University of Illinois at Urbana-Champaign Dept. of Electrical and Computer Engineering

ECE 120: Introduction to Computing

Multiplexers (MUXes)

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Task: Checking for a Lower-Case Letter

What if we also need logic to check whether an ASCII character is a lower-case letter.

In **ASCII**, 'a' is **1100001** (0x61), and 'z' is **1111010** (0x7A).

Recall that 'A' is **1000001** (0x41), and 'Z' is **1011010** (0x5A).

Can we reuse our solutions for upper-case letters?

Of course we can!

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Change C₅' to C₅ to Obtain L(C) from U(C)

Let's again say that the ASCII character is in $C = C_6C_5C_4C_3C_2C_1C_0$.

By breaking up the truth table, we obtained

$$\mathbf{U(C)} = \mathbf{C_6C_5'C_4'}(\mathbf{C_3} + \mathbf{C_2} + \mathbf{C_1} + \mathbf{C_0}) + \mathbf{C_6C_5'C_4}(\mathbf{C_3'} + \mathbf{C_2'})(\mathbf{C_3'} + \mathbf{C_1'} + \mathbf{C_0'})$$

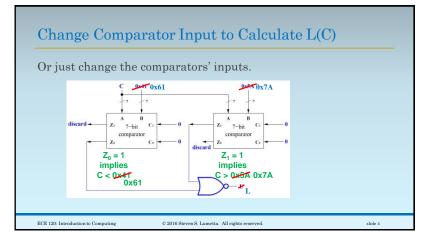
But lower-case characters are only different from upper-case in C_5 , which is 1 instead of 0.

$$L(C) = C_6 \frac{C_5}{C_5} C_4' (C_3 + C_2 + C_1 + C_0) + C_6 \frac{C_5}{C_4} C_4' (C_3' + C_2') (C_3' + C_1' + C_0')$$

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Want Logic to Choose Between Two Signals

What if we want one design to check for either upper-case or lower-case letters?

In a few examples,

- we added a control signal S
- to select between functions.

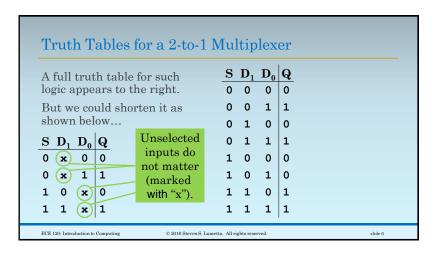
Can we design logic

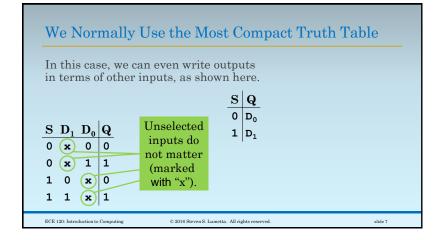
- that uses a control signal S to select
- between two arbitrary signals,
- D_1 (when S = 1) and D_0 (when S = 0)?

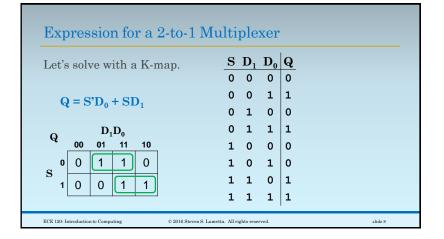
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Expression for a 2-to-1 Multiplexer

But \mathbf{Q} just selects $\mathbf{D_0}$ or $\mathbf{D_1}$ (as desired)!

$$\mathbf{Q} = \mathbf{S'D_0} + \mathbf{SD_1}$$

 $\begin{array}{c|c}
\mathbf{S} & \mathbf{Q} \\
\hline
\mathbf{0} & \mathbf{D_0}
\end{array}$

Could we have just written this expression using the table to the right?

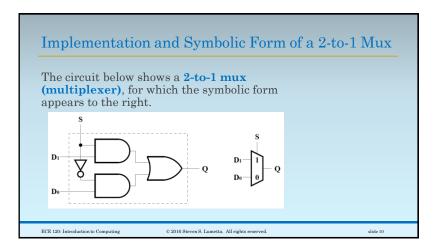
1 | D

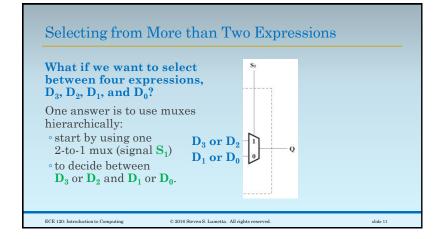
 \mathbf{Q} is \mathbf{D}_0 when $\mathbf{S} = \mathbf{0}$, and \mathbf{D}_1 when $\mathbf{S} = \mathbf{1}$...

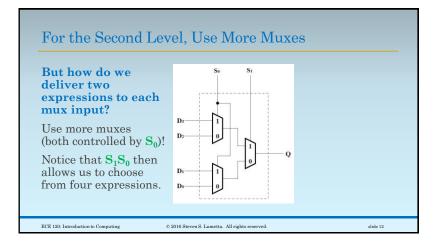
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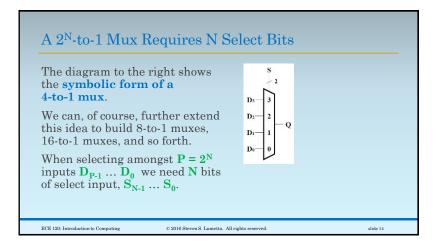
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AND Gates Represent Minterms ANDed with Data Inputs For something as common as a mux, we typically build directly from gates. Notice that each AND gate produces a minterm of S_1 , S_0 ANDed with the corresponding D_i . ECE 120. Introduction to Computing C 2016 Seven S. Lametta. All rights reserved.



Can Use Sets of Muxes to Select Amongst Groups of Bits

We can also generalize the idea of multiplexers by

- using a common control signal
- ${}^{\circ}\, to$ select between groups of inputs.

Generally,

- \circ an N-to-M multiplexer
- represents M separate (N/M)-to-1 muxes
- each with log₂(N/M) select bit inputs
- (typically $N/M = 2^K$ for some integer K).

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Example of a Set of Muxes with Common Select Input

For example, recall the design of the **N-bit** adder and subtractor.

We could have used a 2N-to-N mux

- to choose between **B**_i and **B**_i' for the adder's **B** input
- based on a common (one-bit) control signal **S**.

(Previously, we used the nature of the mux' data inputs, $\boldsymbol{B_i}$ versus $\boldsymbol{B_i}$ ', to simplify each mux' logic to an XOR gate.)

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Another Design Problem: Checking Four Types of ASCII

Now think again about our ASCII checker.

Say that we want four kinds of comparison:

- control characters (0x00 to 0x1F),
- lower-case letters (0x41 to 0x5A),
- oupper-case letters (0x61 to 0x7A), and
- odigits (0x30 to 0x39).

How can we design logic to check for any of the four types?

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