

# Consensus Algorithms in Wireless Blockchain System

## **1 Consensus Algorithm in Each Round**

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**Algorithm 1** The SWIB Protocol

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**Input:** List of consensus nodes  $\{1, 2, \dots, N\}$  with active time  $\{T_1, T_2, \dots, T_N\}$ ; Transaction-  
s  $Txs = \{tx_1, tx_2, \dots\}$ ; Target contention success probability  $\varsigma$ ; Target transmission  
success probability  $\xi$ ; channel compete probability  $p$  Transmission parameters  $\{P_t, \alpha, \beta\}$

**Output:** Blockchain  $BC$

```
1: /** Achieving consensus on block round-by-round,  $r$  round  
2: ▷ Initialization: Slots 1:  
3: Get  $N$  nodes sorted based on public key value;  
4: Compute elected probability of all nodes according to stability;  
5: Compute required contention time slots  $x_{comp}$ ;  
6: Compute required transmission time slots  $x_{trans}$   
7: ▷ Block Proposer Election: Slots 2:  
8:  $Rdm^r = \text{GenerateRandomValue}(r, B_H^{r-1}, sig_{full}^{r-1})$   
9:  $ID_{BP} = \text{Block Proposer Election}(NodeList, Rdm^r)$   
10: ▷ Block Generation:  
11: for  $x_{comp} + T_B \cdot x_{trans}$  Slots do  
12:   if  $BP_{ID} == Node_{ID}$  then  
13:      $B^r = \text{Generate Block}(B_H^{r-1}, Txs)$   
14:     Broadcast the block  $B^r$  to other nodes with transmit power  $P_t$   
15:   else  
16:     Listen on the channel to receive the block  
17:   end if  
18: end for  
19: ▷ Block Verification  
20: for  $N \cdot x_{comp} + T_{sig} \cdot x_{trans}$  Slots do  
21:   for Any node in  $\{1, \dots, N\}$  do  
22:     if  $Node_{ID} \neq BP_{ID}$  then  
23:       if  $isLegal(BP_{Node_{ID}})$  and  $isValid(B^r)$  then  
24:          $sig^r = \text{Generate Signature}(B^r, sk)$   
25:         Broadcast  $sig^r$  to other nodes  
26:       else  
27:         Discard the new block and generate an empty block  $B_{empty}^r$   
28:          $sig^r = \text{Generate Signature}(B_{empty}^r, sk)$   
29:         Broadcast  $sig^r$  to other nodes  
30:       end if  
31:     end if  
32:     if received enough partial signatures  $Count(Sigs^r) > threshold$  then  
33:        $sig_{full}^r = \text{Recover Full Signature}(Sigs^r)$   
34:       Broadcast  $sig^r$  to other nodes  
35:     end if  
36:   end for  
37:   /** Broadcast signatures  
38:   Listen on the channel  
39:   if Node  $v$  decides to send a signature with transmit probability  $p_v$  then  
40:     Broadcast( $sig_v^r$ ) with transmit power  $P_t$   
41:   else  
42:     if channel is idle then  
43:        $e_v = e_v + 1$  /** Count idle slots within  $T_v$   
44:     else  
45:       Receive a message from others
```

```

46:     end if
47: end if
48: /**maintain the estimate of adversary time window
49: for Any nodes  $v \in \{1, \dots, N\}$  do
50:      $count_v = count_v + 1$ 
51:     if  $count_v > T_v$  then
52:          $count_v = 1$ 
53:         if  $e_v == 0$  then /** No idle round in the past  $T_v$  slots
54:              $\hat{p}_v = p_v / (1 + \frac{1}{T_v})$ 
55:              $\hat{T}_v = \hat{T}_v + 2$ 
56:         else if  $e_v \geq 1$  then
57:              $\hat{p}_v = \hat{p}_v * (1 + \frac{e_v}{T_v})$ 
58:              $\hat{T}_v = \hat{T}_v - 1$ 
59:         end if
60:     end if
61: end for
62: end for
63: ▷ Block Finalization Slots 2:
64: for Any node  $\{1, \dots, N\}$  do
65:     if  $r$  then received or generated  $sig_{full}^r$ 
66:          $AddSig(B^r, sig_{full}^r)$ 
67:          $Append(BC, B^r)$ 
68:     end if
69: end for

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**Algorithm 1** The SWIB Protocol

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**Input:** List of consensus nodes  $\{1, 2, \dots, N\}$  with active time  $\{T_1, T_2, \dots, T_N\}$ ; Transactions  $Txs$ ; Target contention success probability  $\varsigma$ ; Target transmission success probability  $\xi$

**Output:** Blockchain  $BC$

```
1: /** Achieving consensus on block round-by-round,  $r$  round  
2: ▷ Initialization:  
3:  $Finalized = False$ ;  
4: ▷ Block Proposer Election:  
5: Slot 1:  $Rdm^r = GenerateRandomValue(r, B_H^{r-1}, sig_{full}^{r-1})$ ;  
6: Slot 2: Compute elected probability of all nodes according to stability;  
7: Slot 3: Get sorted node list  $NodeList$  based on public key value;  
8: Slot 4:  $ID_{BP} = \text{Block Proposer Election}(NodeList, Rdm^r)$ ;  
9: ▷ Block Generation:  
10: for  $x_{comp} + T_B \cdot x_{trans}$  Slots do  
11:   if  $BP_{ID} == Node_{ID}$  then  
12:     if node has not enough transactions then  
13:       Request transactions from other nodes  
14:     end if  
15:      $B^r = \text{Generate Block}(B_H^{r-1}, Txs)$   
16:     Broadcast the block  $B^r$  to other nodes with transmit power  $P_t$   
17:   else  
18:     Listen on the channel to receive the block  
19:     if Receive a request from block proposer then  
20:       run broadcastMessage( $Txs$ )  
21:     end if  
22:   end if  
23: end for  
24: ▷ Block Verification  
25: for  $N \cdot x_{comp} + T_{sig} \cdot x_{trans}$  Slots do  
26:   for Any node in  $\{1, \dots, N\}$  do  
27:     if  $Node_{ID} \neq BP_{ID}$  then  
28:       if  $isLegal(BP_{Node_{ID}})$  and  $isValid(B^r)$  then  
29:          $sig^r = \text{Generate Signature}(B^r, sk)$   
30:         Broadcast  $sig^r$  to other nodes with transmit probability and transmit power  
31:       else  
32:         Discard the new block and generate an empty block  $B_{empty}^r$   
33:          $sig^r = \text{Generate Signature}(B_{empty}^r, sk)$   
34:         run broadcsatSignature  
35:       end if  
36:     end if  
37:     if collect enough partial signatures  $Count(Sigs^r) > threshold$  then  
38:        $sig_{full}^r = \text{Recover Full Signature}(Sigs^r)$   
39:       run broadcsatMessage( $Sigs$ )  
40:     end if  
41:   end for  
42: end for  
43: ▷ Block Finalization:  
44: for Any node  $\{1, \dots, N\}$  do  
45:   if received or generated the  $sig_{full}^r$  then
```

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```

46:       $AddSig(B^r, sig_{full}^r)$ 
47:       $Append(BC, B^r)$ 
48:       $Update(NodeList)$ 
49:       $Finalized = True$ 
50:  end if
51: end for

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**Algorithm 3** Synchronization Mechanism

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**Input:** Latest blockchain length  $Length$  Neighbor list  $Neighbors$

**Output:** blockchain

```

1: for node  $v$  in  $Neighbors$  do
2:   if  $Len(BC_v) == Length$  and  $Stability_v > threshold$  then
3:     add the node to RequestNeighbors
4:   end if
5: end for
6: for node  $i$  in the Requested Neighbors do
7:   Request  $m$  blocks from node
8:   if all blocks are valid then
9:     Add missing block to local blockchain
10:  else
11:    request these blocks from other nodes in RequestNeighbors
12:  end if
13: end for

```

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**Algorithm 2** broadcastMessage Subroutine

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```

1: for Any node  $v$  in  $\{1, \dots, N\}$  do
2:   if Node  $v$  decides to send a message with transmit probability  $p_v$  then
3:      $Broadcast(msg)$  with transmit power  $P_t$ 
4:   else
5:     if channel is idle then
6:        $e_v = e_v + 1$  /** Count idle slots within  $T_v$ 
7:     else
8:       Receive a message from others
9:     end if
10:  end if
11:  /**maintain the estimate of adversary time window
12:   $count_v = count_v + 1$ 
13:  if  $count_v > \hat{T}_v$  then
14:     $count_v = 1$ 
15:    if  $e_v == 0$  then /** No idle slot in the past  $\hat{T}_v$  slots
16:       $\hat{p}_v = p_v / (1 + \frac{1}{\hat{T}_v})$ 
17:       $\hat{T}_v = \hat{T}_v + 2$ 
18:    else if  $e_v \geq 1$  then
19:       $\hat{p}_v = \hat{p}_v * (1 + \frac{e_v}{\hat{T}_v})$ 
20:       $\hat{T}_v = \hat{T}_v - 1$ 
21:    end if
22:  end if
23: end for

```

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**Algorithm 3** The SWIB Blockchain Consensus Protocol for each node  $v$

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```

1: while true do

```

```

2:  /** Iteration for round  $r$ 
3:  ▷ Initialization:
4:  for  $j < K$  slots do
5:      BroadcastMSG()
6:       $j = j + 1$ 
7:  end for
8:   $Rds^r = GenerateRandomValue(r, B_H^{r-1}, sig_{full}^{r-1})$ 
9:  ▷ Consensus Process:
10:  Block Proposer Election();
11:  Block Verification();
12:  Block Finalization();
13:   $r = r + 1$ 
14: end while

```

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**Algorithm 4** Block Verification for each node  $v$ 

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```
1:  $B^r, proof = RcvMSG()$ 
2: /**Check the validation of new block
3:  $result_v = \text{Verify Block Proposer}(pk_{BP}, proof, Rdm^r)$ 
4: if  $result_v == True$  then
5:   if  $H_{pre}^r == B_H^{r-1}$  then
6:     if  $isvalid(Txs)$  then
7:        $sig_v^r = \text{Generate Signature}(B_H^r, sk_v)$ 
8:     end if
9:   end if
10: end if
```

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**Algorithm 5** Block Finalization for each node  $v$ 

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```
1: while !finalized do
2:   BroadcastMSG()
3:    $sig_u^r, sig_{full}^r = RcvMSG()$ 
4:   /**Check the Finalization of new block
5:   if isValid( $sig_{full}^r$ ) then
6:     AddSig( $B^r, sig_{full}^r$ )
7:     Append( $BC, B^r$ )
8:     finalized = True
9:   else if Count( $Sigs^r$ )  $\geq \lceil \frac{N+1}{2} \rceil$  then
10:     $sig_{full}^r = \text{Recover Full Signature}(Sigs^r)$ 
11:    broadcast( $sig_{full}^r$ ) with probability  $p_{max}$  and power  $P_{max}$ 
12:    AddSig( $B^r, sig_{full}^r$ )
13:    Append( $BC, B^r$ )
14:    finalized = True
15:   else if  $sig_u^r \notin Sigs^r$  then
16:     Append Signature( $Sigs^r, sig_u^r$ )
17:   end if
18: end while
```

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**Algorithm 6** Stable Wireless Blockchain Protocol

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```
1:  $\triangleright$  Initialization:
2:  $Sortition(PKs^r, S^r)$ 
3:  $Rds^r = GenerateRandomness(r, B_{hash}^{r-1}, sig_{final}^r)$ 
4:  $\triangleright$  Leader Election and Block Proposal:
5:  $result = BlockProposerSelection(sk, Rds^r)$ 
6: if  $result == True$  then  $\triangleright$  As Block Proposer
7:    $B^r = GenerateBlock(B^{r-1}, Tx)$ 
8:    $sig_{partial}^r = Sign(B_{hash}^r)$ 
9:    $broadcast(B^r, sig_{partial}^r)$  with probability  $p$ 
10: else  $\triangleright$  As Ordinary Nodes
11:   Waiting to receive new Block
12: end if
13:  $\triangleright$  Block Verification and Finalization:
14: while  $!finalized$  do  $\triangleright$  All Consensus Nodes
15:    $(B^r, Signs^r, sig_{full}^r, Tx) = RcvMSG()$ 
16:   /**Check the validation of new block
17:   if  $isValid(B^r)$  and  $VerifyBlockProposer(pk_{BP}, Rds^r)$  then
18:      $sig_v^r = GenerateSignature(B_{hash}^r, sk_v)$ 
19:   end if
20:   if  $isValid(sig_{full}^r)$  then
21:      $\sigma_F^r = sig_{full}^r$ 
22:      $broadcast(\sigma_F^r)$  with probability  $p$ 
23:      $Append(B^r, \sigma_F^r)$ 
24:      $finalized = True$ 
25:   else if  $Count(Signs^r) \geq \lceil \frac{N}{2} \rceil$  then
26:      $\sigma_F^r = RecoverFullSignature(Signs^r)$ 
27:      $broadcast(\sigma_F^r)$  with probability  $p$ 
28:      $Append(B^r, \sigma_F^r)$ 
29:      $finalized = True$ 
30:   else if  $sig_u^r \notin Signs^r$  then
31:      $Signs^r = AppendSignature(sig_u^r)$ 
32:   else if  $v$  did not broadcast its partial signature then
33:      $broadcast(sig_v^r)$  with probability  $p$ 
34:   else
35:      $broadcast(Tx)$  with probability  $p$ 
36:   end if
37:    $count = count + 1$ 
38:   if  $count > T$  then
39:      $count = 1$ 
40:     if Received  $T$  consecutive transactions in the past  $T$  rounds then
41:        $p = p * (1 + \delta)^{-1}$ 
42:        $T = T + 2$ 
43:     end if
44:   end if
45: end while
```

```

46: function RECNEWBLOCK( $m_B, \sigma_v$ )
47:   if  $\sigma_v \notin sigShares$  then
48:      $sigShares = AppendSignature(\sigma_v)$ 
49:   end if
50:   if  $Count(sigShares) > K$  then
51:      $FinalSig = RecoverFinalSig(sigShares)$ 
52:   else
53:      $FinalSig = null$ 
54:   end if
55:   return  $sigShares, FinalSig, B_v^{new}$ 
56: end function
57: function APPENDSIGNATURE( $\sigma_v$ )
58:   if  $\sigma_v \notin sigShares$  then
59:      $sigShares \leftarrow sigShares + \sigma_v$ 
60:   end if
61:   return  $sigShares$ 
62: end function

```

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