MATLAB 科学计算语言与应用

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Lecture 1

Outline

I. Getting Started

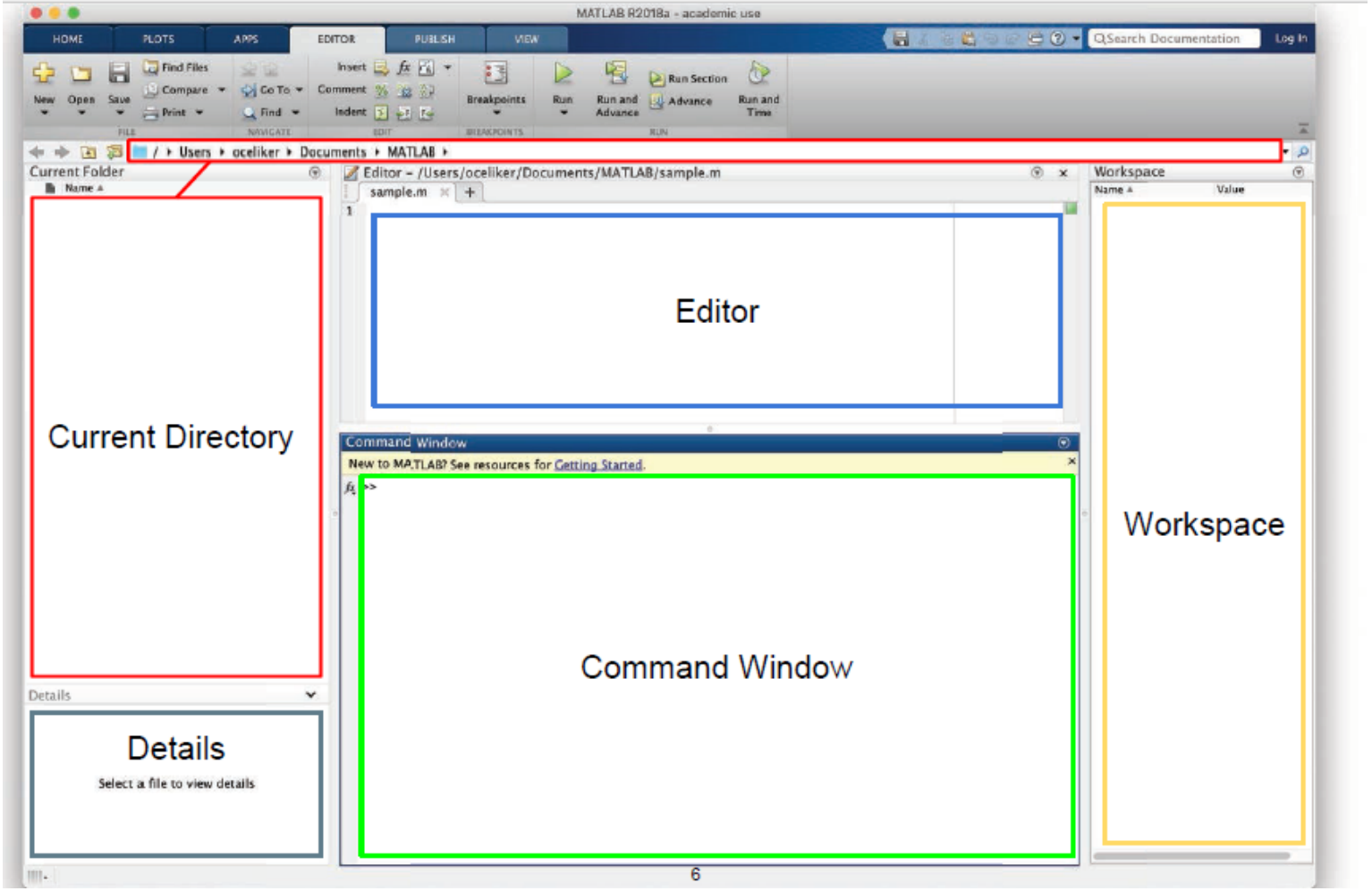
II. Scripts

III. Making Variables

IV. Manipulating Variables

V. Basic Plotting

I. Getting Started


MATLAB R2018a - academic use
HOME
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/ ▸ Users ▸ oceliker ▸ Documents ▸ MATLAB ▸
Current Folder
Name
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sample.m
Workspace
Name
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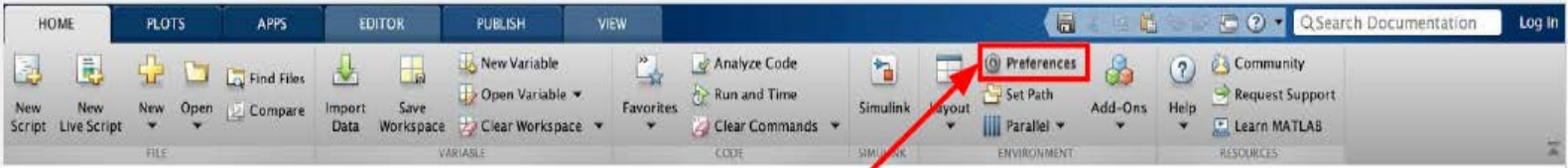
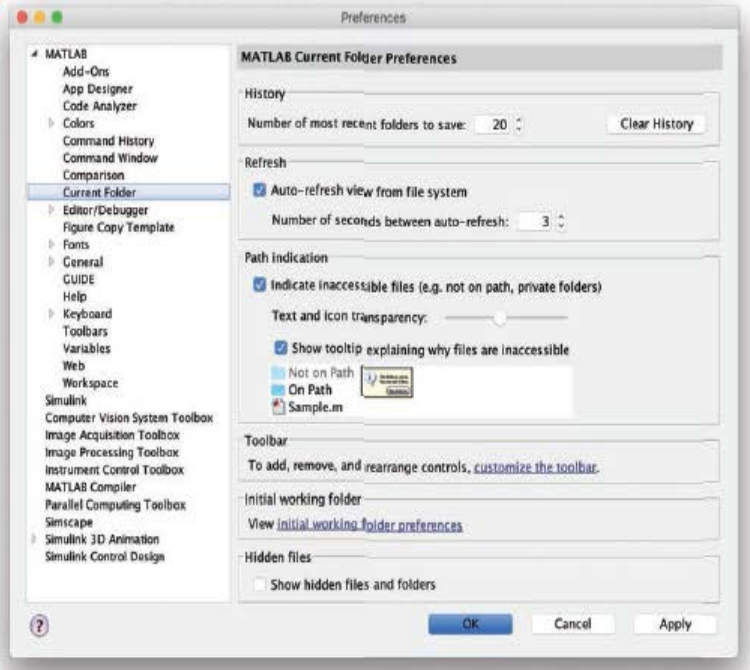
Command Window
New to MATLAB? See resources for Getting Started.
>>
Workspace
Details
Details
Select a file to view details
Command Window
6

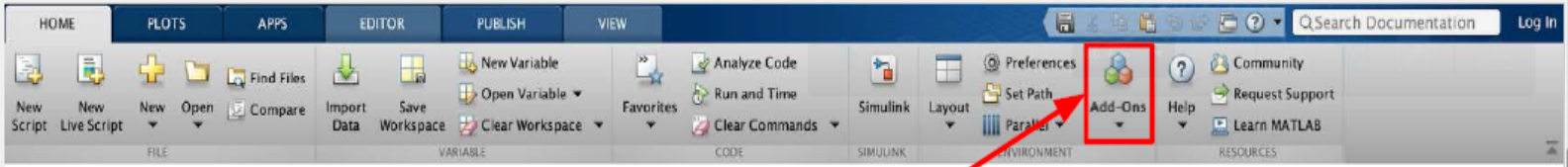


Customization

- In the top ribbon, navigate to: Home -> Environment -> Preferences

- Allows you to customize your MATLAB experience (colors, fonts, etc.)



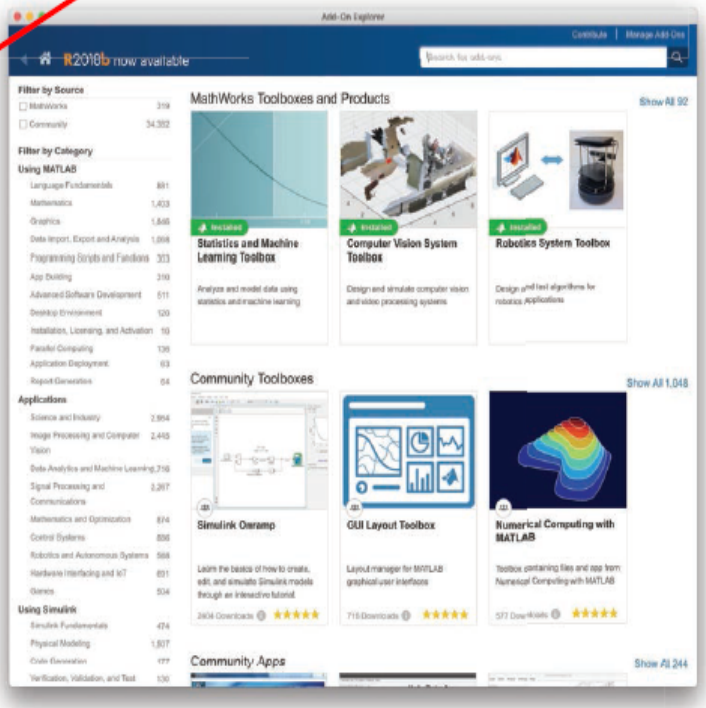


Installing Toolboxes

- In the top ribbon, navigate to:
  Home -> Environment -> Add-Ons

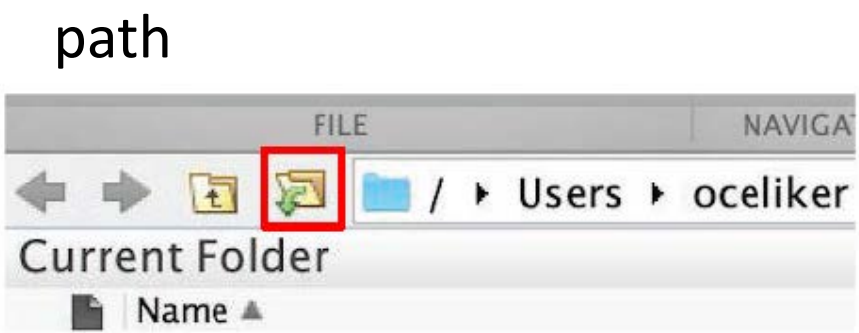
- Allows you to install toolboxes included with your license

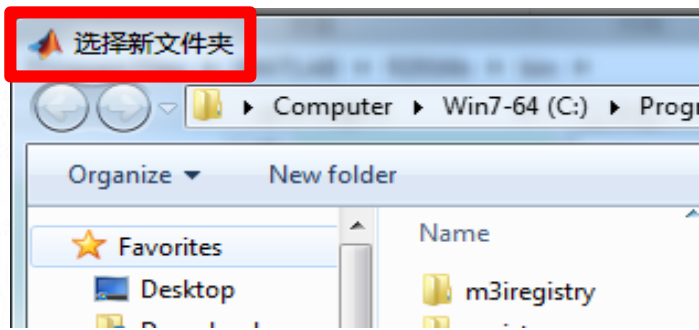
- Recommended toolboxes:
  - Curve Fitting Toolbox
  - Computer Vision System Toolbox
  - Image Processing Toolbox
  - Optimization Toolbox
  - Signal Processing Toolbox
  - and anything related to your field!



Making Folders

- Use folders to keep your programs organized
- To select a new folder, click "Browse" next to the file path





- In the MATLAB folder, make the following folder structure:

MATLAB

↳ Lecture1

Help/Docs

- help
  - The most important command for learning MATLAB on your own!
- To get info on how to use a function:
  - help sin
    - Help lists related functions at the bottom and links to the documentation
- To get a nicer version of help with examples and easy-to-read description:
  - doc sin
- To search for a function by specifying keywords:
  - doc search sin trigonometric

II. SCRIPTS

Scripts: Overview

- Scripts are :
  - Collection of commands executed in sequence
  - Written in the Matlab editor
  - Saved as m-files (*.m)
- To create an m-file:
  - From command line: edit Lecture1.m
  - Click the “new script” button on the top left

Scripts: Some notes

- Comment!
  - Anything following a % sign is interpreted as a comment
  - The first continuous comment becomes the script's help file
  - Comment thoroughly to avoid wasting time later
  - Mark beginning of a code block by using %%
- Scripts are static, with no explicit input or output
- All variables created in a script retain their values after script execution

Exercise1-1: Scripts

- Make a script with the name HelloWord.m
- When run, the script should show the following text:

```
Hello World!
I am going to learn Matlab
```

Hint: use disp(…) to display strings.
Strings are written in single quotes. Eg: ‘ This is a string’.

III. MAKING VARIABLES

Variable Types

- Matlab is a “weakly typed” language
  - No need to declare a variable
- Most variables you will deal with are doubles, chars, vectors and matrices
- Other types are also supported, such as complex, symbolic, 16bits or 8bits integers(uint16 or uint8), etc.

Naming Variables

- To create a variable, simply assign a value to a name:

```
myNumberVariable = 3.14
myStringVariable = 'hello world!'
```

- Variable name rules
  - First character must be a LETTER
  - After that, any combination of numbers, letters and _
  - Names are CASE-SENSITIVE

Naming Variables (cont.)

Built-in variables (don't use these names for anything else):

i, j: can be used to indicate complex numbers

a = 2.5 + 3.4i

a = 2.5 + 3.4j

use ii, jj, kk, etc. for loop counters.

pi: has the value 3.1415……

ans: stores the result of the last unassigned value

Inf, -Inf: infinities

NaN: "Not a Number"

Scalars

- A variable can be given a value explicitly
  - a = 10
  - Shows up in workspace
- Or as a function of explicit values and existing variables
  - c = 1.3 * 45 – 2 * a
- To suppress output, end the line with a semicolon
  - d = 13/3;

Arrays

- Like other programming languages, arrays are an important part of MATLAB
- Two types of arrays:
  - Matrix of numbers (either double or complex)
  - Cell array of objects (more advanced data structure)

Row vectors

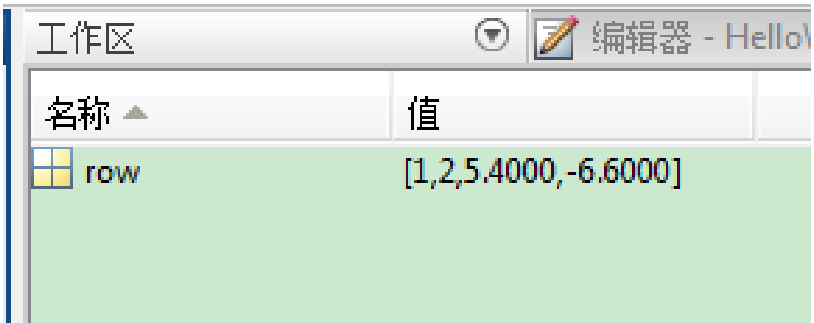
- Row vector: comma- or space-separated values between square brackets[ ]
  - row = [1 2 3 4 5 6]
  - Row = [1, 2, 3, 4, 5, 6]
- Command window:

```
>> row = [1 2 5.4 -6.6]

row =

    1.0000    2.0000    5.4000   -6.6000
```

- Workspace:



Column vectors

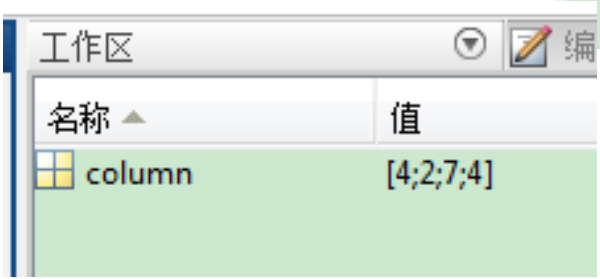
- Column vector: semicolon-separated values between square brackets [ ]
  - col = [1; 2; 3.2; 4; 6; -5.4];
- Command window

```
>> column = [4;2;7;4]

column =

     4
     2
     7
     4
```

- Workspace:



Size and length

- You can tell the difference between a row and a column by:
  - Looking in the workspace;
  - Displaying the variable in the command window
  - Using the size function

```
>> size(row)

ans =

>> length(row)

ans =

     4
```

```
>> size(column)

ans =

>> length(column)

ans =

     4
```

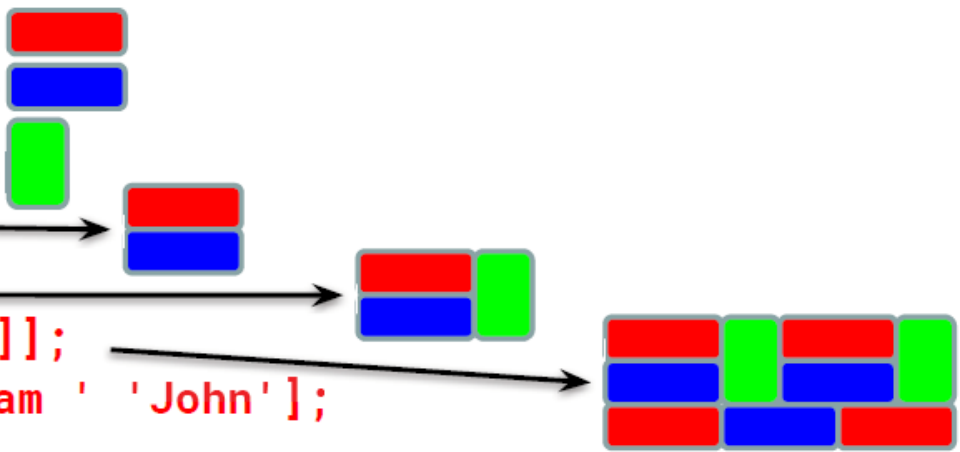
Matrices

- Make matrices like vectors, element by element
  - a = [1 2; 3 4];

$$a = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

- By concatenating vectors or matrices(dimension matters)

```
a = [1 2];
b = [3 4];
c = [5;6];
d = [a;b];
e = [d c];
f = [[e e];[a b a]];
str = ['Hello, I am ' 'John'];
```



- Strings are character vectors

save/clear/load

- Use save to save variables to a file
  - save myFile a b
  - Saves variables a and b to the file myFile.mat in the current directory
- clear and load

```
>> save myFile str;
>> clear str;   % look at workspace, a and b are gone
>> load myFile  % look at workspace, a and b are back
>>
```

Exercise1-2: Variables

Get and save the current date and time

- Create a variable start using the function clock
- What is the size of start? Is it a row or column?
- What does start contain? See help clock
- Convert the vector start to a string. Use the function datestr and name the new variable startString
- Save start and startString into a mat file named startTime

Exercise1-3: Variables II

- In HelloWorld.m, read in variables you saved using load
- Display the following text:
  - ***I started learning MATLAB on [date, time]***
- Hint: use the disp command again
- Remember that strings are just vectors of characters, so you can join 2 strings by making a row vector with the 2 strings as sub-vectors

IV.
MANIPULATING VARIABLES

Basic Scalar Operations

- Arithmetic operations (+, -, *, /)
  - `7/45`
  - `(1+1i)*(1+2i)`
  - `1/0`
  - `0/0`
- Exponentiation
  - `4^2`
  - `(3+4*1j)^2`
- Complicated expressions: use parentheses
  - `((2+3)*3)^0.1`

Built-in Functions

- MATLAB has an enormous library of built-in functions
- Call using parentheses, passing parameters to function
  - `sqrt(2)`
  - `log(2), log10(0.23)`
  - `cos(1.2), atan(-.8)`
  - `exp(2+4*1i)`
  - `round(1.4), floor(3.3), ceil(4.23)`
  - `angle(1i); abs(1+1i);`

```
>> ceil(4.23)

ans =

     5
```

```
>> angle(i)

ans =

    1.5708
```

```
>> abs(1+i)

ans =

    1.4142
```

Exercise1-4: Scalars

HelloWorld script:

- Your learning time constant is 0.75 hrs. Calculate seconds in 0.75 hrs and name this variable tau
- This class lasts 30 hrs. Calculate seconds in 30 hrs and name this variable endOfClass
- This equation describes your knowledge as a function of time t $k = 1 - e^{-t/\tau}$
- How well will you know MATLAB at endOfClass? Name this variable knowledgeAtEnd (use exp)
- Using the value of knowledgeAtEnd, display the phrase:
  - ***At the end of class, I will know X% of MATLAB.***
  - Hint: to convert a number to a string, us num2str

Transpose

- The transpose operator turns a column vector into a row vector, and vice versa
  - `a = [1 2 3 4+i]`
  - `transpose(a)`
  - `a'`
  - `a.'`
- The ' gives the Hermitian-transpose
  - Transposes and conjugates all complex numbers
- For vectors of real numbers .' and ' give same result
  - For transposing a vector, always use .' to be safe

Addition and Subtraction

- Addition and subtraction are element-wise
- Sizes must match (unless one is a scalar):

$$\begin{array}{r} [12 \quad 3 \quad 32 \quad -11] \\ +[2 \quad 11 \quad -30 \quad 32] \\ \hline =[14 \quad 14 \quad 2 \quad 21] \end{array}$$

$$\begin{bmatrix} 12 \\ 1 \\ -10 \\ 0 \end{bmatrix} - \begin{bmatrix} 3 \\ -1 \\ 13 \\ 33 \end{bmatrix} = \begin{bmatrix} 9 \\ 2 \\ -23 \\ -33 \end{bmatrix}$$

Addition and Subtraction

- `c = row + column`

Use the transpose to make sizes compatible

- `c = row.' + column`
- `c = row + column.'`

Can sum up or multiply elements of vector

- `s=sum(row);`
- `p=prod(row);`

Element-wise functions

- All the functions that work on scalars also work on vectors
  - t = [1 2 3];
    f = exp(t);
    is the same as
    f = [exp(1) exp(2) exp(3)];
- If in doubt, check a function's help file to see if it handles vectors element-wise
- Operators (* / ^) have two modes of operation
  - element-wise
  - standard

Element-wise functions

- To do element-wise operations, use the dot: . (.*, ./, .^)
- BOTH dimensions must match (unless one is scalar)!

```
a=[1 2 3];b=[4;2;1];

a.*b  , a./b  , a.^b → all errors

a.*b.', a./b.', a.^(b.') → all valid
```

Operators

- Multiplication can be done in a standard way or element-wise
- Standard multiplication (*) is matrix product
  - Remember from linear algebra: inner dimensions must MATCH!!
- Standard exponentiation (^) can only be done on square matrices or scalars
- Left and right division (/ \) is same as multiplying by inverse
  - Our recommendation: for now, just multiply by inverse (more on this later)

$$\begin{bmatrix}1 & 2 & 3\end{bmatrix} * \begin{bmatrix}4\\2\\1\end{bmatrix} = 11$$

$$1\times 3 * 3\times 1 = 1\times 1$$

$$\begin{bmatrix}1 & 2\\3 & 4\end{bmatrix} \wedge 2 = \begin{bmatrix}1 & 2\\3 & 4\end{bmatrix} * \begin{bmatrix}1 & 2\\3 & 4\end{bmatrix}$$

Must be square to do powers

$$\begin{bmatrix}1 & 1 & 1\\2 & 2 & 2\\3 & 3 & 3\end{bmatrix} * \begin{bmatrix}1 & 2 & 3\\1 & 2 & 3\\1 & 2 & 3\end{bmatrix} = \begin{bmatrix}3 & 6 & 9\\6 & 12 & 18\\9 & 18 & 27\end{bmatrix}$$

$$3\times 3 * 3\times 3 = 3\times 3$$

Exercise1-5: Vector Operations

Calculate how many seconds elapsed since start of class

- In helloWorld.m, make variables called secPerMin, secPerHour, secPerDay, secPerMonth (assume 30.5 days per month), and secPerYear (12 months in year), which have the number of seconds in each time period
- Assemble a row vector called secondConversion that has elements in this order: secPerYear, secPerMonth, secPerDay, secPerHour, secPerMin, 1
- Make a currentTime vector by using clock
- Compute elapsedTime by subtracting currentTime from start
- Compute t (the elapsed time in seconds) by taking the dot product of secondConversion and elapsedTime (transpose one of them to get the dimensions right)

Exercise1-5: Vector Operations

Display the current state of your knowledge

- Calculate currentKnowledge using the same relationship as before, and the t we just calculated:

$$k = 1 - e^{-t/\tau}$$

- Display the following text:
  At this time, I know X% of MATLAB

Automatic Initialization

- Initialize a vector of **ones**, **zeros**, or **random** numbers
  - » `o=ones(1,10)`
    - ➢ Row vector with 10 elements, all 1
  - » `z=zeros(23,1)`
    - ➢ Column vector with 23 elements, all 0
  - » `r=rand(1,45)`
    - ➢ Row vector with 45 elements (uniform (0,1))
  - » `n=nan(1,69)`
    - ➢ Row vector of NaNs (representing uninitialized variables)

Automatic Initialization

- To initialize a linear vector of values use **linspace**
  - » `a=linspace(0,10,5)`
    - ➢ Starts at 0, ends at 10 (inclusive), 5 values
- Can also use colon operator (**:**)
  - » `b=0:2:10`
    - ➢ Starts at 0, increments by 2, and ends at or before 10
    - ➢ Increment can be decimal or negative
  - » `c=1:5`
    - ➢ If increment is not specified, default is 1
- To initialize logarithmically spaced values use **logspace**
    - ➢ Similar to **linspace**, but see **help**

Exercise1-6: Vector Functions

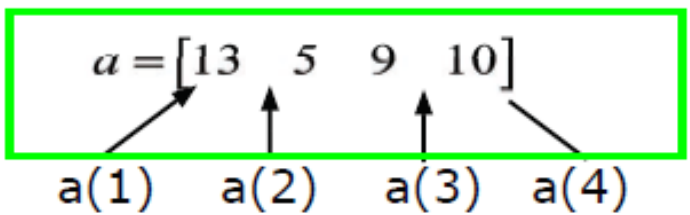
Calculate your learning trajectory

- In helloWorld.m, make a linear time vector `tVec` that has 10,000 samples between 0 and `endOfClass`
- Calculate the value of your knowledge (call it `knowledgeVec`) at each of these time points using the same equation as before:

$$k = 1 - e^{-t/\tau}$$

Vector Indexing

- MATLAB indexing starts with **1**, not **0**
  - ➢ We will not respond to any emails where this is the problem.
- a(n) returns the n^{th} element

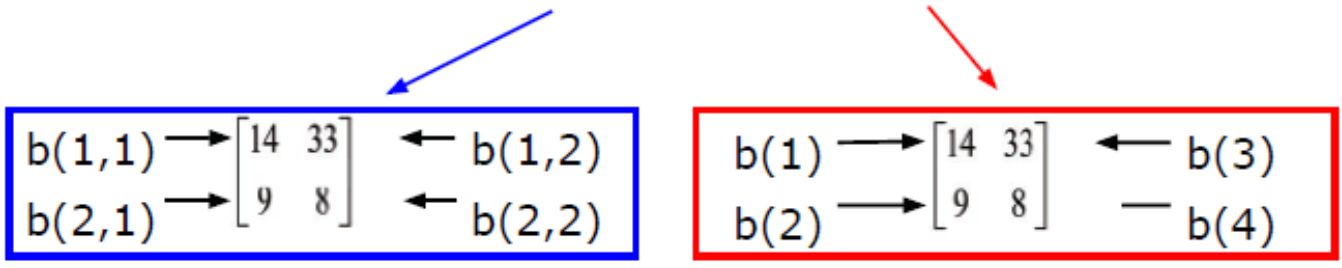


- The index argument can be a vector. In this case, each element is looked up individually, and returned as a vector of the same size as the index vector.

```
» x=[12 13 5 8];
```

Matrix Indexing

- Matrices can be indexed in two ways
  - ➢ using **subscripts** (row and column)
  - ➢ using linear **indices** (as if matrix is a vector)
- Matrix indexing: subscripts or linear indices



- Picking submatrices

```
» A = rand(5) % shorthand for 5x5 matrix
```

Advanced Indexing 1

- To select rows or columns of a matrix, use the **:**

$$c = \begin{bmatrix} 12 & 5 \\ -2 & 13 \end{bmatrix}$$

```
» d=c(1,:);          d=[12 5];
» e=c(:,2);          e=[5;13];
» c(2,:)=[3 6];   %replaces second row of c
```

Advanced Indexing 2

- MATLAB contains functions to help you find desired values

```
» vec = [5 3 1 9 7]
```

- To get the minimum value and its index (similar for `max`):

```
» [minVal,minInd] = min(vec);
```

- To find the indices of specific values or ranges

```
» ind = find(vec == 9); vec(ind) = 8;
» ind = find(vec > 2 & vec < 6);
```

  - ➢ **find** expressions can be very complex, more on this later
  - ➢ When possible, **logical indexing** is faster than **find**!
  - ➢ E.g., `vec(vec == 9) = 8;`

Exercise1-7: Vector Functions

When will you know 50% of MATLAB?

- First, find the index where **knowledgeVec** is closest to 0.5. Mathematically, what you want is the index where the value of ~ $|knowledgeVec - 0.5|$ is at a minimum (use **abs** and **min**)
- Next, use that index to look up the corresponding time in **tVec** and name this time **halfTime**
- Finally, display the string:
  Convert **halfTime** to days by using secPerDay. I will know half of MATLAB after X days

V. BASIC PLOTTING

Plotting

- Example

```
» x=linspace(0,4*pi,10);
» y=sin(x);
```

- Plot values against their index

```
» plot(y);
```

- Usually we want to plot y versus x

```
» plot(x,y);
```

What does plot do?

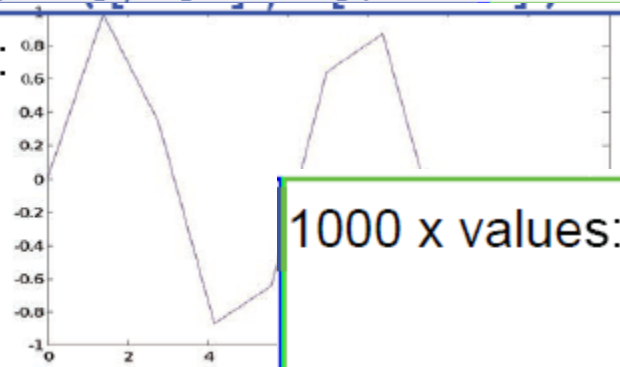
- **plot** generates dots at each (x,y) pair and then connects the dots with a line
- To make plot of a function look smoother, evaluate at more points

```
» x=linspace(0,4*pi,1000);
» plot(x,sin(x));
```

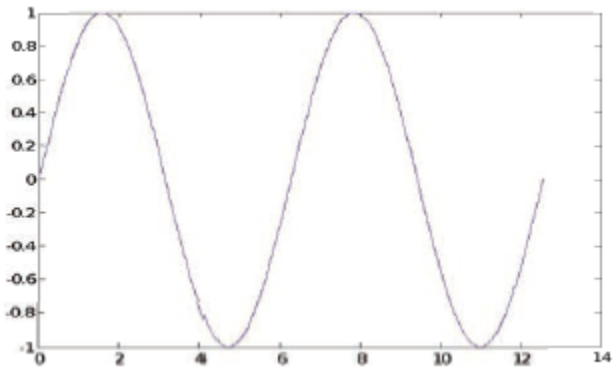
- x and y vectors must be same size or else you'll get an error

```
» plot([1 2], [1 2 3])
```

10 x values:



1000 x values:



Axis

- Built-in axis modes (see `doc axis` for more modes)

  - `axis square`
    - makes the current axis look like a square box
  - `axis tight`
    - fits axes to data
  - `axis equal`
    - makes x and y scales the same
  - `axis xy`
    - puts the origin in the lower left corner (default for plots)
  - `axis ij`
    - puts the origin in the upper left corner (default for matrices/images)

Axis Label, limit figure title, legend

xlabel('label')
ylabel('label')

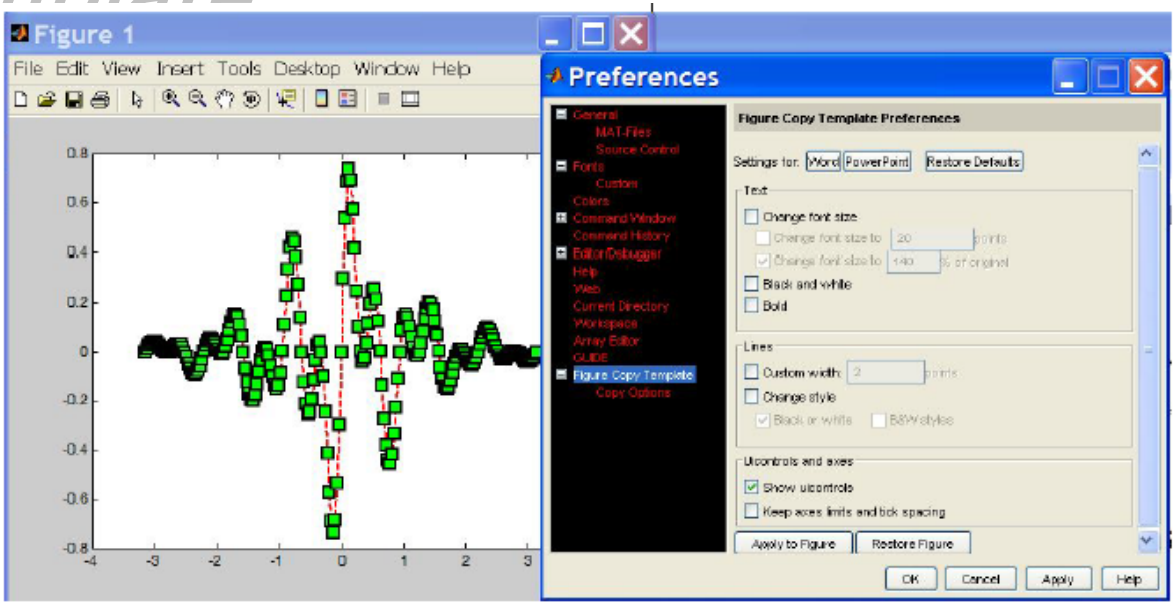
xlimit([xmin xmax])
ylimit([ymin ymax])

title('figure title')

legend('str1' ,' str2' ,....)

Copy/Paste Figures

- Figures can be pasted into other apps (word, ppt, etc)
- *Edit → copy options→ figure copy template*



Saving Figures

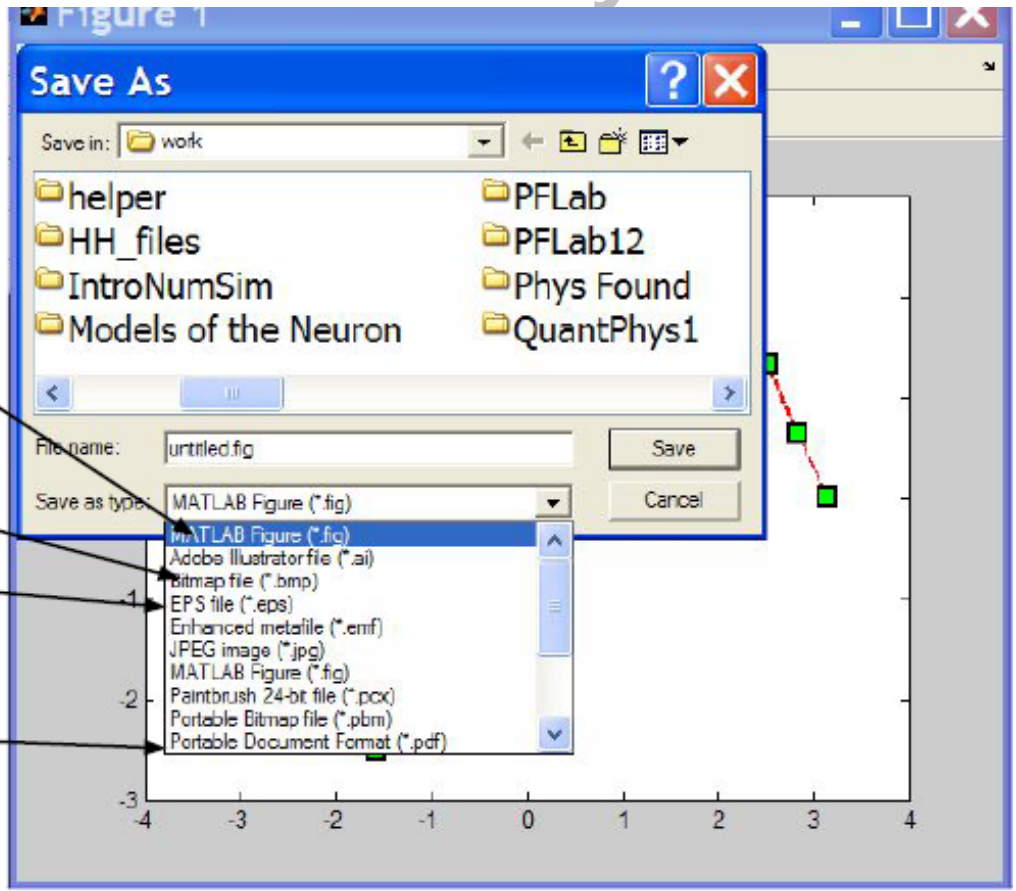
Figures can be saved in many formats.

.fig preserves all information

.bmp uncompressed image

.eps high-quality scaleable format

.pdf compressed image



Exercise1-8: Plotting

Plot the learning trajectory

- In helloWorld.m, open a new figure (use `figure`)
- Plot knowledge trajectory using `tVec` and `knowledgeVec`
- When plotting, convert `tVec` to days

柱状图

bar(x, width, ‘mode’)

width: 竖条宽度，>1则竖条重叠；

mode：默认分组式’grouped’； ‘stacked’ 堆栈式

bar3(x, width, ‘mode’) %三维柱状图

barh(x, width, ‘mode’), barh3(x, y, width, ‘mode’)

柱为水平

例：已知某班4位同学，在5门课程考试中取得如下表所示成绩，分别用垂直柱状图、水平柱状图、三维垂直柱状图和三维水平柱状图显示成绩。

	课程1	课程2	课程3	课程4	课程5
学生1	98	90	60	75	80
学生2	78	87	90	80	65
学生3	50	70	89	99	92
学生4	86	83	70	60	94

```
>> x=[98 90 60 75 80;78 87 90 80 65;50 70 89 99 92;86 83 70 60 94]
>> subplot(2,2,1);
>> bar(x);
>> subplot(2,2,2);barh(x,'stacked');
>> subplot(2,2,3);bar3(x);
>> subplot(2,2,4);bar3h(x);
```