Discussion

- Possible directions on model training, improving
 - Simulation-free, Iterative Markovian fitting
 - Learnable references? Networked-noising process?
- Other models: e.g., based on Wasserstein gradient flow interpretation
 - TSHeat-BM driven TSBP solves a WGF of a functional [Caluya]

Dirichlet energy

$$\mathcal{F}(\nu) = c \int_{\mathbb{R}^n} \frac{1}{2} x^{\mathsf{T}} Lx \cdot \nu(x) \, \mathrm{d}x + \frac{1}{2} g^2 \int_{\mathbb{R}^n} \nu \log \nu \, \mathrm{d}x := c \mathbb{E}_{\nu}[D(x)] + \frac{1}{2} g^2 S(\nu)$$

• JKO (Jordan-Kinderlehrer-Otto) flow based learning [Bunne 2022]

Discussion

- Time-varying domain
- Discrete distributions on graphs instead of continuous
 - Noising process? Random walk with Jump measure
- Conclusion:
 - SBP on topological domains
 - Tractable topological stochastic dynamics
 - Optimal solutions (general case, Gaussian case)
 - TSB-based learning model for generation and matching