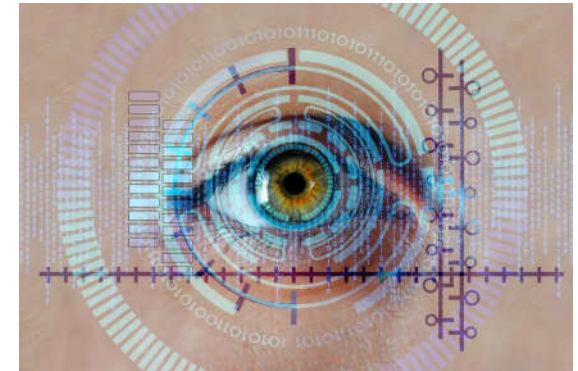




**北京理工大学**  
**BEIJING INSTITUTE OF TECHNOLOGY**

**Computer Vision**



# Lecture 9 Panorama

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# Outline

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- Quick review of keypoints and RANSAC
- Panorama formulation
- Matching corresponding keypoints
- Stitching images together with affine transformation

# Outline

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- Quick review of keypoints and RANSAC
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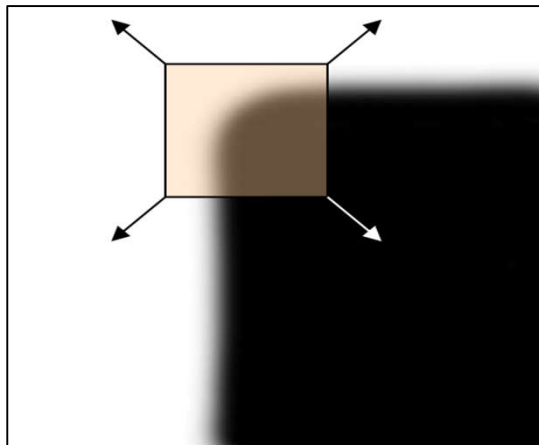
# What are keypoints?

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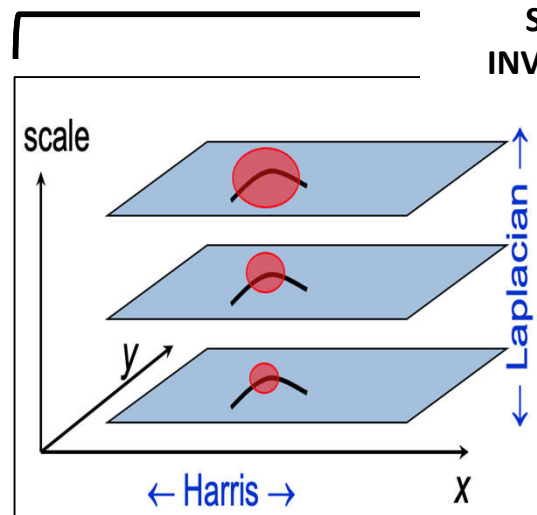
*Reliable, unique points in images which can be used to find corresponding regions in different images of the same scene*

# Finding keypoints



## Harris Corner Detector

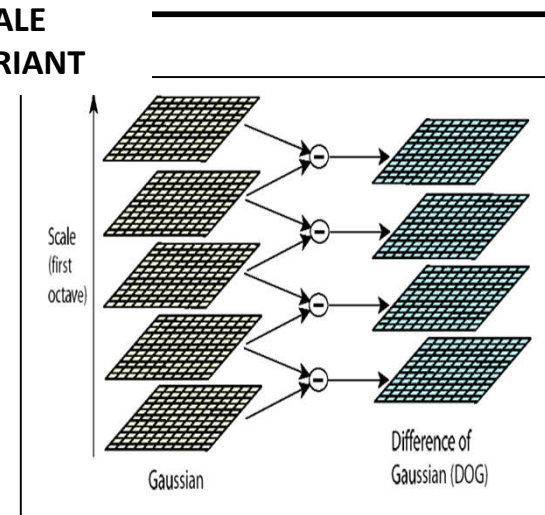
*Use gradient Eigenvalues to find corners at a certain scale*



## Harris-Laplacian

*Find keypoints using Harris and scale using Laplacian filter*

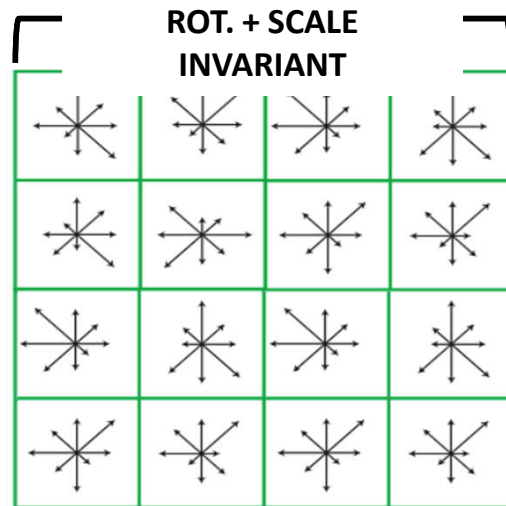
## SCALE INVARIANT



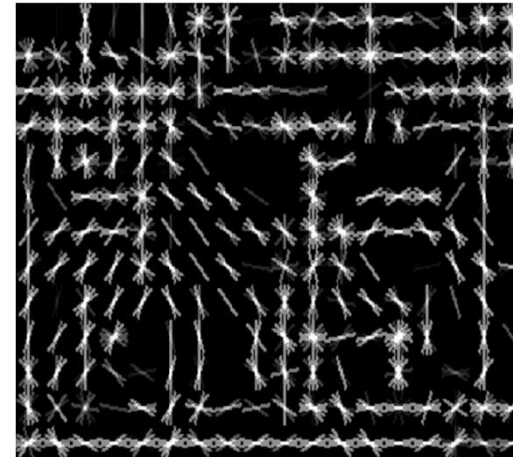
## DoG

*Use DoG filters to find keypoints across space and scale*

# Describing keypoints



**SIFT Descriptor**  
*Keypoints as histogram of  
normalize gradient orientation*



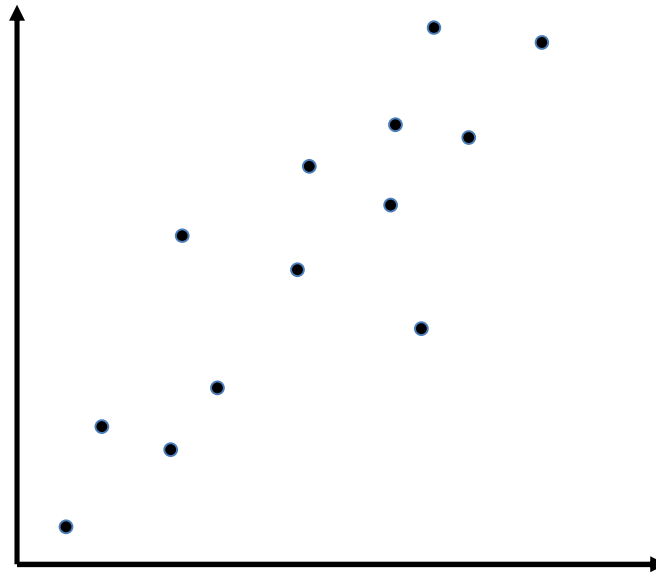
**HoG**  
*Region (or image) as histograms  
of local gradients*

# RANSAC – algorithm for model fitting

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- Repeat n times:
  - Sample and form hypothesis
  - Find number of inliers
  - If max\_inliers, save model
- Recompute model on inliers

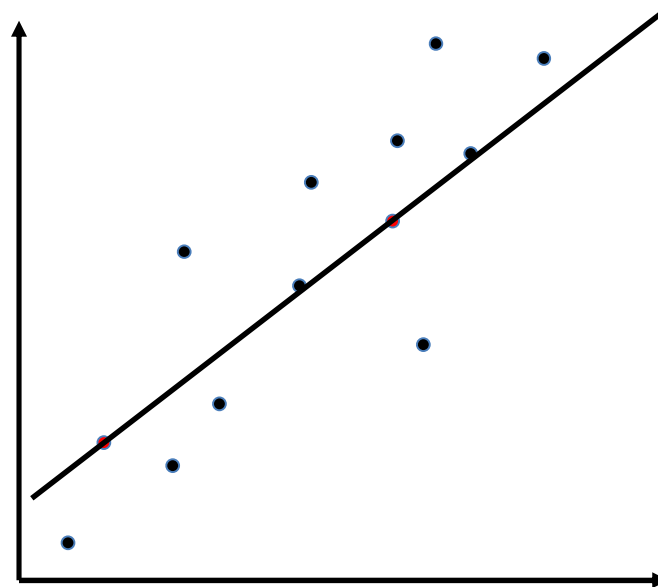


# RANSAC – algorithm for model fitting

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- Repeat n times:
  - **Sample and form hypothesis**
  - Find number of inliers
  - If max\_inliers, save model
- Recompute model on inliers



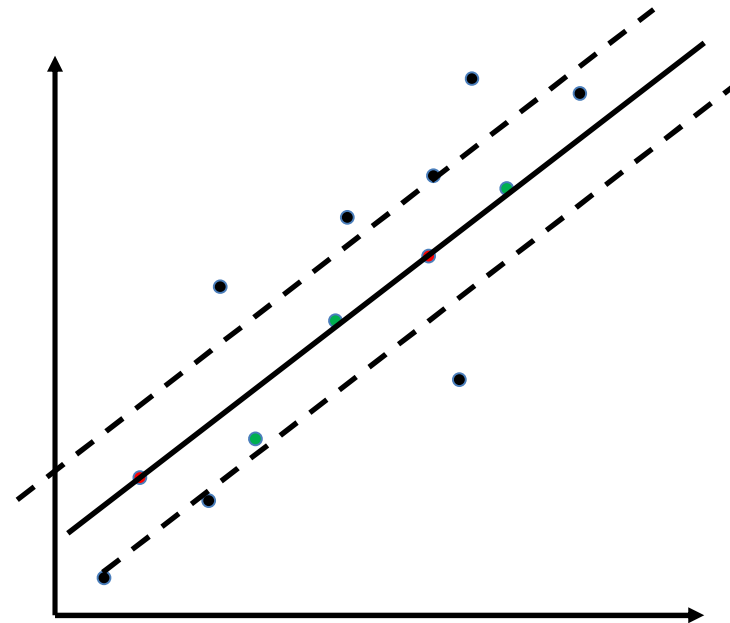


# RANSAC – algorithm for model fitting

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- Repeat n times:
  - Sample and form hypothesis
  - **Find number of inliers**
  - If max\_inliers, save model
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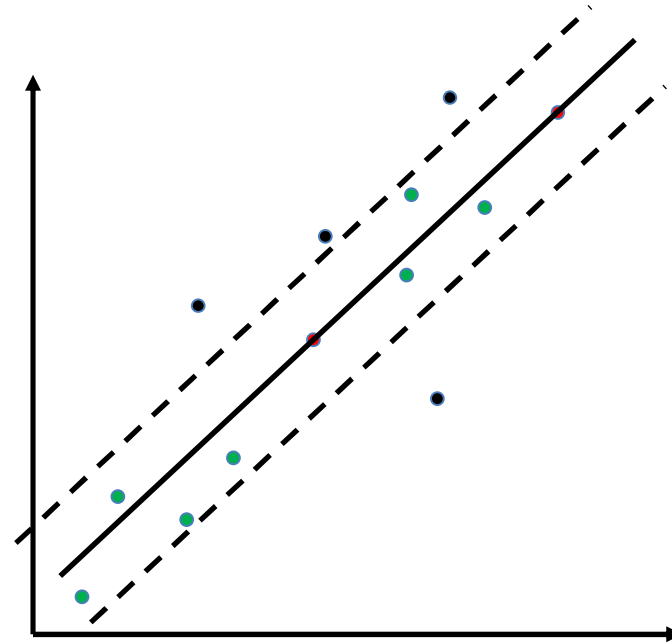


# RANSAC – algorithm for model fitting

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- Repeat n times:
  - Sample and form hypothesis
  - Find number of inliers
  - **If max\_inliers, save model**
- Recompute model on inliers

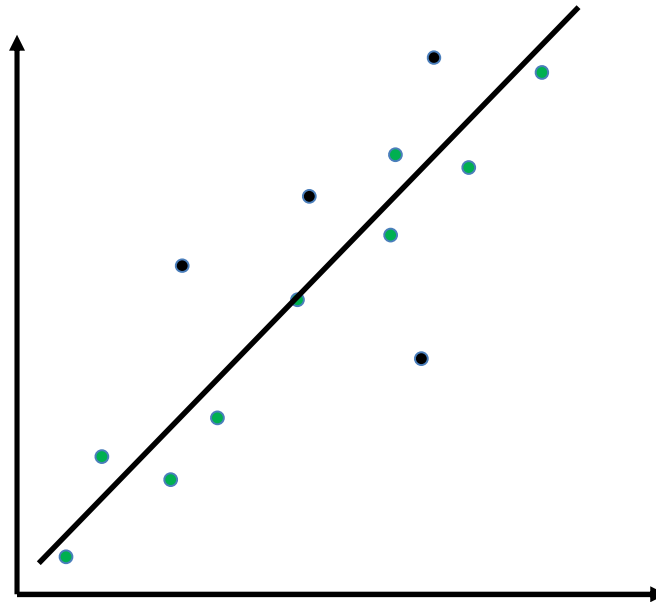


# RANSAC – algorithm for model fitting

---



- Repeat n times:
  - Sample and form hypothesis
  - Find number of inliers
  - If max\_inliers, save model
- **Recompute model on inliers**



# Outline

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- Quick review of keypoints and RANSAC
- **Panorama formulation**
- Matching corresponding keypoints
- Stitching images together with affine transformation

# Panorama

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# Panorama

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# Key insight: leverage corresponding keypoints



# Problem 1: how to match keypoints?

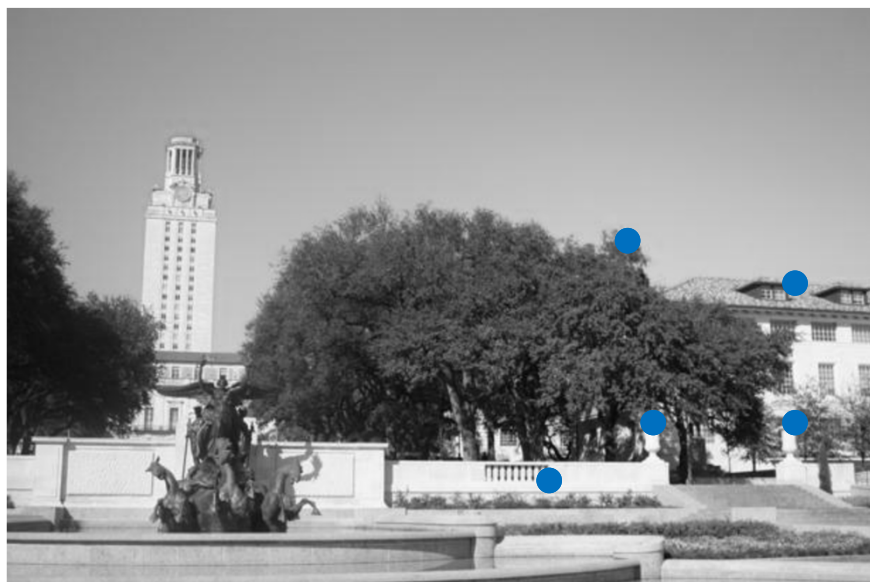
---





# Problem 2: how to fit images?

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# Outline

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- Quick review of keypoints and RANSAC
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# How to know if keypoints are “the same”?

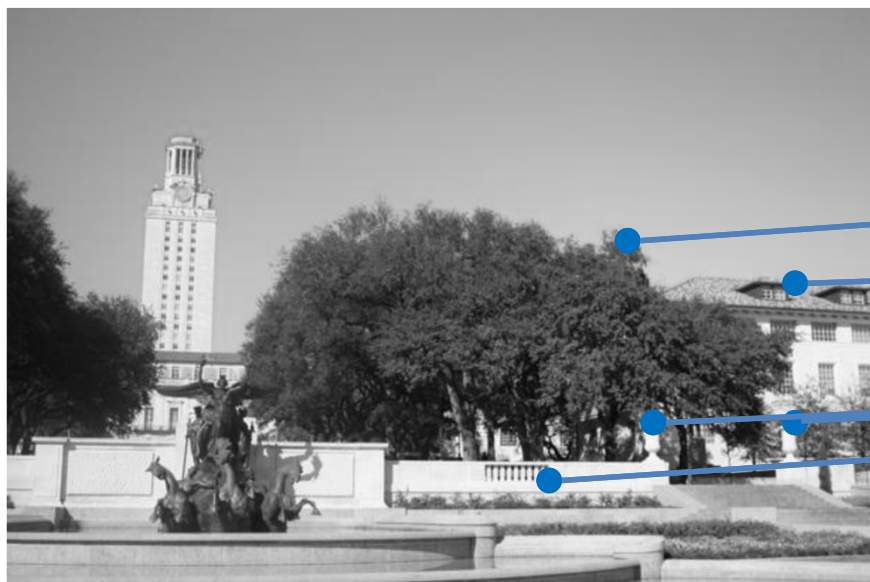
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*Use keypoint descriptors!*

# Matching result

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# Outline

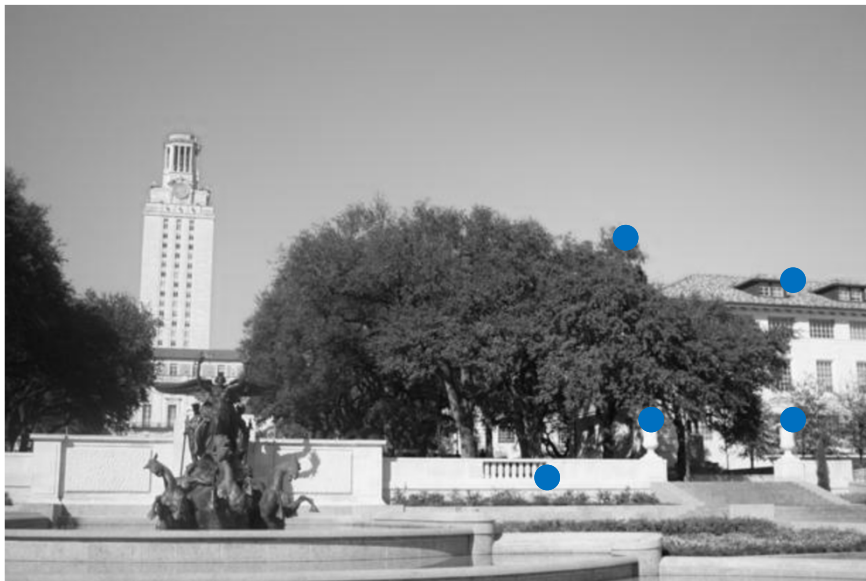
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- Quick review of keypoints and RANSAC
- Panorama formulation
- Matching corresponding keypoints
- **Stitching images together with affine transformation**

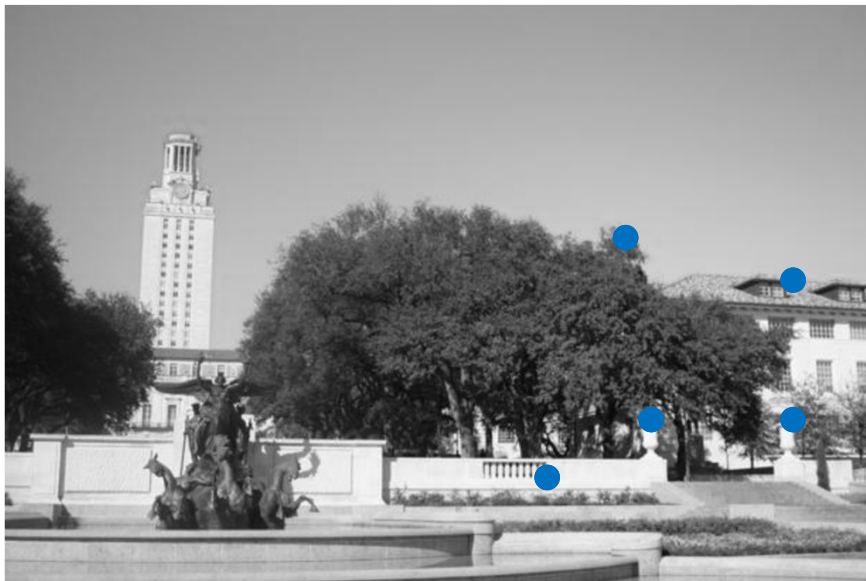
# Easy case: pictures taken from same angle

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# Hard case: pictures taken from diff angles

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# Find transformation between matches

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Given:

$p1$

$m_{1,x}^1$	$m_{1,y}^1$	1
$m_{1,x}^2$	$m_{1,y}^2$	1
$m_{1,x}^3$	$m_{1,y}^3$	1
$m_{1,x}^4$	$m_{1,y}^4$	1

$p2$

$m_{2,x}^1$	$m_{2,y}^1$	1
$m_{2,x}^2$	$m_{2,y}^2$	1
$m_{2,x}^3$	$m_{2,y}^3$	1
$m_{2,x}^4$	$m_{2,y}^4$	1

Find transformation matrix  $H$  such that:

$$p2 \cdot H = p1$$



# What if we have noisy matches?

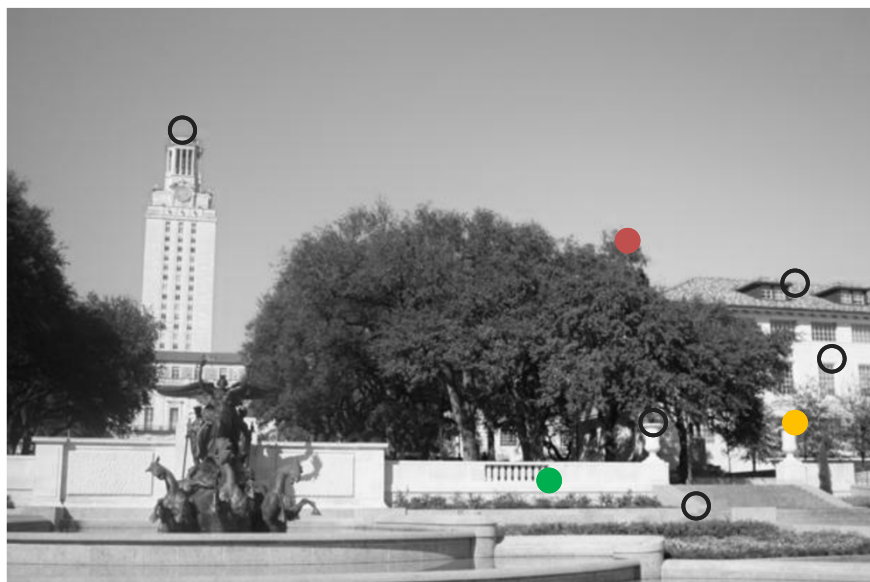
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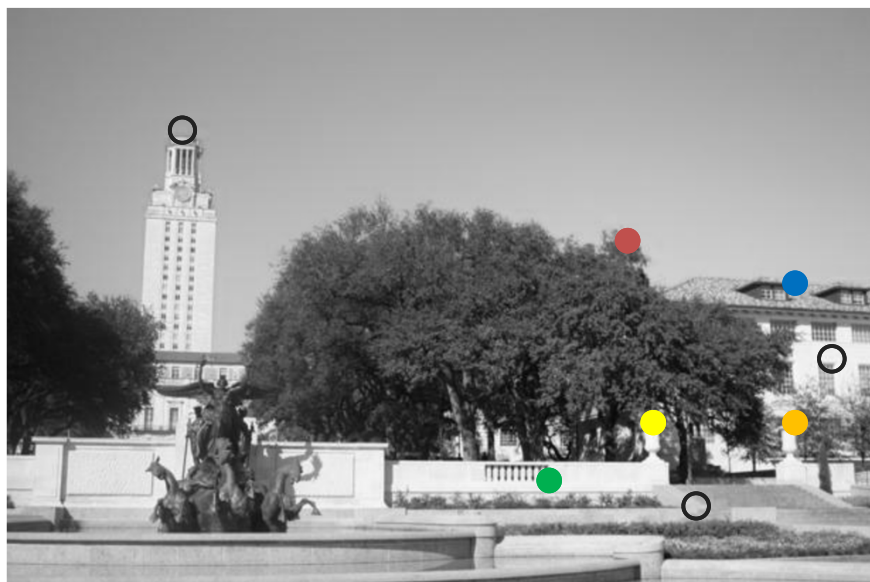
*Refine transformation matrix with RANSAC!*

# Pick subset

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# Fit affine matrix and find inliers



# Recompute matrix with all inliers and stitch!

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# Reading

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- Szeliski (2<sup>st</sup> edition): Chapter 8