Xi'an Jiaotong-Liverpool University
西交利物浦大学

XJTLU Entrepreneur College (Taicang) Cover Sheet

Module code and Title	**DTS201TC Pattern Recognition**	
School Title	**School of AI and Advanced Computing**	
Assignment Title	**Final project**	
Submission Deadline	**23:59, 31st Dec.**	
Final Word Count		
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<tr><th rowspan="2" colspan="2">Stage of Marking</th><th rowspan="2">Marker Code</th><th colspan="3">Learning Outcomes Achieved (F/P/M/D)
(please modify as appropriate)</th><th rowspan="2">Final Score</th></tr>
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<tr><td colspan="3">For Academic Office Use</td><td colspan="4">Possible Academic Infringement (please tick as appropriate)</td></tr>
<tr><td>Date Received</td><td>Days late</td><td>Late Penalty</td><td colspan="2">☐ Category A</td><td colspan="2" rowspan="5">Total Academic Infringement Penalty (A,B, C, D, E, Please modify where necessary) ____________________</td></tr>
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DTS201TC Classification Demonstration

Project (Individual)

1 Mathematical problems [40 marks]

Derive the Maximum Likelihood Estimate.

1.1 [20 marks]

Let $x_1, x_2, ..., x_N$ be vectors stemmed from a normal distribution with known covariance matrix and unknown mean, that is

$$p(x_k; \mu) = \frac{1}{(2\pi)^{D/2}|\Sigma|^{1/2}} exp(-\frac{1}{2}(x_k - \mu)^T \Sigma^{-1}(x_k - \mu)) \tag{1}$$

where D is the dimension of vector x_k $(k = 1, ..., N)$.

TASK 1: **Derive the ML estimate of the mean μ.**
Solution:

1.2 [20 marks]

Let $x_1, x_2, ..., x_N$ be vectors stemmed from a normal distribution with unknown mean μ and unknown convariance matrix Σ, that is

$$p(x_k; \mu, \Sigma) = \frac{1}{(2\pi)^{D/2}|\Sigma|^{1/2}} exp(-\frac{1}{2}(x_k - \mu)^T \Sigma^{-1}(x_k - \mu)) \tag{2}$$

where D is the dimension of vector x_k $(k = 1, ..., N)$.

***TASK 2:* Derive the ML Estimate of μ and Σ.**
Solution:

2 Practical problems [60 marks]

This assignment is designed to deal with MSRC-12 Kinect gesture data set of Microsoft Research Cambridge. The dataset contains lots of sequences of skeletal body movements recorded from a kinect device. However, this assignment only consider a small fraction of it, which consists of static body positions.

Assignment: classify the body positions with Bayes model.
Data: MSRC-12 Kinect gesture dataset of Microsoft Research Cambridge (provided on LMO together with this sheet)

- The dataset consists of 2045 instances of body positions with 4 categories of positions. "arms lifted", "right arm extended to one side", "crouched" and "right arm extended to the front". These classes are represented with distinctive numbers.
- The body positions are encoded with a 20×3 matrix, in which the row is the position in space (x,y,z) of each of the 20 joints. Each variable is modeled with a Gaussian distribution.
- Assume the 60 variables that define the body position are considered independent given the class.

Formulation: To be specific, you are expected to use Naive Bayes model. In Naive Bayes model, each of the 60 variables is considered independent given the class. Each variable is modeled with a Gaussian distribution. The training process for the model is to estimate the values for the mean and variance for each variable and class with MLE.

$$p(x_i|C) = Normal(\mu_{x_i}; \sigma^2_{x_i})$$
$$p(y_i|C) = Normal(\mu_{y_i}; \sigma^2_{y_i})$$
$$p(z_i|C) = Normal(\mu_{z_i}; \sigma^2_{z_i})$$

Where $p(i)$ is the probability density function of i-th joint,

$$P(C = k|sample) \propto P(C = k) \prod_{i=1}^{N} p(x_i, y_i, z_i|C = k)$$
$$p(x_i, y_i, z_i|C = k) = p(x_i|C = k) \times p(y_i|C = k) \times p(z_i|C = k)$$

Where, N is the number of samples, k indicates k-th label.

2.1 TASK 3:[20 marks]

Implement the function to estimate the parameters of the Gaussian distributions using MLE.

function: ***fit_model***

- Input: a vector which is the observation for a given variable
- Output: the mean and the standard deviation for these observations.

2.2 TASK 4: [20 marks]

Implement a function to build a model composed of priors, and model parameters.

*function :**learn_model***

- Input: the dataset and the labels

- Output: compute the parameters from the dataset to build the model

2.3 TASK 5: [20 marks]

Implement the classification function
function ***:classify_samples***

- Input: a set of instances that have the same format as the dataset given in *learn_model*
- Output: posterior probability for each instance belonging to each class

Marking Scheme for Task 3-5:

- You can choose to write Pseudocode in stead of implementing functions by coding.
- Write Pseudocode will get 2-10 marks for each function.
- Codes of each function can run properly, and can output accuracy on the test data, the accuracy is incorrect: incorrectly implemented function will get 5-15 marks accordingly.
- Codes of each function can run properly, and can output accuracy on the test data, the accuracy is correct : 60 marks in total.