University of Illinois at Urbana-Champaign Dept. of Electrical and Computer Engineering

ECE 120: Introduction to Computing

Building with Abstraction and a First Example

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Optimization at the Level of Gates is Always Possible

One can always solve a problem by

- · developing complete Boolean expressions,
- ° solving for "good" forms with K-maps (or algebra, with more variables),
- \circ implementing the resulting equations,
- tuning logic to reduce gate sizes (number of inputs) and fanout (the number of gates using a single gate's output).

You can now perform such a process.

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But Optimization at Gate Level is Rarely Needed

Such detail is rarely needed for a satisfactory solution.

Instead, humans can

- use abstraction and build with components such as adders and comparators, or
- use extra levels of logic to describe functions more intuitively.

Computer-aided design (CAD) tools

- o can help with low-level optimizations.
- In many cases, CAD tools can do better than humans because they explore more options.

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Tradeoffs are Always Made in Some Context

Context is important!

If a mechanical engineer produces a 0.5% boost in efficiency for internal combustion engines sized for automobiles, that engineer will probably win a major prize.

In our field, engineers spend a lot of time

- improving the designs of arithmetic units and memory, and
- \circ improving CAD tools' ability to optimize.

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But Optimization at Gate Level is Rarely Needed

"Premature optimization is the root of all evil."
- Sir C.A.R. "Tony" Hoare

Don't spend time optimizing

- o something that is likely to change, nor
- something that does not contribute much to the overall system goodness (any metric).

The flip side:

- don't ignore scaling issues when choosing algorithms, and
- don't design in a way that prohibits/inhibits optimization.

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First Example: Subtraction

Let's start with something simple.

Let's build a subtractor.

How do we subtract as humans?

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Example: Subtraction of 5-Digit Numbers

Let's do an example with 5-digit numbers

12345 - 871

> Negate by finding the "9's complement" and adding 1.

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Example: Subtraction of 5-Digit Numbers

Let's do an example with **5-digit numbers**

We have no space for that digit! + 99129

Good, we got the right answer (12345 - 871 = 11474)!

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Use an Adder to Implement a Subtractor

Ok, maybe your elementary school taught subtraction a different way.

But you probably did use that approach in your ECE120 homework to subtract **unsigned** and **2's complement** values.

$$A - B = A + (NOT B) + 1$$

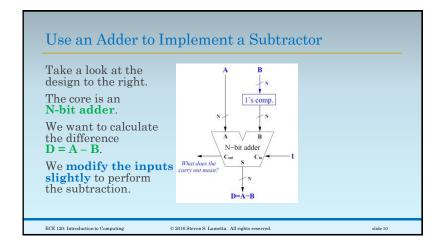
(where "NOT" applies to all bits of **B**)

Instead of mimicking the human subtraction process, let's use an adder to implement a subtractor...

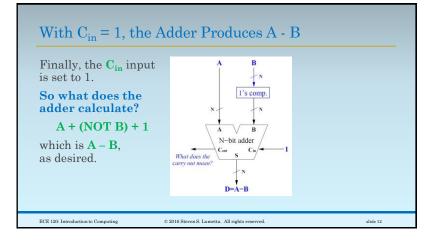
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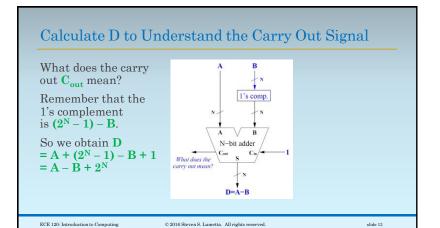
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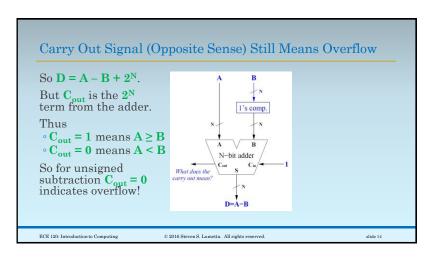
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Convert B to its 1's Complement The input **A** is unchanged. The input **B** is transformed to its 1's complement. How do we N-bit adder implement What does the 1's complement? carry out mean? N inverters! ECE 120: Introduction to Computing © 2016 Steven S. Lumetta. All rights reserved slide 11







Use a Control Signal to Select between Operations

What if we want a device that does both addition and subtraction?

We need a way to choose the operation.

Add a control signal S

 \circ **S** = **0**: addition

 \circ **S** = **1**: subtraction

And the modify the adder inputs with S

· A ... unmodified

• B ... B XOR S (bitwise)

 $\circ C_{in} \dots S$

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