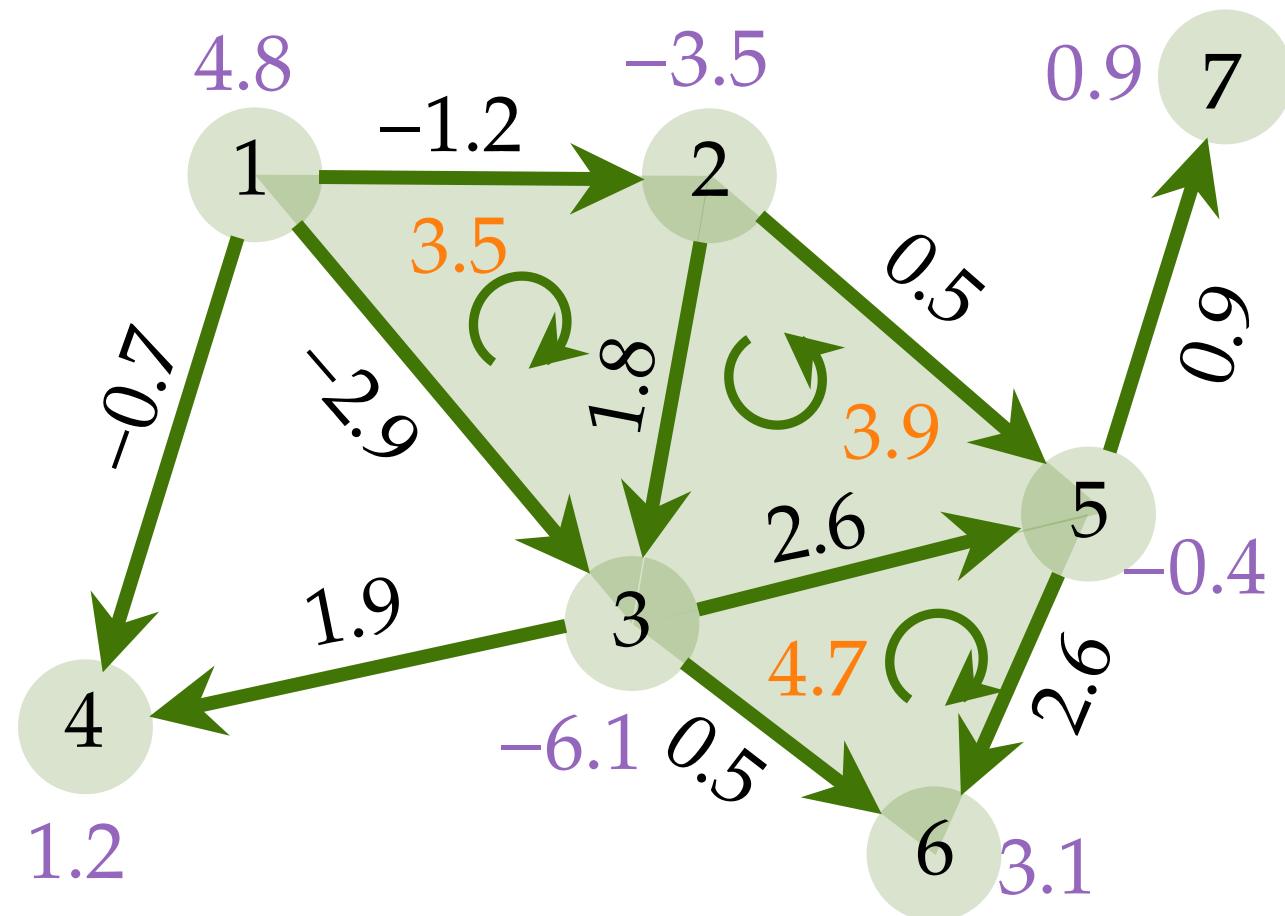


Incidence & Laplacians

1st and 2nd order Discrete Derivatives



$$[\mathbf{f}_G]_{[i,j]} = [\mathbf{v}]_j - [\mathbf{v}]_i$$

Divergence of edge flows: $[\mathbf{B}_1 \mathbf{f}]_i = \sum_{j < i} \mathbf{f}_{[j,i]} - \sum_{i < k} \mathbf{f}_{[i,k]}$

Net-flow = in_flow - out_flow

Net-circulation in triangles

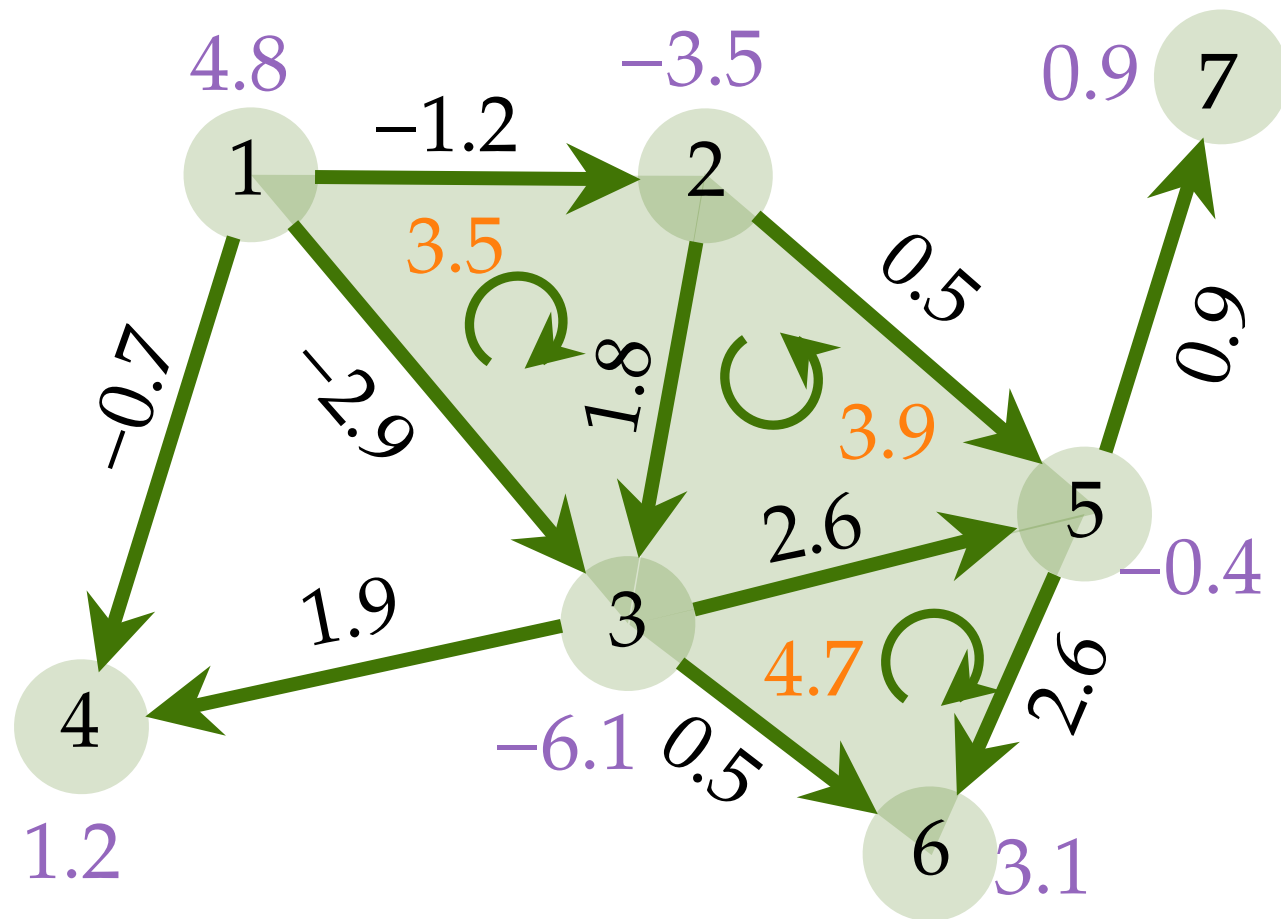
$$[\mathbf{B}_1 \mathbf{f}]_5 = 0.5 + 2.6 - (0.9 + 2.6) = -0.4$$

$$[\mathbf{B}_2^T \mathbf{f}]_{[1,2,3]} = -1.2 + 1.8 - (-2.9) = 3.5$$

$$\text{Laplacians} = \text{Grad Div} + \text{Curl}^* \text{Curl}$$

Incidence & Laplacians

1st and 2nd order Discrete Derivatives



$$[\mathbf{f}_G]_{[i,j]} = [\mathbf{v}]_j - [\mathbf{v}]_i$$

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Curl of edge flows: $[\mathbf{B}_2^T \mathbf{f}]_t = \mathbf{f}_{[i,j]} + \mathbf{f}_{[j,k]} - \mathbf{f}_{[i,k]}$, for $t = [i, j, k]$

Net-circulation in triangles

$$[\mathbf{B}_1 \mathbf{f}]_5 = 0.5 + 2.6 - (0.9 + 2.6) = -0.4$$

$$[\mathbf{B}_2^T \mathbf{f}]_{[1,2,3]} = -1.2 + 1.8 - (-2.9) = 3.5$$

$$\text{Laplacians} = \text{Grad Div} + \text{Curl}^* \text{Curl}$$