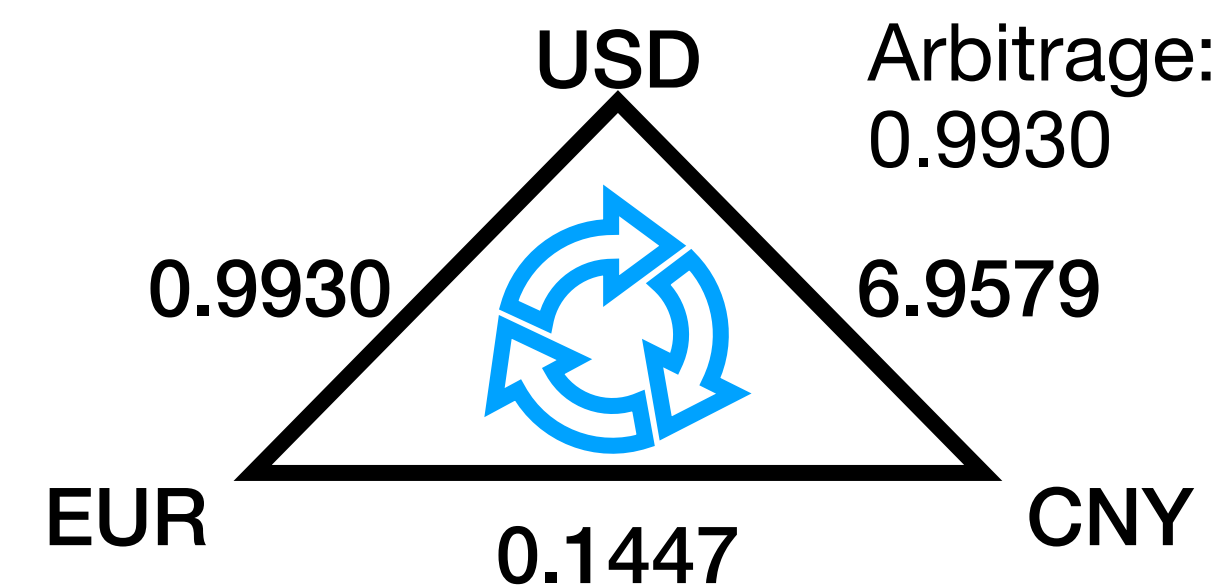
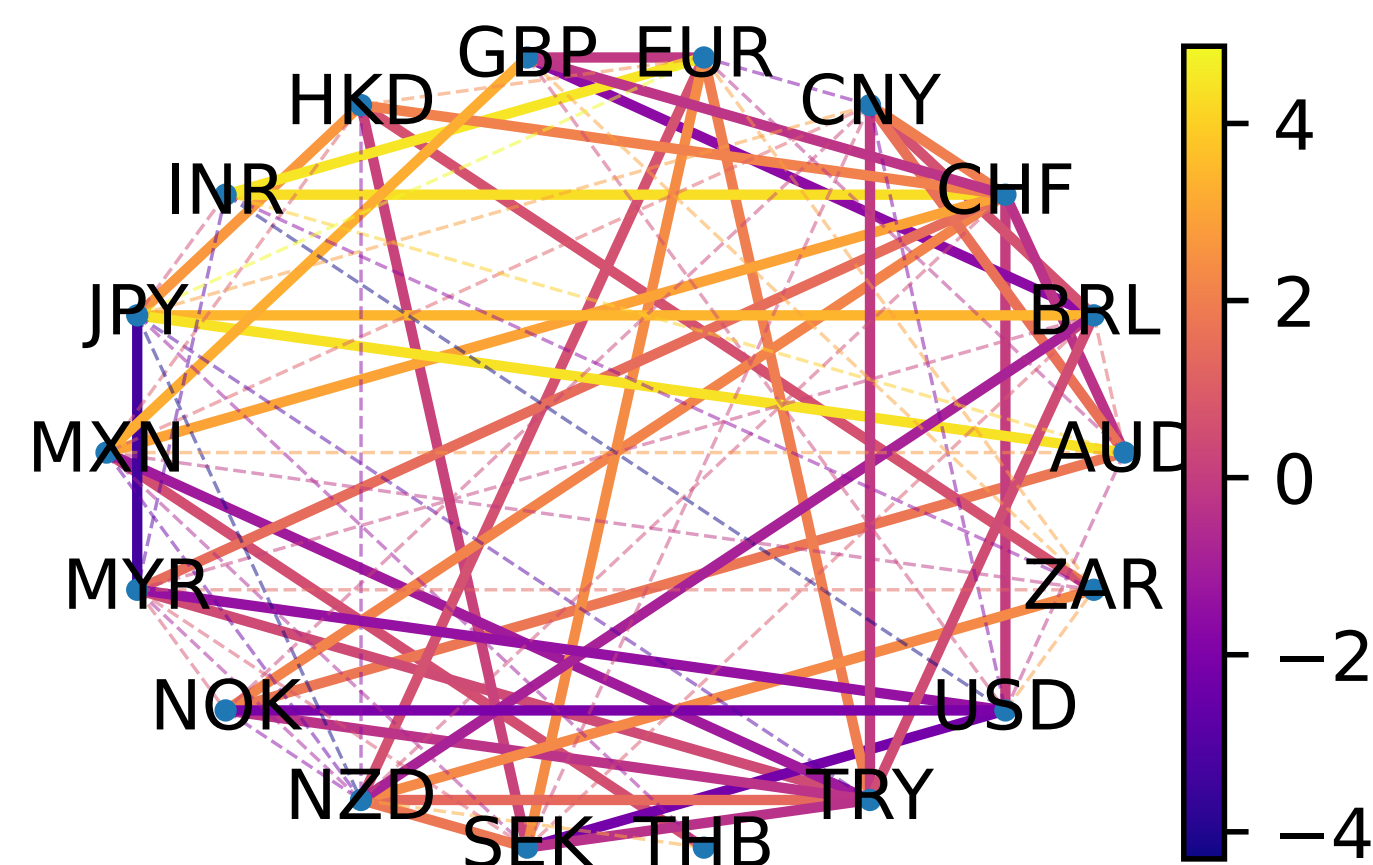
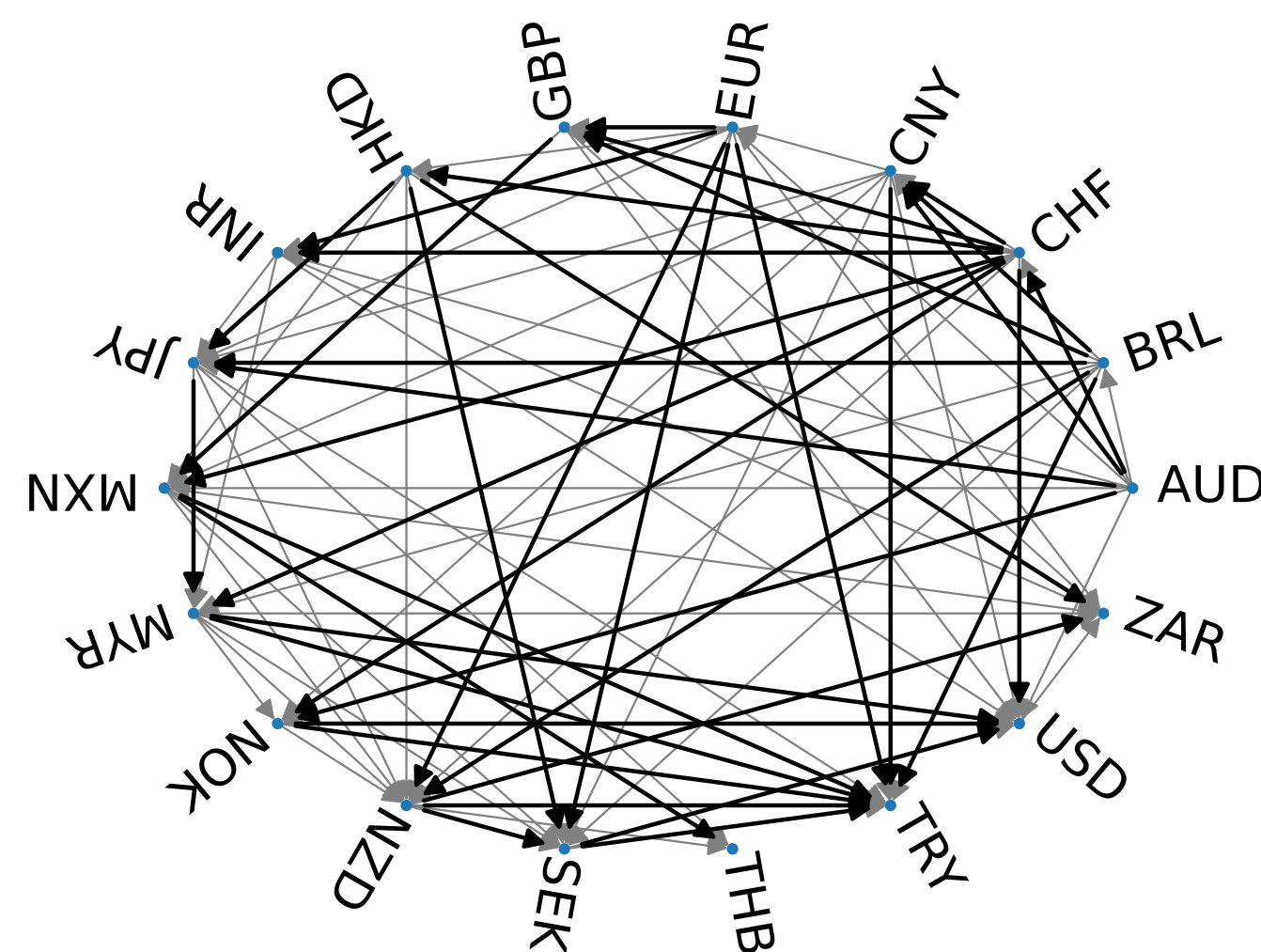


# Learning for Forex



$$r^{a/b} r^{b/c} = r^{a/c} \quad \text{Arbitrage-free}$$

$$f_{[a,b]} + f_{[b,c]} - f_{[a,c]} = 0 \quad \text{Curl-free}$$

Table 1: Forex results (nmse|total arbitrage, ↓).

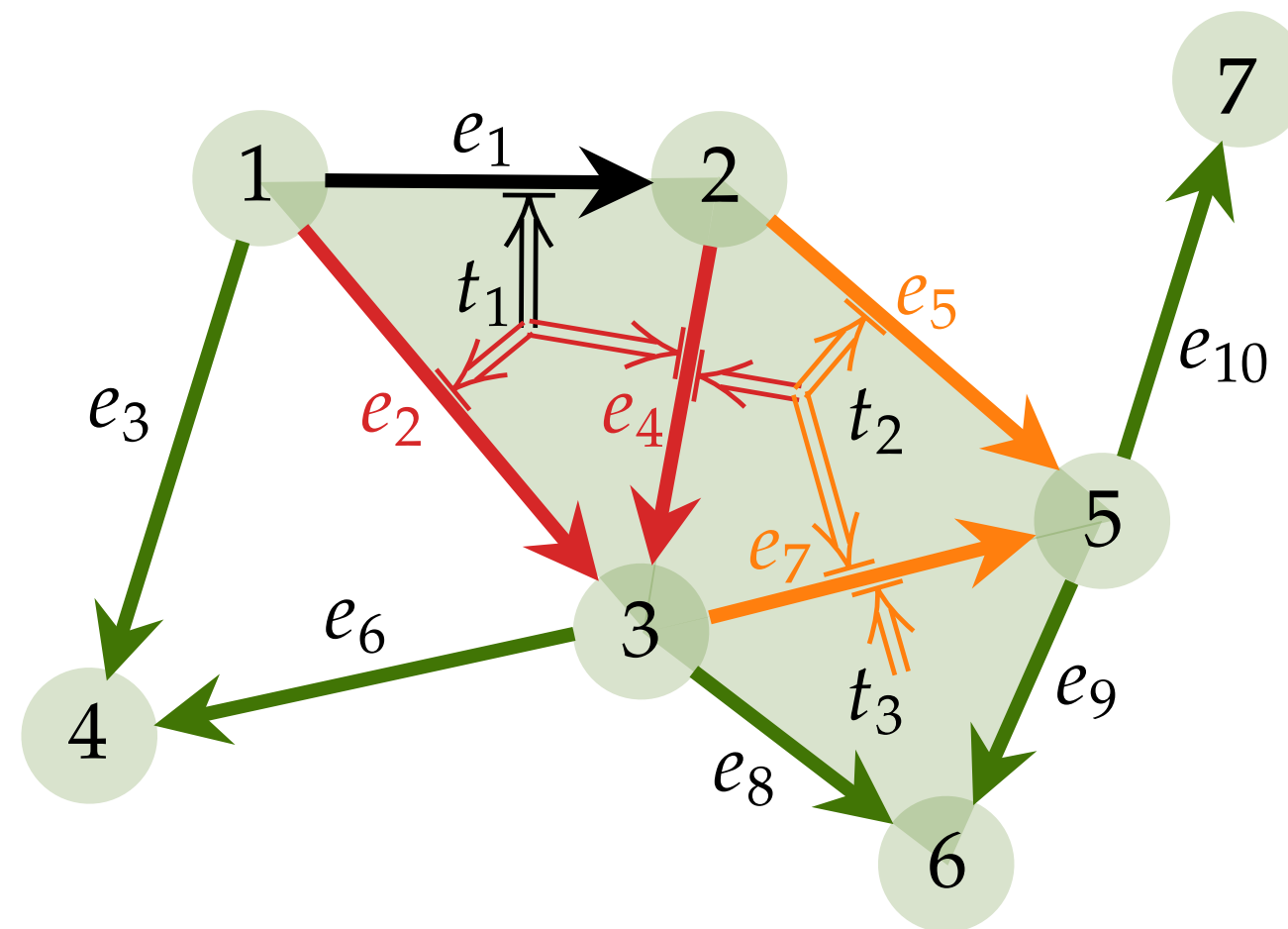
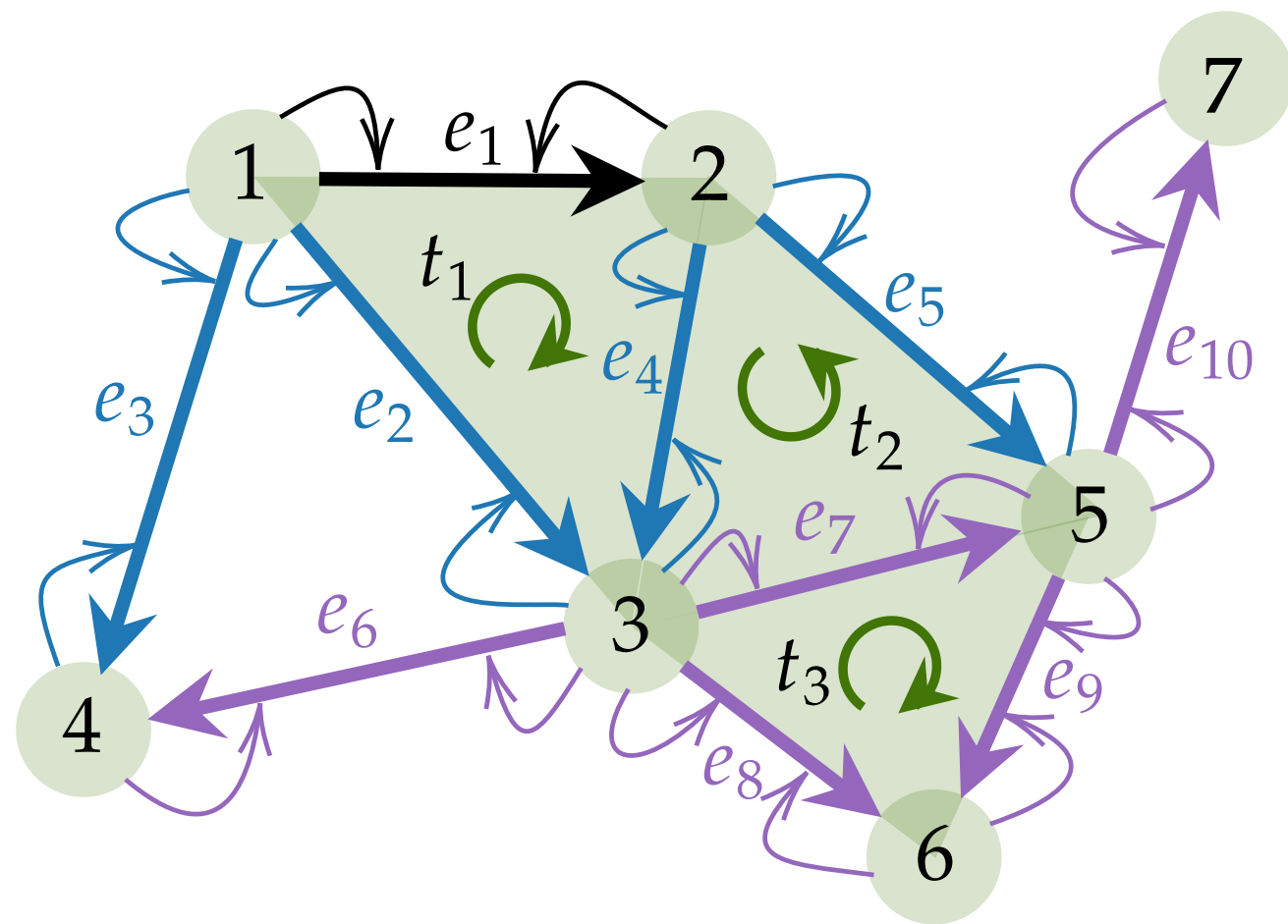
Methods	Random Noise	Curl Noise	Interpolation
Input	0.119 $\pm$ 0.004 29.19 $\pm$ 0.874	0.552 $\pm$ 0.027 122.4 $\pm$ 5.90	0.717 $\pm$ 0.030 106.4 $\pm$ 0.902
Baseline ( $\ell_2$ regularization)	0.036 $\pm$ 0.005 2.29 $\pm$ 0.079	0.050 $\pm$ 0.002 11.12 $\pm$ 0.537	0.534 $\pm$ 0.043 9.67 $\pm$ 0.082
SNN (Ebli et al., 2020)	0.110 $\pm$ 0.005 23.24 $\pm$ 1.03	0.446 $\pm$ 0.017 86.95 $\pm$ 2.20	0.702 $\pm$ 0.033 104.74 $\pm$ 1.04
PSNN (Roddenberry et al., 2021)	0.008 $\pm$ 0.001 0.984 $\pm$ 0.170	0.000 $\pm$ 0.000 0.000 $\pm$ 0.000	0.009 $\pm$ 0.001 1.13 $\pm$ 0.329
MPSN (Bodnar et al., 2021b)	0.039 $\pm$ 0.004 7.74 $\pm$ 0.88	0.076 $\pm$ 0.012 14.92 $\pm$ 2.49	0.117 $\pm$ 0.063 23.15 $\pm$ 11.7
SCCNN, id	0.027 $\pm$ 0.005 0.000 $\pm$ 0.000	0.000 $\pm$ 0.000 0.000 $\pm$ 0.000	0.265 $\pm$ 0.036 0.000 $\pm$ 0.000
SCCNN, tanh	<b>0.002<math>\pm</math>0.000</b>   <b>0.325<math>\pm</math>0.082</b>	0.000 $\pm$ 0.000 0.003 $\pm$ 0.003	<b>0.003<math>\pm</math>0.002</b>   <b>0.279<math>\pm</math>0.151</b>

# Convolutional Learning on SCs

## Node-edge-triangle interactions

- $\text{SCCNN}_k^l : \{x_{k-1}^{l-1}, x_k^{l-1}, x_{k+1}^{l-1}\} \rightarrow x_k^l$ , with simplicial order  $k$  and layer  $l$

$$\mathbf{x}_k^l = \sigma(\mathbf{H}_{k,d}^l \mathbf{x}_{k,d}^{l-1} + \mathbf{H}_k^l \mathbf{x}_k^{l-1} + \mathbf{H}_{k,u}^l \mathbf{x}_{k,u}^{l-1})$$



$$\begin{aligned} \mathbf{x}_0^l &= \sigma(\mathbf{H}_0^l \mathbf{x}_0^{l-1} + \mathbf{H}_{0,u}^l \mathbf{B}_1 \mathbf{x}_1^{l-1}) \\ \mathbf{x}_1^l &= \sigma(\mathbf{H}_{1,d}^l \mathbf{B}_1^\top \mathbf{x}_0^{l-1} + \mathbf{H}_1^l \mathbf{x}_1^{l-1} + \mathbf{H}_{1,u}^l \mathbf{B}_2 \mathbf{x}_2^{l-1}) \\ \mathbf{x}_2^l &= \sigma(\mathbf{H}_{2,d}^l \mathbf{B}_2^\top \mathbf{x}_1^{l-1} + \mathbf{H}_2^l \mathbf{x}_2^{l-1}) \end{aligned}$$

Properties: locality, symmetry  
Dirichlet energy perspective  
Hodge-invariant  
Stability to weights perturbations

Convolution based (Ebli et al. 2020; Roddenberry et al. 2021; Yang et al. 2022, 2023)  
Message passing (Bodnar et al. 2021)