

1. 2 Add Two Numbers

Problem.

```

1  class Solution {
2  public:
3      ListNode* addTwoNumbers(ListNode* l1, ListNode* l2) {
4          int s = 0;
5          ListNode* ans = new ListNode;
6          ListNode* ansTmp = ans;
7
8          while(l1 != nullptr || l2 != nullptr){
9              ListNode* node = new ListNode;
10             ansTmp->next = node;
11             ansTmp = node;
12
13             int tmp = 0;
14             if(l1 != nullptr && l2 != nullptr){
15                 tmp = l1->val + l2->val + s;
16                 l1 = l1->next;
17                 l2 = l2->next;
18             }
19             else if(l1 != nullptr){
20                 tmp = l1->val + s;
21                 l1 = l1->next;
22             }
23             else{
24                 tmp = l2->val + s;
25                 l2 = l2->next;
26             }
27
28             s = 0;
29
30             if(tmp >= 10){
31                 s = 1;
32                 tmp -= 10;
33             }
34
35             ansTmp->val = tmp;
36         }
37
38         if(s==1){
39             ListNode* node = new ListNode;
40             ansTmp->next = node;
41             ansTmp = node;
42             ansTmp->val = 1;
43         }
44
45         ans = ans->next;
46         return ans;
47     }
48 };

```

2. 5 Longest Palindromic Substring

Problem.

(input) a ; $a_i \in \mathbb{Z}$

$$\begin{aligned}
 & \max_{x \in \mathbb{Z}^{1:\dim(a)}} n \\
 & s.t. \quad n = \dim(x) \\
 & \quad x_i = a_{s+i} \quad ; i = 1 : n \\
 & \quad x_i = x_{n-i} \quad ; i = 1 : n
 \end{aligned}$$

(子序列约束)

(回文约束)

Algorithm.

- 动态规划

$$f(s, e) = \begin{cases} f(s-1, e+1) + 2 & f(s, e) > 0 \text{ and } a_{s-1} = a_{e-1} \\ 0 & \text{other.} \end{cases}$$
$$f(s, s) = 1$$
$$f(s, s+1) = 2 \quad ; a_s = a_{s+1}$$

(初始易知值)

- $f()$: $a_{s:e}$ 的回文字数, 不是回文序列则为 0.

```
1 class Solution {
2 public:
3     string longestPalindrome(string s) {
4         int n = s.length();
5
6         int f[n][n];
7
8         for (int i = 0; i < n; i++) {
9             for (int j = i; j < n; j++) {
10                 f[i][j] = 0;
11             }
12         }
13
14         for (int i = 0; i < n; i++) {
15             f[i][i] = 1;
16
17             if (i != n - 1 && s[i] == s[i + 1]) {
18                 f[i][i + 1] = 2;
19             }
20         }
21
22         for (int i = 0; i < n; i++) {
23             int k = 1;
24             while (i - k >= 0 && i + k < n && s[i - k] == s[i + k]) {
25                 f[i - k][i + k] = f[i - k + 1][i + k - 1] + 2;
26                 k++;
27             }
28         }
29
30         for (int i = 0; i < n - 1; i++) {
31             int k = 1;
32             while (s[i] == s[i + 1] && i - k >= 0 && i + 1 + k < n && s[i - k] == s[i + 1 + k]) {
33                 f[i - k][i + 1 + k] = f[i - k + 1][i + 1 + k - 1] + 2;
34                 k++;
35             }
36         }
37
38         int max = 0, I = 0;
39         for (int i = 0; i < n; i++) {
40             for (int j = i; j < n; j++) {
41                 if (max < f[i][j]) {
42                     max = f[i][j];
43                     I = i;
44                 }
45             }
46         }
47
48         return s.substr(I, max);
49
50     }
51 };
```

3. 22 Generate Parentheses

Problem.

Given n pairs of parentheses, write a function to generate all combinations of well-formed parentheses.

Input: n = 3

Output: ["((()))", "(()())", "(())()", "()(())", "()()()"]

```

1  class Solution {
2  public:
3      vector<string> generateParenthesis(int n) {
4          vector<string> ans;
5
6          string a = "magenta";
7          for(int j = 0; j < n; j++){
8              a += "magenta(magenta";
9          }
10
11         ans.push_back(a);
12
13         for(int i=0; i < n-1; i++){
14             int m = ans.size();
15
16             for(int j=0; j < m; j++){
17                 string b = ans[j].substr(0, i + (ans[j].length() - n) + 1);
18                 int kn = n + i + 1 - ans[j].length();
19
20                 for(int k = 0; k < kn; k++){
21                     b += "magenta(magenta";
22                     ans.push_back(
23                         b + ans[j].substr(i + (ans[j].length() - n) + 1, ans[j].length() - (i +
24                             (ans[j].length() - n) + 1));
25                 }
26             }
27         }
28
29         int m = ans.size();
30
31         for (int j = 0; j < m; j++) {
32             for (int i = ans[j].length(); i < 2 * n; i++) {
33                 ans[j] += "magenta(magenta";
34             }
35         }
36
37         for (int j = 0; j < m; j++) {
38             for (int i = j + 1; i < m; i++) {
39
40                 if (ans[i] == ans[j]) {
41                     ans.erase(ans.begin() + i);
42                     i--; m--;
43                 }
44             }
45         }
46
47         return ans;
48     }
49 };
50

```

4. 39 Combination Sum

Problem.

(input) $a \in \mathbb{Z}_+^n, b \in \mathbb{Z}_+$; $a_i \leq b$

$$\begin{aligned}x^T a &= b \\ x &\in \mathbb{N}^n\end{aligned}$$

Algorithm.

```

1  class Solution {
2  public:
3      int dot(vector<int>& a, vector<int>& b) {
4          int n = a.size(), ans = 0;
5
6          for (int i = 0; i < n; i++) {
7              ans += a[i] * b[i];
8          }
9
10         return ans;
11     }
12
13     vector<vector<int>> combinationSum(vector<int>& candidates, int target) {
14         vector<vector<int>> ans;
15         vector<int> x;
16
17         int n = candidates.size();
18         for (int i = 0; i < n; i++) {
19             x.push_back(0);
20         }
21
22         fun(0, x, candidates, target, ans);
23
24         return ans;
25     }
26
27     void fun(int ind, vector<int>& x, vector<int>& a, int target, vector<vector<int>>&
28             ans) {
29         int n = a.size();
30
31         if (ind == n - 1) {
32             while (1) {
33                 int t = dot(x, a);
34
35                 for (int i = 0; i < x.size(); i++) {
36                     printf(magenta"magenta%magentadmagenta magenta", x[i]);
37                 }printf(magenta"magenta>%magentadmagenta magenta\magentanmagenta", t);
38
39                 if (t > target) {
40                     x[ind] = 0;
41                     return;
42                 }
43
44                 else if (t == target) {
45                     getAns(x, a, ans);
46
47                     x[ind] = 0;
48                     return;
49                 }
50
51                 x[ind]++;
52             }
53         }
54
55         while (1) {

```

```

56     fun(ind + 1, x, a, target, ans);
57
58     x[ind]++;
59
60     int t = dot(x, a);
61     if (t > target) {
62         x[ind] = 0;
63         return;
64     }
65 }
66
67 x[ind] = 0;
68 return;
69 }
70
71 void getAns(vector<int>& x, vector<int>& a, vector<vector<int>>& ans) {
72     vector<int> t;
73     int n = a.size();
74
75     for (int i = 0; i < n; i++) {
76         for (int j = 0; j < x[i]; j++) {
77             t.push_back(a[i]);
78         }
79     }
80     ans.push_back(t);
81 }
82 };

```

5. 45 Jump Game II

Problem.

(input) \mathbf{a} ; $a_i \in \mathbb{N}$

$$\begin{aligned}
 & \min_{\mathbf{x} \in \mathbb{N}^{1: (\dim \mathbf{a} - 1)}} \dim \mathbf{x} \\
 & s.t. \quad x_i \leq a \left(\sum_{k=0}^{i-1} x_k \right) \\
 & \quad \mathbf{1}^T \mathbf{x} = \dim \mathbf{a} - 1
 \end{aligned}$$

Algorithm.

- 动态规划

$$\begin{aligned}
 f(i) &= \min \{ f(i-k) + 1 \mid k \in 1 : \min(a_i, i), f(i-k) > 0 \text{ when } i-k > 0 \} \\
 \Rightarrow f(i+k) &\leftarrow \min(f(i+k), f(i) + 1) \quad ; k \in 1 : \min(a_i, \dim \mathbf{a} - i) \\
 f(0) &= 0 && \text{(初始易知值)} \\
 f(\dim \mathbf{a}) &= \dim \mathbf{x}^* && \text{(答案)}
 \end{aligned}$$

- $f(k)$: 当 $\mathbf{1}^T \mathbf{x} = i$ 时的优化问题的解, 无解时为 0.

```

1 class Solution {
2 public:
3     int jump(vector<int>& nums) {
4         int n = nums.size();
5         int f[n];
6
7         for (int i = 0; i < n; i++) {
8             f[i] = 0xFFFFFFFF;

```

```

9      }
10     f[0] = 0;
11
12     for (int i = 0; i < n - 1; i++) {
13         for (int k = 1; k <= nums[i]; k++) {
14             if (i + k >= n)
15                 break;
16
17             f[i + k] = min(f[i + k], f[i] + 1);
18         }
19     }
20
21     return f[n - 1];
22 }
23 };

```

6. 54

```

1  class Solution {
2  public:
3      vector<int> spiralOrder(vector<vector<int>>& matrix) {
4          vector<int> ans;
5
6          int m = matrix.size(), n = matrix[0].size();
7
8          int x = 0, y = 0, dimX = 0, dimY = 1;
9
10         for(int i=0;i<m*n;i++){
11             ans.push_back(matrix[x][y]);
12             matrix[x][y] = 0xFFFFFFFF;
13
14             if(dimY > 0 && (y + dimY == n || matrix[x][y + dimY] == 0xFFFFFFFF)){
15                 dimX = 1;
16                 dimY = 0;
17             }
18
19             else if(dimY < 0 && (y + dimY == -1 || matrix[x][y + dimY] == 0xFFFFFFFF)){
20                 dimX = -1;
21                 dimY = 0;
22             }
23
24             else if(dimX > 0 && (x + dimX == m || matrix[x + dimX][y] == 0xFFFFFFFF)){
25                 dimX = 0;
26                 dimY = -1;
27             }
28
29             else if(dimX < 0 && (x + dimX == -1 || matrix[x + dimX][y] == 0xFFFFFFFF)){
30                 dimX = 0;
31                 dimY = 1;
32             }
33
34             x += dimX;
35             y += dimY;
36         }
37
38         return ans;
39     }
40 };

```

7. 62 Unique Paths

Problem.

(input) $x_0, y_0 \in \mathbb{N}$

方块图, $(0, 0) \rightarrow (x_0, y_0)$, 只能走右、下的所有路径数.

Algorithm.

- 动态规划

$$f(x, y) = f(x - 1, y) + f(x, y - 1)$$

$$f(0, y) = 1$$

$$f(x, 0) = 1$$

(初始易知值)

- $f(x, y)$: 位置 x, y 处的路径数.

```

1 class Solution {
2 public:
3     int uniquePaths(int m, int n) {
4         int f[m][n];
5
6         for(int i = 0; i < m; i++){
7             f[i][0] = 1;
8         }
9
10        for(int i = 0; i < n; i++){
11            f[0][i] = 1;
12        }
13
14        for(int i = 1; i < m; i++){
15            for(int j = 1; j < n; j++){
16                f[i][j] = f[i][j-1] + f[i-1][j];
17            }
18        }
19
20        return f[m-1][n-1];
21    }
22 };

```

8. 145

```

1 class Solution {
2 public:
3     bool is(int* a) {
4         int t = a[0] * a[4] * a[8] + a[1] * a[5] * a[6] + a[2] * a[3] * a[7]
5             - a[2] * a[4] * a[6] - a[1] * a[3] * a[8] - a[0] * a[5] * a[7];
6         return t == 0 ? 1 : 0;
7     }
8
9     int maxPoints(vector<vector<int>>& points) {
10        int n = points.size(), ans = 0;
11        if(n == 1)
12            return 1;
13        if(n == 2)
14            return 2;
15
16        int a[9];
17        a[2] = a[5] = a[8] = 1;
18
19        for (int i = 0; i < n; i++) {
20            a[0] = points[i][0];
21            a[1] = points[i][1];
22
23            for (int j = i + 1; j < n; j++) {
24                a[3] = points[j][0];
25                a[4] = points[j][1];
26
27                int num = 2;
28
29                for (int k = 0; k < n; k++) {
30
31                    if (k == i || k == j)
32                        continue;

```

```

33
34     a[6] = points[k][0];
35     a[7] = points[k][1];
36
37     if (is(a))
38         num++;
39 }
40
41     ans = max(num, ans);
42 }
43 }
44
45     return ans;
46 }
47 };

```

9. 233 Number of Digit One

Problem.

(input) $n \in \mathbb{N}$

求所有比 n 小 (包括 n) 的正整数中, 含数字 1 的个数.

Property.

- 第 i 出现 1 的现象, 是一个周期 10^{i+1} 宽 10^i 高 1 的矩形波.
第 i 位 1 的矩形位于整个周期的第 $10^i + 1 \sim 2 \times 10^i$ 个数上,

数位 i	周期	波峰宽度	波峰高度
0	10	1	1
1	100	10	1
2	1000	100	1
\vdots	\vdots	\vdots	\vdots
i	10^{i+1}	10^i	1

eg.

0	1	2	3	4	5	6	7	8	9	(一位 1 在第 2 个)
0	1	...	10	...	19	99	(二位 1 在第 11 – 20 个)
0	1	...	100	...	199	999	(三位 1 在第 101 – 200 个)

Algorithm.

- 将 $0 \sim n$ 的数分解为每一位上的 1 的矩形波, 并求和波峰即可.
- 步骤
 - 首先, 求完成的周期数, 周期数 \times 波峰宽便是第一部分数字 1 的数量.
 - 然后, 分析正在进行的周期, 求余剩下的数的长度 $rest$
 - * $rest \geq 2 \times 10^i$ 时, 波峰部分已完成, 直接加波峰宽度即可.
 - * $10^i + 1 \leq rest < 2 \times 10^i$ 时, 波峰部分正在进行, 加剩余数的数目即可
 - * $rest < 10^i + 1$ 时, 波峰部分未开始, 不用计算.

```

1 class Solution {
2 public:
3     long long countDigitOne(long long n) {
4         long long ans = 0;
5
6         long long nt = n, dim = 0;
7         while (nt != 0) {
8             dim++;

```



```

9      nt /= 10;
10    }
11
12    for (long long i = 0; i < dim; i++) {
13    red      red//red red完red成red的red周red期
14      long long tmp = (n + 1) / (long long)pow(10, i + 1) * pow(10, i);
15
16    red      red//red red正red在red进red行red的red周red期
17      long long rest = (n + 1) % (long long)pow(10, i + 1),
18      tmp2 = rest / pow(10, i);
19
20      if (tmp2 > 1) { red      red//red red完red成red一red个red波red峰
21        tmp += pow(10, i);
22      }
23      else if (tmp2 == 1) { red red//red red正red在red完red成red一red个red波red峰
24        tmp += rest % (long long)pow(10, i);
25      }
26    red      red//red red未red完red成red一red个red波red峰red red(red不red用red计
           red算red)
27      ans += tmp;
28    }
29
30    return ans;
31  }
32 };

```

10. 322

Problem.

(input) a, b ; $a_i, b \in \mathbb{N}$

$$\begin{aligned}
 \min_x \quad & \|x\|_1 = \mathbf{1}^T x \\
 s.t. \quad & \mathbf{a}^T x = b \\
 & x_i \in \mathbb{N}
 \end{aligned}$$

Algorithm.

- 动态规划

$$\begin{aligned}
 f(k) &= \begin{cases} f(k - a_i) + 1 & f(k - a_i) > 0 \text{ or } k - a_i = 0 \\ 0 & other \end{cases} & k \in 1 : \dim(\mathbf{a}_i) \\
 f(0) &= 0 & (\text{初始易知值}) \\
 f(b) &= \min_x \|x\|_1 & (\text{答案})
 \end{aligned}$$

- $f(k)$: 当 $b \leftarrow k$ 时的优化问题的解, 无解时为 0.

```

1  class Solution {
2  public:
3      int coinChange(vector<int>& coins, int amount) {
4          if (amount == 0)
5              return 0;
6
7          sort(coins.begin(), coins.end());
8
9          int table[amount + 1];
10         table[0] = 0;
11         for (int i = 1; i < amount + 1; i++) {
12             table[i] = 0xFFFFFFFF;

```

```

13     }
14
15     int size = coins.size();
16
17     for (int i = 1; i <= amount; i++) {
18         for (int j = 0; j < size; j++) {
19             if (coins[j] > i)
20                 break;
21
22             int tmp = table[i - coins[j]] + 1;
23
24             table[i] = table[i] < tmp ? table[i] : tmp;
25         }
26     }
27
28     return table[amount] == 0xFFFFFFFF ? -1 : table[amount];
29 }
30 };

```

end