

Lecture 5

Logistic

Midterm: Today at 5pm CST
Due next Friday (July 10 11:59pm)
CST

No need to write any 66/56
check-expect. Total: 56
Total + Extra Credit: J2

20 - 22

Map, Filter, Foldl, Foldr

Map

(map f my-list)

↑ ↑
Input 1 Input 2
↓ ↓
function List

(list 1 2 3 4)

f is a function that adds 1
to any number. $f(n) = n + 1$

$f(2) = f(3)$

(map f (list 1 2 3 4))

(list f(1) f(2) f(3) f(4))

(list 2 3 4 5)

(: add1 : Integer → Integer)
;; Adds one to any integer

(define (add1 x)
(+ x 1))

(map add1 (list 1 2 3 4))
⇒ '(2 3 4 5)

Write a function that takes
a list as input and adds to
every element.

(: add1-list : (Listof Integer) → (Listof Integer))

(define (add1-list my-list))
(map add1 my-list))

Example: Append ! to a every
string in a list

(: append-! : String → String)

(define (append!) input)
(string-append input "!"))

(map append-! (list "no" "good"))

⇒ (list "no!" "good!") .

Write a program which takes
a list of Point and
outputs the list X-coordinate.

(λ x-cor : (Listof Point) \rightarrow (Listof Real))

(define (x-cor my-list)

(map Point-x my-list))

For this to work the structure
Point has to be defined before.

Filter

(filter f? my-list)



Boolean (It's output is a boolean)

Example

Write a function which takes list of integers and outputs a list containing only the odd integers.

```
(: my-odd? : Integer → Boolean)
(define (my-odd? num)
  (if (= (remainder num 2) 1)
      #t
      #f))
```

(\therefore list-odd : (Listof Integer)
 \rightarrow (Listof Integer))

(define (list-odd my-list)
(filter my-odd? my-list))

Output

(filter my-odd? (list 1 2 3 4 5))

\Rightarrow

1 2 3 4 5
↓ ↗
(my-odd? 1) (my-odd? 2)
#t false.

Apply (my-odd?) to every element)

$\Rightarrow '(1 3 5)$

(list 1 2 3 4 5)

(my-odd? 1) (my-odd? 2)
↓ ↓
#t #f

(my-odd? 3) (my-odd? 4)
#t #f

(my-odd? 5)
#t

(1 3 5)

Recursive idea is this

- Take the first element
- check if $(func (\text{first my-list}))$ is true
 - Recursively call on the (rest my-list)

$(1 \ 2 \ 3 \ 4 \ 5)$

| $(2 \ 3 \ 4 \ 5)$
↓ Taken care by the
Since list $(3 \ 5)$ recursion
odd we will add to our list

(1 3 5)

Example

Write a function which takes a list of strings as input and outputs those strings which starts with 'S'.

Step1: Write a function which takes a string as input and output true if it starts with 'S' else f.

(
C: starts-with-S? : String → Boolean)
(define (starts-with-S? title)

(and (λ (string-length title) 0))

(char=? (string-ref title 0)
#\S))))

(: list-starts : (Listof String)
→ (Listof String))

(define (list-starts my-list)
(filter starts-with-S? my-list))



Function which
checks if a string
starts with S Input

Foldr and Foldl

$$(\text{foldr} + 0 \ (\text{list } 1 \ 2 \ 3 \ 4))$$

$\Rightarrow \underline{10}$

←

Acc = 0

(Binary operator \rightarrow A function
which takes two inputs of
the same type and outputs
something of the same type)

Before val

$$4 + \text{Acc} = 4$$

$$\text{Acc} = 0$$

$$\text{Acc} = \text{Acc} + 3$$

$$\text{Acc} = 4$$

$$\text{Acc} = \text{Acc} + 2$$

$$\text{Acc} = 7$$

$$\text{Acc} = \text{Acc} + 1$$

$$\text{Acc} = 9$$

$$\text{Acc} = 10.$$

Write a program which takes a list of integers as input and sums all its elements

(: sum-list : (Listof Integer) → Integer)
(define (sum-list my-list)

(foldr + 0 my-list))

(foldl + 0 (list 1 2 3 4))

⇒ 10.

The ↓ string-append is
foldr string-append " " the binary
(list "h" "e" "l" "l" "o") operator

⇒
Step): Element from + hb
Acc
string-append "O" " " ⇒ "O"

String-append "l" "O" ⇒ "lo"

String-append "l" "lo" ⇒ "llo"

String-append "e" "llo" ⇒ "ello"

String-append "h" "ello" ⇒ "hello"

```
(foldl string-append ""  
  (list "h" "e" "l" "l" "o"))
```

⇒ "olleh"

Polymorphism

There is function called length.

```
(length (list 5 10 100))
```

⇒ 3

```
(length (list "Hyde" "Pork"))
```

$\Rightarrow 2.$

length works on list of any type.

polymorphism - polymorphic function

(: length : (A :: (A) (Listof A) → Integer)).

First

What is the type annotation for first?

(: first : (A :: (A) (Listof A) → A))

$(\vdash \text{rest} : (\text{All } (A) \text{ } (\text{Listof } A) \rightarrow (\text{Listof } A)))$

What is the type of map

Input 1: Function $(A \rightarrow B)$
Input 2: List of A . . .

Output: List of B .

$(\vdash \text{map} : (\text{All } (A \text{ } B) \text{ } (A \rightarrow B) \text{ } (\text{Listof } A) \rightarrow (\text{Listof } B)))$

Type annotations for foldl and foldr

First-Class function

Function are Data

Example of a function
which outputs a function.

Example

Write a function which takes
two functions and a real
number as input, the
function which was greater
value at the that real
number.

Input: f , g , t

$$f(+)>-g(+)$$

$$\Rightarrow f$$

otherwise

$$\Rightarrow g$$

(: max-func : (Real → Real))

(Real → Real) Real

→ (Real → Real)

(define (max-func f g z))

(if (> (f z) (g z))
 f
 g))

$$f(x) = x + 1$$

$$g(x) = x^3$$

Inputs $f(x) = x + 1$
 $g(x) = x^3$

2

Output: $f(2) = 3$
 $g(2) = 8$

$\Rightarrow g$

```
(: add-one : Real → Real)
(define (add-one x)
  (+ x 1))
```

```
(: cube : Real → Real)
(define (cube x)
  (* x x x))
```

```
(check-expect ((max-func-add-one cube 2) 5)
               (cube 5))
```

Example

```
(define-type Int-set (Integers
                       → Boolean))
```

Concept of set of integers.
Set of Integers : \mathbb{Z}
 $\{2, 3\} \subseteq \mathbb{Z}$

$$\{1, 5, 6, 7\} \subseteq \mathbb{Z}$$

$$\{2, 4, 6, 8, 10, 12, \dots\} \subseteq \mathbb{Z}$$

The set of all even integers

A set of integers can
thought of as a function.

It's function from Integers
to Boolean

$\{2, 3\} \subseteq \mathbb{Z}$.

$f(2) \Rightarrow \text{true}$

$f(3) \Rightarrow \text{true}$

$f(n) \Rightarrow \text{false}$

for any other integer n .

$f(4) \Rightarrow \underline{\text{false}}$

Function representation
of sets.

Want to represent the
set $\{2, 3\}$

(\because 2-or-3 : Int-Set)

; This function represents
the set {2, 3}

(define (2-or-3 n))

(match n

[2 #t] \leftarrow True

[3 #t] \leftarrow True

[- #f] \leftarrow False.

2-or-3 "represents" the
set {2, 3}

Example 2:

Write a function which takes
two Int-set (two sets)
outputs the union.

$$\{2, 3\} \cup \{3, 4, 5\} \\ \Rightarrow \{2, 3, 4, 5\}$$

In other words.

$$f1 = \{2, 3\}$$

$$f2 = \{3, 4, 5\}$$

Then my output should be
 $f3$ which outputs true on
 $\{2, 3, 4, 5\}$ else false.

(: union-int-set : Int-Set
Int-Set → Int→Set)

; takes the union of

; two int-sets

I am defining the set.

(define (union-int-set set1 set2))

(local {
} ← This lets define things
inside a function

(: set3 : Int→Set)

(define (set3 n)

(or (set1 n) (set2 n))))

set3)

Set1 and set2
are available here

```
(define (S n))  
(or (set1 n) (get2 n)))
```

Homework 4 2c

Mutual Recursion

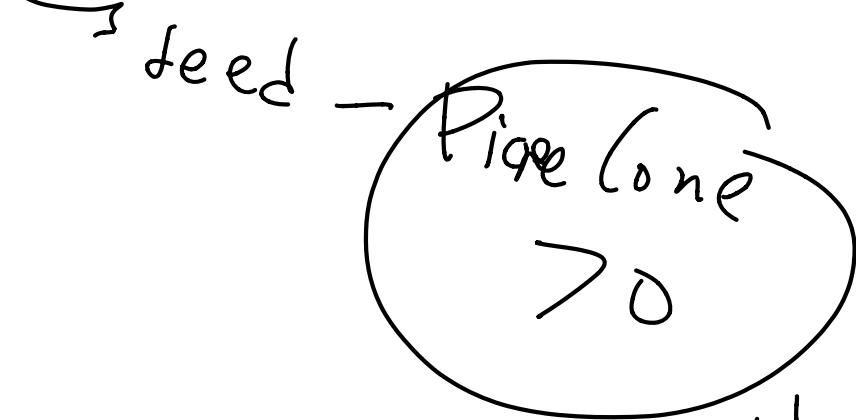
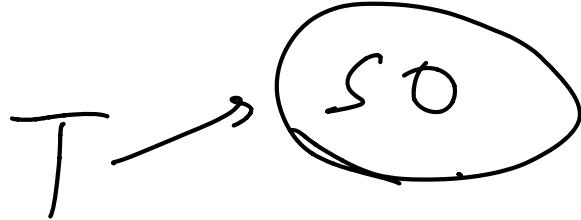
Suppose there is a tree T

T — height
 ↓
 seed

max-tree-descendant(T)

$$= \max \left\{ \begin{array}{l} \text{height} \\ \uparrow \\ \text{max-cone-descendant} \\ - \text{height}(\text{seed}) \end{array} \right\}$$

height of T .

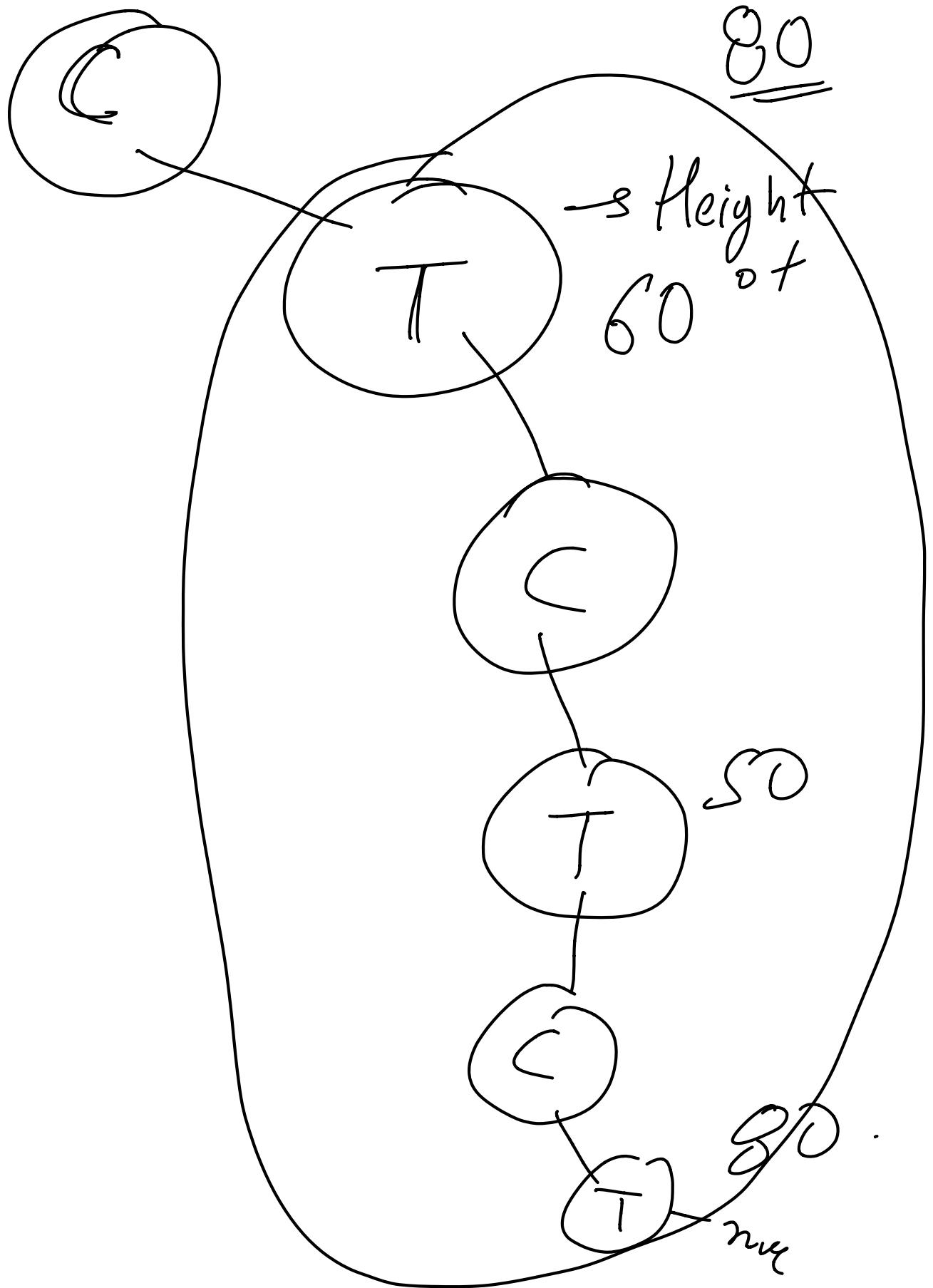


max-cone-descendant(C)

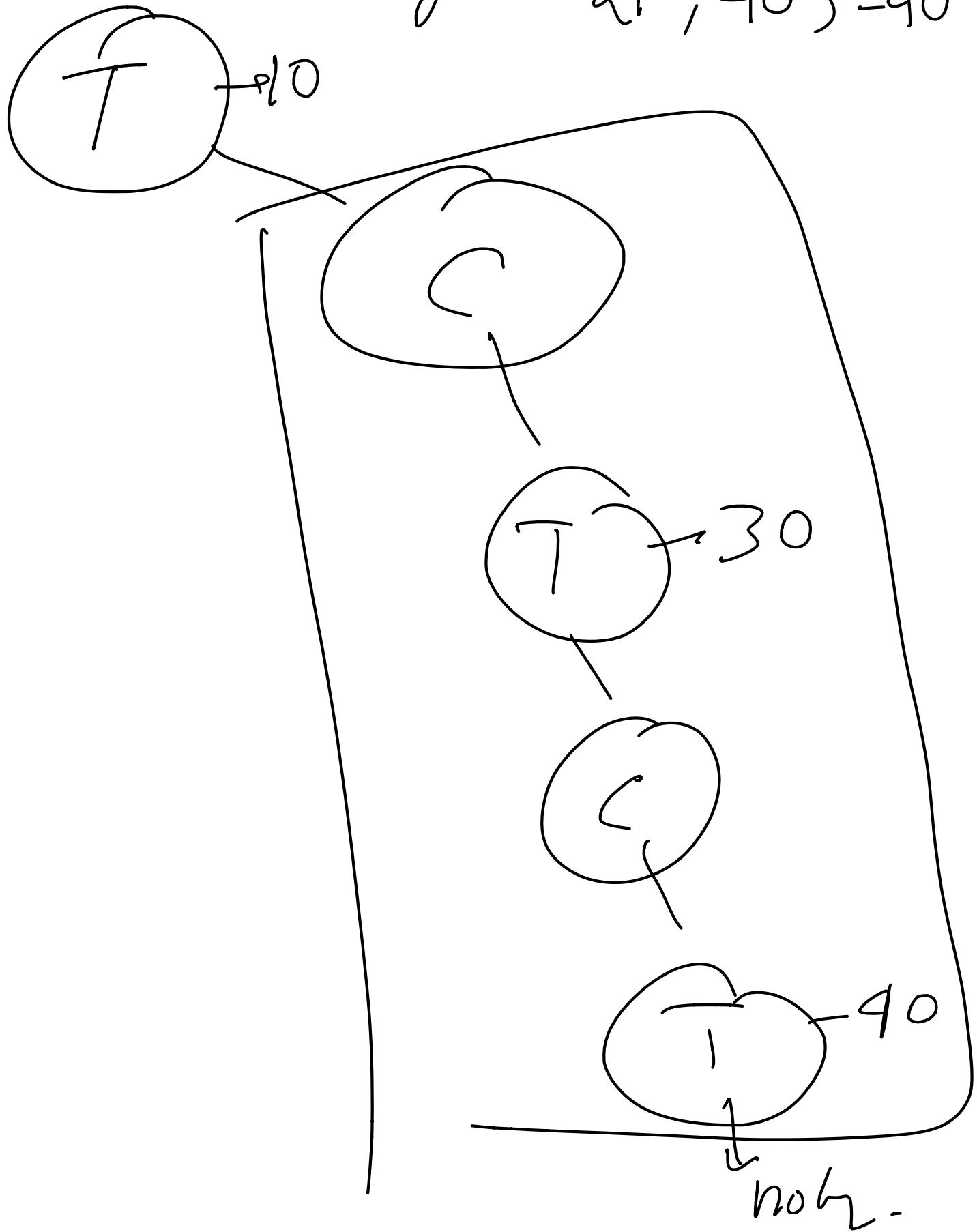
$$= \text{max-tree-descendant}(T)$$

C is a cone here

C grows in T.



max height = $\{10, 40\} = 40$



Base case for
max-tree-descendant
- height

If tree has no seeds -

$$\overline{T} \rightarrow 60 \quad (60)$$

→ seed = 'nothing'

Base case for max-cone
- descendant → height

If my cone grows into
nothing, its height is 0.

(: max-tree-descendant-height
 : Pine-Tree → Real)

(define (max-tree-descendant-height
 tree)

(cond

[(symbol? (Pine-Tree-seed tree))
 (Pine-Tree-height tree)]

[else (max (Pine-Tree-height tree)

 (max-one-descendant-height
 (Pine-Tree-seed tree))))])

(: max-cone-descendant-height :
Pine-Cone → Real)

(define (max-one-descendant-height
cone) -

(cond

[(symbol? (Pine-Cone-grows-into
cone)) 0]

[else (max-tree-descendant-height
(Pine-Cone-grows-into cone))])

Zb

(: germinate : Pine-Tree → Pine-Tree)

(define (germinate tree)

(cond

[(Pine-Cone? (Pine-Tree-seed tree))

tree]
[else (Pine-Tree (Pine-Cone
`nothing 40) (Pine-Tree-height
tree ??)])