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```
clear; close all; clc;
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problem1()
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problem2()
```

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problem3()
```

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problem4()
```

## Functions

```
function problem1()
    fprintf("\nProblem 1:\n")
    A = [-1.10188, 0.90528, -.00212;
         4.0639, -.77013, -.169190;
         0, 0, 10];
    B = [0, 0;
         0, 1;
         10, 0];
    C = eye(3);

    lam1 = -2+2i;
    lam2 = conj(lam1);
    lam3 = -15;
    des_poles = [lam1, lam2, lam3];

    vec1 = [0.20 - .35i, -.98 - .07i, 0]';
    vec2 = conj(vec1);
    vec3 = [0; 0; 1];
    des_vec = [vec1, vec2, vec3];

    EigStructAssign(A, B, C, des_poles, des_vec);
end
```

```
function problem2()
    fprintf("\nProblem 2:\n")
    A = [-1.10188, 0.90528, -.00212;
         4.0639, -.77013, -.169190;
         0, 0, 10];
    B = [0, 0;
         0, 1;
         10, 0];
    C = [1, 0, 0;
         0, 1, 0];

    lam1 = -2+2i;
    lam2 = conj(lam1);
    des_poles = [lam1, lam2];

    vec1 = [0.20 - .35i, -.98 - .07i]';
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    vec2 = conj(vec1);
    des_vec = [vec1, vec2];

    EigStructAssign(A, B, C, des_poles, des_vec);
    fprintf("The acuator pole is moved from -15 to 9.5 now that we are not
\n")
    fprintf("able to directly assign the actuator pole\n\n")
end

function problem3()
    fprintf("\nProblem 3:\n")
    A = [-1.10188, 0.90528, -.00212;
         4.0639, -.77013, -.169190;
         0, 0, 10];
    B = [0, 0, 10]';
    C = [1, 0, 0;
         0, 1, 0];

    lam1 = -2+2i;
    lam2 = conj(lam1);
    des_poles = [lam1, lam2];

    vec1 = [0.20 - .35i, -.98 - .07i]';
    vec2 = conj(vec1);
    des_vec = [vec1, vec2];

    EigStructAssign(A, B, C, des_poles, des_vec);
    fprintf("The actuator pole has moved increasingly positive to 12.15\n\n")
end

function problem4()
    fprintf("\nProblem 4:\n")
    A = [0, 1;
         -2, -3];
    poles = eig(A);
    fprintf("Open Loop Poles are \\\lamda = \n")
    disp(poles)
    fprintf("The poles are negative so the open loop system is stable\n")
    B = [0; 2];
    Ackermann(A, B);
end

function K = Ackermann(A, B)
    n = length(A);

    syms s
    fdes_s = collect((s+3)*(s+5));
    coef = sym2poly(fdes_s);
    fdes_A = coef(1).*A*A + coef(2).*A + coef(3).*eye(n);

    Con = [];
    for ii = 1:n
        Con = [Con, A^(ii-1)*B];
    end
end

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    leftv = [zeros(1,n-1), 1];
    K = leftv*inv(Con)*fdes_A;
    fprintf("Control Gains are K = \n")
    disp(K)
end

function K = EigStructAssign(A, B, C, des_lambda, des_vec)
    poles = eig(A);
    fprintf("Open Loop Poles are \\\lamda = \n")
    disp(poles)

    cont_matrix = [B, A*B, A^2*B];
    fprintf("Controllable since controllability matrix is rank %i and A is
rank %i\n\n", [rank(cont_matrix), rank(A)])

    n = length(A);
    m = size(B,2);
    p = length(des_lambda);

    I = eye(n);
    D = diag(ones(1,p));
    O = zeros(p,(n+m)-p);
    top = zeros(n,1);
    uv = @(lambda,vec) pinv([lambda.*I - A, B; D, O])*[top;vec];

    for ii = 1:p
        uvii = uv(des_lambda(ii), des_vec(:,ii));
        vd(:,ii) = uvii(1:n);
        ud(:,ii) = uvii(n+1:end);
    end
    K = ud*inv(C*vd);
    fprintf("Control Gains are K = \n")
    disp(K)
    poles = eig(A-B*K*C);
    fprintf("Closed Loop Poles are \\\lamda = \n")
    disp(poles)
    fprintf("Desired Eigen Vectors are v = \n")
    disp(des_vec)
    fprintf("Achievable Eigen Vectors are v = \n")
    disp(vd)
end

```

*Problem 1:*

*Open Loop Poles are \lamda =*  
*-2.8612*  
*0.9892*  
*10.0000*

*Controllable since controllability matrix is rank 3 and A is rank 3*

*Control Gains are K =*

*0.0000 - 0.0000i    0.0000 + 0.0000i    2.5000 + 0.0000i*

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$9.3880 + 0.0000i \quad 2.1373 + 0.0000i \quad -0.1699 - 0.0000i$

Closed Loop Poles are  $\lambda =$

$-2.0047 + 2.0012i$   
 $-2.0047 - 2.0012i$   
 $-15.0000 - 0.0000i$

Desired Eigen Vectors are  $v =$

$0.2000 + 0.3500i \quad 0.2000 - 0.3500i \quad 0.0000 + 0.0000i$   
 $-0.9800 + 0.0700i \quad -0.9800 - 0.0700i \quad 0.0000 + 0.0000i$   
 $0.0000 + 0.0000i \quad 0.0000 + 0.0000i \quad 1.0000 + 0.0000i$

Achievable Eigen Vectors are  $v =$

$0.1943 + 0.3553i \quad 0.1943 - 0.3553i \quad 0.0002 + 0.0000i$   
 $-0.9790 + 0.0730i \quad -0.9790 - 0.0730i \quad 0.0000 + 0.0000i$   
 $-0.0000 - 0.0000i \quad -0.0000 + 0.0000i \quad 1.0000 + 0.0000i$

Problem 2:

Open Loop Poles are  $\lambda =$

$-2.8612$   
 $0.9892$   
 $10.0000$

Controllable since controllability matrix is rank 3 and A is rank 3

Control Gains are  $K =$

$-33.9273 - 0.0000i \quad -0.4173 + 0.0000i$   
 $14.4728 + 0.0000i \quad 2.5964 - 0.0000i$

Closed Loop Poles are  $\lambda =$

$9.5316 + 0.0000i$   
 $-2.0000 - 2.0000i$   
 $-2.0000 + 2.0000i$

Desired Eigen Vectors are  $v =$

$0.2000 + 0.3500i \quad 0.2000 - 0.3500i$   
 $-0.9800 + 0.0700i \quad -0.9800 - 0.0700i$

Achievable Eigen Vectors are  $v =$

$0.2000 + 0.3500i \quad 0.2000 - 0.3500i$   
 $-0.9800 + 0.0700i \quad -0.9800 - 0.0700i$   
 $-3.5615 - 10.5134i \quad -3.5615 + 10.5134i$

The actuator pole is moved from  $-15$  to  $9.5$  now that we are not able to directly assign the actuator pole

Problem 3:

Open Loop Poles are  $\lambda =$

$-2.8612$   
 $0.9892$   
 $10.0000$

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Controllable since controllability matrix is rank 3 and A is rank 3

Control Gains are  $K =$

$$68.0400 + 0.0000i \quad 10.5561 + 0.0000i$$

Closed Loop Poles are  $\lambda =$

$$12.1511 + 0.0000i$$

$$-2.0116 + 1.9966i$$

$$-2.0116 - 1.9966i$$

Desired Eigen Vectors are  $v =$

$$0.2000 + 0.3500i \quad 0.2000 - 0.3500i$$

$$-0.9800 + 0.0700i \quad -0.9800 - 0.0700i$$

Achievable Eigen Vectors are  $v =$

$$0.1804 + 0.3599i \quad 0.1804 - 0.3599i$$

$$-0.9791 + 0.0790i \quad -0.9791 - 0.0790i$$

$$-1.8516 + 20.7926i \quad -1.8516 - 20.7926i$$

The actuator pole has moved increasingly positive to 12.15

Problem 4:

Open Loop Poles are  $\lambda =$

$$-1$$

$$-2$$

The poles are negative so the open loop system is stable

Control Gains are  $K =$

$$6.5000 \quad 2.5000$$

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