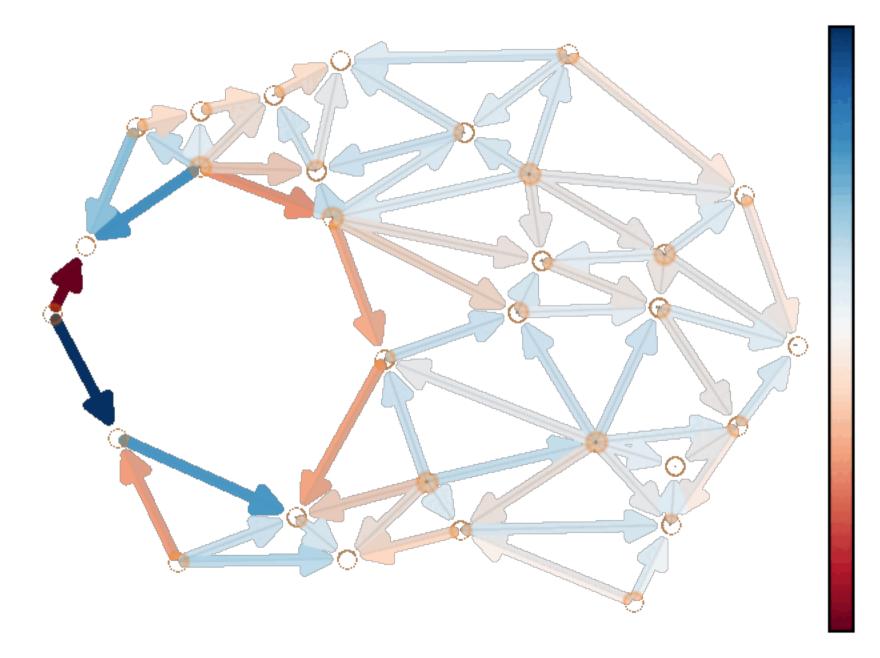
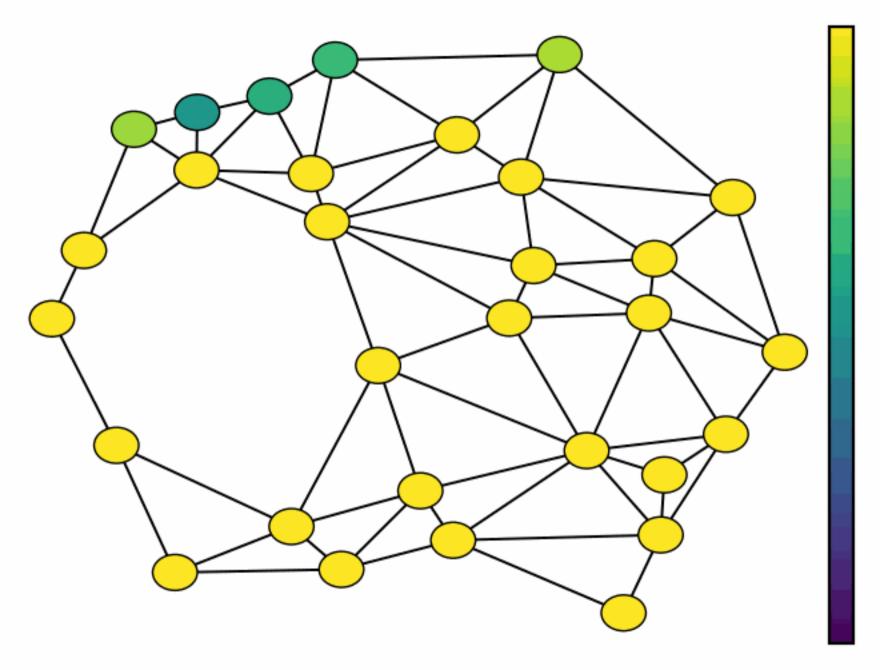
## Jiffusion GPs

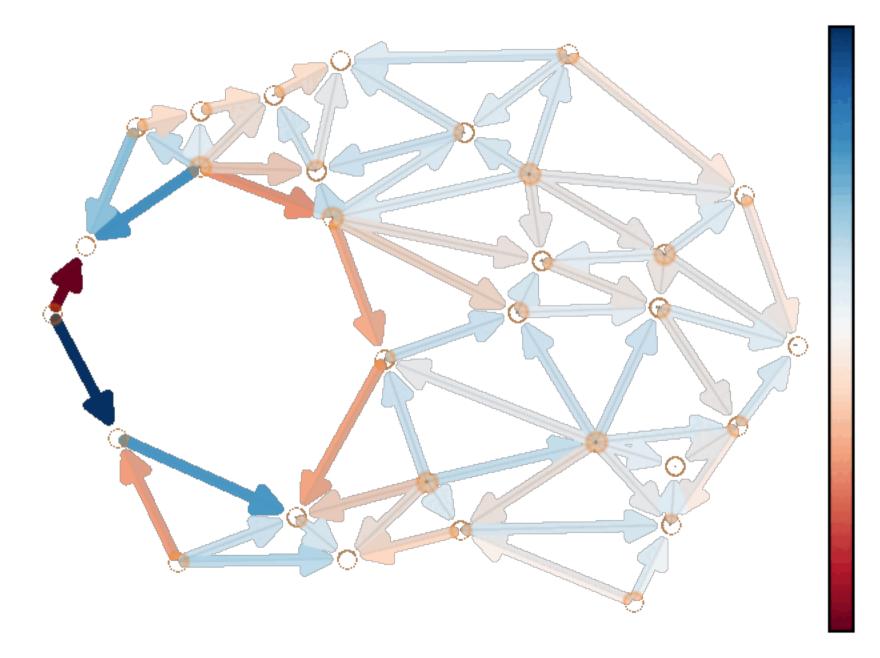
### Diffusion processes on nodes and edges

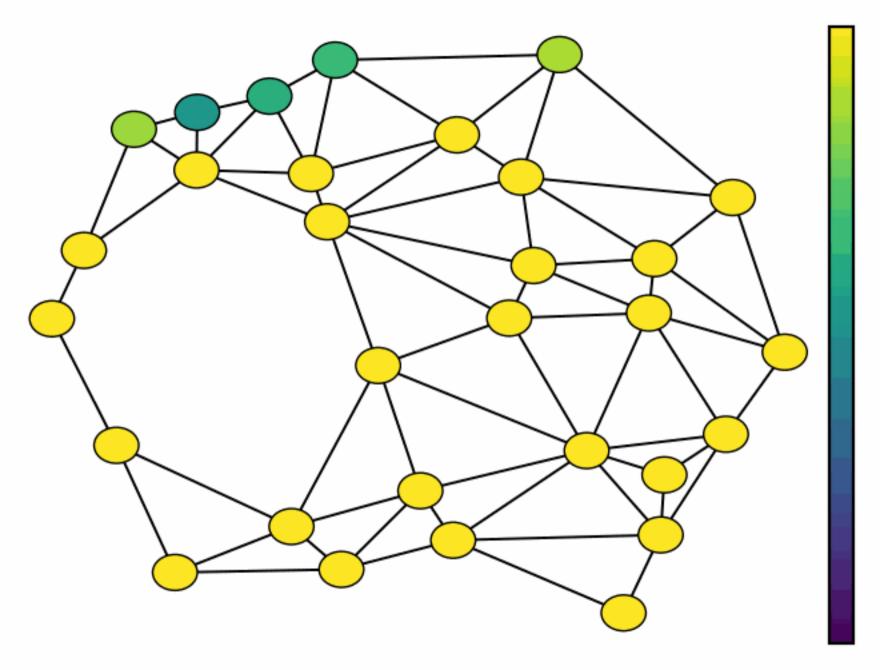




#### Diffusion on nodes

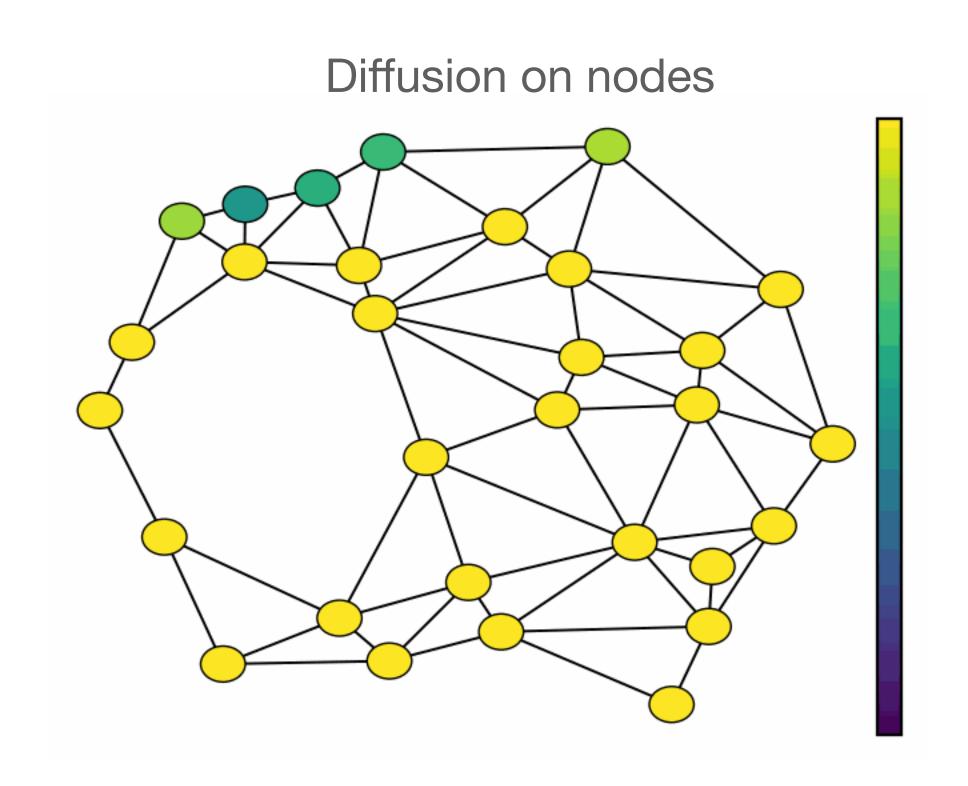
#### Diffusion on edges

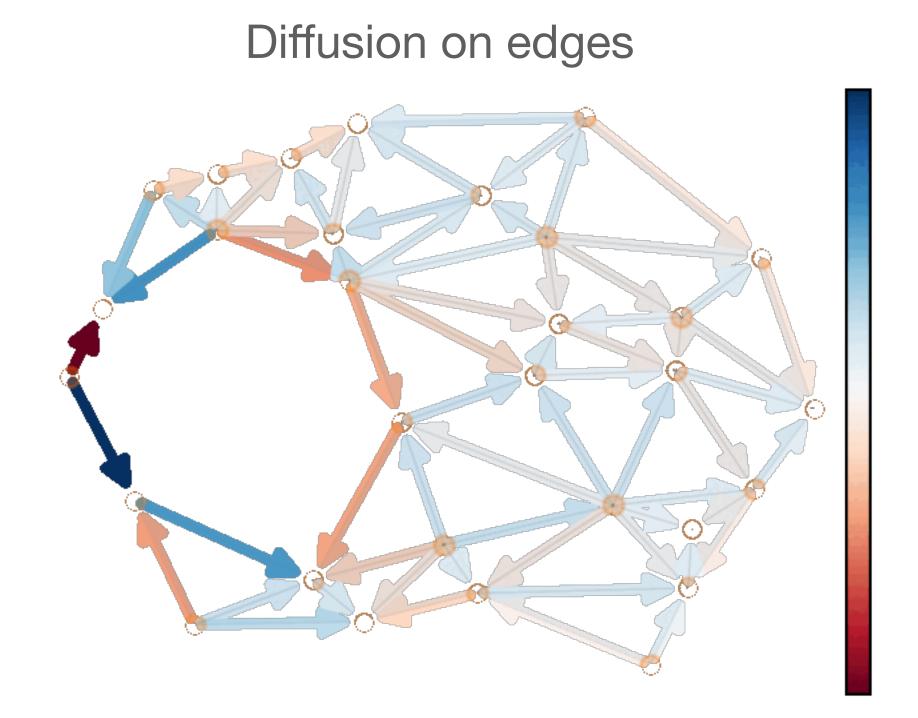




## Diffusion GPs

## Diffusion processes on nodes and edges

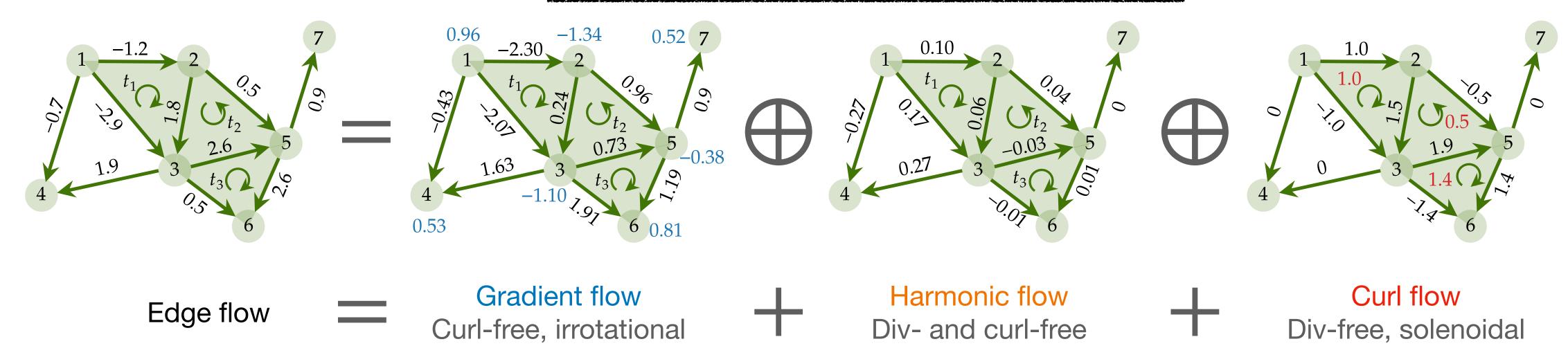




# Hodge decomposition

Lovász et al. 2004; Lim et al. 2020

$$\mathbb{R}^{N_1} = \operatorname{im}(\mathbf{B}_1^{\mathsf{T}}) \oplus \ker(\mathbf{L}_1) \oplus \operatorname{im}(\mathbf{B}_2)$$
$$\mathbf{f}_1 = \mathbf{f}_G + \mathbf{f}_H + \mathbf{f}_C$$





### Hodge-compositional Edge GP

$$\mathbf{f}_{G} \sim \mathrm{GP}(\mathbf{0}, \mathbf{K}_{G})$$
 $\mathbf{f}_{H} \sim \mathrm{GP}(\mathbf{0}, \mathbf{K}_{H})$ 
 $\mathbf{f}_{C} \sim \mathrm{GP}(\mathbf{0}, \mathbf{K}_{C})$