

**CS252**  
**Graduate Computer Architecture**

**Lecture 12:**  
**Multiprocessor 2: Snooping Protocol,  
Directory Protocol, Synchronization,  
Consistency**

**February 28, 2001**  
**Prof. David A. Patterson**  
**Guest Lecturer: Yujia Jin**  
**Computer Science 252**  
**Spring 2001**

## Review: Multiprocessor

- Basic issues and terminology
- Communication: share memory, message passing
- Parallel Application:
  - Commercial workload: OLTP, DSS, Web index search
  - Multiprogramming and OS
  - Scientific/Technical

App	Scaling compu- tation	Scaling communi cation	Scaling comp - to-comm
FFT	$n \log n / p$	$n / p$	$\log n$
LU	$n / p$	$n^{1/2} / p^{1/2}$	$n^{1/2} / p^{1/2}$
Barnes	$n \log n / p$	$n^{1/2} \log n / p^{1/2}$	$n^{1/2} / p^{1/2}$
Ocean	$n / p$	$n^{1/2} / p^{1/2}$	$n^{1/2} / p^{1/2}$

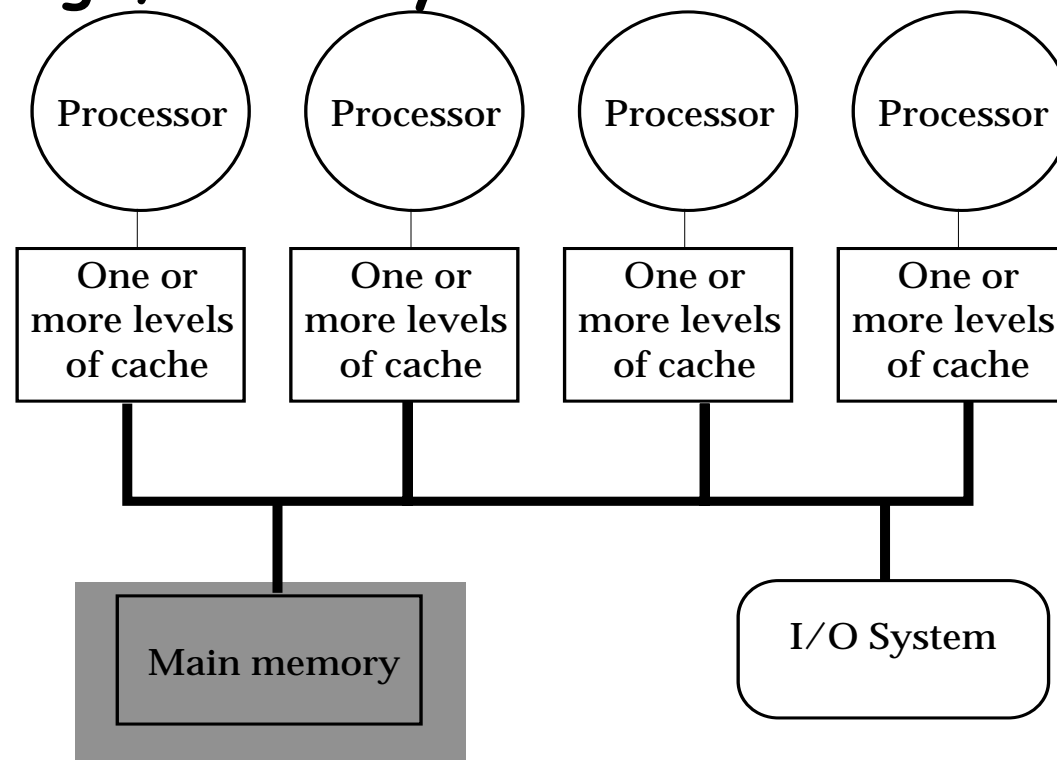
- Amdahl's Law:  $\text{Speedup} \leq 1 / \text{Sequential\_Frac}$
- Cache Coherence: serialization

# Potential HW Coherency Solutions

- **Snooping Solution (Snoopy Bus):**
  - Send all requests for data to all processors
  - Processors snoop to see if they have a copy and respond accordingly
  - Requires broadcast, since caching information is at processors
  - Works well with bus (natural broadcast medium)
  - Dominates for small scale machines (most of the market)
- **Directory-Based Schemes (discuss later)**
  - Keep track of what is being shared in 1 centralized place (logically)
  - Distributed memory => distributed directory for scalability (avoids bottlenecks)
  - Send point-to-point requests to processors via network
  - Scales better than Snooping
  - Actually existed BEFORE Snooping-based schemes

# Bus Snooping Topology

- **Memory:** centralized with uniform access time (“uma”) and bus interconnect
- **Examples:** Sun Enterprise 5000 , SGI Challenge, Intel SystemPro



# Basic Snoopy Protocols

- Write Invalidate Protocol:
  - Multiple readers, single writer
  - Write to shared data: an invalidate is sent to all caches which snoop and invalidate any copies
  - Read Miss:
    - » Write-through: memory is always up-to-date
    - » Write-back: snoop in caches to find most recent copy
- Write Broadcast Protocol (typically write through):
  - Write to shared data: broadcast on bus, processors snoop, and update any copies
  - Read miss: memory is always up-to-date
- Write serialization: bus serializes requests!
  - Bus is single point of arbitration

# Basic Snoopy Protocols

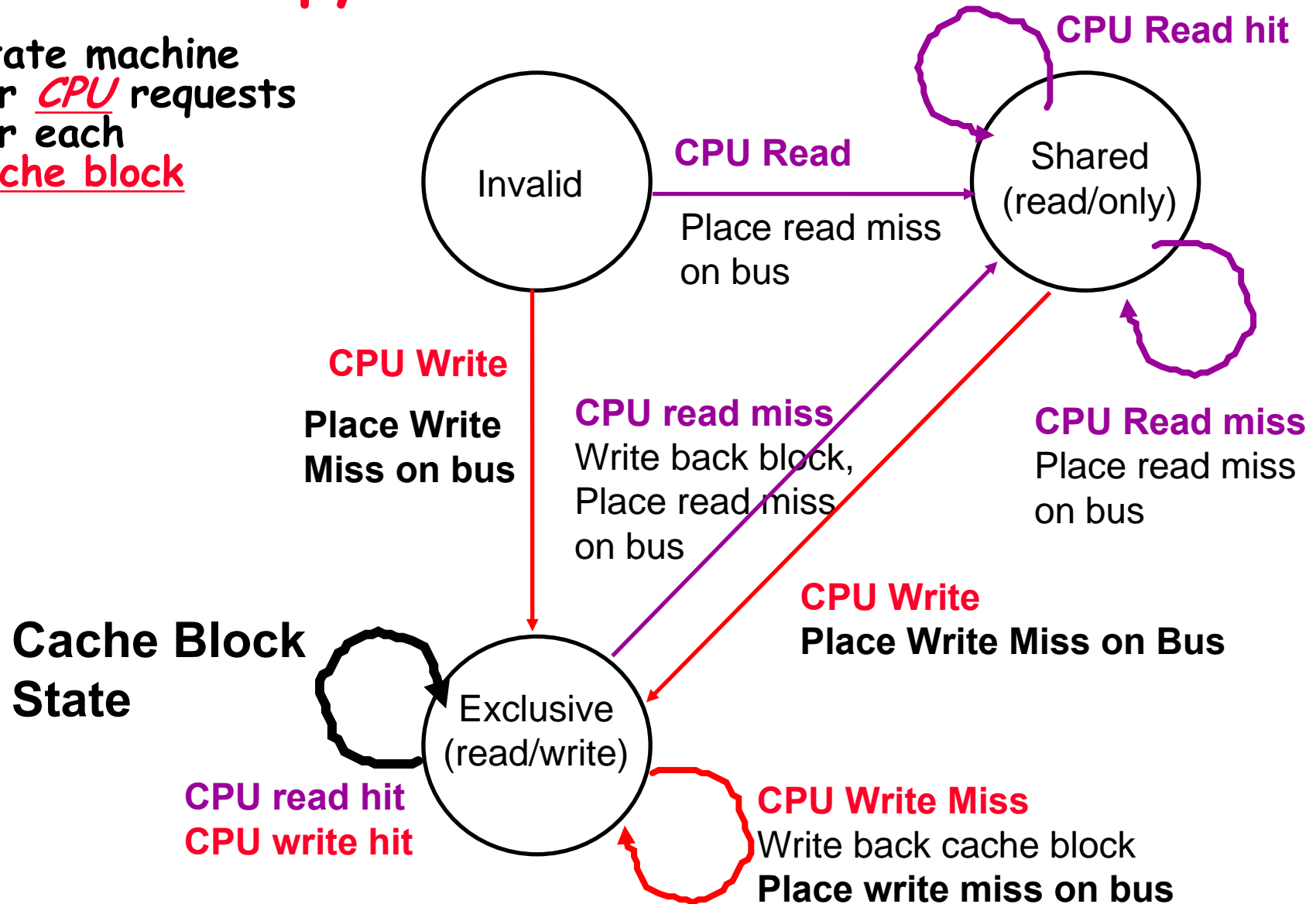
- **Write Invalidate versus Broadcast:**
  - Invalidate requires one transaction per write-run
  - Invalidate uses spatial locality: one transaction per block
  - Broadcast has lower latency between write and read

# An Example Snoopy Protocol

- Invalidation protocol, write-back cache
- Each block of memory is in one state:
  - Clean in all caches and up-to-date in memory (Shared)
  - OR Dirty in exactly one cache (Exclusive)
  - OR Not in any caches
- Each cache block is in one state (track these):
  - Shared : block can be read
  - OR Exclusive : cache has only copy, its writeable, and dirty
  - OR Invalid : block contains no data
- Read misses: cause all caches to snoop bus
- Writes to clean line are treated as misses

# Snoopy-Cache State Machine-I

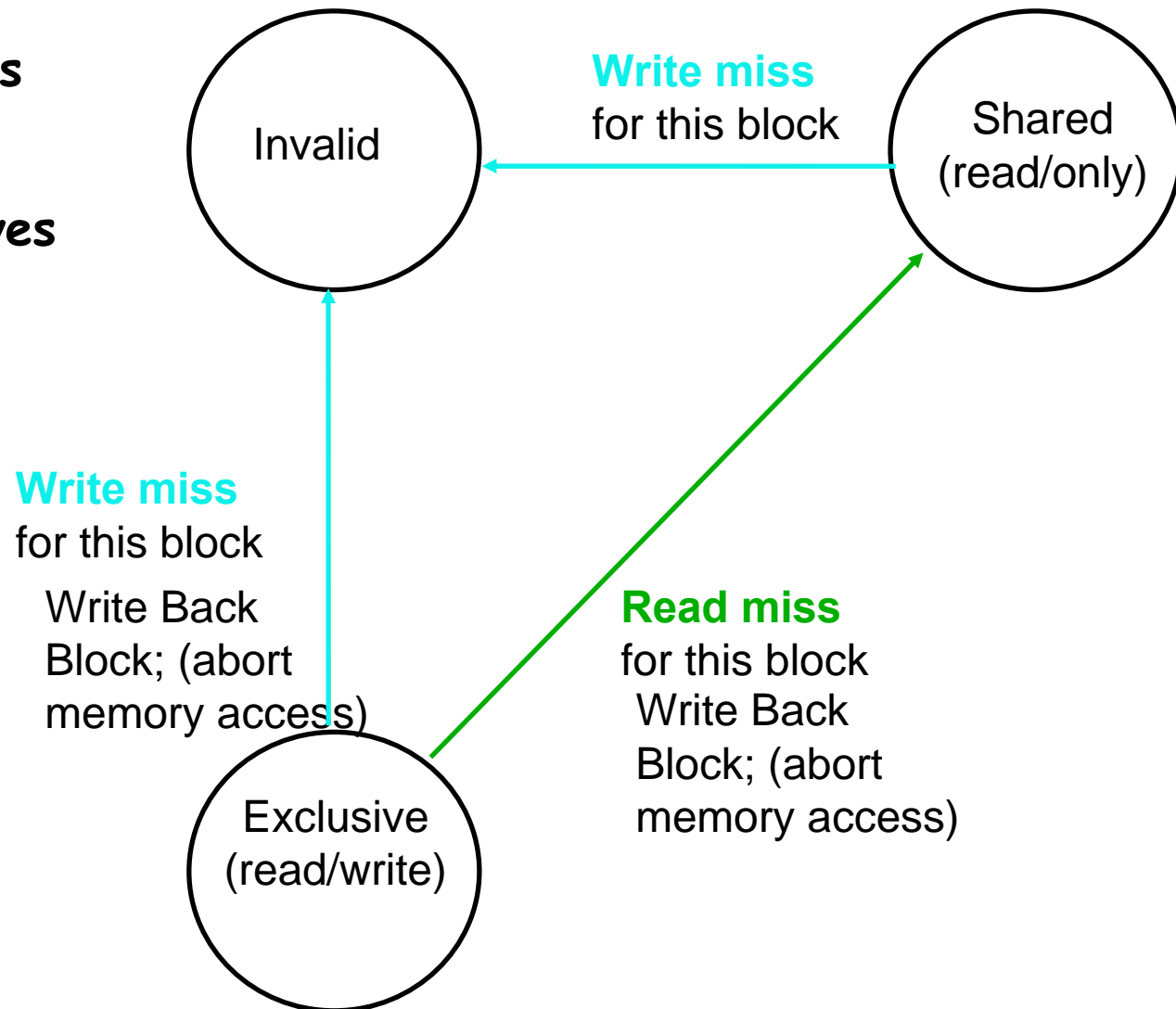
- State machine for CPU requests for each cache block





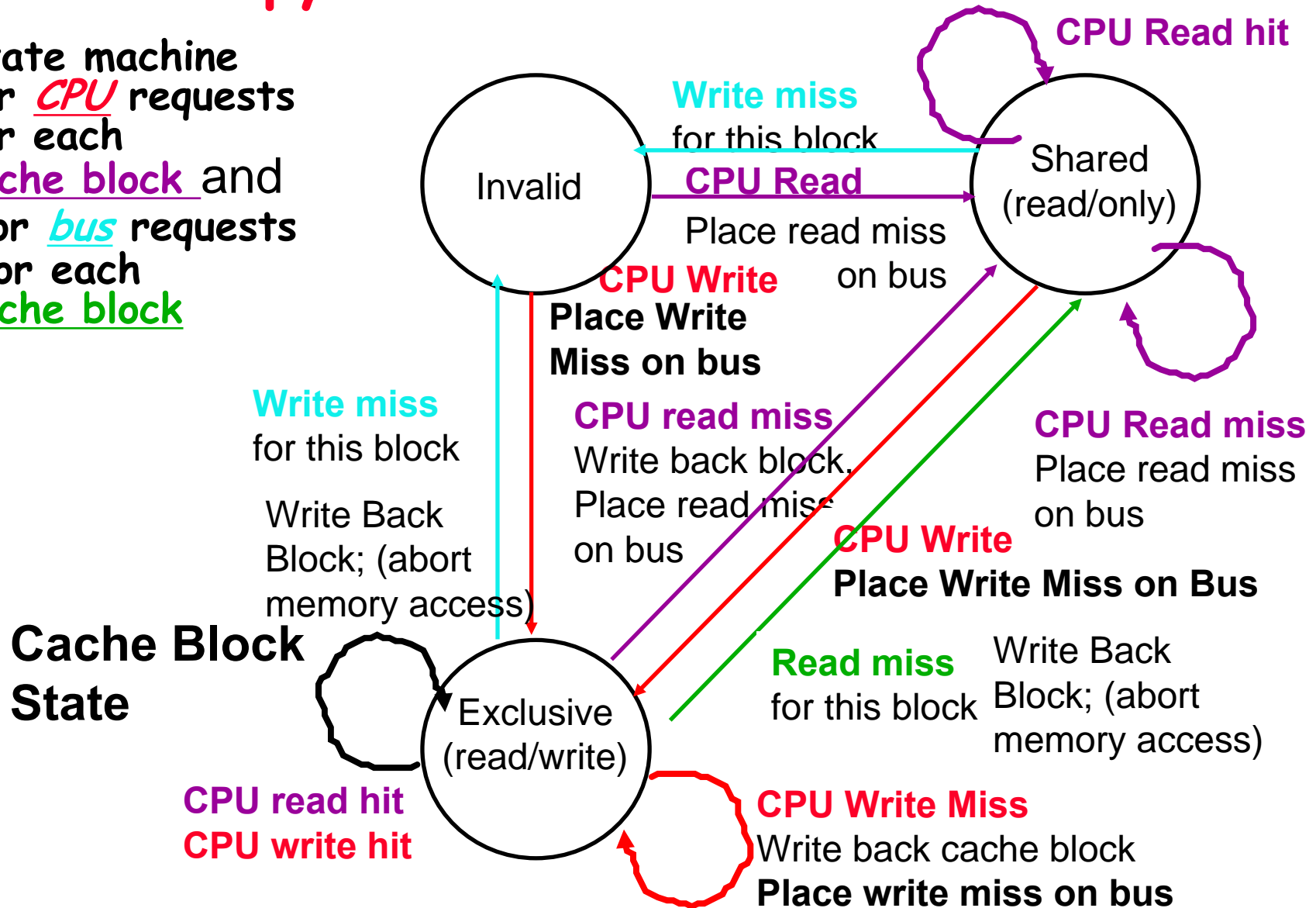
# Snoopy-Cache State Machine-II

- State machine for bus requests for each cache block
- Appendix E? gives details of bus requests



# Snoopy-Cache State Machine-III

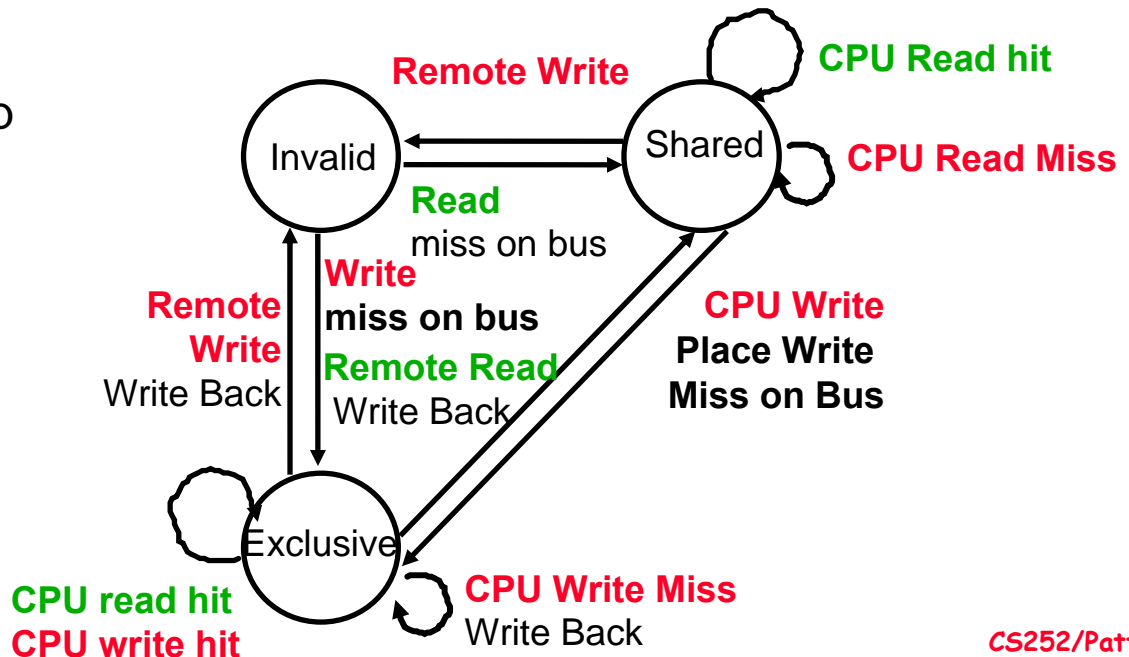
- State machine for **CPU** requests for each **cache block** and for **bus** requests for each **cache block**



# Example

	Processor 1			Processor 2			Bus			Memory		
	<i>P1</i>			<i>P2</i>			<i>Bus</i>				<i>Memory</i>	
<i>step</i>	<i>State</i>	<i>Addr</i>	<i>Value</i>	<i>State</i>	<i>Addr</i>	<i>Value</i>	<i>Action</i>	<i>Proc.</i>	<i>Addr</i>	<i>Value</i>	<i>Addr</i>	<i>Value</i>
P1: Write 10 to A1												
P1: Read A1												
P2: Read A1												
P2: Write 20 to A1												
P2: Write 40 to A2												

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 != A2

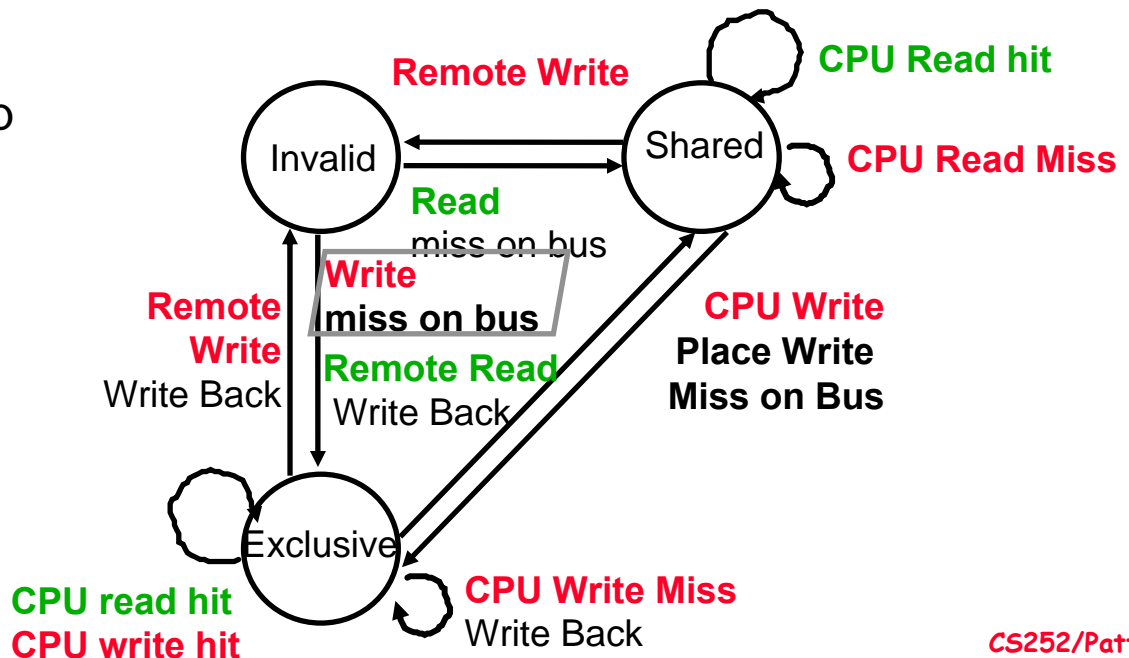


## Example: Step 1

[illegible]

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but  $A1 \neq A2$ .

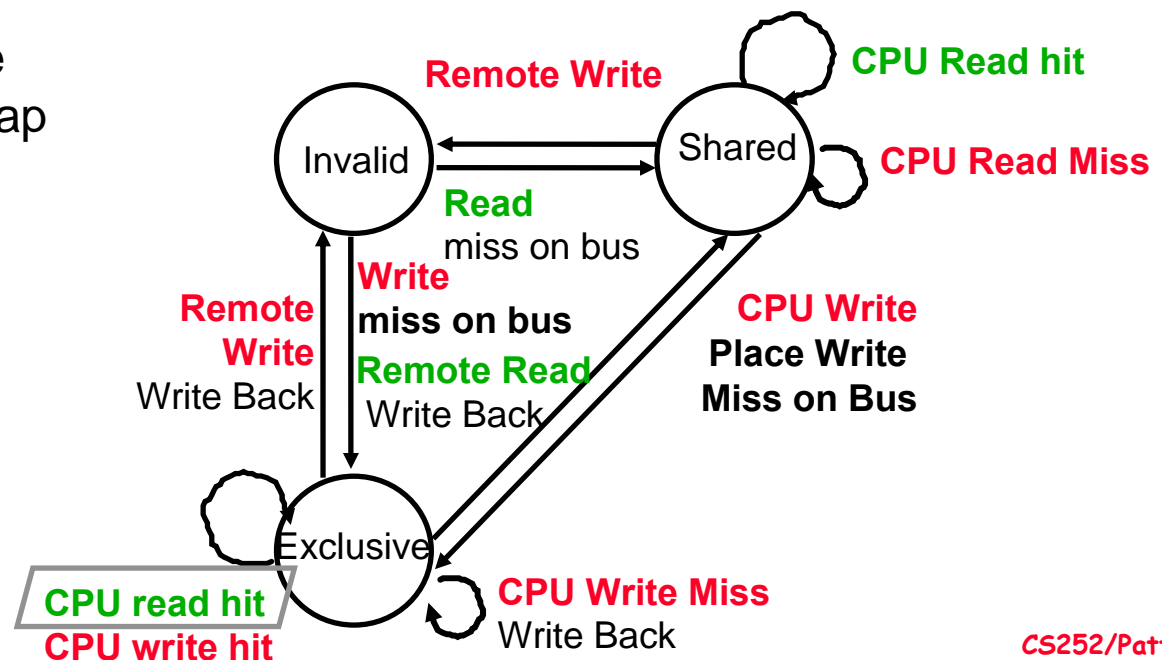
Active arrow =



## Example: Step 2

	P1			P2			Bus			Memory		
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	Value
P1: Write 10 to A1	<u>Excl.</u>	<u>A1</u>	<u>10</u>				<u>WrMs</u>	P1	A1			
P1: Read A1	Excl.	A1	10									
P2: Read A1												
P2: Write 20 to A1												
P2: Write 40 to A2												

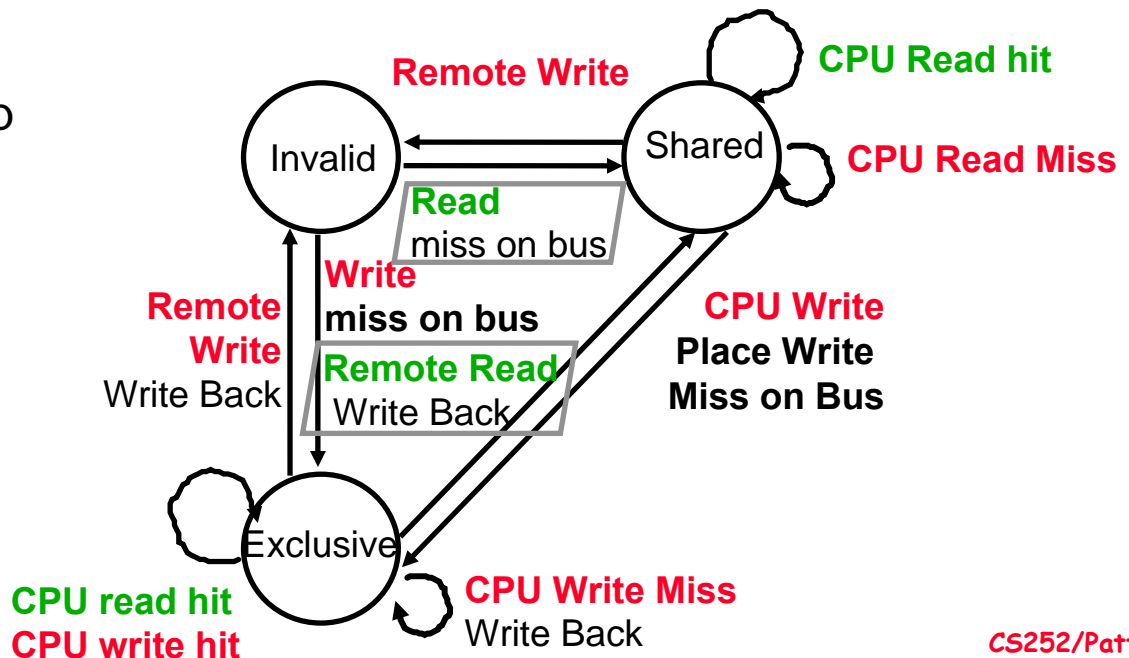
Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 != A2



## Example: Step 3

[illegible]

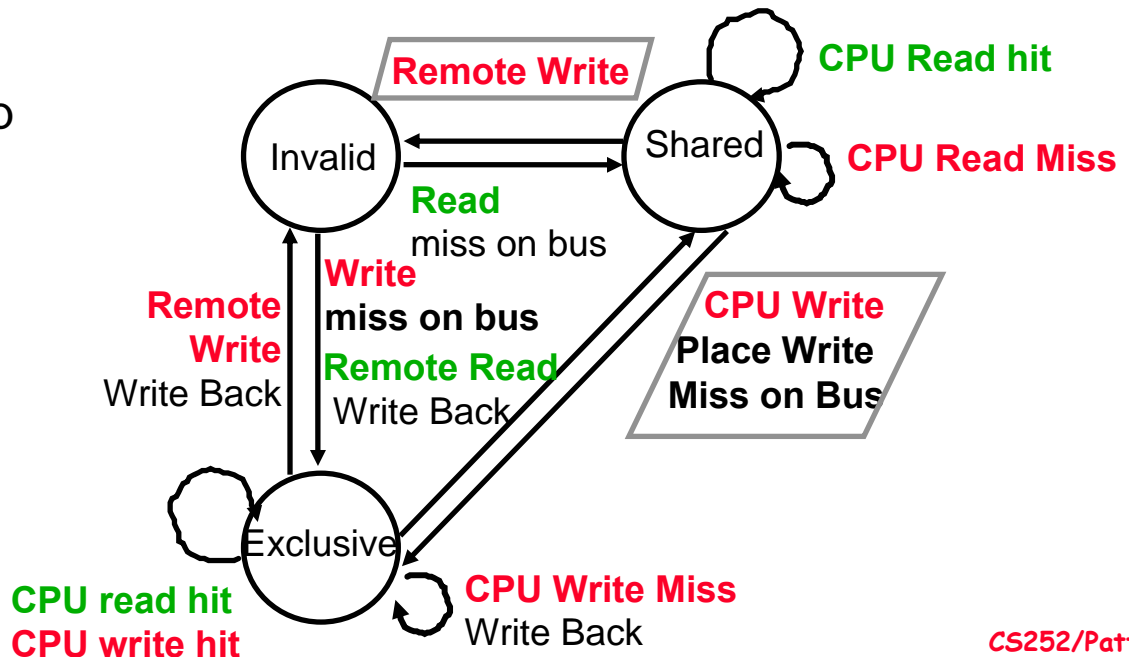
Assumes initial cache state is invalid and A1 and A2 map to same cache block, but  $A1 \neq A2$ .



## Example: Step 4

	P1			P2			Bus			Memory		
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	Value
P1: Write 10 to A1	<u>Excl.</u>	<u>A1</u>	<u>10</u>				<u>WrMs</u>	P1	A1			
P1: Read A1	Excl.	A1	10									
P2: Read A1				<u>Shar.</u>	<u>A1</u>		<u>RdMs</u>	P2	A1			
	<u>Shar.</u>	A1	10				<u>WrBk</u>	P1	A1	10	<u>A1</u>	<u>10</u>
				Shar.	A1	<u>10</u>	<u>RdDa</u>	P2	A1	10	A1	10
P2: Write 20 to A1	<u>Inv.</u>			<u>Excl.</u>	A1	<u>20</u>	<u>WrMs</u>	P2	A1		A1	10
P2: Write 40 to A2												-

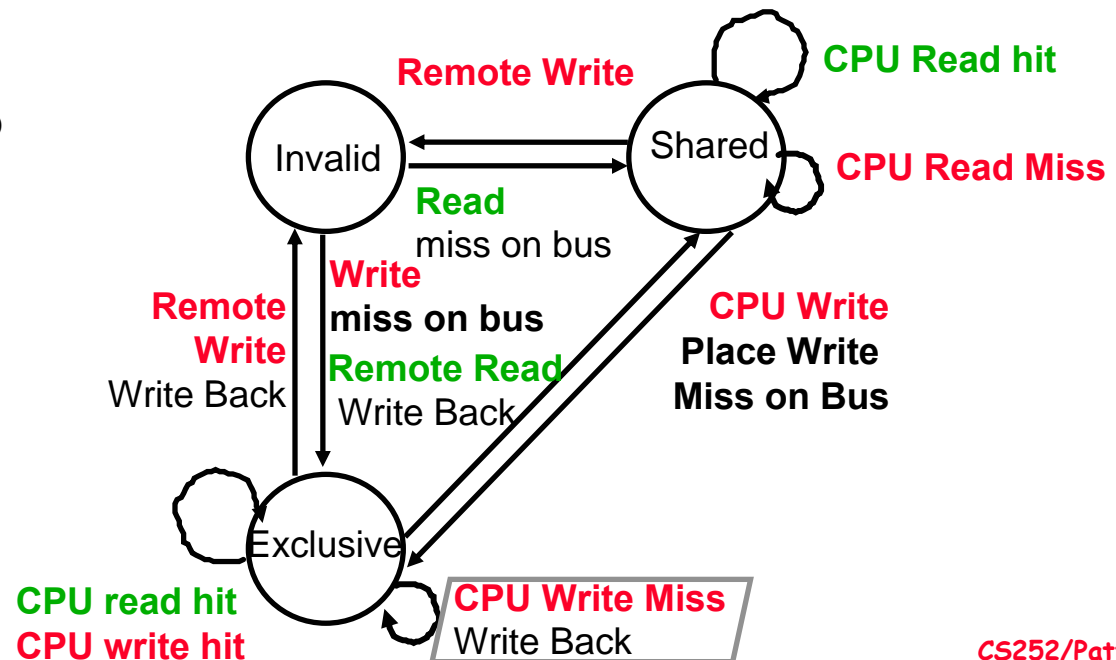
Assumes initial cache state is invalid and A1 and A2 map to same cache block, but A1 != A2



## Example: Step 5

	P1			P2			Bus				Memory	
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	Value
P1: Write 10 to A1	<u>Excl.</u>	<u>A1</u>	<u>10</u>				<u>WrMs</u>	P1	A1			
P1: Read A1	Excl.	A1	10									
P2: Read A1				<u>Shar.</u>	<u>A1</u>		<u>RdMs</u>	P2	A1			
	<u>Shar.</u>	A1	10				<u>WrBk</u>	P1	A1	10	<u>A1</u>	<u>10</u>
				Shar.	A1	<u>10</u>	<u>RdDa</u>	P2	A1	10	A1	10
P2: Write 20 to A1	<u>Inv.</u>			<u>Excl.</u>	A1	<u>20</u>	<u>WrMs</u>	P2	A1		A1	10
P2: Write 40 to A2							<u>WrMs</u>	P2	A2		A1	10
				Excl.	<u>A2</u>	<u>40</u>	<u>WrBk</u>	P2	A1	20	<u>A1</u>	<u>20</u>

Assumes initial cache state is invalid and A1 and A2 map to same cache block, but  $A1 \neq A2$





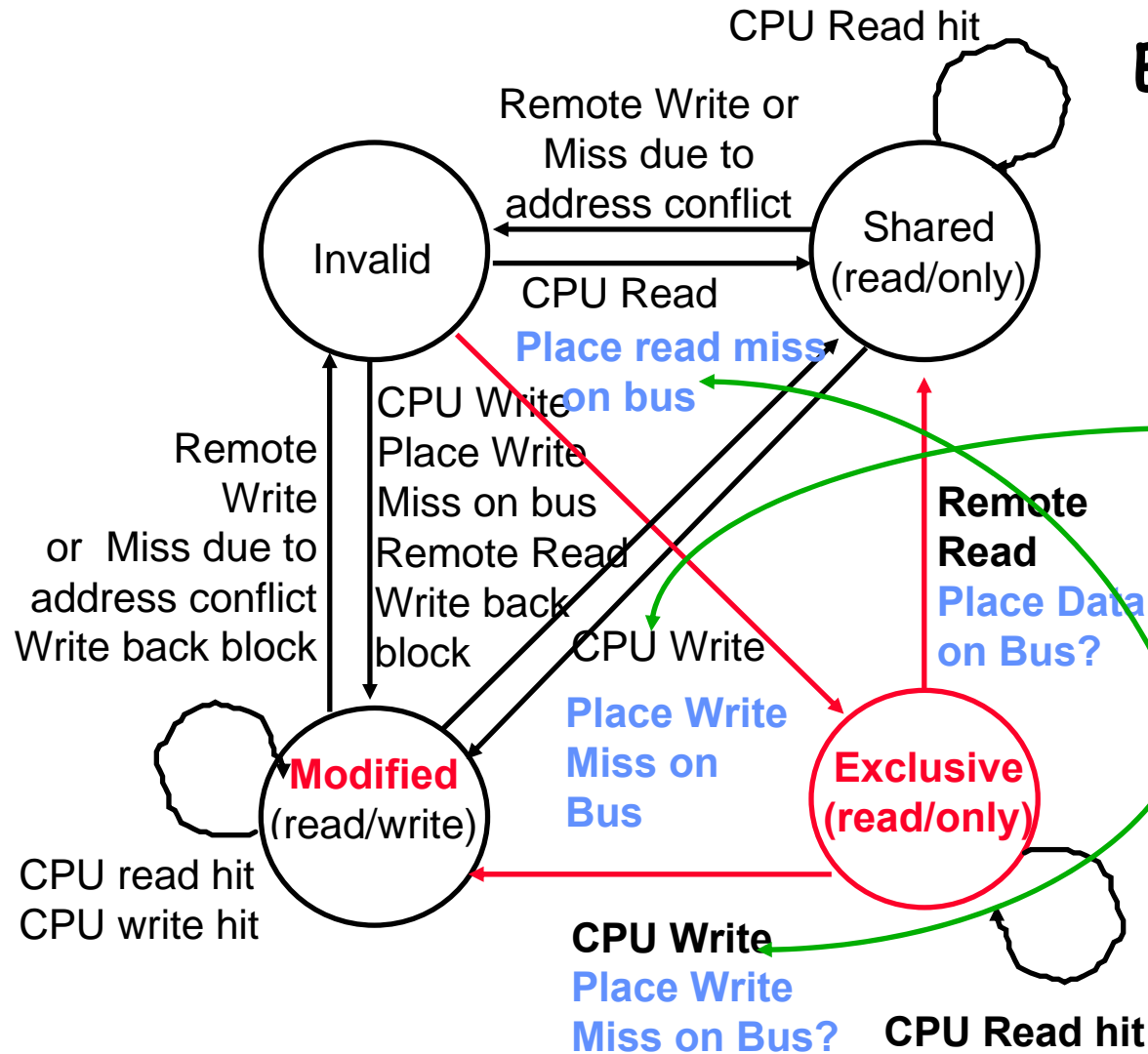
# Snooping Cache Variations

Basic Protocol	Berkeley Protocol	Illinois Protocol	MESI Protocol
Exclusive	Owned Exclusive	Private Dirty	<u>M</u> odified (private, !=Memory)
Shared	Owned Shared	Private Clean	<u>E</u> xclusive (private, =Memory)
Invalid	Shared	Shared	<u>S</u> hared (shared, =Memory)
	Invalid	Invalid	<u>I</u> nvalid

Owner can update via bus invalidate operation  
 Owner must write back when replaced in cache

If read sourced from memory, then Private Clean  
 if read sourced from other cache, then Shared  
 Can write in cache if held private clean or dirty

# Snoop Cache Extensions



## Extensions:

- Fourth State: Ownership
- Shared -> Modified, need invalidate only (upgrade request), don't read memory

**Berkeley Protocol**

- Clean exclusive state (no miss for private data on write)

**MESI Protocol**

Cache supplies data when shared state (no memory access)

**Illinois Protocol**

# Implementation Complications

- **Write Races:**
  - Cannot update cache until bus is obtained
    - » Otherwise, another processor may get bus first, and then write the same cache block!
  - Two step process:
    - » Arbitrate for bus
    - » Place miss on bus and complete operation
  - If miss occurs to block while waiting for bus, handle miss (invalidate may be needed) and then restart.
  - Split transaction bus:
    - » Bus transaction is not atomic: can have multiple outstanding transactions for a block
    - » Multiple misses can interleave, allowing two caches to grab block in the Exclusive state
    - » Must track and prevent multiple misses for one block
- **Must support interventions and invalidations**

# Implementing Snooping Caches

- Multiple processors must be on bus, access to both addresses and data
- Add a few new commands to perform coherency, in addition to read and write
- Processors continuously snoop on address bus
  - If address matches tag, either invalidate or update
- Since every bus transaction checks cache tags, could interfere with CPU cache access:
  - solution 1: **duplicate set of tags for L1 caches** just to allow checks in parallel with CPU
  - solution 2: L2 cache already duplicate, **provided L2 obeys inclusion** with L1 cache
    - » block size, associativity of L2 affects L1

## Implementing Snooping Caches

- Bus serializes writes, getting bus ensures no one else can perform memory operation
- On a miss in a write back cache, may have the desired copy and its dirty, so must reply
- Add extra state bit to cache to determine shared or not
- Add 4th state (MESI)

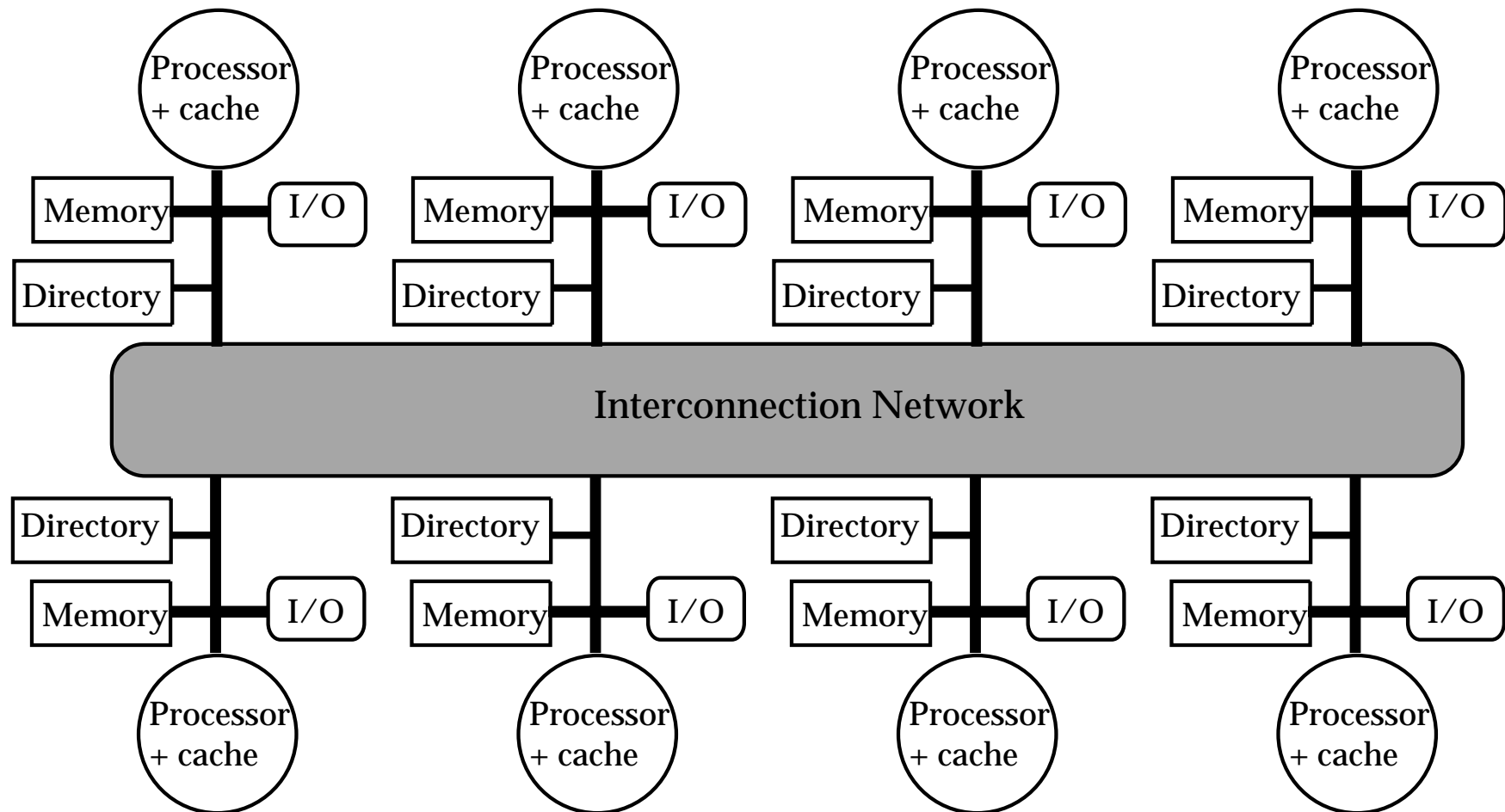
## CS 252 Administtrivia

- Chapter 8 survey
- Quiz #1 Wed March 7 5:30-8:30 306 Soda
- La Val's afterward quiz: free food and drink

## Larger MPs

- Separate Memory per Processor
- Local or Remote access via memory controller
- 1 Cache Coherency solution: non-cached pages
- Alternative: directory per cache that tracks state of every block in every cache
  - Which caches have a copies of block, dirty vs. clean, ...
- Info per memory block vs. per cache block?
  - PLUS: In memory => simpler protocol (centralized/one location)
  - MINUS: In memory => directory is  $f(\text{memory size})$  vs.  $f(\text{cache size})$
- Prevent directory as bottleneck?  
distribute directory entries with memory, each keeping track of which Procs have copies of their blocks

# Distributed Directory MPs





# Directory Protocol

- Similar to Snoopy Protocol: Three states
  - Shared:  $\geq 1$  processors have data, memory up-to-date
  - Uncached (no processor has it; not valid in any cache)
  - Exclusive: 1 processor (**owner**) has data; memory out-of-date
- In addition to cache state, must track which processors have data when in the shared state (usually bit vector, 1 if processor has copy)
- Keep it simple(r):
  - Writes to non-exclusive data  
=> write miss
  - Processor blocks until access completes
  - Assume messages received and acted upon in order sent

# Directory Protocol

- No bus and don't want to broadcast:
  - interconnect no longer single arbitration point
  - all messages have explicit responses
- Terms: typically 3 processors involved
  - **Local node** where a request originates
  - **Home node** where the memory location of an address resides
  - **Remote node** has a copy of a cache block, whether exclusive or shared
- Example messages on next slide:  
P = processor number, A = address

# Directory Protocol Messages

Message type	Source	Destination	Msg Content
Read miss	Local cache	Home directory	P, A

- Processor *P* reads data at address *A*;  
make *P* a read sharer and arrange to send data back

Write miss	Local cache	Home directory	P, A
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- Processor *P* writes data at address *A*;  
make *P* the exclusive owner and arrange to send data back

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Invalidate	Home directory	Remote caches	A
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- Invalidate a shared copy at address *A*.

Fetch	Home directory	Remote cache	A
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- Fetch the block at address *A* and send it to its home directory

Fetch/Invalidate	Home directory	Remote cache	A
------------------	----------------	--------------	---

- Fetch the block at address *A* and send it to its home directory;  
invalidate the block in the cache

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Data value reply	Home directory	Local cache	Data
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- Return a data value from the home memory (read miss response)

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Data write-back	Remote cache	Home directory	A, Data
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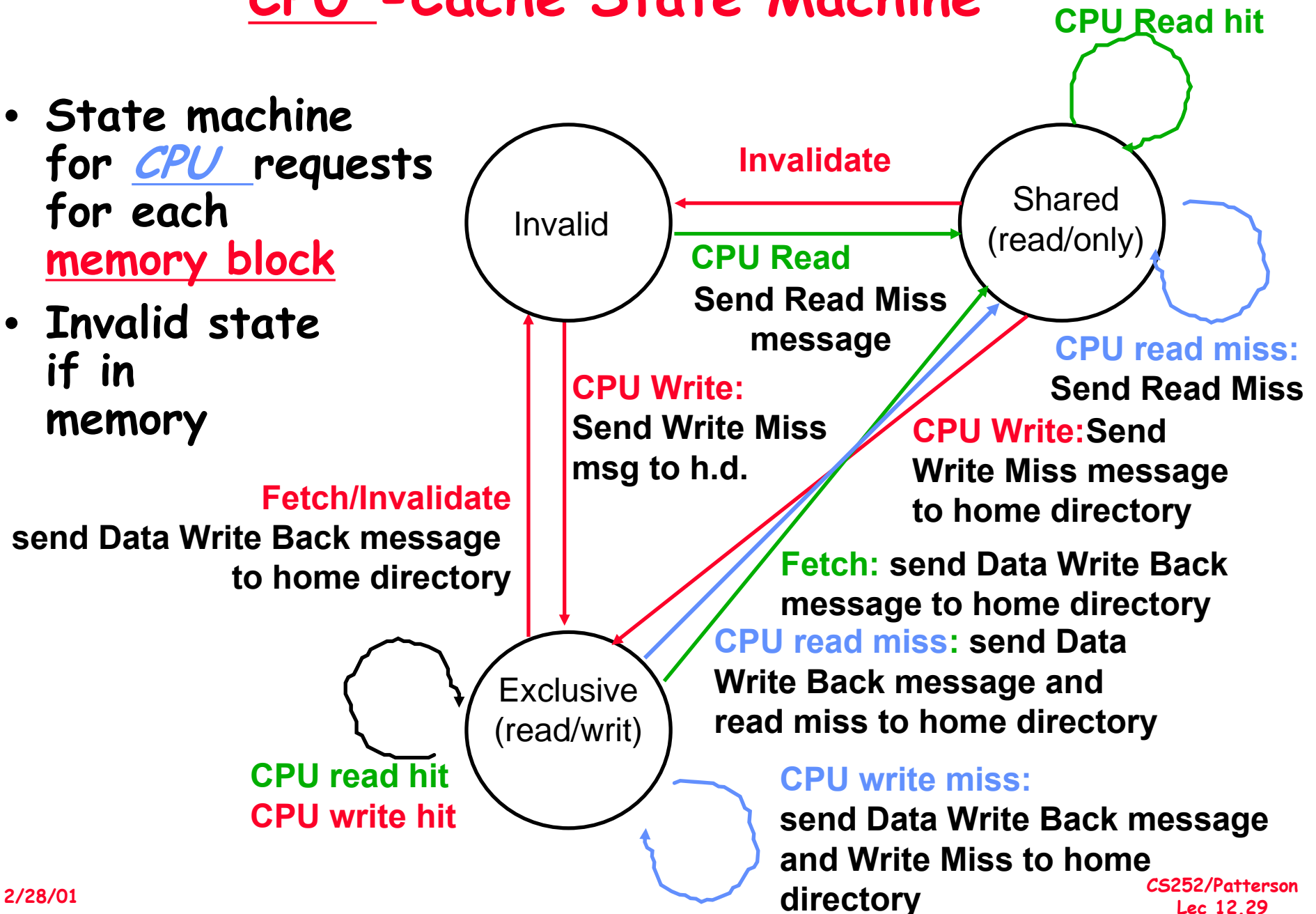
- Write-back a data value for address *A* (invalidate response)

# State Transition Diagram for an Individual Cache Block in a Directory Based System

- States identical to snoopy case; transactions very similar.
- Transitions caused by read misses, write misses, invalidates, data fetch requests
- Generates read miss & write miss msg to home directory.
- Write misses that were broadcast on the bus for snooping => explicit invalidate & data fetch requests.
- Note: on a write, a cache block is bigger, so need to read the full cache block

# CPU -Cache State Machine

- State machine for CPU requests for each memory block
- Invalid state if in memory

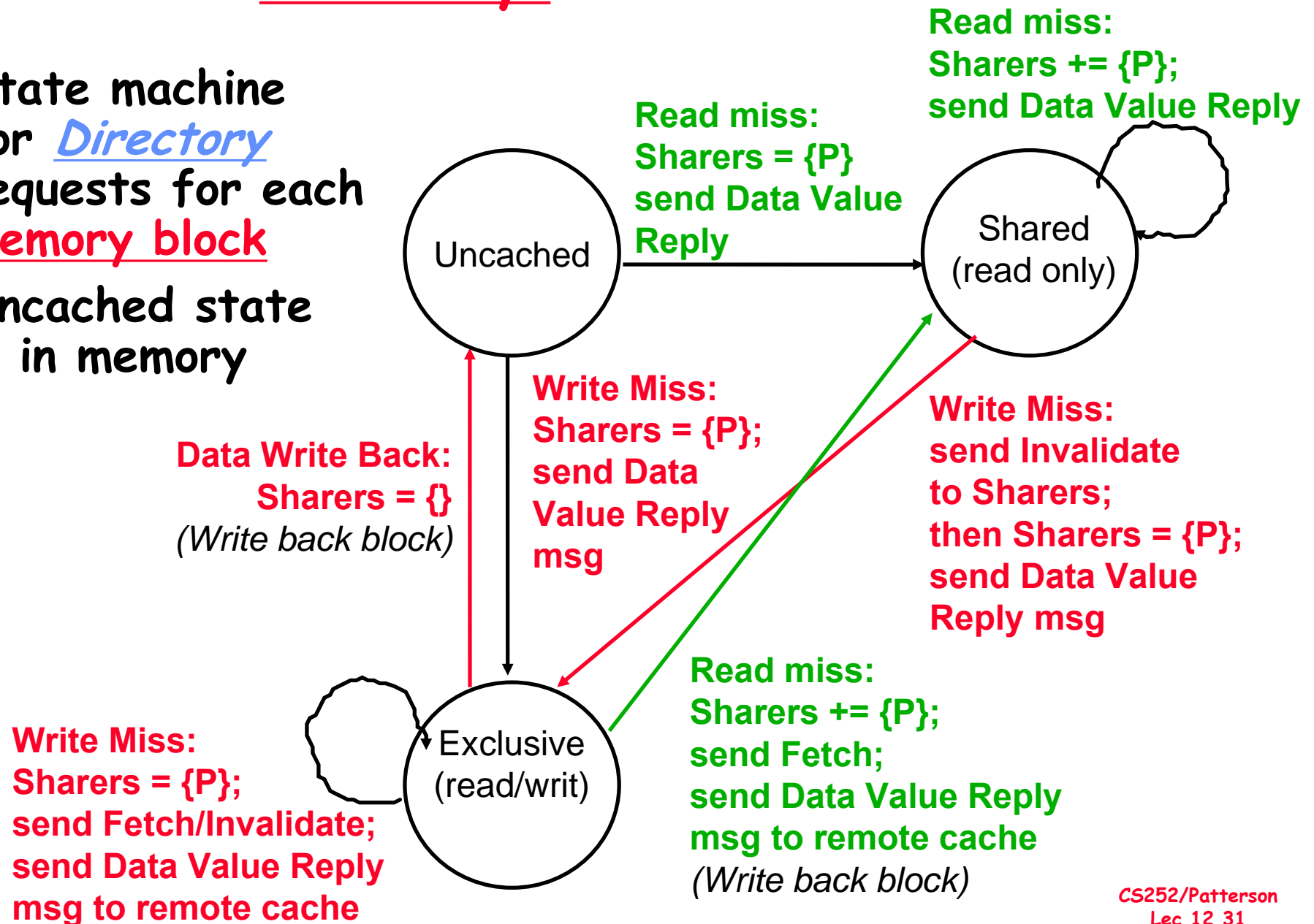


# State Transition Diagram for the Directory

- Same states & structure as the transition diagram for an individual cache
- 2 actions: update of directory state & send msgs to satisfy requests
- Tracks all copies of memory block.
- Also indicates an action that updates the sharing set, Sharers, as well as sending a message.

# Directory State Machine

- State machine for Directory requests for each memory block
- Uncached state if in memory



## Example Directory Protocol

- Message sent to directory causes two actions:
  - Update the directory
  - More messages to satisfy request
- Block is in **Uncached** state: the copy in memory is the current value; only possible requests for that block are:
  - **Read miss**: requesting processor sent data from memory & requestor made only sharing node; state of block made Shared.
  - **Write miss**: requesting processor is sent the value & becomes the Sharing node. The block is made Exclusive to indicate that the only valid copy is cached. Sharers indicates the identity of the owner.
- Block is **Shared** => the memory value is up-to-date:
  - **Read miss**: requesting processor is sent back the data from memory & requesting processor is added to the sharing set.
  - **Write miss**: requesting processor is sent the value. All processors in the set Sharers are sent invalidate messages, & Sharers is set to identity of requesting processor. The state of the block is made Exclusive.



## Example Directory Protocol

- Block is **Exclusive**: current value of the block is held in the cache of the processor identified by the set Sharers (the owner) => three possible directory requests:
  - **Read miss**: owner processor sent data fetch message, causing state of block in owner's cache to transition to Shared and causes owner to send data to directory, where it is written to memory & sent back to requesting processor.  
Identity of requesting processor is added to set Sharers, which still contains the identity of the processor that was the owner (since it still has a readable copy). State is shared.
  - **Data write-back**: owner processor is replacing the block and hence must write it back, making memory copy up-to-date (the home directory essentially becomes the owner), the block is now Uncached, and the Sharer set is empty.
  - **Write miss**: block has a new owner. A message is sent to old owner causing the cache to send the value of the block to the directory from which it is sent to the requesting processor, which becomes the new owner. Sharers is set to identity of new owner, and state of block is made Exclusive.

# Example

## Processor 1   Processor 2   Interconnect   Directory   Memory

	P1			P2			Bus			Directory				Memor
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	State	{Procs}	Value
P1: Write 10 to A1														
P1: Read A1														
P2: Read A1														
P2: Write 20 to A1														
P2: Write 40 to A2														

A1 and A2 map to the same cache block

# Example

Processor 1			Processor 2			Interconnect			Directory			Memory		
	<i>P1</i>			<i>P2</i>			<i>Bus</i>				<i>Directory</i>			<i>Memor</i>
<i>step</i>	<i>State</i>	<i>Addr</i>	<i>Value</i>	<i>State</i>	<i>Addr</i>	<i>Value</i>	<i>Action</i>	<i>Proc.</i>	<i>Addr</i>	<i>Value</i>	<i>Addr</i>	<i>State</i>	<i>{Procs}</i>	<i>Value</i>
P1: Write 10 to A1							<u>WrMs</u>	P1	A1		<u>A1</u>	<u>Ex</u>	<u>{P1}</u>	
	<u>Excl.</u>	<u>A1</u>	<u>10</u>				<u>DaRp</u>	P1	A1	0				
P1: Read A1														
P2: Read A1														
P2: Write 20 to A1														
P2: Write 40 to A2														

A1 and A2 map to the same cache block

# Example

## Processor 1   Processor 2   Interconnect   Directory   Memory

	<i>P1</i>			<i>P2</i>			<i>Bus</i>			<i>Directory</i>				<i>Memor</i>
<i>step</i>	<i>State</i>	<i>Addr</i>	<i>Value</i>	<i>State</i>	<i>Addr</i>	<i>Value</i>	<i>Action</i>	<i>Proc.</i>	<i>Addr</i>	<i>Value</i>	<i>Addr</i>	<i>State</i>	<i>{Procs}</i>	<i>Value</i>
P1: Write 10 to A1							<u>WrMs</u>	P1	A1		<u>A1</u>	<u>Ex</u>	<u>{P1}</u>	
	<u>Excl.</u>	<u>A1</u>	<u>10</u>				<u>DaRp</u>	P1	A1	0				
P1: Read A1	Excl.	A1	10											
P2: Read A1														
P2: Write 20 to A1														
P2: Write 40 to A2														

A1 and A2 map to the same cache block

# Example

## Processor 1 Processor 2 Interconnect Directory Memory

	P1			P2			Bus			Directory				Memor
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	State	{Procs}	Value
P1: Write 10 to A1							WrMs	P1	A1		A1	Ex	{P1}	
	Excl.	A1	10				DaRp	P1	A1	0				
P1: Read A1	Excl.	A1	10											
P2: Read A1				Shar.	A1		RdMs	P2	A1					
	Shar.	A1	10				Ftch	P1	A1	10	A1			10
				Shar.	A1	10	DaRp	P2	A1	10	A1	Shar.	P1,P2}	10
P2: Write 20 to A1														
P2: Write 40 to A2														

Write Back

A1 and A2 map to the same cache block

# Example

## Processor 1 Processor 2 Interconnect Directory Memory

	P1			P2			Bus			Directory				Memor
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	State	{Procs}	Value
P1: Write 10 to A1							WrMs	P1	A1		A1	Ex	{P1}	
	Excl.	A1	10				DaRp	P1	A1	0				
P1: Read A1	Excl.	A1	10											
P2: Read A1				Shar.	A1		RdMs	P2	A1					
	Shar.	A1	10				Ftch	P1	A1	10	A1			10
				Shar.	A1	10	DaRp	P2	A1	10	A1	Shar.	P1,P2}	10
P2: Write 20 to A1				Excl.	A1	20	WrMs	P2	A1					10
	Inv.						Inval.	P1	A1		A1	Excl.	{P2}	10
P2: Write 40 to A2														-

A1 and A2 map to the same cache block

# Example

## Processor 1 Processor 2 Interconnect Directory Memory

	P1			P2			Bus			Directory				Memor
step	State	Addr	Value	State	Addr	Value	Action	Proc.	Addr	Value	Addr	State	{Procs}	Value
P1: Write 10 to A1							WrMs	P1	A1		A1	Ex	{P1}	
	Excl.	A1	10				DaRp	P1	A1	0				
P1: Read A1	Excl.	A1	10											
P2: Read A1				Shar.	A1		RdMs	P2	A1					
	Shar.	A1	10				Ftch	P1	A1	10	A1			10
				Shar.	A1	10	DaRp	P2	A1	10	A1	Shar.	P1,P2}	10
P2: Write 20 to A1				Excl.	A1	20	WrMs	P2	A1					10
	Inv.						Inval.	P1	A1		A1	Excl.	{P2}	10
P2: Write 40 to A2							WrMs	P2	A2		A2	Excl.	{P2}	0
							WrBk	P2	A1	20	A1	Unca.	{}	20
				Excl.	A2	40	DaRp	P2	A2	0	A2	Excl.	{P2}	0

A1 and A2 map to the same cache block

# Implementing a Directory

- We assume operations atomic, but they are not; reality is much harder; must avoid deadlock when run out of buffers in network (see Appendix E)
- Optimizations:
  - read miss or write miss in Exclusive: send data directly to requestor from owner vs. 1st to memory and then from memory to requestor



# Synchronization

- Why Synchronize? Need to know when it is safe for different processes to use shared data
- Issues for Synchronization:
  - Uninterruptable instruction to fetch and update memory (atomic operation);
  - User level synchronization operation using this primitive;
  - For large scale MPs, synchronization can be a bottleneck; techniques to reduce contention and latency of synchronization

# Uninterruptable Instruction to Fetch and Update Memory

- **Atomic exchange**: interchange a value in a register for a value in memory
  - 0 => synchronization variable is free
  - 1 => synchronization variable is locked and unavailable
  - Set register to 1 & swap
  - New value in register determines success in getting lock
    - 0 if you succeeded in setting the lock (you were first)
    - 1 if other processor had already claimed access
  - Key is that exchange operation is indivisible
- **Test-and-set**: tests a value and sets it if the value passes the test
- **Fetch-and-increment**: it returns the value of a memory location and atomically increments it
  - 0 => synchronization variable is free

# Uninterruptable Instruction to Fetch and Update Memory

- Hard to have read & write in 1 instruction: use 2 instead
- **Load linked** (or load locked) + **store conditional**
  - Load linked returns the initial value
  - Store conditional returns 1 if it succeeds (no other store to same memory location since preceeding load) and 0 otherwise
- Example doing atomic swap with LL & SC:

```
try:  mov    R3,R4           ; mov exchange value
      ll     R2,0(R1)        ; load linked
      sc     R3,0(R1)        ; store conditional
      beqz   R3,try          ; branch store fails (R3 = 0)
      mov    R4,R2          ; put load value in R4
```

- Example doing fetch & increment with LL & SC:

```
try:  ll     R2,0(R1)        ; load linked
      addi   R2,R2,#1        ; increment (OK if reg-reg)
      sc     R2,0(R1)        ; store conditional
      beqz   R2,try          ; branch store fails (R2 = 0)
```

# User Level Synchronization—Operation Using this Primitive

- **Spin locks**: processor continuously tries to acquire, spinning around a loop trying to get the lock

```
lockit:    li      R2,#1
           excl     R2,0(R1)      ;atomic exchange
           bnez     R2,lockit     ;already locked?
```

- What about MP with cache coherency?
  - Want to spin on cache copy to avoid full memory latency
  - Likely to get cache hits for such variables
- Problem: exchange includes a write, which invalidates all other copies; this generates considerable bus traffic
- Solution: start by simply repeatedly reading the variable; when it changes, then try exchange (“test and test&set”):

```
try:       li      R2,#1
lockit:    lw       R3,0(R1)      ;load var
           bnez     R3,lockit     ;not free=>spin
           excl     R2,0(R1)      ;atomic exchange
           bnez     R2,try        ;already locked?
```

## Another MP Issue: Memory Consistency Models

- What is consistency? **When** must a processor see the new value? e.g., seems that

P1: A = 0;

P2: B = 0;

.....  
A = 1;

.....  
B = 1;

L1: if (B == 0) ...

L2: if (A == 0) ...

- Impossible for both if statements L1 & L2 to be true?
  - What if write invalidate is delayed & processor continues?
- Memory consistency models:  
what are the rules for such cases?
- **Sequential consistency**: result of any execution is the same as if the accesses of each processor were kept in order and the accesses among different processors were interleaved => assignments before ifs above
  - SC: delay all memory accesses until all invalidates done

# Memory Consistency Model

- Schemes faster execution to sequential consistency
- Not really an issue for most programs; they are **synchronized**
  - A program is synchronized if all access to shared data are ordered by synchronization operations

write (x)

...

release (s) {unlock}

...

acquire (s) {lock}

...

read(x)

- Only those programs willing to be nondeterministic are not synchronized: “**data race**”: outcome f(proc. speed)
- Several Relaxed Models for Memory Consistency since most programs are synchronized; characterized by their attitude towards: RAR, WAR, RAW, WAW to different addresses

## Summary

- Caches contain all information on state of cached memory blocks
- Snooping and Directory Protocols similar; bus makes snooping easier because of broadcast (snooping => uniform memory access)
- Directory has extra data structure to keep track of state of all cache blocks
- Distributing directory => scalable shared address multiprocessor  
=> Cache coherent, Non uniform memory access