

MESA tutorial: Session 3

Late Evolution of Massive Stars

For this problem set, make a new copy of the `$MESA_DIR/star/work` directory and place `hw3_inlist`, `history_columns.list`, and `profile_columns.list` in your new working directory. In the `inlist` file, change `inlist_project` to `hw3_inlist`...

Pro Tip

Some of the models you will run in this practicum may take a long time to complete. There is no need to wait for *all* models to finish before starting on the analysis and plotting code!

1 Energy Production in Massive Stars

Let's explore the contributions of various nuclear reaction chains to the bolometric luminosities of massive stars.

- Run MESA models at $M = 15, 20, 30, 40, 60M_{\odot}$ through central C exhaustion. To achieve this add to the `&controls` section in `hw3_inlist`

```
1 xa_central_lower_limit_species(1) = 'c12'  
2 xa_central_lower_limit(1) = 1d-5
```

Note the setting `log_directory = 'M15_HW3'`: will redirect your output to a new directory with this name, so you don't have to copy the whole work directory each time you want to run a new model.

- (a) Plot the evolutionary tracks of all five stars on a single HR diagram. Clip the pre-main sequence evolution from your plot for clarity.

Color-code the tracks by the dominant source of nuclear burning. The three output quantities of interest are:

- `log_LH`: H-burning luminosity
- `log_LHe`: He-burning luminosity
- `log_LZ`: Luminosity from burning heavier elements
- **add neutrino luminosity..!**

- (b) Explore different ways of visualizing this data:

- Create three panels, each color-coded by $\log(L_i/L_{\text{bol}})$ where $i = \text{H, He, Z}$.
- Assign unique colors based on which burning source dominates the luminosity, and color the tracks accordingly.
- Identify and mark regions where no single source dominates the total luminosity.

- (c) Interpret your results.

Pro Tip

You will be making a lot of HR diagrams in this practicum. Consider creating a reusable Python function to streamline the plotting process.

2 Evolution of massive stars with mass loss

In this exercise, we will investigate the effect of wind mass loss on the evolution of the star. We will use the same inlist as in Problem 1. As before, *change the log_directory* for each new model you evolve! (Otherwise the data from the previous models will be overwritten.)

- (a) Choose a mass between $20 M_{\odot}$ and $100 M_{\odot}$, and change the inlist. We only want to run the stars until core He exhaustion (this will save you a lot of compute time). Run the same mass model with 3 different mass-loss rates. To do this vary the `Dutch_scaling_factor` between 0 and 1, (for example 0.1, 0.5, and 1.0). During each run, take a close look at the PGSTAR plots. Analyse in detail both the motion of the star in the HR diagram and the changes in structure in the Kippenhahn diagram. Can you identify the different phases in the evolution of massive stars (e.g. RSG, LBV, WR, ...)?
- (b) Plot all 3 evolutionary tracks on an HR diagram, but now color-code the tracks with mass-loss using $\log \dot{M}$ (e.g., range from -6 to -4). Can you explain the difference in the tracks? Discuss with your neighbours to compare stars of different mass.
- (c) Investigate surface abundance changes due to mass-loss.
 - Plot surface abundances of He, C, and N versus time (all masses, one panel per element).
 - Color-code HR tracks by:
 - (a) Surface helium abundance
 - (b) Surface N/C ratio
- (d) Plot the He abundance versus age for all 3 models, and compare how the lifetimes of the MS and of the He-burning phase change with increasing mass loss.
- (e) Next, make separate plots of the *surface abundances* of H, He, C and O vs age, one for each stellar model. Can you explain the changes you see, and their dependence on the mass-loss rate?
- (f) Wolf-Rayet (WR) stars are generally defined by $X < 0.3$ (where X is surface H abundance). WR subclasses are defined based on surface C and N composition (WN vs WC). Indicate where WR stars appear in the HR diagram.
 - After analysing the effects of mass loss, choose one of the models you evolved and continue its evolution, by removing the stopping condition for the lower limit of the central helium abundance. Now follow the evolution and try to identify the different burning stages in the star and their effect on the abundances and the structure.

3 Radius evolution of massive stars

Using your model for the star you picked with a mass between 15 and $100 M_{\odot}$ from the previous exercise (with `Dutch_scaling_factor` set to 1.0.) compute the following:

- (a) Make a plot of the radius of the star versus the age. What are the fast and slow phases of evolution? When does the star expand, and when does it contract? By how much does the star expand during its evolution?
- (b) If the star is in a binary system, in which phase in its evolution is it most likely that the star fills its Roche lobe?
Note: Observations show that the distribution of the orbits of binary stars is roughly

uniform in $\log(a)$. For example, the number of binary stars with separations in the range 10–100 R_\odot is similar to that in the range 100–1000 R_\odot .

- (c) Find the values of the radius of this star that delimit Case A, Case B and Case C of mass transfer. (See p. 225 in Chapter 15 of the lecture notes for a definition of these different cases.)