

## 1. 2 Add Two Numbers

### Problem.

```

1 class Solution {
2 public:
3     ListNode* addTwoNumbers(ListNode* l1, ListNode* l2) {
4         int s = 0;
5         ListNode* ans = new ListNode;
6         ListNode* ansTmp = ans;
7         while(l1 != nullptr || l2 != nullptr){
8             ListNode* node = new ListNode;
9             ansTmp->next = node;
10            ansTmp = node;
11            int tmp = 0;
12            if(l1 != nullptr && l2 != nullptr){
13                tmp = l1->val + l2->val + s;
14                l1 = l1->next;
15                l2 = l2->next;
16            }
17            else if(l1 != nullptr){
18                tmp = l1->val + s;
19                l1 = l1->next;
20            }
21            else{
22                tmp = l2->val + s;
23                l2 = l2->next;
24            }
25            s = 0;
26            if(tmp >= 10){
27                s = 1;
28                tmp -= 10;
29            }
30            ansTmp->val = tmp;
31        }
32        if(s==1){
33            ListNode* node = new ListNode;
34            ansTmp->next = node;
35            ansTmp = node;
36            ansTmp->val = 1;
37        }
38        ans = ans->next;
39        return ans;
40    }
41 };

```

## 2. 5 Longest Palindromic Substring

### Problem.

(input)  $a$  ;  $a_i \in \mathbb{Z}$

$$\begin{aligned}
 & \max_{\mathbf{x} \in \mathbb{Z}^{1:\dim(\mathbf{a})}} n \\
 & s.t. \quad n = \dim(\mathbf{x}) \\
 & \quad x_i = a_{s+i} \quad ; i = 1 : n \quad \text{(子序列约束)} \\
 & \quad x_i = x_{n-i} \quad ; i = 1 : n \quad \text{(回文约束)}
 \end{aligned}$$

### Algorithm.

- 动态规划

$$f(s, e) = \begin{cases} f(s-1, e+1) + 2 & f(s, e) > 0 \text{ and } a_{s-1} = a_{e-1} \\ 0 & \text{other.} \end{cases}$$

$$f(s, s) = 1 \quad \text{(初始易知值)}$$

$$f(s, s+1) = 2 \quad ; a_s = a_{s+1}$$

–  $f()$ :  $a_{s:e}$  的回文字数, 不是回文序列则为 0.

```

1 class Solution {
2 public:
3     string longestPalindrome(string s) {
4         int n = s.length();
5         int f[n][n];
6         for (int i = 0; i < n; i++) {
7             for (int j = i; j < n; j++) {
8                 f[i][j] = 0;
9             }
10        }
11        for (int i = 0; i < n; i++) {
12            f[i][i] = 1;
13            if (i != n - 1 && s[i] == s[i + 1]) {
14                f[i][i + 1] = 2;
15            }
16        }
17        for (int i = 0; i < n; i++) {
18            int k = 1;
19            while (i - k >= 0 && i + k < n && s[i - k] == s[i + k]) {
20                f[i - k][i + k] = f[i - k + 1][i + k - 1] + 2;
21                k++;
22            }
23        }
24        for (int i = 0; i < n - 1; i++) {
25            int k = 1;
26            while (s[i] == s[i + 1] && i - k >= 0 && i + 1 + k < n && s[i - k] == s[i + 1 + k]) {
27                f[i - k][i + 1 + k] = f[i - k + 1][i + 1 + k - 1] + 2;
28                k++;
29            }
30        }
31        int max = 0, I = 0;
32        for (int i = 0; i < n; i++) {
33            for (int j = i; j < n; j++) {
34                if (max < f[i][j]) {
35                    max = f[i][j];
36                    I = i;
37                }
38            }
39        }
40        return s.substr(I, max);
41    }
42 };

```

### 3. 22 Generate Parentheses

#### Problem.

Given n pairs of parentheses, write a function to generate all combinations of well-formed parentheses.

Input: n = 3

Output: ["((()))", "(()())", "(())()", "()(())", "()()()"]

```

1 class Solution {
2 public:
3     vector<string> generateParenthesis(int n) {
4         vector<string> ans;
5         string a = "magenta";
6         for(int j = 0; j < n; j++){
7             a += "magenta(magenta";
8         }
9         ans.push_back(a);
10        for(int i=0; i<n-1; i++){
11            int m = ans.size();
12            for(int j=0; j<m; j++){
13                string b = ans[j].substr(0, i + (ans[j].length() - n) + 1);
14                int kn = n + i + 1 - ans[j].length();
15                for(int k = 0; k < kn; k++){

```

```

16         b += magenta'magenta)magenta';
17         ans.push_back(
18             b + ans[j].substr(i + (ans[j].length() - n) + 1, ans[j].length() - (i +
19                 (ans[j].length() - n) + 1))
20         );
21     }
22 }
23 int m = ans.size();
24 for (int j = 0; j < m; j++) {
25     for (int i = ans[j].length(); i < 2 * n; i++) {
26         ans[j] += magenta'magenta)magenta';
27     }
28 }
29 for (int j = 0; j < m; j++) {
30     for (int i = j + 1; i < m; i++) {
31         if (ans[i] == ans[j]) {
32             ans.erase(ans.begin() + i);
33             i--; m--;
34         }
35     }
36 }
37 return ans;
38 }
39 };

```

#### 4. 39 Combination Sum

##### Problem.

(input)  $\mathbf{a} \in \mathbb{Z}_+^n, \mathbf{b} \in \mathbb{Z}_+$  ;  $a_i \leq b$

$$\mathbf{x}^T \mathbf{a} = b$$

$$\mathbf{x} \in \mathbb{N}^n$$

##### Algorithm.

```

1 class Solution {
2 public:
3     int dot(vector<int>& a, vector<int>& b) {
4         int n = a.size(), ans = 0;
5         for (int i = 0; i < n; i++) {
6             ans += a[i] * b[i];
7         }
8         return ans;
9     }
10    vector<vector<int>> combinationSum(vector<int>& candidates, int target) {
11        vector<vector<int>> ans;
12        vector<int> x;
13        int n = candidates.size();
14        for (int i = 0; i < n; i++) {
15            x.push_back(0);
16        }
17        fun(0, x, candidates, target, ans);
18        return ans;
19    }
20    void fun(int ind, vector<int>& x, vector<int>& a, int target, vector<vector<int>>&
21        ans) {
22        int n = a.size();
23        if (ind == n - 1) {
24            while (1) {
25                int t = dot(x, a);
26                for (int i = 0; i < x.size(); i++) {
27                    printf(magenta"magenta\%magenta magentadmagenta magenta", x[i]);
28                } printf(magenta"magenta>\%magenta magentadmagenta magenta\magentanmagenta", t);
29                if (t > target) {
30                    x[ind] = 0;
31                    return;

```

```

31     }
32     else if (t == target) {
33         getAns(x, a, ans);
34         x[ind] = 0;
35         return;
36     }
37     x[ind]++;
38 }
39 }
40 while (1) {
41     fun(ind + 1, x, a, target, ans);
42     x[ind]++;
43     int t = dot(x, a);
44     if (t > target) {
45         x[ind] = 0;
46         return;
47     }
48 }
49 x[ind] = 0;
50 return;
51 }
52 void getAns(vector<int>& x, vector<int>& a, vector<vector<int>>& ans) {
53     vector<int> t;
54     int n = a.size();
55     for (int i = 0; i < n; i++) {
56         for (int j = 0; j < x[i]; j++) {
57             t.push_back(a[i]);
58         }
59     }
60     ans.push_back(t);
61 }
62 };

```

## 5. 45 Jump Game II

### Problem.

(input)  $\mathbf{a}$  ;  $a_i \in \mathbb{N}$

$$\begin{aligned}
 & \min_{\mathbf{x} \in \mathbb{N}^{1: (\dim \mathbf{a} - 1)}} \dim \mathbf{x} \\
 & s.t. \quad x_i \leq a \left( \sum_{k=0}^{i-1} x_k \right) \\
 & \quad \mathbf{1}^T \mathbf{x} = \dim \mathbf{a} - 1
 \end{aligned}$$

### Algorithm.

- 动态规划

$$\begin{aligned}
 & f(i) = \min \{f(i-k) + 1 | k \in 1 : \min(a_i, i), f(i-k) > 0 \text{ when } i-k > 0\} \\
 & \Rightarrow f(i+k) \leftarrow \min(f(i+k), f(i) + 1) \quad ; k \in 1 : \min(a_i, \dim \mathbf{a} - i) \\
 & f(0) = 0 \quad \quad \quad \text{(初始易知值)} \\
 & f(\dim \mathbf{a}) = \dim \mathbf{x}^* \quad \quad \quad \text{(答案)}
 \end{aligned}$$

–  $f(k)$ : 当  $\mathbf{1}^T \mathbf{x} = i$  时的优化问题的解, 无解时为 0.

```

1 class Solution {
2 public:
3     int jump(vector<int>& nums) {
4         int n = nums.size();
5         int f[n];
6         for (int i = 0; i < n; i++) {
7             f[i] = 0xFFFFFFFF;
8         }
9         f[0] = 0;
10        for (int i = 0; i < n - 1; i++) {

```

```

11     for (int k = 1; k <= nums[i]; k++) {
12         if (i + k >= n)
13             break;
14         f[i + k] = min(f[i + k], f[i] + 1);
15     }
16 }
17 return f[n - 1];
18 }
19 };

```

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```

1  class Solution {
2  public:
3      vector<int> spiralOrder(vector<vector<int>>& matrix) {
4          vector<int> ans;
5          int m = matrix.size(), n = matrix[0].size();
6          int x = 0, y = 0, dimX = 0, dimY = 1;
7          for(int i=0;i<m*n;i++){
8              ans.push_back(matrix[x][y]);
9              matrix[x][y] = 0xFFFFFFFF;
10             if(dimY > 0 && (y + dimY == n \|| matrix[x][y + dimY] == 0xFFFFFFFF)){
11                 dimX = 1;
12                 dimY = 0;
13             }
14             else if(dimY < 0 && (y + dimY == -1 \|| matrix[x][y + dimY] == 0xFFFFFFFF)){
15                 dimX = -1;
16                 dimY = 0;
17             }
18             else if(dimX > 0 && (x + dimX == m \|| matrix[x + dimX][y] == 0xFFFFFFFF)){
19                 dimX = 0;
20                 dimY = -1;
21             }
22             else if(dimX < 0 && (x + dimX == -1 \|| matrix[x + dimX][y] == 0xFFFFFFFF)){
23                 dimX = 0;
24                 dimY = 1;
25             }
26             x += dimX;
27             y += dimY;
28         }
29         return ans;
30     }
31 };

```

7. 62 Unique Paths

### Problem.

(input)  $x_0, y_0 \in \mathbb{N}$

方块图,  $(0, 0) \rightarrow (x_0, y_0)$ , 只能走右、下的所有路径数.

### Algorithm.

- 动态规划

$$f(x, y) = f(x - 1, y) + f(x, y - 1)$$

$$f(0, y) = 1$$

$$f(x, 0) = 1$$

(初始易知值)

- $f(x, y)$ : 位置  $x, y$  处的路径数.

```

1  class Solution {
2  public:
3      int uniquePaths(int m, int n) {
4          int f[m][n];
5          for(int i = 0; i < m; i++){
6              f[i][0] = 1;
7          }
8          for(int i = 0; i < n; i++){

```

```

9      f[0][i] = 1;
10    }
11    for(int i = 1; i < m; i++){
12      for(int j = 1; j < n; j++){
13        f[i][j] = f[i][j-1] + f[i-1][j];
14      }
15    }
16    return f[m-1][n-1];
17  }
18 };

```

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```

1  class Solution {
2  public:
3      bool is(int* a) {
4          int t = a[0] * a[4] * a[8] + a[1] * a[5] * a[6] + a[2] * a[3] * a[7]
5              \begin{itemize}
6              \item a[2] * a[4] * a[6] - a[1] * a[3] * a[8] - a[0] * a[5] * a[7];
7              \end{itemize}
8          return t == 0 ? 1 : 0;
9      }
10     int maxPoints(vector<vector<int>>& points) {
11         int n = points.size(), ans = 0;
12         if(n == 1)
13             return 1;
14         if(n == 2)
15             return 2;
16         int a[9];
17         a[2] = a[5] = a[8] = 1;
18         for (int i = 0; i < n; i++) {
19             a[0] = points[i][0];
20             a[1] = points[i][1];
21             for (int j = i + 1; j < n; j++) {
22                 a[3] = points[j][0];
23                 a[4] = points[j][1];
24                 int num = 2;
25                 for (int k = 0; k < n; k++) {
26                     if (k == i || k == j)
27                         continue;
28                     a[6] = points[k][0];
29                     a[7] = points[k][1];
30                     if (is(a))
31                         num++;
32                 }
33                 ans = max(num, ans);
34             }
35         }
36         return ans;
37     }
38 };

```

9. 233 Number of Digit One

**Problem.**

(input)  $n \in \mathbb{N}$

求所有比  $n$  小 (包括  $n$ ) 的正整数中, 含数字 1 的个数.

**Property.**

- 第  $i$  出现 1 的现象, 是一个周期  $10^{i+1}$  宽  $10^i$  高 1 的矩形波.

第  $i$  位 1 的矩形位于整个周期的第  $10^i + 1 \sim 2 \times 10^i$  个数上,

数位 $i$	周期	波峰宽度	波峰高度
0	10	1	1
1	100	10	1
2	1000	100	1
$\vdots$	$\vdots$	$\vdots$	$\vdots$
$i$	$10^{i+1}$	$10^i$	1

eg.

0	1	2	3	4	5	6	7	8	9	(一位 1 在第 2 个)
0	1	...	10	...	19	...	...	...	99	(二位 1 在第 11 – 20 个)
0	1	...	100	...	199	...	...	...	999	(三位 1 在第 101 – 200 个)

#### Algorithm.

- 将  $0 \sim n$  的数分解为每一位上的 1 的矩形波, 并求和波峰即可.
- 步骤
  - 首先, 求完成的周期数, 周期数  $\times$  波峰宽便是第一部分数字 1 的数量.
  - 然后, 分析正在进行的周期, 求余剩下的数的长度  $rest$ 
    - \*  $rest \geq 2 \times 10^i$  时, 波峰部分已完成, 直接加波峰宽度即可.
    - \*  $10^i + 1 \leq rest < 2 \times 10^i$  时, 波峰部分正在进行, 加剩余数的数目即可
    - \*  $rest < 10^i + 1$  时, 波峰部分未开始, 不用计算.

```

1  class Solution {
2  public:
3      long long countDigitOne(long long n) {
4          long long ans = 0;
5          long long nt = n, dim = 0;
6          while (nt != 0) {
7              dim++;
8              nt /= 10;
9          }
10         for (long long i = 0; i < dim; i++) {
11             red//red red完red成red的red周red期
12             long long tmp = (n + 1) / (long long)pow(10, i + 1) * pow(10, i);
13             red//red red正red在red进red行red的red周red期
14             long long rest = (n + 1) \% (long long)pow(10, i + 1),
15                 tmp2 = rest / pow(10, i);
16             if (tmp2 > 1) { red red//red red完red成red一red个red波red峰
17                 tmp += pow(10, i);
18             }
19             else if (tmp2 == 1) { red red//red red正red在red完red成red一red个red波red峰
20                 tmp += rest \% (long long)pow(10, i);
21             }
22             red red//red red未red完red成red一red个red波red峰red red(red不red用red计
23                 red算red)
24             ans += tmp;
25         }
26         return ans;
27     };

```

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#### Problem.

(input)  $a, b$  ;  $a_i, b \in \mathbb{N}$

$$\begin{aligned}
 \min_x \quad & \|x\|_1 = \mathbf{1}^T x \\
 s.t. \quad & \mathbf{a}^T x = b \\
 & x_i \in \mathbb{N}
 \end{aligned}$$

#### Algorithm.

- 动态规划

$$f(k) = \begin{cases} f(k - a_i) + 1 & f(k - a_i) > 0 \text{ or } k - a_i = 0 \\ 0 & \text{other} \end{cases} \quad k \in 1 : \dim(\mathbf{a}_i)$$

(初始易知值)

$$f(0) = 0$$

(答案)

$$f(b) = \min_x \|\mathbf{x}\|_1$$

–  $f(k)$ : 当  $b \leftarrow k$  时的优化问题的解, 无解时为 0.

```

1 class Solution {
2     public:
3         int coinChange(vector<int>& coins, int amount) {
4             if (amount == 0)
5                 return 0;
6             sort(coins.begin(), coins.end());
7             int table[amount + 1];
8             table[0] = 0;
9             for (int i = 1; i < amount + 1; i++) {
10                 table[i] = 0xFFFFFFFF;
11             }
12             int size = coins.size();
13             for (int i = 1; i <= amount; i++) {
14                 for (int j = 0; j < size; j++) {
15                     if (coins[j] > i)
16                         break;
17                     int tmp = table[i - coins[j]] + 1;
18                     table[i] = table[i] < tmp ? table[i] : tmp;
19                 }
20             }
21             return table[amount] == 0xFFFFFFFF ? -1 : table[amount];
22         }
23     };

```