

$$5. f^3(x) = (x_2 \oplus \bar{x}_3) \downarrow (x_1 \bar{x}_2)$$

$$= (\bar{x}_2 \bar{x}_3 \vee x_2 x_3) \downarrow (x_1 \bar{x}_2)$$

$$= \overline{(\bar{x}_2 \bar{x}_3 \vee x_2 x_3) \vee (x_1 \bar{x}_2)}$$

$$= \overline{\bar{x}_2 \bar{x}_3 \vee x_2 x_3} \cdot \overline{x_1 \bar{x}_2}$$

$$= [(x_2 \vee x_3)(\bar{x}_2 \vee \bar{x}_3)] (\bar{x}_1 \vee x_2)$$

$$= (x_2 \vee x_3)(\bar{x}_2 \vee \bar{x}_3)(\bar{x}_1 \vee x_2) \quad \text{[KHP]}$$

$$= (x_2 \bar{x}_3 \vee \bar{x}_2 x_3)(\bar{x}_1 \vee x_2)$$

$$= \bar{x}_1 x_2 \bar{x}_3 \vee \bar{x}_1 \bar{x}_2 x_3 \vee \bar{x}_2 x_2 \bar{x}_3 \quad \text{[DHP]}$$

omnem: $(x_2 \vee x_3)(\bar{x}_2 \vee \bar{x}_3)(\bar{x}_1 \vee x_2) \Rightarrow \text{KHP}$

$$\bar{x}_1 x_2 \bar{x}_3 \vee \bar{x}_1 \bar{x}_2 x_3 \vee x_2 x_3 \Rightarrow \text{DHP}$$

6

x_1
x_2
x_3