

# COMP9024: Data Structures and Algorithms

## Week Four: Lists and Iterators

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Session 1, 2015

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## Outline

- Array lists
- Node lists
- Iterators

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## Lists



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## Lists

- A list is a collection of elements of the same type that are stored in a certain linear order.
- An element can be accessed, inserted or removed.
- Two types of lists:
  - Array lists
  - Node lists

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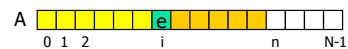
## Array List ADT

- A list that supports access to its elements by their indices.
- The List ADT extends the notion of array by storing a sequence of arbitrary objects.
- An element can be accessed, inserted or removed by specifying its index.
- An exception is thrown if an incorrect rank is specified (e.g., a negative rank)
- Main methods:
  - `get(i)`: Return the element with index *i*.
  - `set(i, e)`: Replace with *e* and return the element at index *i*.
  - `add(i, e)`: Insert a new element *e* at index *i*.
  - `remove(i)`: Remove the element at index *i*.

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## Array-Based Implementation

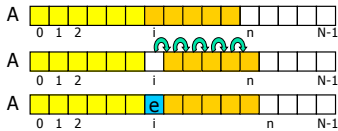
- Use an array *A* of size *N*.
- A variable *n* keeps track of the size of the list (the number of elements stored).
- Method `get(i)` is implemented in  $O(1)$  time by returning *A*[*i*].
- Method `set(i, e)` is implemented in  $O(1)$  time by setting *A*[*i*] to *e*.



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## Insertion (1/2)

- In method `add(i, e)`, we need to make room for the new element by shifting forward the  $n - i$  elements  $A[i], \dots, A[n-1]$ .
- In the worst case ( $i = 0$ ), this takes  $\mathcal{O}(n)$  time.



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## Insertion (2/2)

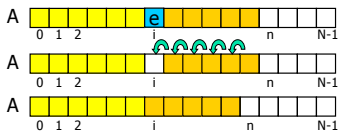
```

Algorithm add(i, e)
{
    for ( j = n-1, n-2, ..., i )
        A[j+1]=A[j];
    A[i]=e;
    n=n+1;
}
    
```

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## Deletion(1/2)

- In method `remove(i)`, we need to fill the hole left by the removed element by shifting backward the  $n - i - 1$  elements  $A[i+1], \dots, A[n-1]$ .
- In the worst case ( $i = 0$ ), this takes  $\mathcal{O}(n)$  time.



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## Deletion (2/2)

```

Algorithm remove(i)
{
    e=A[i];
    for ( j = i, i+1, ..., n-2 )
        A[j]=A[j+1];
    n=n-1;
    return e;
}
    
```

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## A Simple Interface

```

public interface IList<E> {
    /** Returns the number of elements in this list. */
    public int size();
    /** Returns whether the list is empty. */
    public boolean isEmpty();
    /** Inserts an element e to be at index i, shifting all elements after this. */
    public void add(int i, E e) throws IndexOutOfBoundsException;
    /** Returns the element at index i, without removing it. */
    public E get(int i) throws IndexOutOfBoundsException;
    /** Removes and returns the element at index i, shifting the elements after this. */
    public E remove(int i) throws IndexOutOfBoundsException;
    /** Replaces the element at index i with e, returning the previous element at i. */
    public E set(int i, E e) throws IndexOutOfBoundsException;
}
    
```

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## Extendable-Array-Based Array Lists (1/4)

Algorithm `add(i, e)`

- In an `add` operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one.
- How large should the new array be?
  - Incremental strategy: increase the size by a constant  $c$ .
  - Doubling strategy: double the size.

```

{ if ( size == N )
    { create a new array B with size 2N;
      for ( j = 0, 1, ..., size-1 )
          B[j]=A[j];
      A = B;
      N=2N;
    }
    insert e in A at i;
    size=size+1;
}
    
```

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## Extendable-Array-Based Array Lists (2/4)

```
/** Realization of an indexed list by means of an array, which is doubled when
the size of the indexed list exceeds the capacity of the array. */
public class ArrayIndexList<E> implements IndexList<E> {
    private E[] A; // array storing the elements of the indexed list
    private int capacity = 16; // initial length of array A
    private int size = 0; // number of elements stored in the indexed list /** Creates
the indexed list with initial capacity 16. */
    public ArrayIndexList() {
        A = (E[]) new Object[capacity]; // the compiler may warn, but this is ok
    }
}
```

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## Extendable-Array-Based Array Lists (3/4)

```
/** Inserts an element at the given index. */
public void add(int r, E e) throws IndexOutOfBoundsException {
    checkIndex(r, size() + 1);
    if (size == capacity) // an overflow
    { capacity *= 2; E[] B = (E[]) new Object[capacity];
      for (int i=0; i<size; i++) B[i] = A[i];
      A = B;
    }
    for (int i=size-1; i>=r; i--) // shift elements up
        A[i+1] = A[i];
    A[r] = e;
    size++;
}
```

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## Extendable-Array-Based Array Lists (4/4)

```
/** Removes the element stored at the given index. */
public E remove(int r) throws IndexOutOfBoundsException {
    checkIndex(r, size());
    E temp = A[r];
    for (int i=r; i<size-1; i++) // shift elements down
        A[i] = A[i+1];
    size--;
    return temp;
}
```

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## Comparison of the Strategies

- We compare the incremental strategy and the doubling strategy by analyzing the total time  $T(n)$  needed to perform a series of  $n$  push operations.
  - A push operation is to add an element at the end of the list.
- We assume that we start with an empty list represented by an array of size 1.
- We call amortized time of a push operation the average time taken by a push over the series of operations, i.e.,  $T(n)/n$ .

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## Incremental Strategy Analysis

- We replace the array  $k = n/c$  times.
- The total time  $T(n)$  of a series of  $n$  push operations is proportional to
$$n + c + 2c + 3c + 4c + \dots + kc$$
$$= n + c(1 + 2 + 3 + \dots + k)$$
$$= n + ck(k+1)/2.$$
- Since  $c$  is a constant,  $T(n)$  is  $O(n + k^2)$ , i.e.,  $O(n^2)$ .
- The amortized time of a push operation is  $O(n)$ .

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## Doubling Strategy Analysis

- We replace the array  $k = \log n$  times.
- The total time  $T(n)$  of a series of  $n$  push operations is proportional to
$$n + 1 + 2 + 4 + 8 + \dots + 2^k$$
$$= n + 2^{k+1} - 1 = 2n - 1.$$
- $T(n)$  is  $O(n)$ .
- The amortized time of a push operation is  $O(1)$ .

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## Position ADT

- The **Position** ADT models the notion of place within a data structure where a single object is stored
- It gives a unified view of diverse ways of storing data, such as
  - a cell of an array
  - a node of a linked list
- Just one method:
  - object `element()`: returns the element stored at the position

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## Java Interface for the Position ADT

```
public interface Position<E> {
    /** Return the element stored at this position. */
    E element();
}
```

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## Node List ADT

- The **Node List** ADT models a sequence of positions storing arbitrary objects
- It establishes a before/after relation between positions
- Generic methods:
  - `size()`, `isEmpty()`

Accessor methods:

- `first()`, `last()`
- `prev(p)`, `next(p)`

Update methods:

- `set(p, e)`
- `addBefore(p, e)`, `addAfter(p, e)`
- `addFirst(e)`, `addLast(e)`
- `remove(p)`

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## Java Interface for the Node List ADT (1/2)

```
public interface PositionList<E> {
    /** Returns the number of elements in this list. */
    public int size();
    /** Returns whether the list is empty. */
    public boolean isEmpty();
    /** Returns the first node in the list. */
    public Position<E> first();
    /** Returns the last node in the list. */
    public Position<E> last();
    /** Returns the node after a given node in the list. */
    public Position<E> next(Position<E> p) throws InvalidPositionException,
        BoundaryViolationException;
    /** Returns the node before a given node in the list. */
    public Position<E> prev(Position<E> p) throws InvalidPositionException,
        BoundaryViolationException;
}
```

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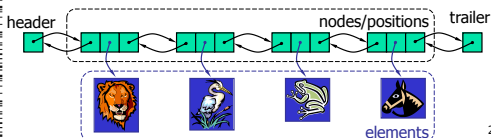
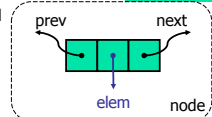
## Java Interface for the Node List ADT (2/2)

```
/** Inserts an element at the front of the list, returning new position. */
public void addFirst(E e);
/** Inserts an element at the end of the list, returning new position. */
public void addLast(E e);
/** Inserts an element after the given node in the list. */
public void addAfter(Position<E> p, E e) throws InvalidPositionException;
/** Inserts an element before the given node in the list. */
public void addBefore(Position<E> p, E e) throws InvalidPositionException;
/** Removes a node from the list, returning the element stored there. */
public E remove(Position<E> p) throws InvalidPositionException;
/** Replaces the element stored at the given node, returning old element. */
public E set(Position<E> p, E e) throws InvalidPositionException;
}
```

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## Doubly Linked List Implementation

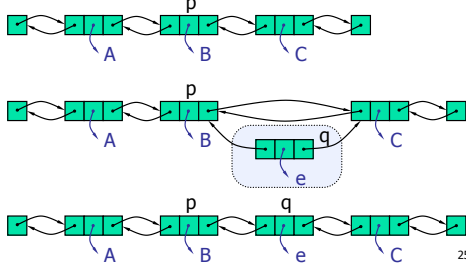
- A doubly linked list provides a natural implementation of the Node List ADT
- Nodes implement Position and store:
  - element
  - link to the previous node
  - link to the next node
- Special trailer and header nodes



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## Insertion

- We visualize operation `addAfter(p, e)`, which returns position `q`



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## Insertion Algorithm

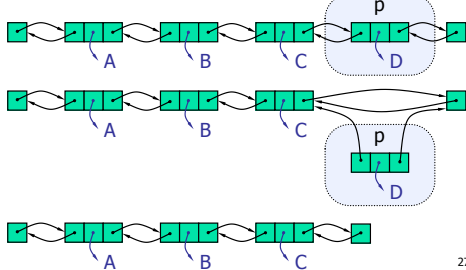
**Algorithm** `insertAfter(p, e)`

```
{
    Create a new node v;
    v.setElement(e);
    v.setPrev(p);           // link v to its predecessor
    v.setNext(p.getNext()); // link v to its successor
    (p.getNext()).setPrev(v); // link p's old successor to v
    p.setNext(v);           // link p to its new successor, v
    return v;               // the position for the element e
}
```

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## Deletion

- We visualize `remove(p)`, where `p = last()`



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## Deletion Algorithm

**Algorithm** `remove(p)`

```
{
    t = p.element; // a temporary variable to hold the return value
    (p.getPrev()).setNext(p.getNext()); // linking out p
    (p.getNext()).setPrev(p.getPrev());
    p.setPrev(null); // invalidating the position p
    p.setNext(null);
    return t;
}
```

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## Implementation of the Position Interface ADT (1/2)

```
public class DNode<E> implements Position<E> {
    private DNode<E> prev, next; // References to the nodes before and after
    private E element; // Element stored in this position

    /** Constructor */
    public DNode(DNode<E> newPrev, DNode<E> newNext, E elem) {
        prev = newPrev;
        next = newNext;
        element = elem;
    }

    // Method from interface Position
    public E element() throws InvalidPositionException {
        if ((prev == null) && (next == null)) throw new
            InvalidPositionException("Position is not in a list");
        return element;
    }
}
```

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## Implementation of the Position Interface ADT (1/2)

// Accessor methods

```
public DNode<E> getNext() { return next; }
public DNode<E> getPrev() { return prev; }

// Update methods
public void setNext(DNode<E> newNext) { next = newNext; }
public void setPrev(DNode<E> newPrev) { prev = newPrev; }
public void setElement(E newElement) { element = newElement; }
}
```

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## Java Implementation of the Node List ADT (1/7)

```
public class NodePositionList<E> implements PositionList<E> {
    protected int numElts; // Number of elements in the list
    protected DNode<E> header, trailer; // Special sentinels
    /** Constructor that creates an empty list; O(1) time */
    public NodePositionList() {
        numElts = 0;
        header = new DNode<E>(null, null, null); // create header
        trailer = new DNode<E>(header, null, null); // create trailer
        header.setNext(trailer); // make header and trailer point to each other
    }
}
```

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## Java Implementation of the Node List ADT (2/7)

```
/** Checks if position is valid for this list and converts it to DNode if it is valid;
    O(1) time */
protected DNode<E> checkPosition(Position<E> p)
    throws InvalidPositionException {
    if (p == null) throw new InvalidPositionException("Null position passed
    to NodeList");
    if (p == header) throw new InvalidPositionException("The header node
    is not a valid position");
    if (p == trailer) throw new InvalidPositionException("The trailer node is
    not a valid position");
    try {
        DNode<E> temp = (DNode<E>) p;
        if ((temp.getPrev() == null) || (temp.getNext() == null))
            throw new InvalidPositionException
                ("Position does not belong to a valid NodeList");
        return temp;
    } catch (ClassCastException e) {
        throw new InvalidPositionException("Position is of wrong type
        for this list");
    }
}
```

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## Java Implementation of the Node List ADT (3/7)

```
/** Returns the number of elements in the list; O(1) time */
public int size() { return numElts; }

/** Returns whether the list is empty; O(1) time */
public boolean isEmpty() { return (numElts == 0); }

/** Returns the first position in the list; O(1) time */
public Position<E> first() throws EmptyListException {
    if (isEmpty()) throw new EmptyListException("List is empty");
    return header.getNext();
}
```

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## Java Implementation of the Node List ADT (4/7)

```
/** Returns the position before the given one; O(1) time */
public Position<E> prev(Position<E> p) throws InvalidPositionException,
    BoundaryViolationException {
    DNode<E> v = checkPosition(p);
    DNode<E> prev = v.getPrev();
    if (prev == header) throw new BoundaryViolationException("Cannot
    advance past the beginning of the list");
    return prev;
}

/** Insert the given element before the given position, returning the new
    position; O(1) time */
public void addBefore(Position<E> p, E element) throws
    InvalidPositionException {
    DNode<E> v = checkPosition(p);
    numElts++;
    DNode<E> newNode = new DNode<E>(v.getPrev(), v, element);
    v.getPrev().setNext(newNode);
    v.setPrev(newNode);
}
```

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## Java Implementation of the Node List ADT (5/7)

```
/** Insert the given element at the beginning of the list, returning the new
    position; O(1) time */
public void addFirst(E element) {
    numElts++;
    DNode<E> newNode = new DNode<E>(header, header.getNext(),
    element);
    header.getNext().setPrev(newNode);
    header.setNext(newNode);
}
```

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## Java Implementation of the Node List ADT (6/7)

```
/** Remove the given position from the list; O(1) time */
public E remove(Position<E> p) throws InvalidPositionException
{
    DNode<E> v = checkPosition(p);
    numElts--;
    DNode<E> vPrev = v.getPrev();
    DNode<E> vNext = v.getNext();
    vPrev.setNext(vNext);
    vNext.setPrev(vPrev);
    E vElem = v.element();
    // unlink the position from the list and make it invalid
    v.setNext(null);
    v.setPrev(null);
    return vElem;
}
```

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## Java Implementation of the Node List ADT (7/7)

*/\*\* Replace the element at the given position with the new element and return the old element;  $O(1)$  time \*/*

```
public E set(Position<E> p, E element) throws InvalidPositionException
{
    DNode<E> v = checkPosition(p);
    E oldElt = v.element();
    v.setElement(element);
    return oldElt;
}
```

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## Performance

- In the implementation of the List ADT by means of a doubly linked list
  - The space used by a list with  $n$  elements is  $O(n)$ .
  - The space used by each position of the list is  $O(1)$ .
  - All the operations of the List ADT run in  $O(1)$  time.
  - Operation `element()` of the Position ADT runs in  $O(1)$  time.

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## Iterators

- An iterator provides a way to access the elements of an aggregate object sequentially without exposing its underlying representation.
- Extends the concept of Position by adding a traversal capability.
- An iterator consists of a sequence  $S$ , a current element in  $S$ , and a way of stepping to the next element in  $S$  and making it the current element.
- Methods of the Iterator ADT:
  - boolean `hasNext()`: Test whether there are elements left in the iterator.
  - object `next()`: Return the next element in the iterator.

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## Simple Iterators in JAVA (1/2)

```
public interface PositionList<E> extends Iterable<E>
{
    // ...all the other methods of the list ADT ...
    /** Returns an iterator of all the elements in the list. */
    public Iterator<E> iterator();
}
```

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## Simple Iterators in JAVA (2/2)

```
/** Returns a textual representation of a given node list */
public static<E> String toString(PositionList<E> l)
{
    Iterator<E> it = l.iterator();
    String s = "[";
    while (it.hasNext())
    {
        s += it.next(); // implicit cast of the next element to String
        if (it.hasNext())
            s += ", ";
    }
    s += "]";
    return s;
}
```

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## Implementing Iterators

- Two notions of iterator:
  - snapshot: freezes the contents of the data structure at a given time
  - dynamic: follows changes to the data structure

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## Snapshot

- This approach makes a “snapshot” of a collection of elements and iterates over it.
- It would involve storing the collection in a separate data structure that supports sequential access to its elements.
- Uses a cursor to keep track of the current position of the iterator.
- Creating a new iterator involves creating an iterator object that represents a cursor placed just before the first element of the collection, taking  $O(1)$  time.
- `next()` returns the next element, if any, and moves the cursor just past this element's position.

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## Dynamic (1/3)

- This approach iterates over the data structure directly.
- No separate copy of the data structure is needed.

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## Dynamic (2/3)

```
public class ElementIterator<E> implements Iterator<E>
{
    protected PositionList<E> list; // the underlying list
    protected Position<E> cursor; // the next position
    /** Creates an element iterator over the given list. */
    public ElementIterator(PositionList<E> L) {
        list = L; cursor = (list.isEmpty())? null : list.first();
    }
    public boolean hasNext() { return (cursor != null); }
    public E next() throws NoSuchElementException {
        if (cursor == null) throw new NoSuchElementException("No next
        element");
        E toReturn = cursor.element();
        cursor = (cursor == list.last())? null : list.next(cursor);
        return toReturn;
    }
}
```

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## Dynamic (3/3)

```
/** Returns an iterator of all the elements in the list. */
public Iterator<E> iterator() { return new ElementIterator<E>(this); }
```

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## References

1. Chapter 6, Data Structures and Algorithms by Goodrich and Tamassia.

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