

Generation Of Quarks

$$\begin{array}{ccc}
 \begin{pmatrix} u \\ d \end{pmatrix} & \begin{pmatrix} c \\ s \end{pmatrix} & \begin{pmatrix} t \\ b \end{pmatrix} \begin{array}{l} \longrightarrow \\ \longrightarrow \end{array} \begin{array}{l} + \frac{2e}{3} \\ - \frac{1e}{3} \end{array} \\
 \text{(I)} & \text{(II)} & \text{(III)}
 \end{array}$$

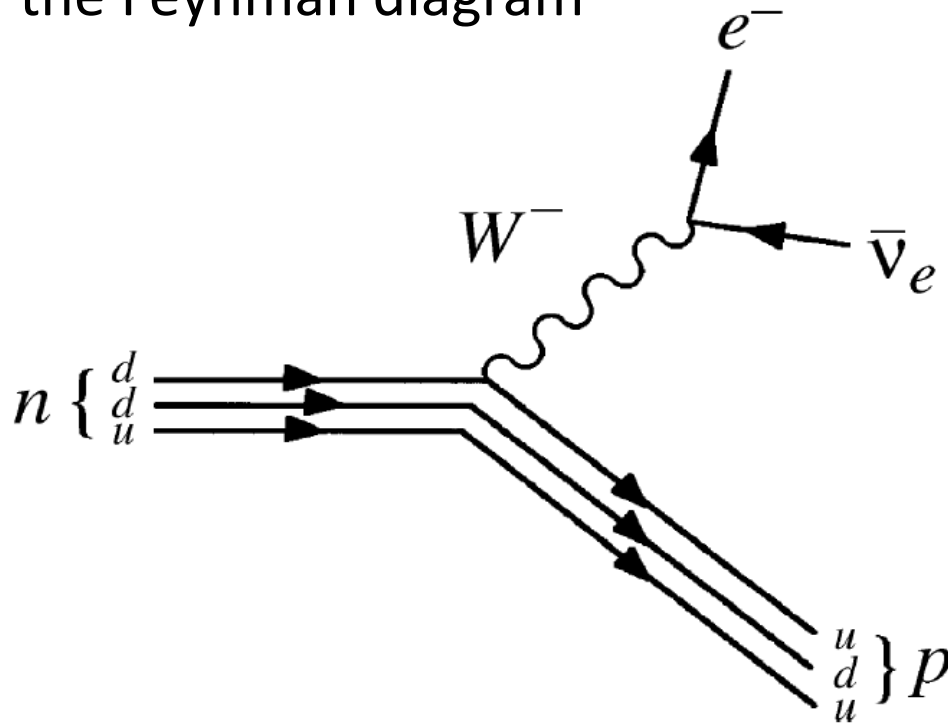
$$\begin{array}{ccc}
 \begin{pmatrix} \bar{d} \\ \bar{u} \end{pmatrix} & \begin{pmatrix} \bar{s} \\ \bar{c} \end{pmatrix} & \begin{pmatrix} \bar{b} \\ \bar{t} \end{pmatrix} \begin{array}{l} \longrightarrow \\ \longrightarrow \end{array} \begin{array}{l} + \frac{1e}{3} \\ - \frac{2e}{3} \end{array}
 \end{array}$$

Properties of Quarks: All have spin $\frac{1}{2}$

Name	Symbol	Mass	GeV/c ²	Q	Lifetime (s)	Major decays
Down	d	$m_d \approx 0.3$		$-1/3$		
Up	u	$m_u \approx m_d$		$2/3$		
Strange	s	$m_s \approx 0.5$		$-1/3$	10^{-8} – 10^{-10}	$s \rightarrow u + X$
Charmed	c	$m_c \approx 1.5$		$2/3$	10^{-12} – 10^{-13}	$c \rightarrow s + X$ $c \rightarrow d + X$
Bottom	b	$m_b \approx 4.5$		$-1/3$	10^{-12} – 10^{-13}	$b \rightarrow c + X$
Top	t	$m_t = 180 \pm 12$		$2/3$	$\sim 10^{-25}$	$t \rightarrow b + X$

X denotes other particle

- The decay of quarks always takes place within a hadron, with the other bound quarks acting as spectators i.e. not taking part in the interaction.
- It is assumed that the exchanged particle interacts with only one constituent quark in the nucleons. This is the essence of the spectator model. For example: Neutron decay at the quark level is shown by the Feynman diagram



Spectator model quark Feynman for the decay $n \rightarrow p + e^- + \bar{\nu}_e$

- In **strong and em – interactions**, quarks can be created or destroyed as particle – anti – particle pairs. For example,

$$e^+ + e^- \longrightarrow c + \bar{c} \quad \text{is allowed}$$

$$e^+ + e^- \longrightarrow c + \bar{u} \quad \text{is not allowed}$$

Moreover, it implies the conservation of each of the six quark numbers,

$$N_f = N(f) - N(\bar{f})$$

($f = u, d, s, c, b, t$)

Where $N(f)$ is the number of quarks of flavor f present and $N(\bar{f})$ is the number of antiquarks of flavor \bar{f} present.

For ex: for single – particle states; $N_c = 1$ for the c – quark;
 $N_c = -1$ for the c antiquark
and $N_c = 0$ for all other particles.

- In weak interactions, more general possibilities are allowed, and **only the total quark number is conserved**

$$N_q = N(q) - N(\bar{q})$$

Where $N(q)$ and $N(\bar{q})$ are the total no. of quarks and antiquarks **irrespective of their flavor**.

- For example, the main decay mode of the charmed quark,

$$c \rightarrow s + u + \bar{d}$$

Where conservation of individual quark numbers N_c , N_s , N_u and N_d are violated but the total quark number N_q is conserved.

- It is convenient to replace the quark number N_q by the Baryon Number B , defined by,

$$B = N_q/3 = [N(q) - N(\bar{q})]/3$$

Quark Model Spectroscopy

- In the quark model of hadrons the baryons are assumed to be bound states of three quarks (qqq), antibaryons are assumed to be bound states of three anti-quantities ($q'q'q'$) and mesons are assumed to be bound states of a quark and an antiquark ($q q'$).
- Mesons are a type of hadrons that have integral spin. Pions are the lightest known mesons with masses $\pi^+(140)$ and $\pi^0(135)$.

- Charged pions have unique composition while the neutral pion is composed of both uu' and dd' pairs in equal amounts. Pions are produced in high-energy collisions by strong interaction processes such as $p + p \rightarrow p + n + \pi$.
- Kaons are completely different mesons that have non zero values for strangeness quantum number. Strangeness is conserved in strong and electromagnetic interactions, but not necessarily conserved in weak interactions.
- The strangeness S , apart from a sign is the strangeness quark number, i.e. $S = -N_s$

- The lightest strange baryon is the lambda, with the quark composition $\Lambda = uds$.
- The charm and bottom quantum numbers are defined as

$$C = N_c = N(C) - N(C'), \quad B' = -N_b = -[N(b) - N(b')]$$
- We could construct all the mesons states of the form qq' , where q can be any of the six quark flavors. Each of these is labeled by its spin and its intrinsic parity P .
- The simplest states would have the spins of the quark and the antiquark antiparallel with no orbital angular momentum between them and so have spin parity $J^P = 0^-$.

- If we consider those states composed of just u, d, and s quarks there will be **nine such mesons** and they have a quantum number which may be identified with the mesons (K^0, K^+) , (\bar{K}^0, K^-) , (π^\pm, π^0) and two neutral particles, which are called η and η' .
- The supermultiplet is shown as a plot of Y , the hypercharge is defined as,

$$Y = B + S + C + B' + T$$

- The Simplest meson state is $J^P = 0^-$ (the spins of the quark and the antiquark antiparallel with no orbital angular momentum between them).

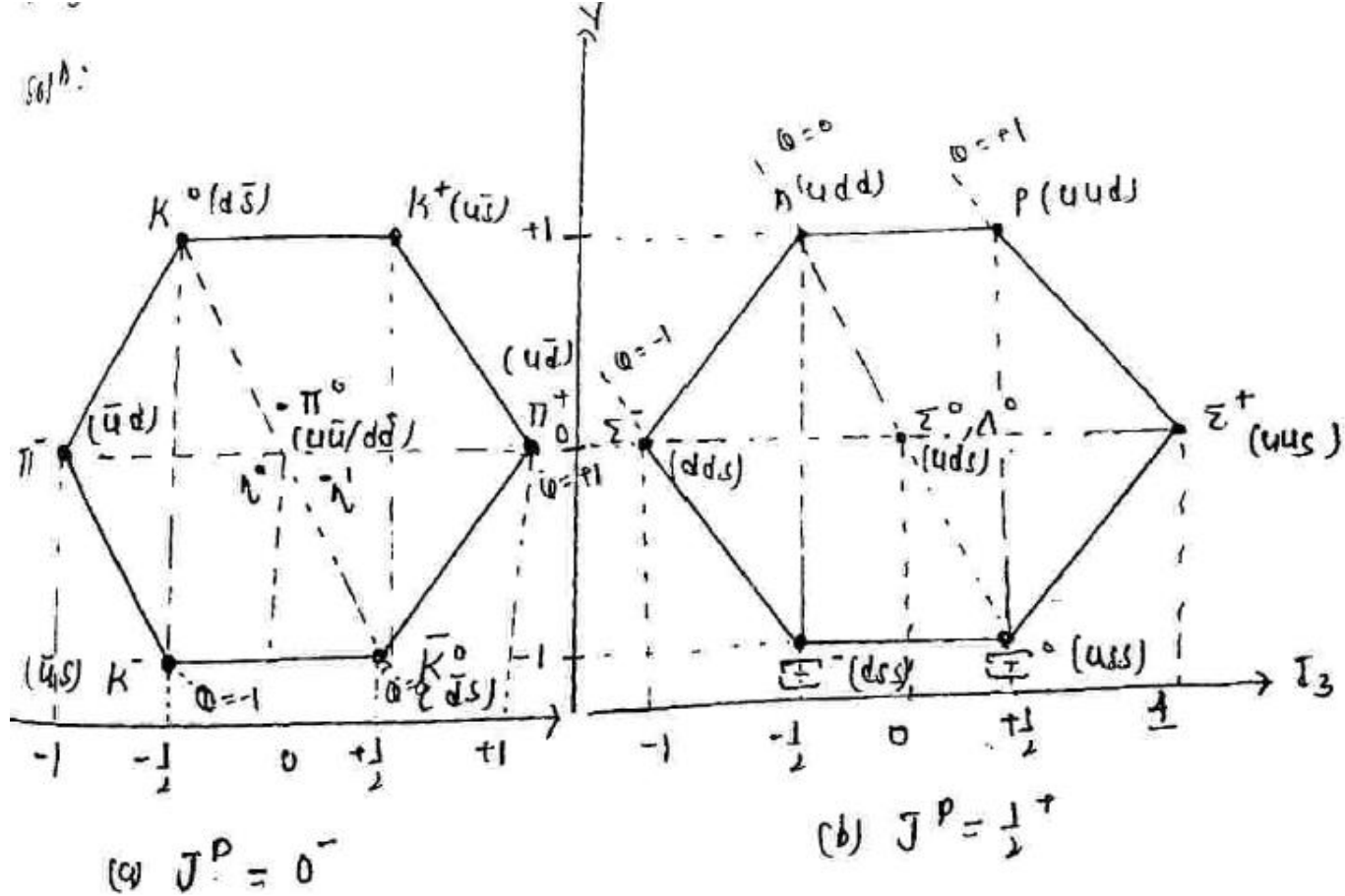
Considering those states composed of just u, d, and s quarks there will be nine such mesons. The hypercharge for this meson state is $Y = S$

- Similarly the lowest lying 3 quarks ($q q q$) states and the lowest lying supermultiplet consists of the eight ($J^P = \frac{1}{2}^+$) baryons as shown below.

For $J^P = \frac{1}{2}^+$ state $Y = S + B$.

Some examples of baryons and mesons, with their major decay modes masses are in MeV/c²

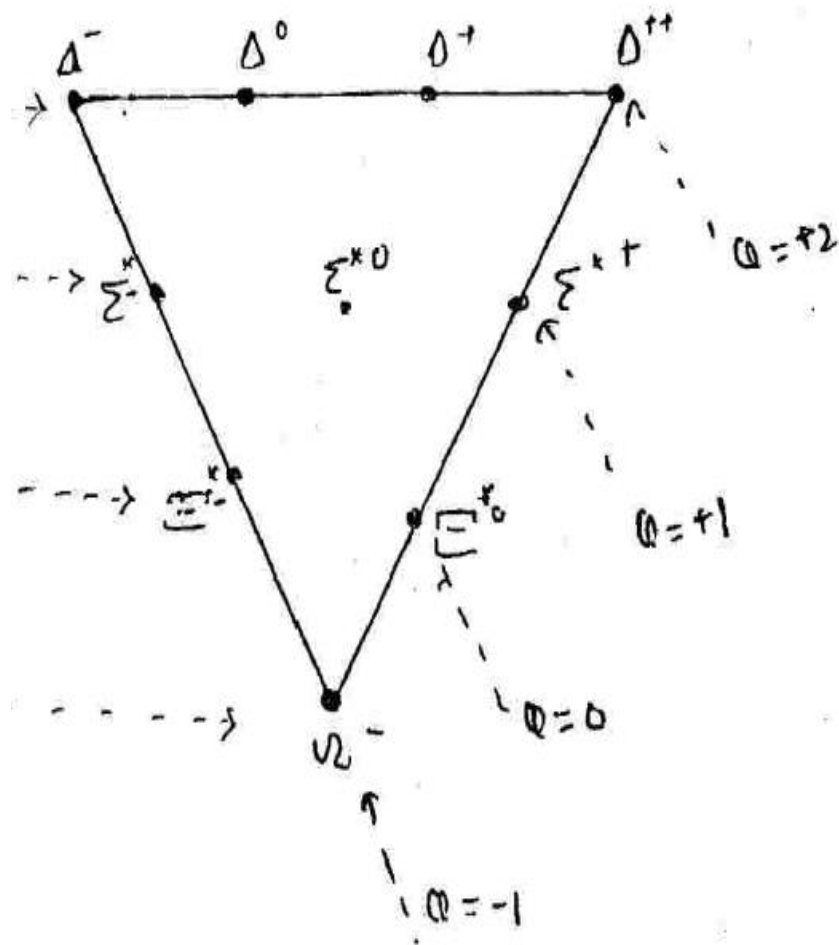
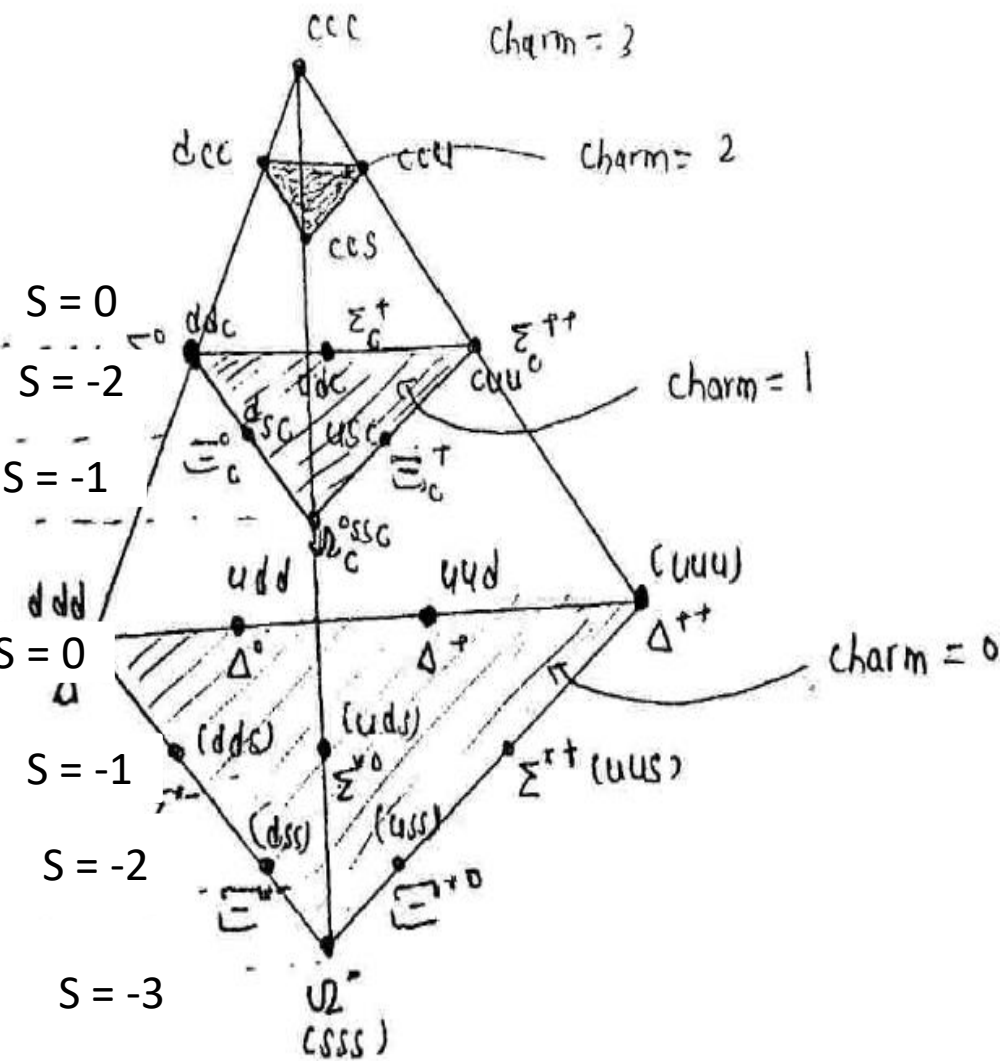
Particle	Mass	Lifetime (s)	Major decays
$\pi^+(u\bar{d})$	140	2.6×10^{-8}	$\mu^+\nu_\mu$ ($\sim 100\%$)
$\pi^0(u\bar{u}, d\bar{d})$	135	8.4×10^{-17}	$\gamma\gamma$ ($\sim 100\%$)
$K^+(u\bar{s})$	494	1.2×10^{-8}	$\mu^+\nu_\mu$ (64%) $\pi^+\pi^0$ (21%)
$K^{*+}(u\bar{s})$	892	$\sim 1.3 \times 10^{-23}$	$K^+\pi^0, K^0\pi^+$ ($\sim 100\%$)
$D^-(d\bar{c})$	1869	1.1×10^{-12}	Several seen
$B^-(b\bar{u})$	5278	1.6×10^{-12}	Several seen
$p(uud)$	938	Stable	None
$n(udd)$	940	887	$pe^-\bar{\nu}_e$ (100%)
$\Lambda(uds)$	1116	2.6×10^{-10}	$p\pi^-$ (64%) $n\pi^0$ (36%)
$\Delta^{++}(uuu)$	1232	$\sim 0.6 \times 10^{-23}$	$p\pi^+$ (100%)
$\Omega^-(sss)$	1672	0.8×10^{-10}	ΛK^- (68%) $\Xi^0\pi^-$ (24%)
$\Lambda_c^+(udc)$	2285	2.1×10^{-13}	Several seen



The lowest – lying states with (a) $J^P = 0^-$ and (b) $J = \frac{1}{2}^+$ that are composed of u, d and s quarks

In the above diagrams, particles along the same horizontal line share the same strangeness q . no. (S), while those on the same vertical, line share the same I_3 and those on the same diagonals share the same charge.

- The scheme may also be extended to more quark flavors, although the diagrams become increasingly complex.
- For example, figure below shows the predicted $J^P = \frac{3}{2}^+$ baryon states formed from u, d, and s quarks when all the three quarks have their spins aligned, but still with zero orbital angular momentum between them.
- In the baryon decuplet the particles indicated with an **asterisk** are **excited states** of corresponding particles in Baryon octet. These excited states have higher mass and spin.



The $J = \frac{3}{2}^+$ baryon states composed of u, d, s and c quarks

Hadronic Magnetic moments:

Magnetic moments have been measured only for the $\frac{1}{2}^+$ octet states composed of u, d and s quarks. In this supermultiplet, the quarks have **zero orbital angular momentum** and so the hadronic magnetic moments are just the **sums of contribution from the constituent quark magnetic moments**.

If we assume the quark magnetic moments are of the Dirac form then

$$\begin{aligned}\mu_q &= \langle q, S_z = \frac{1}{2} | \mu_z | q, S_z = \frac{1}{2} \rangle \\ &= e_q \frac{e\hbar}{2m_q} = e_q \frac{Mp\mu_N}{m_q} \dots\dots (1)\end{aligned}$$

Where, e_q is the quark charge in units of e and $\mu_N = \frac{e\hbar}{2m_p}$ is the nuclear magneton.

$$\text{Thus, } \mu_u = \frac{2Mp\mu_N}{3m_u}, \mu_d = \frac{-1Mp\mu_N}{3m_d}, \mu_s = \frac{-1Mp\mu_N}{3m_s},$$

For example, in the case of $\Lambda = uds$, the u d pair in a spin-0 state and no contribution to the Λ spin or magnetic moment. Thus we have the predicted

$$\mu_\Lambda = \mu_s = \frac{-1Mp\mu_N}{3m_s}$$