

1. Maximum Speedup—Parallel Program Example

Given:

- Problem size: $n = 10,000$
- Sequential I/O time: $18000 + n = 28,000 \mu\text{sec}$
- Parallelizable computation: $n^2 / 100 = 10,000^2 / 100 = 1,000,000 \mu\text{sec}$
- Step 1: Maximum speedup without communication overhead

Maximum speedup formula: $\text{Speedup} = \text{Total sequential + parallel time} / \text{Sequential part} + \text{Parallel part} / p$

- Sequential part (T_s) = $28,000 \mu\text{sec}$
 - Parallel part (T_p) = $1,000,000 \mu\text{sec}$
 - For ideal infinite processors, parallel part $\rightarrow 0$
 - Maximum speedup = $(T_s + T_p) / T_s = (28,000 + 1,000,000) / 28,000 \approx 36.7$
- Step 2: Include parallel communication overhead
 - Number of communication points: $\lceil \log n \rceil = \lceil \log 10,000 \rceil \approx 14$
 - Communication time at each point: $n \lceil \log p \rceil + n/10 \mu\text{sec}$
 - Assume very large p , $\lceil \log p \rceil$ grows slowly; just include $n/10$ as main term
 - Total overhead $\approx 14 \times (10,000 / 10) = 14 \times 1,000 = 14,000 \mu\text{sec}$
 - New sequential equivalent = $28,000 + 14,000 = 42,000 \mu\text{sec}$

Maximum speedup with overhead: $\text{Speedup} = (28,000 + 1,000,000) / 42,000 \approx 24.8$

2. Parallel Code Segment Outcomes

All possible final values (x , y):

x	y
3	5
4	2
4	3
4	5
4	6
6	8

3. Maximum Achievable Speedup for 8% Sequential Computation

- Fraction sequential, $f = 0.08$
- Fraction parallel, $1 - f = 0.92$

(a) Amdahl's Law (for very large $p \rightarrow \infty$):

$$\text{Maximum speedup} = 1 / f = 1 / 0.08 = 12.5$$

(b) Gustafson-Barsis Law (scales with problem size):

Speedup = $f + (1 - f) \times p$ = For very large p , speedup scales almost linearly with p

- Maximum speedup grows, essentially unbounded in theory

(c) When to prefer Amdahl vs Gustafson-Barsis:

- Use Amdahl: When problem size is fixed, and you want to know the maximum speedup possible by parallelization.
- Use Gustafson-Barsis: When problem size can increase with more processors, and you want to predict realistic scaling with larger workloads.