

# **MATLAB 科学计算语言与应用**

## **Lecture 5: Various functions and toolboxes**

# Outline

- **Symbolic Toolbox**
- Simulink
- Image Processing
- Miscellaneous Useful Functions
- Graphical User Interfaces

# Miscellaneous Matlab (1)

- The command deal can make variable initialization simpler
  - »[x, y, z] = deal(zeros(20, 30));
  - »[a, b, c, d] = deal(5);
  - »[m, n] = deal(1, 100);
- The command eval can execute a string!
  - »a1 = 1; n = 1;
  - »eval([ 'a' num2str(n) ' = 5;' ]);
  - »disp([ 'a1 is now ' num2str(a1)]);
- The command repmat can create replicas easily
  - »A = repmat([1 2;3 4], 2, 2);

# Symbolic Toolbox

- Don't do nasty calculations by hand!
- Symbolics vs. Numerics

	Advantages	Disadvantages
Symbolic	<ul style="list-style-type: none"><li>• Analytical solutions</li><li>• Lets you intuit things about solution form</li></ul>	<ul style="list-style-type: none"><li>• Sometimes can't be solved</li><li>• Can be overly complicated</li></ul>
Numeric	<ul style="list-style-type: none"><li>• Always get a solution</li><li>• Can make solutions accurate</li><li>• Easy to code</li></ul>	<ul style="list-style-type: none"><li>• Hard to extract a deeper understanding</li><li>• Num. methods sometimes fail</li><li>• Can take a while to compute</li></ul>

# Symbolic Variables

- Symbolic variables are a type, like **double** or **char**
- To make symbolic variables, use **sym**
  - » **a=sym('1/3');** %fractions remain as fractions
  - » **b=sym('4/5');**
  - » **mat=sym([1 2;3 4]);**
- can add tags to narrow down scope
  - » **c=sym('c','positive');**
  - see **help sym** for a list of tags
- Or use **syms**
  - » **syms x y real**
    - shorthand for **x=sym('x','real');** **y=sym('y','real');**

# Symbolic Expressions

- Multiply, add, divide expressions

» `d=a*b`  $\longrightarrow$  d =  
4/15

➤ does  $1/3 * 4/5 = 4/15$ ;

» `expand((a-c)^2)` ;  $\longrightarrow$  ans =  
 $1/9 - 2/3 * c + c^2$

➤ multiplies out

» `factor(ans)`  $\longrightarrow$  ans =  
[ 1/9, 3\*c - 1, 3\*c - 1]

➤ factors the expression

» `pretty(ans)`  $\longrightarrow$  

$$\frac{1}{9} (3c - 1)^2$$

➤ makes it look nicer

# Cleaning up Symbolic Statements

» `collect(3*x+4*y-1/3*x^2-x+3/2*y)`

➤ collects terms

ans =  
2\*x+11/2\*y-1/3\*x^2

**`collect(g, v)`**: 按指定的表达式或变量v整理表达式g

» `simplify(cos(x)^2+sin(x)^2)`

➤ simplifies expressions

ans =  
1

» `subs(c^2, c, 5)`

➤ replaces variables with numbers

ans =  
25

or expressions. To do multiple substitutions

pass a cell of variable names followed by a cell of values

» `subs(c^2, c, x/7)`

ans =  
x^2/49

# More Symbolic Operations

- We can do symbolics with matrices too

- » `mat = sym([a b; c d])`

- » `mat=sym('A%d%d', [2 2]);`

- symbolic matrix of specified size

- » `mat2=mat*[1 3;4 -2];` →

- compute the product

```
mat2 =  
[      a+4*b, 3*a-2*b]  
[      c+4*d, 3*c-2*d]
```

- » `d=det(mat)` →

- compute the determinant

```
d =  
a*d-b*c
```

- » `i=inv(mat)` →

- find the inverse

```
i =  
[  d/(a*d-b*c), -b/(a*d-b*c)]  
[ -c/(a*d-b*c),  a/(a*d-b*c)]
```

- You can access symbolic matrix elements as before

- » `i(1,2)` →

```
ans =  
-b/(a*d-b*c)
```



## • 求符号根

```
>> syms x a b c;  
>> m=a*x^2+b*x+c;  
>> n=[a b c];  
>> roots(n)
```

```
ans =  
-(b + (b^2 - 4*a*c)^(1/2))/(2*a)  
-(b - (b^2 - 4*a*c)^(1/2))/(2*a)
```

## • 求反函数

**g=finverse(f, v)** %对指定变量v ( 默认为x ) 求反函数

```
>> syms t x a b;  
>> f1=b*exp(-t+a*x);  
>> g1=finverse(f1,t)  
g1 =  
a*x - log(t/b)  
>> g2=finverse(f1)  
g2 =  
(t + log(x/b))/a
```

## • 求复合函数

<code>compose(f, g)</code>	%用g代替f中x的位置
<code>compose(f, g, t)</code>	%用g代替f中t的位置
<code>compose(f, g, x, z)</code>	%用g(z)代替f(x)中x的位置
<code>compose(f, g, t, u, z)</code>	%用g(z)代替f(t,u)中的t，用z代替u

## • 求函数极限

<code>limit(f, x, a)</code>	%相当于 $\lim_{x \rightarrow a} f(x)$
<code>limit(f, x, a, 'right')</code>	% x右趋近于a
<code>limit(f, x, a, 'left')</code>	% x左趋近于a

## • 级数求和

`symsum(s,x,a,b)` %求s当x从a到b的级数和

例：

```
>> syms n k;  
>> symsum(n,0,k-1)  
ans =  
(k*(k - 1))/2
```

## • 符号微分（符号函数求导）

`diff(f, x, n)` %计算f对x的n阶导数

`diff(f, x, y, z)` %f先对x求偏导，再对y求偏导，再对z求偏导

## • 符号积分

`int(S, v, a, b)` %求函数S对变量v在[a, b]区间上的定积分

`int(S, v)` %求函数S对变量v的不定积分

例：求定积分  $\int_0^{\infty} \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx$

```
>> syms x;
```

```
>> f=1/sqrt(2*pi)*exp(-x^2/2);
```

```
>> int(f,0,inf)
```

```
ans =
```

```
(7186705221432913*2^(1/2)*pi^(1/2))/36028797018963968
```

# 符号方程求解: solve

- The equation of a circle of radius  $r$  centered at  $(a,b)$  is given by:  $(x-a)^2 + (y-b)^2 = r^2$
- Use `solve` to solve this equation for  $x$  and then for  $y$ 
  - » `syms a b r x y`
  - » `solve( (x-a)^2+(y-b)^2==r^2, x)`
  - » `solve( (x-a)^2+(y-b)^2==r^2, y)`
- It's always annoying to integrate by parts. Use `int` to do the following integral symbolically and then compute the value by substituting 0 for  $a$  and 2 for  $b$ :
$$\int_a^b x e^x dx$$
  - » `Q=int(x*exp(x), a, b)`
  - » `subs(Q, {a,b}, {0,2})`

# 符号常微分方程求解：dsolve

**S=dsolve(equation, condition, 'x')**

微分方程在指定条件下对指定自变量x进行求解

equation和condition，都需要是符号表达式，并且用“==”表示等号

例：求解 $y'' = -a^2 y$ ，初始条件 $y(0) = 1, y'(\frac{\pi}{a}) = 0$

```
>> syms y(t) a;    %定义y是t的函数，a是符号变量
>> Dy=diff(y);      %定义Dy是y的一阶导数
>> D2y=diff(y,2)    %定义D2y是y的二阶导数
>> yt=dsolve(D2y==-a^2*y, y(0)==1, Dy(pi/a)==0)
```

# 符号常微分方程组求解：dsolve

**[Sv1, Sv2, ...]=dsolve(eqn1,eqn2,..., cond1, cond2,..., 'x1', 'x2',....)**

微分方程组在指定条件下对指定自变量进行求解

equation和condition，都需要是符号表达式，并且用“==”表示等号

例：求解下列微分方程组，已知初始条件： $f(0) = 1, g(0) = 2$

$$\begin{cases} f'(t) = f(t) + g(t) \\ g'(t) = g(t) - f(t) \end{cases}$$

```
>> syms f(t) g(t)
```

```
>> Df=diff(f)
```

```
>> Dg=diff(g)
```

```
>> [sf,sg]=dsolve(Df==f+g,Dg==g-f,f(0)==1,g(0)==2)
```

# 符号函数可视化：绘图函数前面+ez

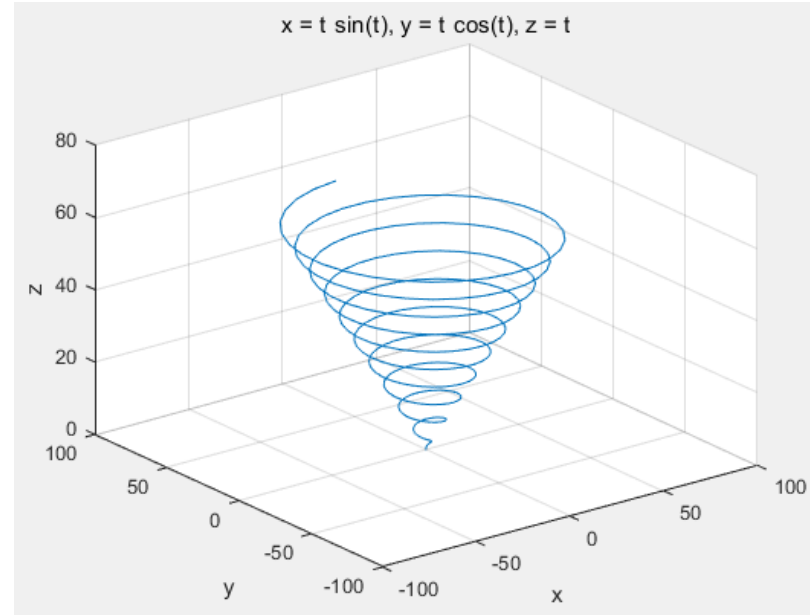
- ezplot, ezplot3, ezpolar, ezsurf, ezmesh, ezcontour,.....

例：绘制以下方程表示的三维图形， $t$ 的范围为 $[0, 20\pi]$

$$\begin{cases} x = t\sin(t) \\ y = t\cos(t) \\ z = t \end{cases}$$

```
>> syms t;  
>> ezplot3(t*sin(t),t*cos(t),t,[0 20*pi])
```

```
>> t=0:20*pi;  
>> plot3(t.*sin(t),t.*cos(t),t)
```



例：绘制函数

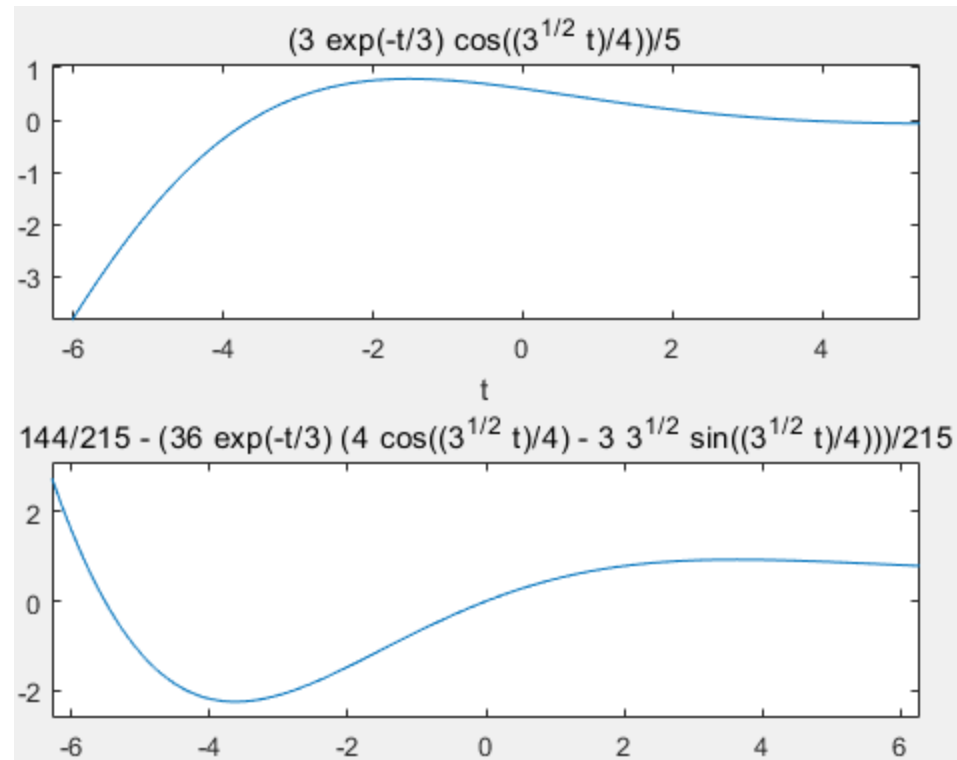
$$y(t) = 0.6e^{-\frac{t}{3}}\cos\frac{\sqrt{3}}{4}t,$$

及其积分上限函数

$$s(t) = \int_0^t y(t)dt$$

的图形。

```
>> syms t;  
>> y=0.6*exp(-t/3)*cos(sqrt(3)/4*t)  
>> subplot(2,1,1);ezplot(y);  
>> syms tao;  
>> s=subs(int(y,t,0,tao),tao,t)  
>> subplot(2,1,2);ezplot(s);
```





# Outline

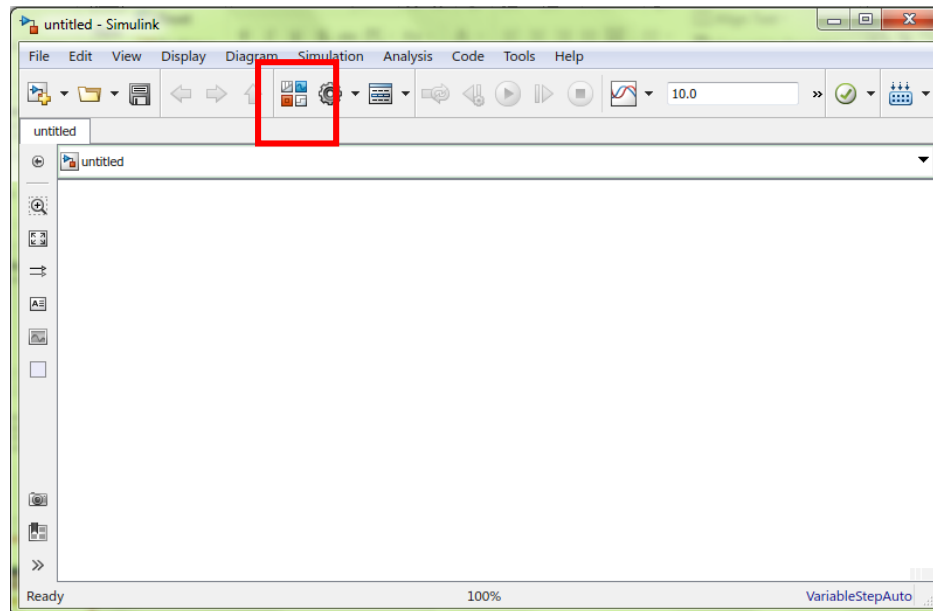
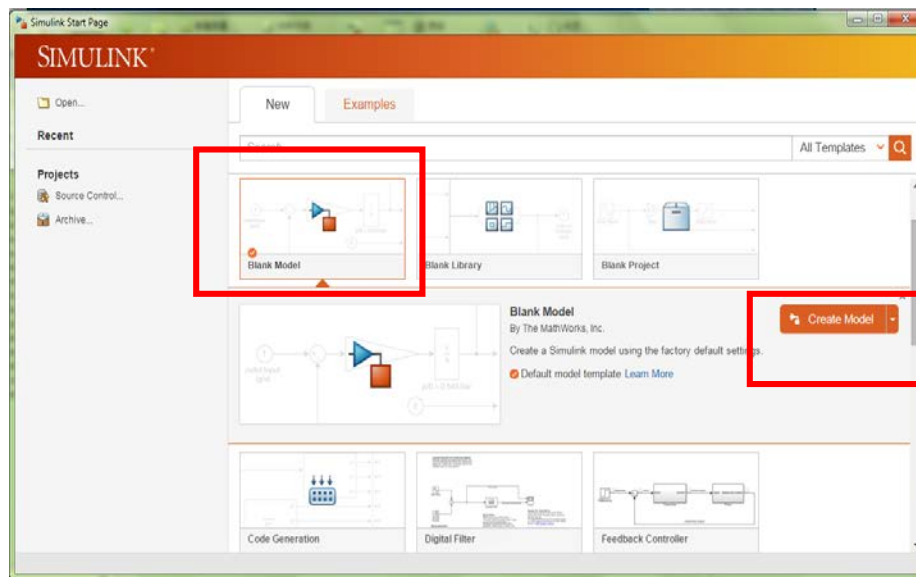
- Symbolic Toolbox
- **Simulink**
- Image Processing
- Miscellaneous Useful Functions
- Graphical User Interfaces

# SIMULINK

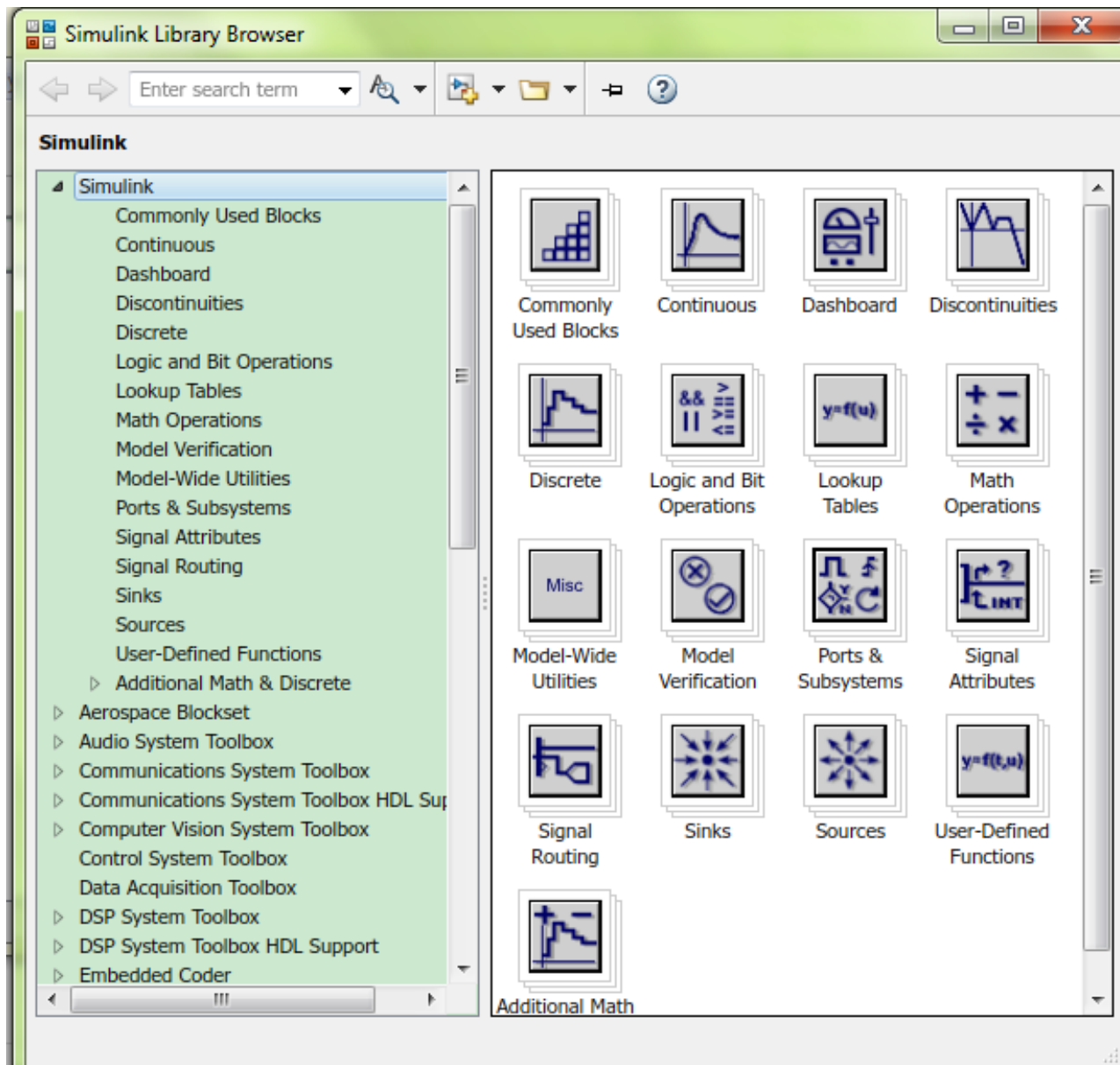
- Interactive graphical environment
- Block diagram based MATLAB add-on environment
- Design, simulate, implement, and test control, signal processing, communications, and other time-varying systems

# Getting Started



- In MATLAB, Start Simulink



# Simulink LibraryBrowser



# 例：将一个正弦信号输出到示波器

1. 打开模块库 ，查找正弦波模块sine
2. 选择0输入单输出的sine wave，拖入
3. 查找示波器模块scope，拖入
4. 连接sine wave的输出和示波器的输入
5. 单击  进行系统仿真
6. 双击示波器看结果

改参数试试：双击sine wave模块

改完参数重新仿真，看结果

Parameters

Sine type:

Time (t):

Amplitude:

Bias:

Frequency (rad/sec):

Phase (rad):

Sample time:

## • 步骤总结：

1. 从模块库中选择合适的模块（信源、信宿、处理系统）；
2. 按照实际系统的控制逻辑连接起来；
3. 设置模块参数（双击模块）和仿真参数（“Simulation” -> “Configuration Parameters”）；
4. 仿真调试

## Simulink 模块库：

- 基本模块(basic building blocks)
- 各种应用工具箱(toolboxes)

# Basic Building Blocks

- **Sources(信号源)**

- Provides input to your system

- » Step input, white noise, custom input, sine wave, ramp input ( 斜阶跃信号 ), constant

- **Sinks ( 信宿 , 输出设备模块库 )**

- » Scope: Outputs to plot , 示波器

- » simout: Outputs to a MATLAB vector (struct) on workspace

- » Matlab mat file

# Toolboxes

- Math
  - Takes the signal and performs a math operation
    - »Add, subtract, round, multiply, gain, product
- Continuous
  - Adds differential equations to the system
    - »Integrals, Derivatives, Transfer Functions, State Space
- Discontinuities
  - Adds nonlinearities to your system
    - »quantizer ( 量化器 ) , dead zone ( 死区 )
- Discrete
  - Simulates discrete difference equations
    - »Delay ( 延时 ) , Difference ( 差分 )
  - Useful for digital systems



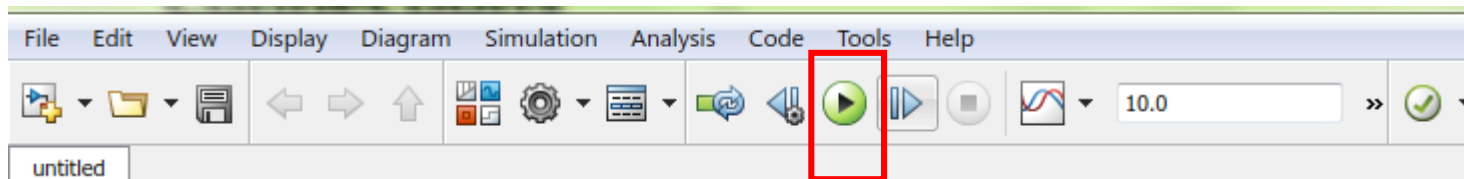
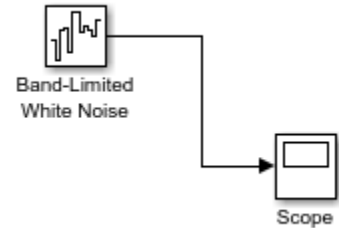
# Simulink Library Browser

- The **Library Browser** contains various blocks that you can put into your model
- Examine some blocks:
  - Click on a library: “Sources”
    - Drag a block into Simulink: “Band limited white noise”
  - Visualize the block by going into “Sinks”
    - Drag a “Scope” into Simulink

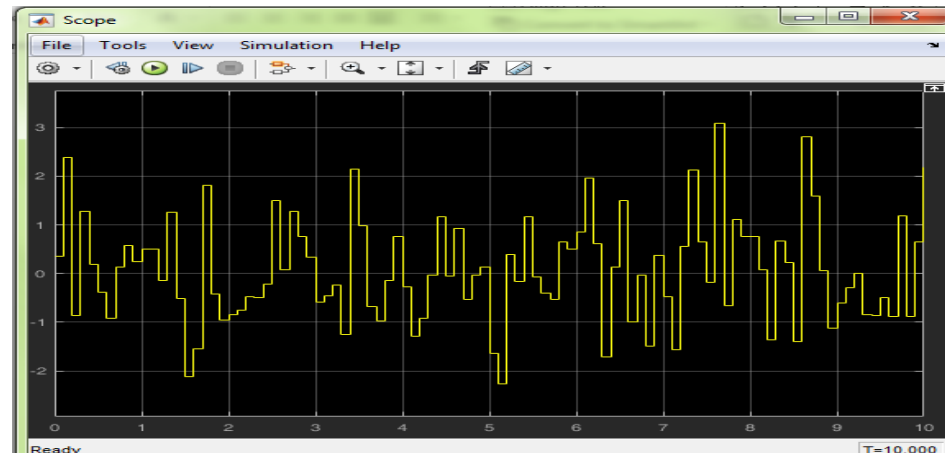


# Connections

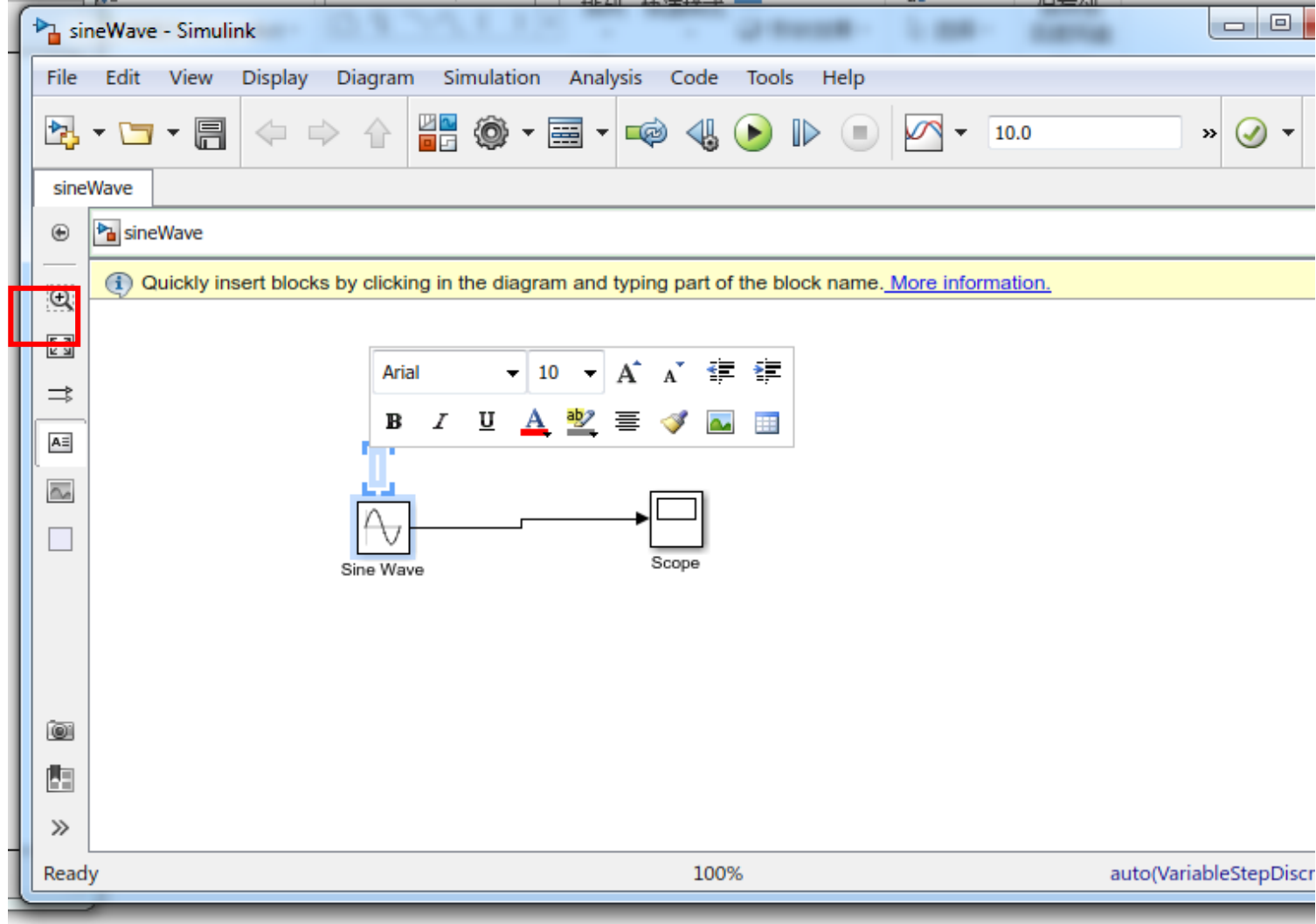
- Click on the arrow on the right of the **band limited white noise** box
- Drag the line to the **scope**
  - Connections between lines represent signal
- Click the **play** button



- Double click on the **scope**.
  - This will open up a chart of the variable over the simulation time



## • 模型注释

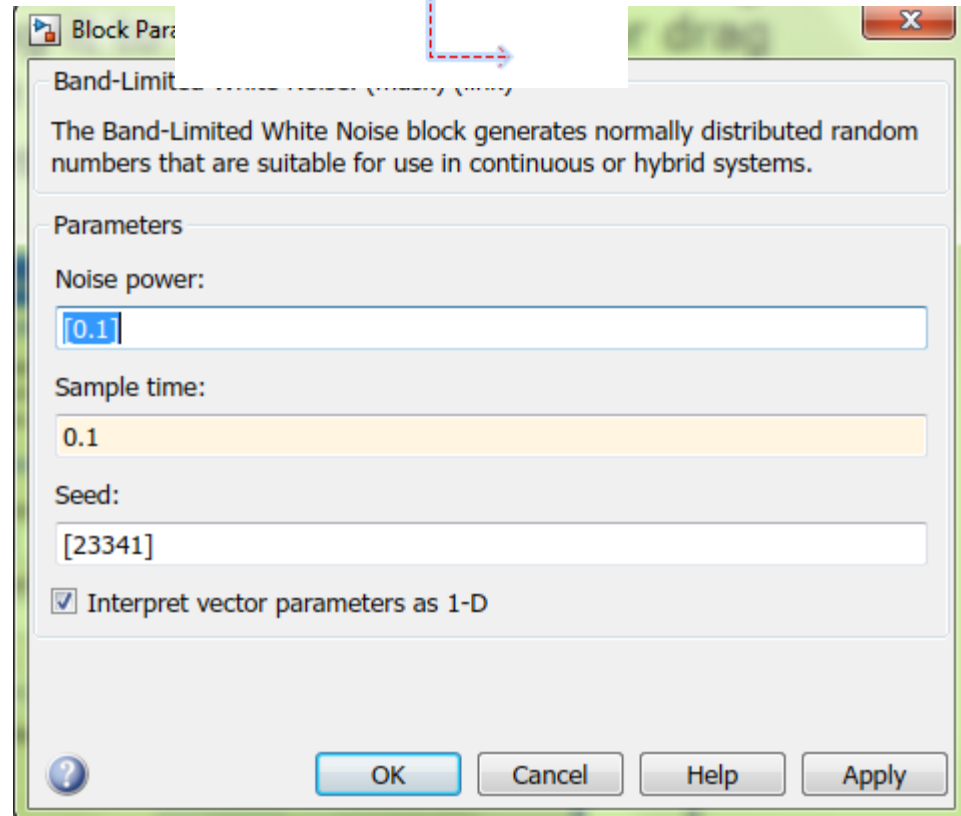
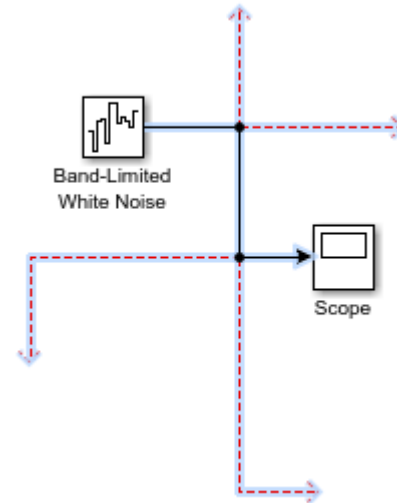


## • 信号标签设置

双击信号（即模块之间的连线），直接写

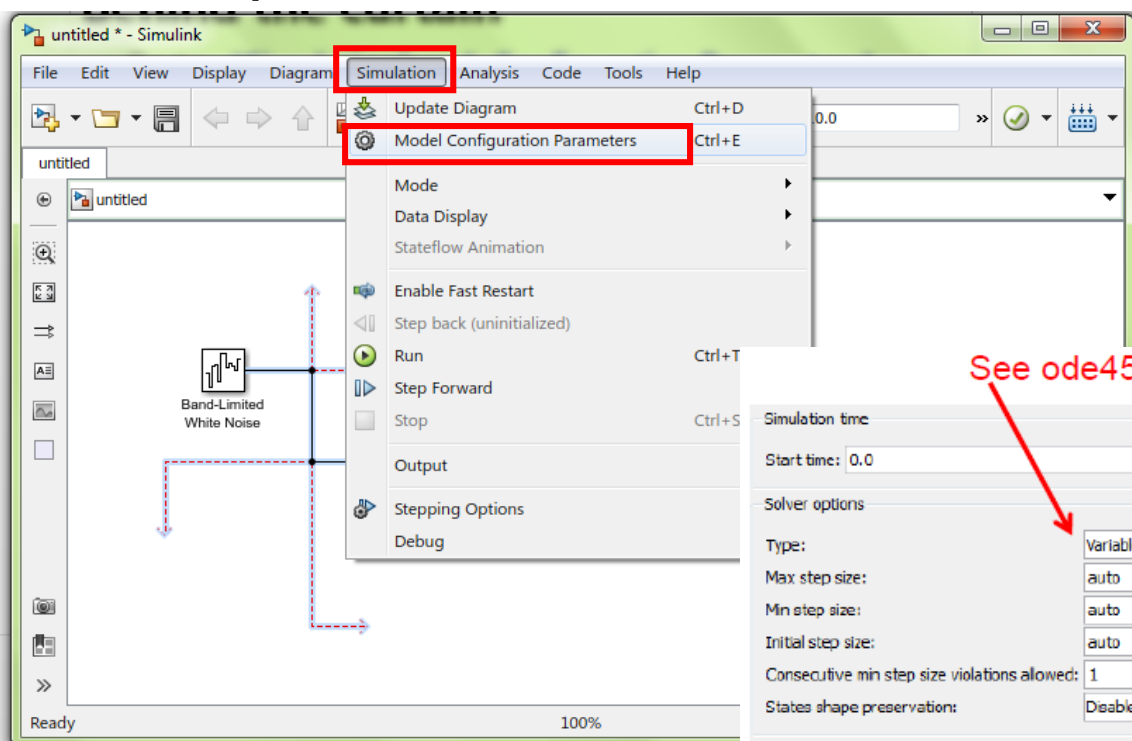
# Connections, Block Specification

- To split connections, hold down 'Ctrl' when clicking on a connection, and drag it to the target block; or drag backwards from the target block
- To modify properties of a block, double-click it and fill in the property values.

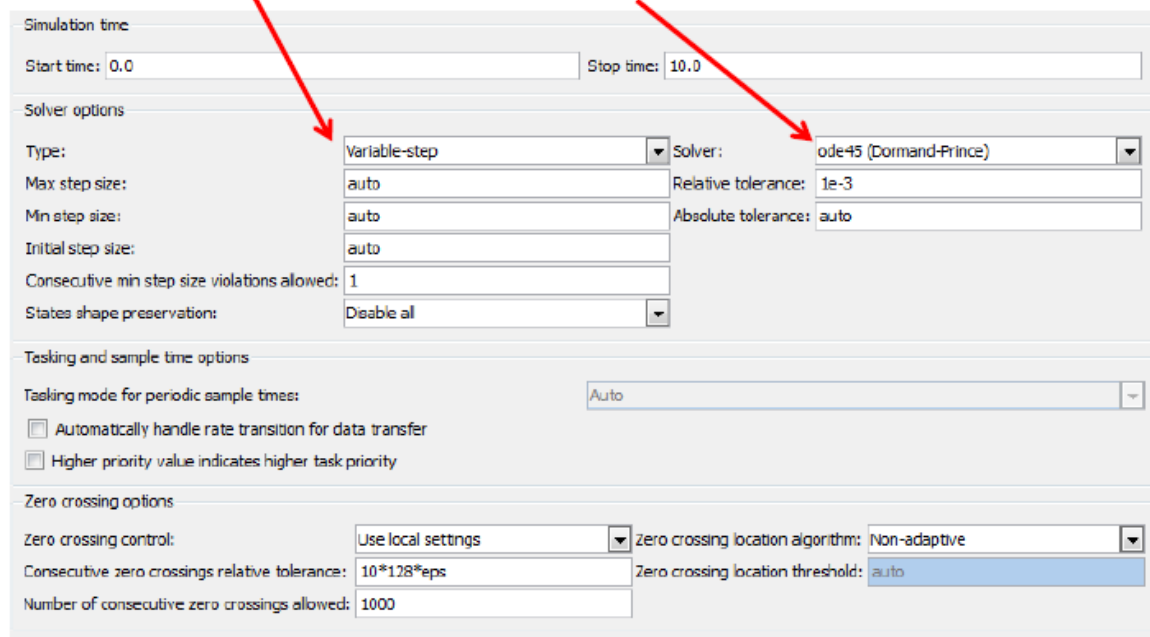


# 仿真参数设置

- Go to “Simulation” -> “Configuration Parameters” at the top menu



See ode45? Change the solver type here



# Exercise: Bouncing Ball Model

- Let's consider the following 1 dimensional problem
- A rubber ball is thrown from height  $h_0$  with initial velocity  $v_0$  in the  $z$ -axis (up/down).
- When the ball hits the ground ( $z=0$ ), its velocity instantaneously flips direction and is attenuated by the impact



# Exercise: Bouncing Ball Model

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$$m \frac{d^2 z}{dt^2} = mg \quad v(t) = \frac{dz}{dt} \quad v\left(t^+ \Big|_{z=0}\right) = -\kappa v\left(t^- \Big|_{z=0}\right)$$

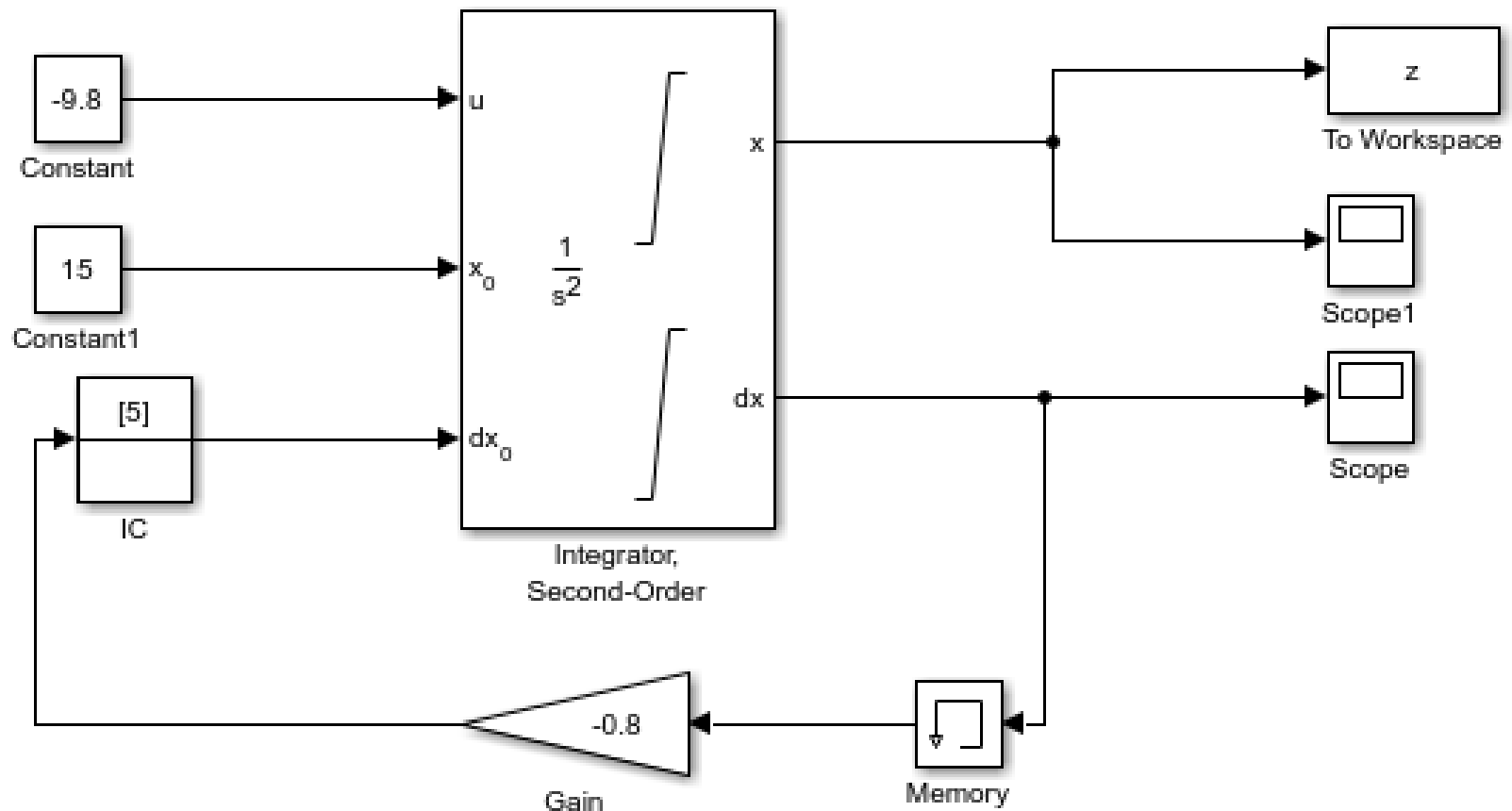
$$z(t=0) = h_0 \quad v(t=0) = v_0$$

- Integrating, we can obtain the balls height and velocity as a function of time

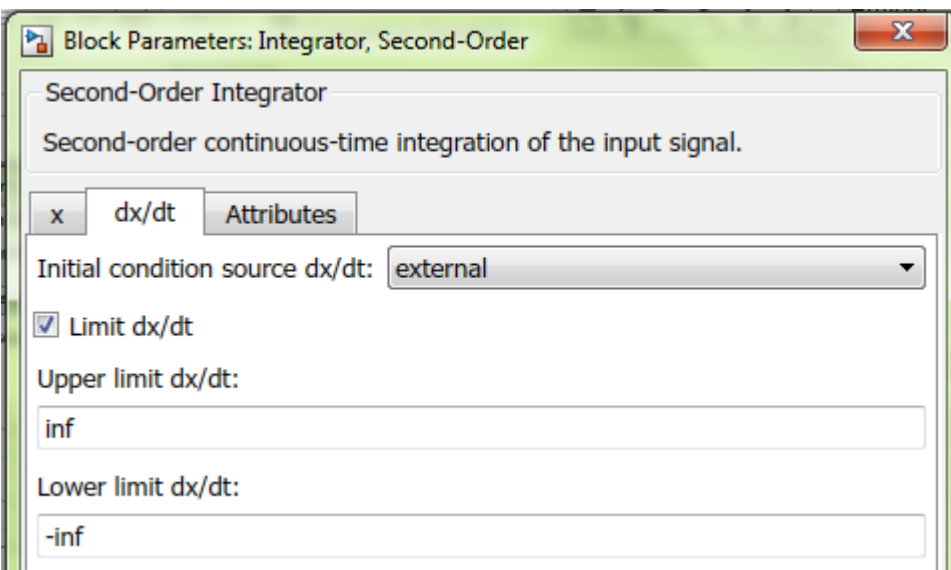
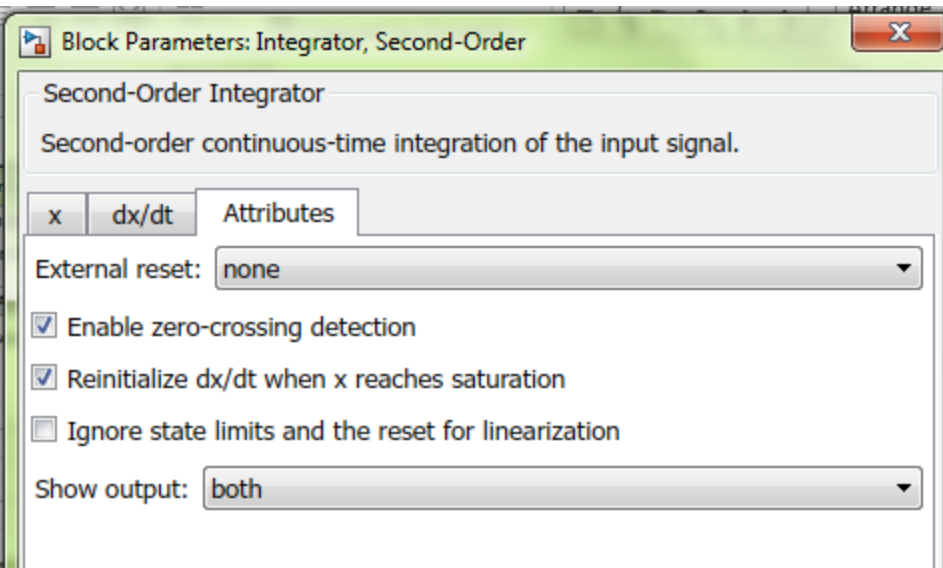
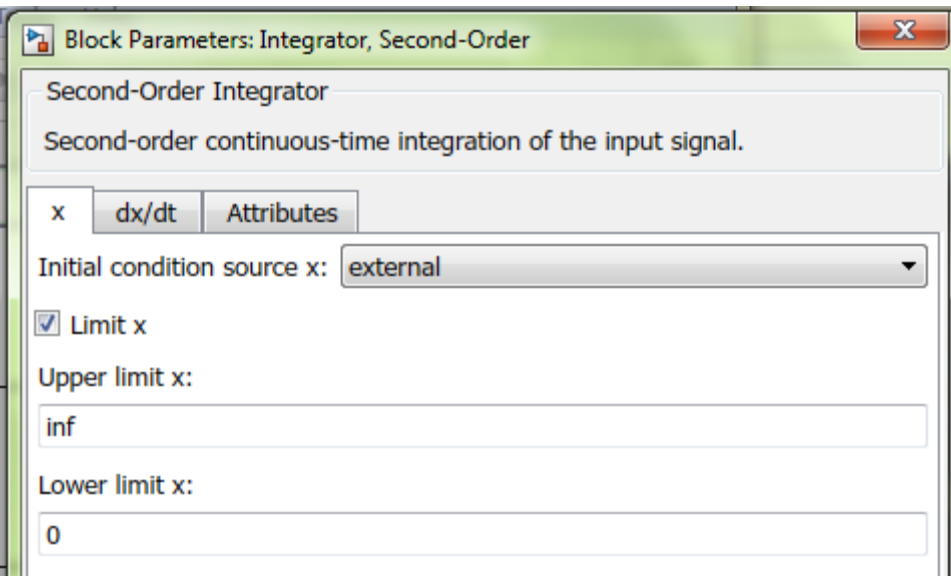
$$v(t) = \int_0^t g d\tau \quad z(t) = \int_0^t v(\tau) d\tau$$

# Exercise: Simulink Model

- Using the **second order integrator** with **limits** and **reset**, your model will look like this



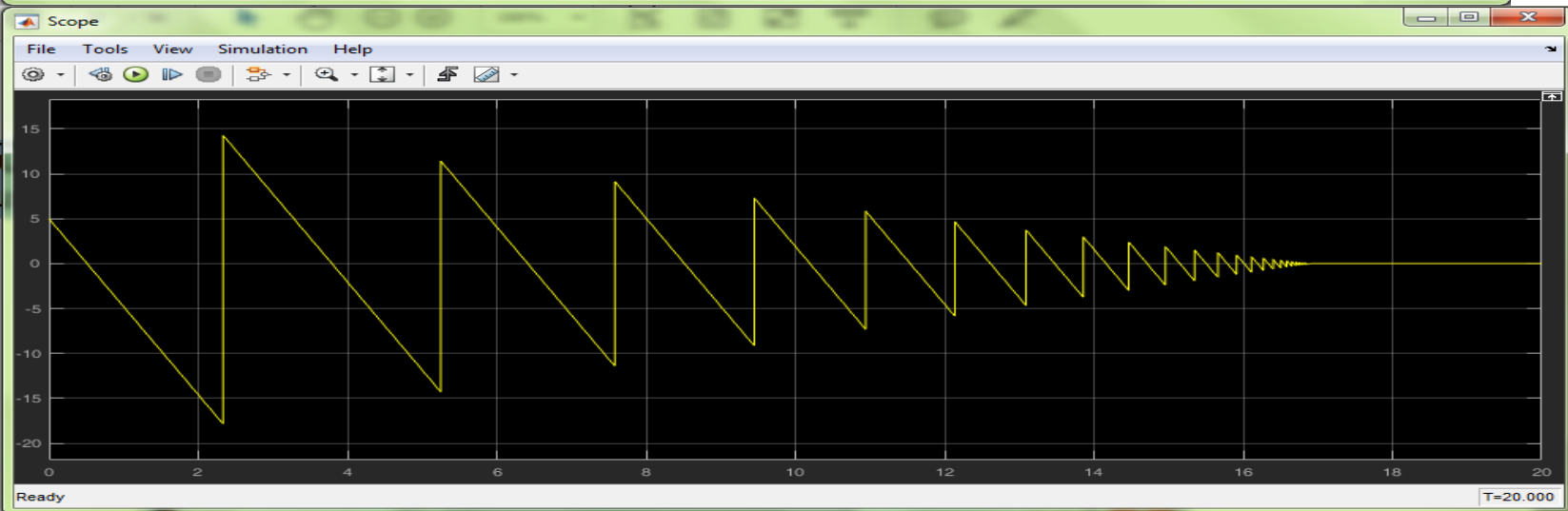
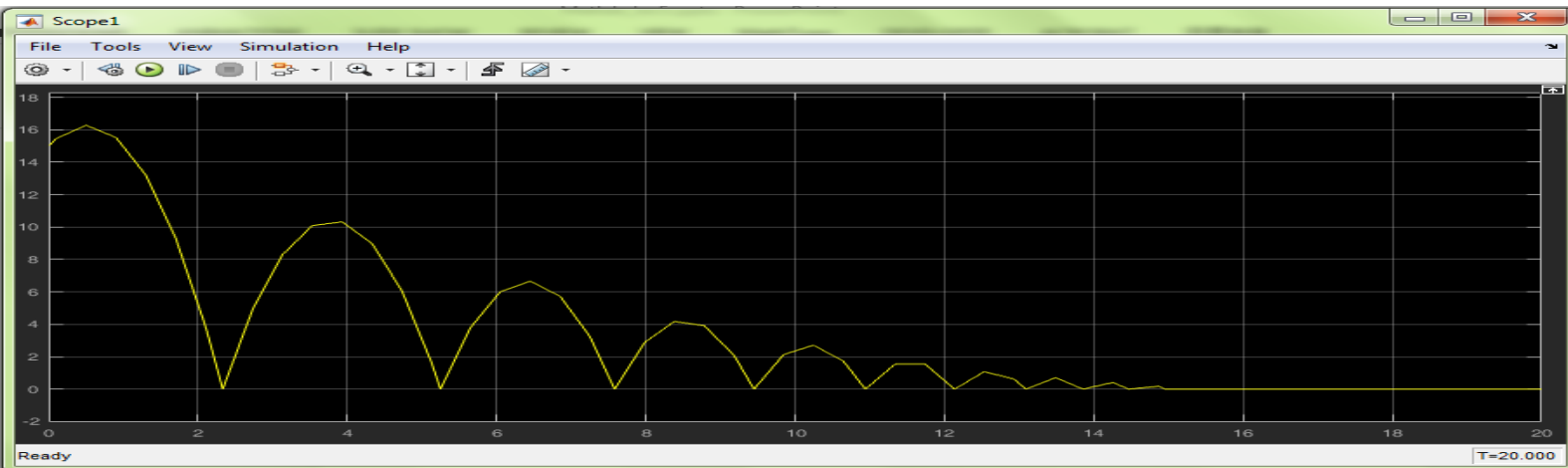




更改输入输出方向：  
模块-右键-rotate and flip-flip  
block

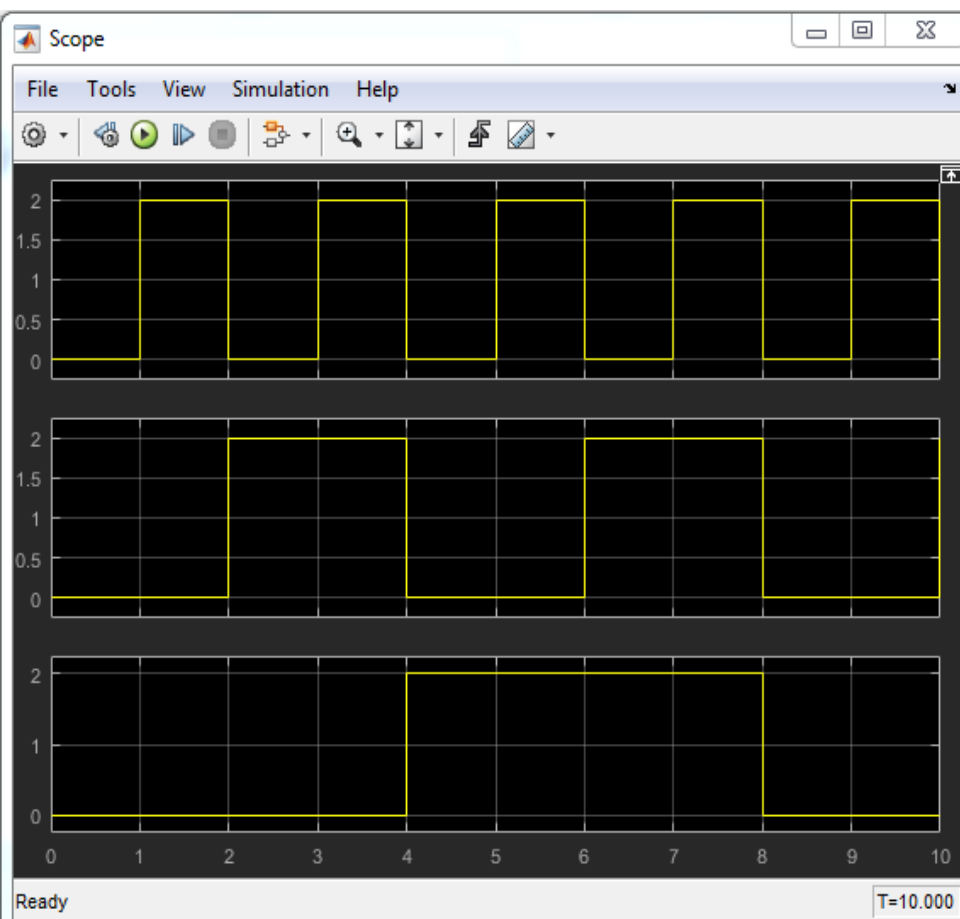
# Simulink Results

- Running the model yields the balls height and velocity as a function of time

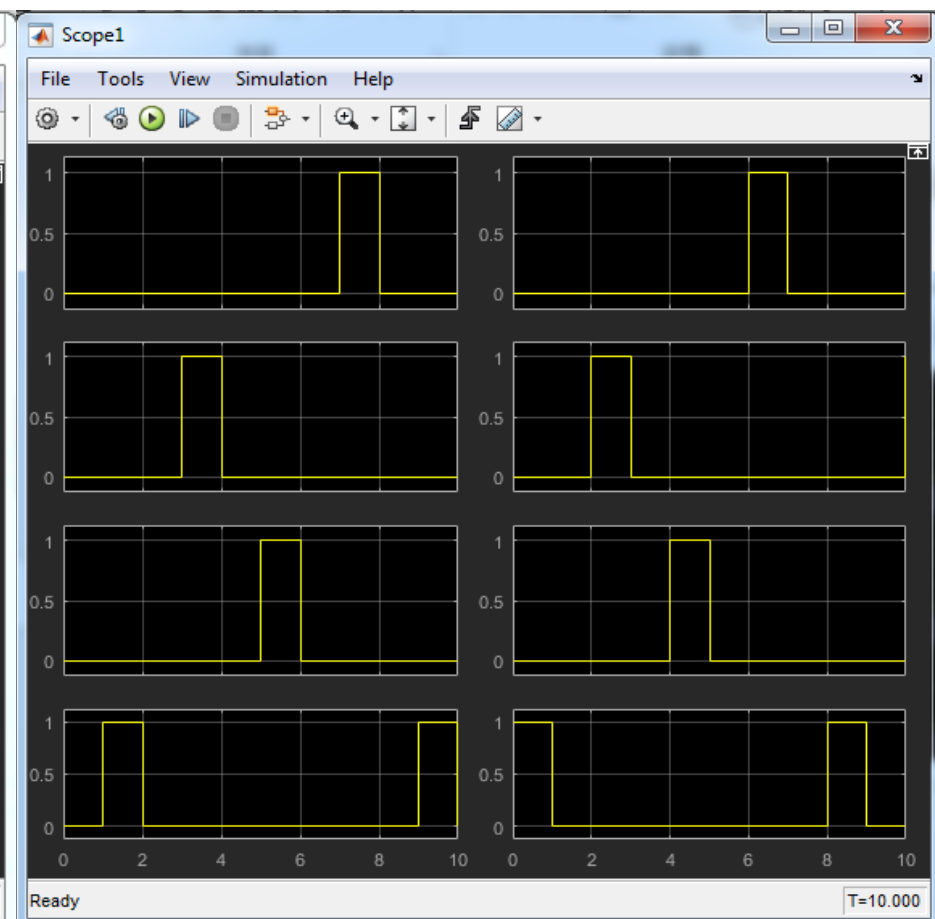


# Simulink仿真三八译码电路

输入信号（3路）



输出信号（8路）



- 用到的模块：pulse generator, logical operator ( 选合适的逻辑运算 ), scope ( 更改输入端口数 )
- 按运算逻辑连线
- 仿真参数设置

Simulation->model configuration parameters->solver->discrete

- 模块参数设置 ( pulse generator模块 )

Pulse type: sample based;

Amplitude: 2

Period: 2

Pulse width: 1

Phase delay:1

Sample time: 1, 2, 4 (respectively)

显示窗口：  
View->layout

# Outline

- Symbolic Toolbox
- Simulink
- **Image Processing**
- Miscellaneous Useful Functions
- Graphical User Interfaces

# Image Processing

- Image enhancement
  - Adjust image contrast, intensities, etc.
- Filtering and deblurring
  - Convolution and deconvolution
- Finding edges
  - Image gradient, edge
- Finding circles
  - Hough transform

# Image Processing

- Image Restoration

- Denoising



- Image Enhancement & Analysis

- Contrast Improvement
    - `imadjust`, `histeq`, `adapthisteq`
  - Edge Detection
    - `edge`
  - Sharpening
  - Segmentation

# Exercise: Contrast Improvement

- In this exercise, first we want to load the image “pout.tif” . You can use **imread**.
- Then for a better comparison we want our image to have a width of 200 pixels. Use **imresize**
- Finally, we want to compare the results of three functions **imadjust**, **histeq**, **adapthisteq** for contrast enhancement. Display the original image and the three enhanced images in a single figure.



# Exercise: Contrast Improvement

Original Image



Enhanced Image using Imadjust



Enhanced Image using Histeq



Enhanced Image using Adapthisteq

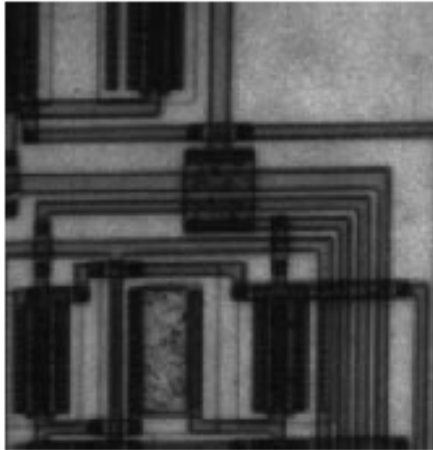


# Exercise: Edge Detection

- We know that edge detection is mainly highpass filtering the image.
- First load the image "circuit.tif" and then plot the edges in that figure using the function **edge** and the filters **"sobel"** , **"prewitt"** . Also use **"canny"** as another method for edge detection using **edge**.

# Exercise: Edge Detection

Original Image



Edges found using sobel filter



Edges found using the "canny" method



Edges found using prewitt filter



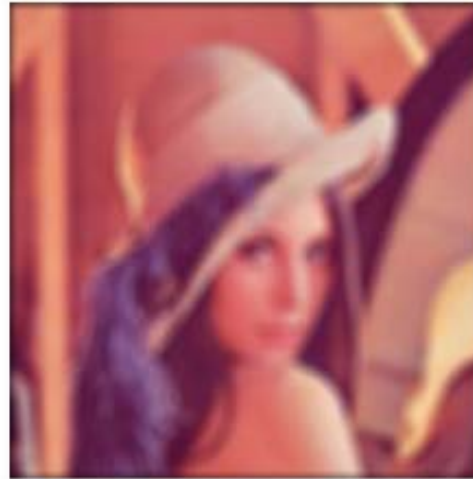
# Image Enhancement

- Commonly-used: **imread**, **imwrite**, **imshow**, **imresize**
  - » **im = imread('pout.tif');**
  - » **imtool(im);**
    - Convenient for editing in figure window
- Adjust intensity values / colormap
  - » **imadjust(im);**
    - Increase contrast (1% of data saturated at low/high intensities)
  - » **imadjust(im,[.4 .6],[0 1]);**
    - Clips off intensities below .4 and above .6, Stretches resulting intensities to 0 and 1
    - What happens if used [1 0] instead of [0 1]?
    - Also works for RGB; see **doc**

# Filtering and Deblurring

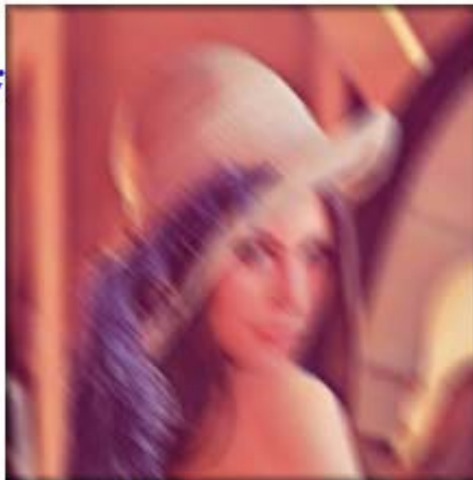
Pillbox filter:

```
f = fspecial('disk',10);  
imblur = imfilter(im,f);  
deconvblind(imblur,f);
```



Linear motion blur:

```
f=fspecial('motion',30,135);  
imblur = imfilter(im,f);  
deconvblind(imblur,f);
```



## Deblurring

<code>deconvblind</code>	Deblur image using blind deconvolution
<code>deconvlucy</code>	Deblur image using Lucy-Richardson method
<code>deconvreg</code>	Deblur image using regularized filter
<code>deconvwnr</code>	Deblur image using Wiener filter

# Finding Edges

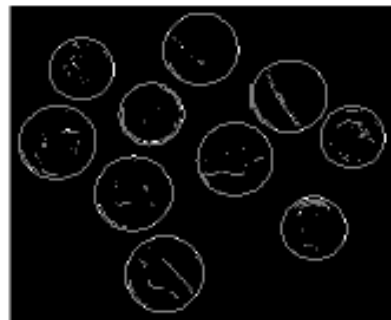
- Image gradients: `imgradient`, `imgradientxy`
- Application: `edge`
  - » `edge(im); % Sobel`
  - » `edge(im, 'canny');`
- Images must be in grayscale
  - » `rgb2gray`



Original  
(coins.png)



Sobel



Laplacian



Canny

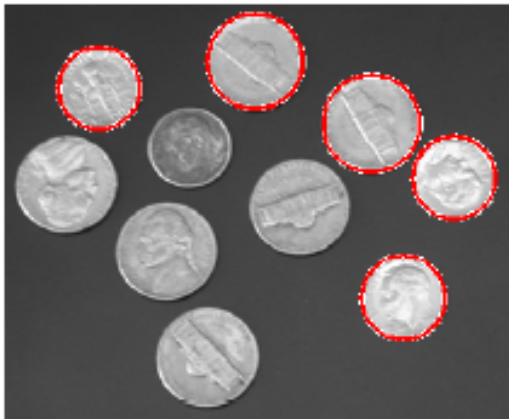


# Other Cool Stuff

- Finding circles

```
» im = imread('coins.png');  
» [centers,radii,metric] = imfindcircles(im, [15 30]);  
    ➤ Finds circles with radii within range, ordered by strength  
» imshow(im)  
» viscircles(centers(1:5,:), radii(1:5));
```

- Extract other shapes with Hough transform



## Image Analysis

### Object Analysis

<code>bwboundaries</code>	Trace region boundaries in binary image
<code>bwtraceboundary</code>	Trace object in binary image
<code>corner</code>	Find corner points in image
<code>cornermetric</code>	Create corner metric matrix from image
<code>edge</code>	Find edges in intensity image
<code>hough</code>	Hough transform
<code>houghlines</code>	Extract line segments based on Hough transform
<code>houghpeaks</code>	Identify peaks in Hough transform
<code>imfindcircles</code>	Find circles using circular Hough transform
<code>ingradient</code>	Gradient magnitude and direction of an image
<code>ingradientxy</code>	Directional gradients of an image

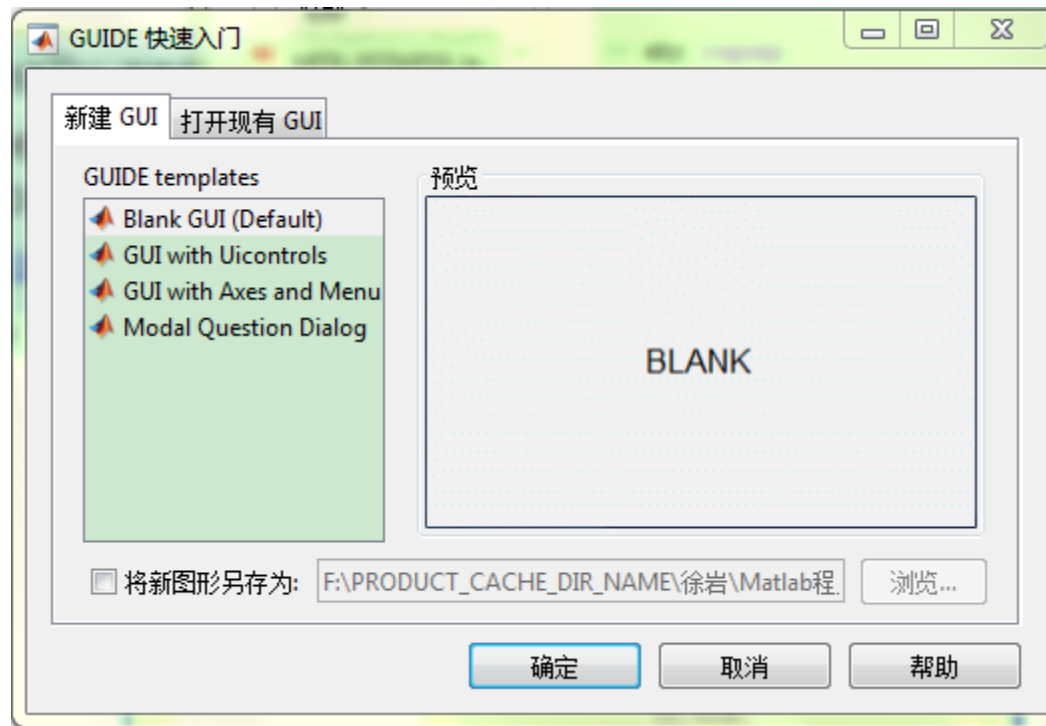
# Outline

- Symbolic Toolbox
- Simulink
- Image Processing
- Miscellaneous Useful Functions
- Graphical User Interfaces**



# Making GUIs

- It's really easy to make a graphical user interface in Matlab
- To open the graphical user interface development environment, type **guide**
  - » **guide**
    - Select **Blank GUI**

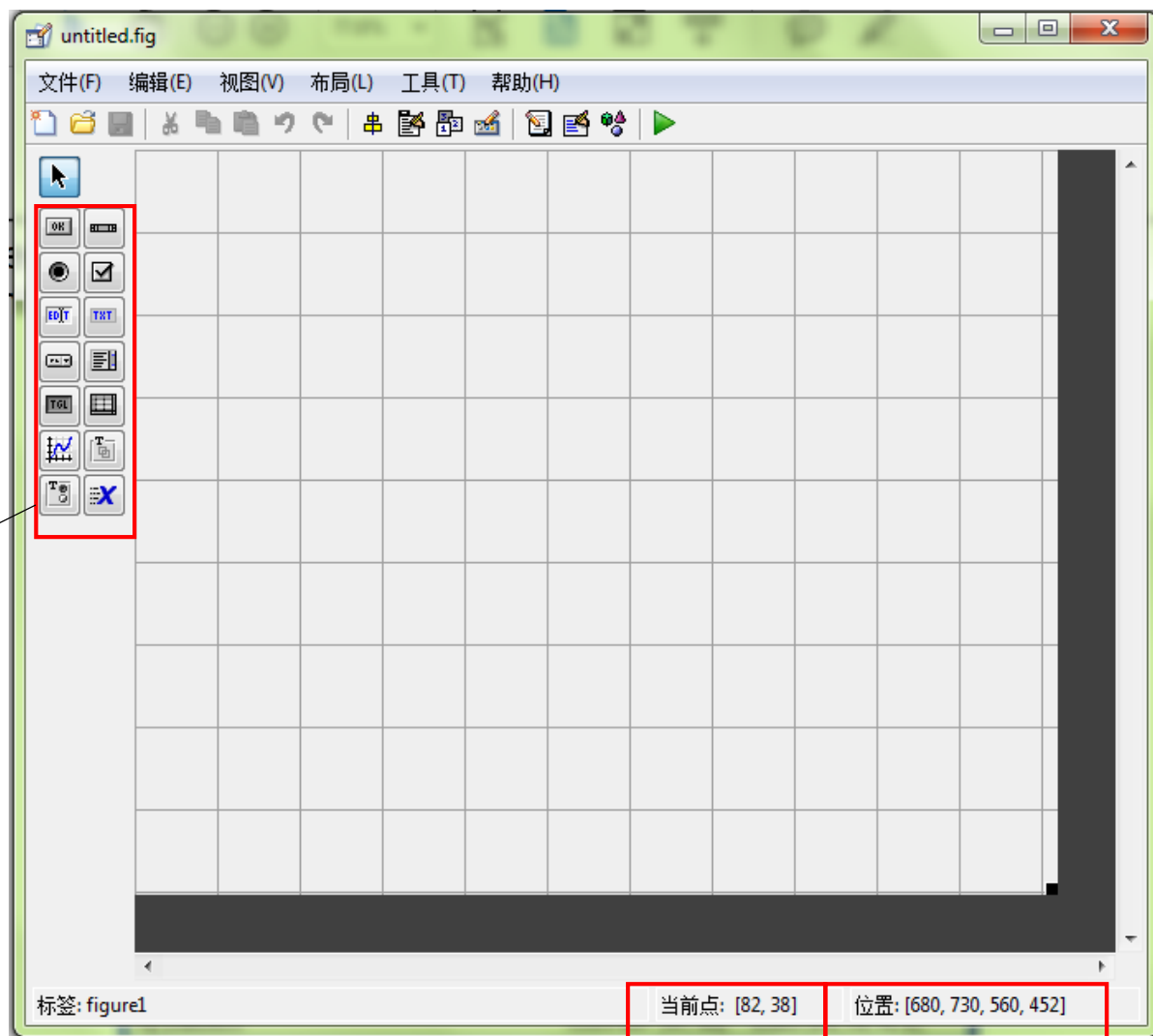


# Draw the GUI

- Select objects from the left, and draw them where you want them

各种对象：

单选、多选、滑动条、  
弹出式菜单，等等

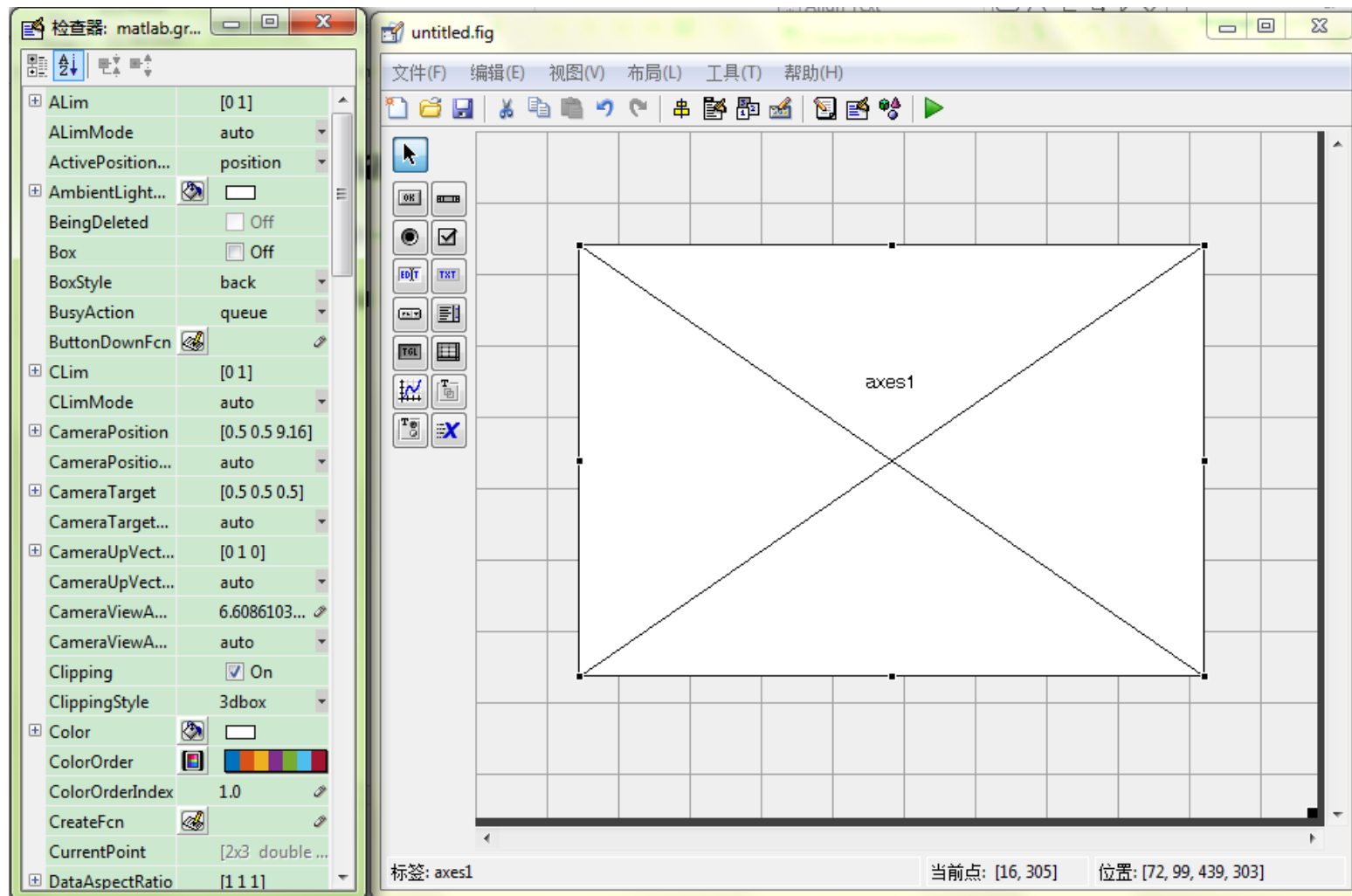


当前鼠标  
所在位置

选定对象  
所在位置

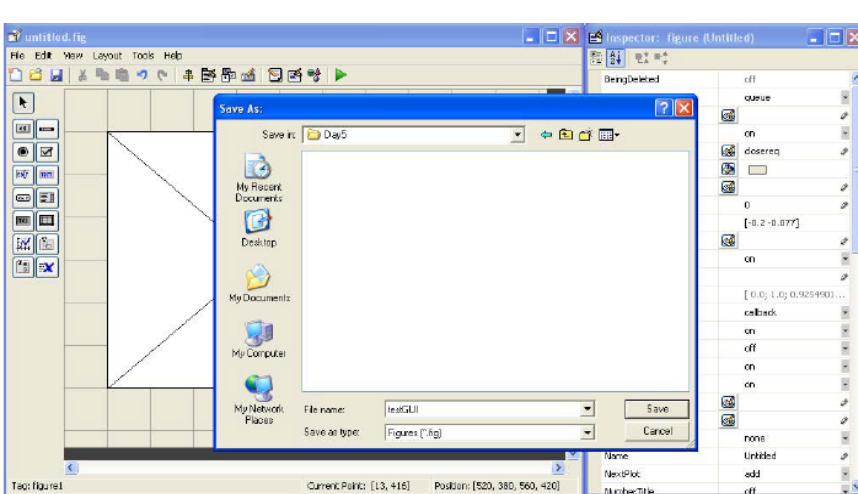
# Change Object Settings

- Double-click on objects to open the **Inspector**. Here you can change all the object's properties.



# Save the GUI

- When you have modified all the properties, you can save the GUI
- Matlab saves the GUI as a **.fig** file, and generates an **m-file**!



```
1 function varargout = TestGUI(varargin)
2 % IESIGUI MATLAB code for TestGUI.fig
3 % IESIGUI, by itself, creates a new IESIGUI or raises the existing
4 % singleton*.
5 %
6 % H = IESIGUI returns the handle to a new IESIGUI or the handle to
7 % the existing singleton*.
8 %
9 % IESIGUI('CALLBACK',hObject,eventData,handles,...) calls the local
10 % function named CALLBACK in IESIGUI.M with the given input arguments.
11 %
12 % IESIGUI('Property','Value',...) creates a new IESIGUI or raises the
```

# Add Functionality to M-File

- To add functionality to your buttons, add commands to the 'Callback' functions in the m-file.
- For example, when the user clicks the Draw Image button, the `drawimage_Callback` function will be called and executed.
- All the data for the GUI is stored in the handles, so use `set` and `get` to get data and change it if necessary.
- Any time you change the handles, save it using `guidata`  
» `guidata(handle,data);`

String	Draw Image	% --- Executes on button press in DrawImage.
Style	pushbutton	function DrawImage_Callback(hObject, eventdata, handles)
Tag	DrawImage	% hObject handle to DrawImage (see GCBO)
TooltipString		% eventdata reserved - to be defined in a future version of MATLAB
		% handles structure with handles and user data (see GUIDATA)

```
f=openfig('TestGUI.fig')
data=guihandles(f)
h=get(data.axes1)
set(data.axes1,'XGrid','on')
```

```
data.axes1.YGrid='on'
guidata(f, data)
```

# Running the GUI

- To run the GUI, just type its name in the command window and the GUI will pop up.

# GUI Helper Functions

- Use keyboard to allow debugging from command window.  
GUI variables will appear in the workspace.  
Use `return` to exit debug mode
- Use built-in GUI modals for user input:
  - » `uigetfile`
  - » `uiputfile`
  - » `inputdlg`
- And more... (see help for details)