Trend filtering

$$\|\mathbf{y} - \mathbf{f}\|_2^2 + \gamma \cdot \|\text{div/curl}\|_1$$





Tabular results

Table 1: Forex rates inference results.

Method	RMSE		NLPD		
	Diffusion	Matérn	Diffusion	Matérn	
Euclidean Line-Graph	2.17 ± 0.13 2.43 ± 0.07	2.19 ± 0.12 2.46 ± 0.07	2.12 ± 0.07 2.28 ± 0.04	2.20 ± 0.18 2.32 ± 0.03	
Non-HC	2.48 ± 0.07	2.47 ± 0.08	2.36 ± 0.07	2.34 ± 0.04	
HC	0.08 ± 0.12	0.06 ± 0.12	-3.52 ± 0.02	-3.52 ± 0.02	

Table 3: WSN inference results.

Method	Node Heads		Edge Flowrates		
THE	RMSE	NLPD	RMSE	NLPD	
Diffusion, non-HC	0.16 ± 0.05	0.72 ± 2.06	0.32 ± 0.05	0.97 ± 1.80	
Matérn, non-HC	0.16 ± 0.04	0.71 ± 2.39	0.26 ± 0.05	0.10 ± 0.13	
Diffusion, HC	0.15 ± 0.04	-0.47 ± 0.14	0.22 ± 0.03	-0.20 ± 0.13	
Matérn, HC	0.15 ± 0.04	-0.25 ± 0.48	0.23 ± 0.03	-0.45 ± 0.49	

Table C.1: Ocean current inference results.

Method	RMSE			NLPD		
	Diffusion	Matérn	Hodge Laplacian	Diffusion	Matérn	Hodge Laplacian
Euclidean	1.00 ± 0.01	1.00 ± 0.00	_	1.42 ± 0.01	1.42 ± 0.10	_
Line-Graph	0.99 ± 0.00	0.99 ± 0.00		1.41 ± 0.00	1.41 ± 0.00	
Non-HC	0.35 ± 0.00	0.35 ± 0.00	0.35 ± 0.00	0.33 ± 0.00	0.36 ± 0.03	0.33 ± 0.01
HC	0.34 ± 0.00	0.35 ± 0.00	0.35 ± 0.00	0.33 ± 0.01	0.37 ± 0.04	0.33 ± 0.01