MESA tutorial: Session 3
Late Evolution of Massive Stars

For this problem set, make a new copy of the `$MESA_DIR/star/work` directory and place `hw3_inlist` and `hw3_history_columns.list` in your new working directory. In the `inlist` file, change `inlist_project` to `hw3_inlist`.

1 Energy Production in Massive Stars

Let's explore the contributions of various nuclear reaction chains to the bolometric luminosities of massive stars. **the 60msun model takes forever, I have to fix that.. (or exlcue it)**

- Run MESA models at $M = 15, 20, 30, 40, 60 M_\odot$ through central carbon exhaustion. To achieve this, add to the `&controls` :

```
xa_central_lower_limit_species(1) = 'c12'
xa_central_lower_limit(1) = 1d-5
```

Note the setting `log_directory = 'M15_HW3'`: will redirect your output to a new directory with this name, so you don't have to copy the whole work directory each time you want to run a new model.

1. Plot the evolutionary tracks of all five stars on a single HR diagram. Clip the first $\sim 10^3$ years of evolution for clarity.

   Color-code the tracks by the dominant source of nuclear burning. The three output quantities of interest are:

   - `log_LH`: H-burning luminosity
   - `log_LHe`: He-burning luminosity
   - `log_LZ`: Luminosity from burning heavier elements

2. Explore different ways of visualizing this data:

   (a) Create three panels, each color-coded by $\log(L_i/L_{\mathrm{bol}})$ where $i = $ H, He, Z.
   (b) Assign unique colors based on which burning source dominates the luminosity, and color the tracks accordingly.
   (c) Identify and mark regions where no single source dominates the total luminosity.

3. Interpret your results:

2 Evolution of massive stars with mass loss

In this exercise, we will evolve a massive star and investigate the effect of wind mass loss on the evolution of the star. As before, *create a new work folder* for each new model you evolve! (Otherwise the data from the previous models will be overwritten.)

1. Choose a mass between 20 M$_\odot$ and 100 M$_\odot$, and change the inlist. Similar to the previous exercise, run several models with a different wind strength. To do this, uncomment all the lines relating to 'wind mass loss' and vary the `Dutch_scaling_factor` between 0 and 1. Run 3 models again with scaling factors of e.g. 0.1, 0.5, and 1.0. During each run, take a close look at the `PGSTAR` plots. Analyse in detail both the motion of the star in the HR diagram and the changes in structure in the Kippenhahn diagram. Can you identify the different phases in the evolution of massive stars (e.g. RSG, LBV, WR, ...)?

2. Make a `Python` script to plot all 3 evolutionary tracks on an HR diagram. Can you explain the difference in the tracks? Discuss again with your neighbours to compare stars of different mass.

3. Plot the He abundance versus age for all 3 models, and compare how the lifetimes of the MS and of the He-burning phase change with increasing mass loss.

4. Next, make separate plots of the *surface abundances* of H, He, C and O vs age, one for each stellar model. Can you explain the changes you see, and their dependence on the mass-loss rate?

5. EXTRA: After analysing the effects of mass loss, choose one of the models you evolved and continue its evolution, by removing the stopping condition for the lower limit of the central helium abundance. Now follow the evolution and try to identify the different burning stages in the star and their effect on the abundances and the structure.

3   Wolf–Rayet stars

We will use the same models as in Problem 1, but investigate the

- Analyze the following:

  (a) Inspect the HR diagram again, but now color-code the tracks with mass-loss using $\log \dot{M}$ (e.g., range from -6 to -4).
      Describe

  (b) Investigate surface abundance changes due to mass-loss.
      - Plot surface abundances of He, C, and N versus time (all masses, one panel per element).
      - Color-code HR tracks by:
        (a) Surface helium abundance
        (b) Surface N/C ratio
      - Wolf–Rayet (WR) stars are generally defined by $X < 0.3$ (where X is surface H abundance). WR subclasses are defined based on surface C and N composition (WN vs WC). Indicate where WR stars appear in the HR diagram.

4   Radius evolution of massive stars

This exercise is a continuation on the second exercise of the previous `MESA` session. In the last session, you evolved a massive star between 15 and 100 M$_\odot$ up to the end of core helium burning. If you have not done this part yet, then modify the inlist from last week to evolve a star between 15 and 100 M$_\odot$ and change the `Dutch_scaling_factor` to 1.0. Next, compile and run the model. Use the output of this model (stored in `LOGS/history.data`) and compute the following:

1. Make a plot of the radius of the star versus the age. What are the fast and slow phases of evolution? When does the star expand, and when does it contract? By how much does the star expand during its evolution?

2. If the star is in a binary system, in which phase in its evolution is it most likely that the star fills its Roche lobe?
   Note: Observations show that the distribution of the orbits of binary stars is roughly uniform in $\log(a)$. For example, the number of binary stars with separations in the range 10–100 $R_\odot$ is similar to that in the range 100–1000 $R_\odot$.

3. Find the values of the radius of this star that delimit Case A, Case B and Case C of mass transfer. (See p. 225 in Chapter 15 of the lecture notes for a definition of these different cases.)