University of Illinois at Urbana-Champaign Dept. of Electrical and Computer Engineering

ECE 120: Introduction to Computing

Bit-Sliced Comparator

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How Do You Compare Unsigned Numbers?

Let's develop a bit-sliced design to compare two unsigned numbers.

Which 8-bit unsigned number is bigger?

 $0\ 1\ 1\ 0\ 1\ 0\ 0$ 0 $0\ 1\ 0\ 1\ 0\ 1\ 1$

How did you know? Did you start on the left or the right?

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Humans Go from Left to Right

Usually, humans start on the left. Why? As soon as we notice a difference, we're done!

humans compare this way

0 1 1 $a_4 a_3 a_2 a_1 a_0$ 0 1 0 $b_4 b_3 b_2 b_1 b_0$

Bit-sliced hardware cannot stop in the middle.

The information flows from one end to the other.

Output wires produce the answer (in bits).

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slide 3

Our Design Compares from Right to Left

Our comparator design will start on the right.

humans compare this way

 $a_7 a_6 a_5 a_4 a_3 a_2 a_1 a_0$ $b_7 b_6 b_5 b_4 b_3 b_2 b_1 b_0$

our design will compare this way

From least significant to most significant bit.

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slide 4

Three Possible Answers for Comparison of A and B

When comparing two numbers, A and B, we have three possible outcomes:

A < B

A = B

A > B

To decide the answer for **N+1** bits, we need:

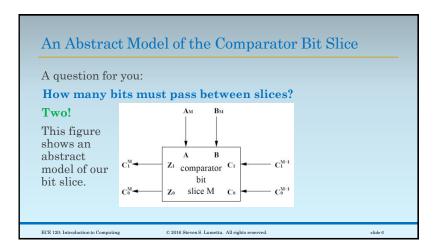
- the answer for N (less significant) bits,
- one bit of A, and
- one bit of B.

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slide 5

slide 7



We Need a Representation for Answers

Another question for you:

How do we represent the three possible answers?

Any way we want!

Our choice of representation will affect the amount of logic we need.

Here's a good one...

 $egin{array}{c|ccc} C_1 & C_0 & \text{meaning} \\ \hline 0 & 0 & A = B \\ 0 & 1 & A < B \\ \hline \end{array}$

1 0 A > B1 1 not used

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A Single Bit Requires Two Minterms on A, B

Let's start by solving a single bit.

In this case, there are no less significant bits.

So we consider only **A** and **B**.

Fill in the meanings, then the bits.

Note that \mathbf{Z}_1 and \mathbf{Z}_0 are minterms.

1 0 1 0 A > B 1 1 0 0 A = B

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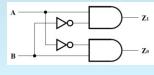
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slide 8

Comparing Two Bits is Fairly Easy

An implementation for a single bit appears below.

This structure forms the core of our bit slice, since it compares one bit of A with one bit of B.



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When A and B are Equal, Pass Along the Answer

Now for the full problem.

We'll start with the case of A = 0 and B = 0.

				meaning			
0	0	0	0	A = B A < B	0	0	A = B
0	0	0	1	A < B	0	1	A < B
0	0	1	0	A > B	1	0	A > B
0	0	1	1	???	x	x	don't care

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When A and B are Equal, Pass Along the Answer

Is there any difference when A = 1 and B = 1?

No, outputs are the same as the last case.

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When A and B Differ, Override the Previous Answer

What about case of A = 0 and B = 1?

Always output A < B (for valid inputs).

A	1	В	$\mathbf{C_1}$	$\mathbf{C_0}$	meaning	\mathbf{Z}_1	\mathbf{Z}_0	meaning
()	1	0	0	A = B	0	1	A < B
()	1	0	1	A < B	0	1	A < B
()	1	1	0	A > B	0	1	A < B
()	1	1	1	???	x	x	don't care

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slide 11

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slide 12

When A and B Differ, Override the Previous Answer And the case of A = 1 and B = 0? Always output A > B (for valid inputs). A B C_1 C_0 Meaning Z_1 Z_0 meaning 1 0 0 0 A = B 1 0 A > B 1001 A < B 1 0 A > B A > B 1 0 A > B 1011 x x don't care ECE 120: Introduction to Computing © 2016 Steven S. Lumetta. All rights reserved

