

2.2

$$\begin{aligned}
 (x + y) \cdot (x + \bar{y}) &= xx + xy + x\bar{y} + y\bar{y} \\
 &= x + xy + x\bar{y} + 0 \\
 &= x(1 + y + \bar{y}) \\
 &= x \cdot 1 \\
 &= x
 \end{aligned}$$

2.10

$$\begin{aligned}
 f &= \bar{x}_1\bar{x}_2x_3 + \bar{x}_1x_2\bar{x}_3 + \bar{x}_1x_2x_3 + x_1\bar{x}_2\bar{x}_3 + x_1\bar{x}_2x_3 + x_1x_2\bar{x}_3 + x_1x_2x_3 \\
 &= x_1(\bar{x}_2\bar{x}_3 + \bar{x}_2x_3 + x_2\bar{x}_3 + x_2x_3) + x_2(\bar{x}_1\bar{x}_3 + \bar{x}_1x_3 + x_1\bar{x}_3 + x_1x_3) \\
 &\quad + x_3(\bar{x}_1\bar{x}_2 + \bar{x}_1x_2 + x_1\bar{x}_2 + x_1x_2) \\
 &= x_1(\bar{x}_2(\bar{x}_3 + x_3) + x_2(\bar{x}_3 + x_3)) + x_2(\bar{x}_1(\bar{x}_3 + x_3) + x_1(\bar{x}_3 + x_3)) \\
 &\quad + x_3(\bar{x}_1(\bar{x}_2 + x_2) + x_1(\bar{x}_2 + x_2)) \\
 &= x_1(\bar{x}_2 \cdot 1 + x_2 \cdot 1) + x_2(\bar{x}_1 \cdot 1 + x_1 \cdot 1) + x_3(\bar{x}_1 \cdot 1 + x_1 \cdot 1) \\
 &= x_1(\bar{x}_2 + x_2) + x_2(\bar{x}_1 + x_1) + x_3(\bar{x}_1 + x_1) \\
 &= x_1 \cdot 1 + x_2 \cdot 1 + x_3 \cdot 1 \\
 &= x_1 + x_2 + x_3
 \end{aligned}$$

2.13

$$\begin{aligned}
 f &= x_1\bar{x}_2\bar{x}_3 + x_1x_2x_4 + x_1\bar{x}_2x_3\bar{x}_4 \\
 &= x_1\bar{x}_2\bar{x}_3(\bar{x}_4 + x_4) + x_1x_2x_4 + x_1\bar{x}_2x_3\bar{x}_4 \\
 &= x_1\bar{x}_2\bar{x}_3\bar{x}_4 + x_1\bar{x}_2\bar{x}_3x_4 + x_1x_2x_4 + x_1\bar{x}_2x_3\bar{x}_4 \\
 &= x_1\bar{x}_2\bar{x}_3 + x_1\bar{x}_2(\bar{x}_3 + x_3)\bar{x}_4 + x_1x_2x_4 \\
 &= x_1\bar{x}_2\bar{x}_3 + x_1\bar{x}_2\bar{x}_4 + x_1x_2x_4
 \end{aligned}$$

2.24

$$\begin{aligned}
 f &= x_1\bar{x}_3\bar{x}_4 + x_2\bar{x}_3x_4 + x_1\bar{x}_2\bar{x}_3 \\
 &= x_1\bar{x}_3\bar{x}_4 + x_2\bar{x}_3x_4 + x_1x_2\bar{x}_3 + x_1\bar{x}_2\bar{x}_3 \\
 &= x_1\bar{x}_3\bar{x}_4 + x_2\bar{x}_3x_4 + x_1\bar{x}_3 \\
 &= x_2\bar{x}_3x_4 + x_1\bar{x}_3
 \end{aligned}$$

2.21

$$\begin{aligned}f &= \bar{x}_1\bar{x}_2x_3 + \bar{x}_1x_2x_3 + x_1\bar{x}_2\bar{x}_3 + x_1x_2\bar{x}_3 + x_1x_2x_3 \\&= \bar{x}_1(\bar{x}_2 + x_2)x_3 + x_1(\bar{x}_2 + x_2)\bar{x}_3 + (\bar{x}_1 + x_1)x_2x_3 \\&= \bar{x}_1x_3 + x_1\bar{x}_3 + x_2x_3\end{aligned}$$

$$f = \bar{x}_1x_3 + x_1\bar{x}_3 + x_1x_2$$

3.2

- (a) 478
(b) -280
(c) -1

3.3

- (a) 478
(b) -281
(c) -2

3.8 (给出一种证明方法提示, 详细步骤请自行补充)

证明

$$A = \begin{pmatrix} 0 & 1 & 1 & \cdots & 1 \\ 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & 0 \end{pmatrix}$$
$$B = \begin{pmatrix} B_{n-1} & B_{n-2} & \cdots & B_0 \end{pmatrix}$$
$$C = \{B_{n-1}, \dots, B_k\}$$
$$a+b-c \rightarrow \begin{cases} m_k = 1 \\ m_i = B_k \quad k < i < n \end{cases}$$

3.10

Since $s_k = x_k \oplus y_k \oplus c_k$, it follows that

$$\begin{aligned}x_k \oplus y_k \oplus s_k &= (x_k \oplus y_k) \oplus (x_k \oplus y_k \oplus c_k) \\&= (x_k \oplus y_k) \oplus (x_k \oplus y_k) \oplus c_k \\&= 0 \oplus c_k \\&= c_k\end{aligned}$$