

A Suite of Advanced Tutorials for the GROMOS Biomolecular Simulation Software [Article v1.0]

Bettina Lier¹, Christoph Öhlknecht¹, Anita de Ruiter¹, Julia Gebhardt², Wilfred F. van Gunsteren³, Chris Oostenbrink^{1*}, Niels Hansen^{2*}

¹Institute of Molecular Modeling and Simulation, University of Natural Resources and Life Sciences, Vienna, Austria; ²Institute of Thermodynamics and Thermal Process Engineering, University of Stuttgart, Stuttgart, Germany; ³Laboratory of Physical Chemistry, Swiss Federal Institute of Technology, ETH, Zürich, Switzerland

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Abstract This tutorial describes the practical use of some recent methodological advances implemented in the GROMOS software for biomolecular simulations. It is envisioned as a living document, with additional tutorials being added in the course of time. Currently, it consists of three distinct tutorials. The first tutorial describes the use of time-averaged restraints to enforce agreement with order parameters derived from NMR experiments. The second tutorial describes the use of extended thermodynamic integration in the double-decoupling method to compute the affinity of a small molecule to a protein. The molecule involved bears a negative charge, necessitating the application of post-simulation corrections. The third tutorial is based on the same molecular system, but computes the binding free energy from a path-sampling method with distance-field distance restraints and Hamiltonian replica exchange simulations. The tutorials are written for users with some experience in the application of molecular dynamics simulations.

***For correspondence:**

chris.oostenbrink@boku.ac.at (CO); niels.hansen@itt.uni-stuttgart.de (NH)

1 Introduction

GROMOSTM is an acronym of the GRONingen MOlecular Simulation computer program package for the dynamic modelling of (bio)molecules, which has been developed since 1978 primarily as a research vehicle for methodological development [1]. Written in the programming language C++, the latest version has a modular, object-oriented structure [2], which, together with extensive documentation [3], makes modification relatively easy. Readability of the code is prioritised over speed. A GROMOS license will be issued for free upon registration of a user at www.gromos.net. The GROMOS soft-

ware is to be distinguished from the GROMOS force fields for biomolecular systems. The development of the successive GROMOS force-field versions during the past 40 years has been summarised in [1, 4]. Recent work showed that time saving approximations employed during force-field development had no effect on the parametrization in terms of agreement with experiment [5]. The GROMOS software comes with a manual that consists of nine volumes. Volume 7 is a basic tutorial that introduces new users to the setup and analyses of molecular simulations with GROMOS [6].

1.1 Scope

The three tutorials presented here cover some of the methodological advances that have been implemented in GROMOS over the last few years and are not treated in the basic tutorials distributed with the software. They address an advanced user who has some experience with MD simulations. Beginners in the field are recommended to start with the basic tutorial of GROMOS [6]. Each of the three current tutorials is based on an original publication and comes with its own learning objectives and expected outcome(s). After completing tutorial 1 “S2 order parameter restraining” the user should be able to

1. Prepare a simulation of a protein solvated in water.
2. Understand how NMR restraints are handled in GROMOS.

After completing tutorial 2 “Double decoupling method & corrections for net-charge changes” the user should be able to

1. Prepare perturbation topologies for binding free energy calculations.
2. Define distance restraints and perturbed distance restraints for simulations in GROMOS.
3. Calculate binding free energies using the double decoupling method and extended-thermodynamic integration.
4. Apply a post-simulation correction scheme to correct artifacted free-energies obtained from charge-changing perturbations.

After completing tutorial 3 “Using HREMD and distance-field” the user should be able to

1. Setup a distance-field restraining potential-energy term.
2. Perform umbrella sampling calculations in GROMOS using perturbed distance(-field) restraints.
3. Extract the binding free energy from the potential of mean force.

Due to the statistical-mechanical nature of the ensembles of molecular configurations, meaningful values of quantities are averages over configurations or trajectories. Individual trajectories are perfectly fine for instructional purposes such as in this tutorial, but are of little utility in “real” research settings, unless there is little or no variation within the configurational ensemble. For most degrees of freedom of interest in biomolecular systems this is certainly not the case. A simple means for generating replicates is to use different seeds of the random number generator for sampling the initial velocities at equilibration.

2 Prerequisites

The tutorials require the latest GROMOS version installed (1.5.0). A GROMOS license will be issued for free upon registration of a user at www.gromos.net.

2.1 Background knowledge

The tutorials assume the user to be familiar with the content of a GROMOS system topology, input files and analysis tools as explained in detail in the basic tutorials distributed with the software [6]. Tutorial 1 (see section 3.1) repeats some of the basic system preparation steps but cannot be comprehensive in explaining all basic operations. We assume that the user is familiar with basic Linux or Unix command line interactions and tools to efficiently edit larger plain text files such as VIM or Emacs. Furthermore a user should be able to visualise molecular structures (e.g. with PyMOL [7] or VMD [8]) and to use basic plotting tools (e.g. Xmgrace, R, matplotlib).

The GROMOS software for biomolecular simulation comprises the molecular dynamics engine MD++ and the GROMOS++ suite of pre- and postprocessing programs. The program is independent of the computer architecture or force field used. The units of the various quantities are defined outside the program through a physical constants block in a force-field file. The only unit conversion performed internally by the program is between degrees and radians. The force-field files come in GROMOS units, that is SI units, but with atomic mass units for mass, nm for distance, ps for time, and electronic charge for charge [9]. No simulation protocols are prescribed. Input parameters specified by a user are not modified inside the program unless incompatible with the code. In all cases a warning message is displayed. The interpretation of the results is simplified by an extensive documentation of the implemented algorithms and their technical details [9, 10].

2.2 Software/system requirements

GROMOS can be compiled on almost any operating system compatible with the POSIX standard. Some of the libraries required are not available on standard operating systems and have to be installed manually as described in detail in volume 8 of the GROMOS documentation [11]. For some of the analyses a basic installation of Python 3 is required. Note that files edited on non-Unix-like operating systems may cause an I/O-error due to a different representation of a line break.

3 Content and links

The tutorials described in this article can be accessed at https://github.com/hansenniels/gromos_tutorial_livecoms. All necessary files for completing each tutorial are provided at that

location.

3.1 Tutorial 1: S^2 order parameter restraining

The backbone N-H order parameter is a measure for the spatial restriction that the N-H vector experiences in a molecular reference frame. Order parameters calculated from ensembles generated by MD simulations are not subject to a specific motional model but depend on the local flexibility inherent in the force field when solving Newton's equation of motion and on whether the assumption of internal motion being independent of overall tumbling is justified. GROMOS features a time-averaging variant of order parameter restraining that is described in detail elsewhere [12]. We will demonstrate the use of time-averaged order parameters by means of the third IgG-binding domain of Protein G (GB3), which is a small 56-residue protein.

3.1.1 Topology

Go into the subdirectory `topo` of the directory `t_01`. The input file `make_top_GB3.arg` is already prepared. We will use the force field 54a7. The molecular topology file for the protein, `GB3_54a7.top`, with SPC water as a solvent can then be generated using the GROMOS++ program `make_top` by typing

```
$ make_top @f make_top_GB3.arg >
  GB3_54a7.top
```

In order to neutralize the net charge of -2e of the protein topology the next step is to build a topology file for a sodium ion using the input file `make_top_Na.arg`:

```
$ make_top @f make_top_Na.arg > Na_54a7.top
```

Next we combine the two topologies using the GROMOS++ program `com_top`

```
$ com_top @f com_top_GB3_2Na.arg >
  GB3_2Na_54a7.top
```

The file `GB3_2Na_54a7.top` contains the complete molecular topology. Using the GROMOS++ program `check_top` with the arguments `@build` and `@param` the topology can be checked against the force field. Be aware that `check_top` may not catch every inconsistency. In the present case the putative inconsistency with the partial charge on atom 5 spotted by `check_top` is actually not an error because the partial charge is adapted for the N-terminus of the peptide chain.

3.1.2 Coordinates

Go into the subdirectory `coord`. The Cartesian coordinates for the protein can be downloaded from the Protein Data-bank, accession code 2OED [13]. By using the GROMOS++ program `pdb2g96` the PDB file will be converted to a GROMOS

coordinate file. Before conversion we make a copy of the downloaded pdb file `2oed.pdb` into the file `2oed_edited.pdb`. In the latter we do a change in line 1010 (replace "O " by "O1") and line 1016 (replace "OXT" by "O2 ") such that `pdb2g96` recognizes these two atoms as belonging to the carboxy terminus. When editing the PDB file the columns must be kept aligned. The remaining differences between the nomenclature used in the PDB file and the one used in the topology are handled via the file `pdb2g96.lib`. With

```
$ pdb2g96 @f pdb2g96_GB3.arg >
  pdb2g96_GB3.cnf
```

we generate a GROMOS coordinate file.

3.1.3 Energy minimization

Before putting the protein in a box of solvent, its configuration has to be relaxed by energy minimization. Go into the subdirectory `min` and open the shell script `em_GB3.run` to adapt the paths and the names of the files according to your system. The energy minimization of the solute in vacuo is very fast and can be run interactively by typing

```
$ ./em_GB3.run
```

Once the energy minimization is finished the minimized coordinates are written to the file `GB3_min.cnf` and the general output file `em_GB3.umd` contains the progress of the minimization.

3.1.4 Solvating the protein in a water box

Now the protein is ready to be placed into a box and solvated, for subsequent simulations under periodic boundary conditions. Go into the subdirectory `box`. The box shape will be chosen to be rectangular, the simple point charge (SPC) water model [14] will be employed (as already specified in the topology file), the minimum solute-to-wall distance will be 1.2 nm such that the closest surface atoms of two periodic copies are at least 2.4 nm apart (longer than the cutoff distance of 1.4 nm). The minimum solute-solvent distance is set to 0.23 nm. The GROMOS++ program `sim_box` is used to generate the box and to solvate the protein by executing

```
$ sim_box @f sim_box_GB3.arg >
  sim_box_GB3.cnf
```

During the immersion into the solvent, water molecules may still have been placed too close or too far away relative to the protein surface. Moreover, their orientation towards the protein surface is not optimized. Therefore, we need an equilibration of the solute-solvent system using energy minimization. During this process the solute atoms will be positionally restrained around their coordinates in the initial structure using harmonic springs while the solvent molecules

can move freely. The list of atoms to be positionally restrained must be specified in a file `sim_box_GB3.por`. The reference positions of these atoms must be specified in a separate file `sim_box_GB3.rpr`. To prepare these files, copy the coordinate file `sim_box_GB3.cnf` to `sim_box_GB3.por` and `sim_box_GB3.rpr`. Open the file `sim_box_GB3.por` in your text editor and

- Write in the title block the text “list of solute atoms to be positionally restrained”
- Change the keyword “POSITION” at the beginning of the atom coordinate block into the keyword “POSRESSPEC”
- Delete all the solvent atoms. This can also be conveniently achieved by using the command line instruction
`$ sed -i "/SOLV/d" sim_box_GB3.por`

When GROMOS reads this file, it will entirely ignore the coordinates and just look at the list of atoms. Next, open the `sim_box_GB3.rpr` in your text editor and

- Write in the title block the text “reference positions of solute atoms to be positionally restrained”
- Change the keyword “POSITION” at the beginning of the atom coordinate block into the keyword “REFPOSITION”

When GROMOS reads this file, it will only use the coordinates of the atoms listed in `sim_box_GB3.por` and ignore the rest. Now, adapt the input file `em_solvent.imd` according to the number of solvent molecules in your box by adjusting the second number in the `SYSTEM` block and by adjusting the index of the last atom in the `FORCE` block. Now, adapt the paths and the names of the files in `em_solvent.run` according to your system. Then start the energy minimization of the solvent interactively by typing

```
$ ./em_solvent.run
```

This will take a few moments. Once the minimization is finished, the new coordinate file, `GB3_h2o.cnf` and the general output file `em_solvent.ond` will be written out.

3.1.5 Adding counter ions

To complete the preparation of the simulation box two sodium ions should be added. Go to the subdirectory `ion`. The two sodium ions are added to the simulation box using the GROMOS++ program `ion` such that they replace the water molecules which have the lowest electrostatic potential. You can run `ion` by typing

```
$ ion @f ion_GB3.arg > GB3_2Na_h2o.cnf
```

3.1.6 Thermalisation and equilibration

For thermalisation we will use a combination of a progressively increasing temperature and progressively decreasing position restraints on the solute atoms. The thermalisation

procedure is facilitated by the use of the GROMOS++ program `mk_script`, which allows the automatic generation of successive MD jobs that (i) slightly differ in their input parameters; (ii) use the final configuration and velocities of one job as the starting configuration and velocities of the next one; (iii) automatically submit the next job upon completion of the previous one. Go into the subdirectory `eq`. Before running the script you need to adjust the number of solvent molecules and the last atom for the set of degrees of freedom in the input file `equilibration.imd` as well as the paths and names in `eq_mk_script.arg`. Moreover new position restraint files `GB3_2Na_h2o.por` and `GB3_2Na_h2o.rpr` have to be prepared as described above based on the output file `GB3_2Na_h2o.cnf` from the `ion` program. Now the job scripts and corresponding input files are created by typing

```
$ mk_script @f eq_mk_script.arg
```

You are now ready to start the thermalisation and equilibration. Run the first job script and the others will be automatically executed as soon as the preceding script has finished.

```
./eq_GB3_1.run
```

After the equilibration is finished you can carry out some basic checks in the `eq/ana` directory. You can for example see that the kinetic energy is increasing at every new job.

3.1.7 Unrestrained molecular dynamics simulation

The equilibration procedure produced short simulations at constant temperature and volume. Now we want to elongate the simulation to 21 ns under constant temperature and pressure. Go to the directory `md` and use the `mk_script` program to create the job scripts and input files:

```
$ mk_script @f md_mk_script.arg
```

Here the simulation is split into 21 jobs that may preferably run on a computer cluster. To run the jobs interactively type

```
$ ./md_GB3_1.run
```

To facilitate the submission to a cluster, adjust the entry `lastcommand` in the file `mk_script.lib`. Depending on your cluster settings, you may also want adjust the entry `workdir` and make sure to use a binary that runs GROMOS in parallel (MPI or openMP) or uses the GPU acceleration [11].

3.1.8 S²-order parameter restrained molecular dynamics simulation

Starting again from the final configuration of the equilibration procedure we now perform the S² order parameter restraining simulation. Go to the directory `md_S2res` and have a look into the input file `md.imd`. Compared to the unrestrained simulation it contains the additional block

```
ORDERPARAMRES
# NTOPR NTOBRA COPR TAUOPR UPDOBR NTWOP
  -1    0    300    200    1    250
END
```

By setting the switch NTOPR to -1 you specify that you use time-averaged restraining without individual weights for the force constant. The switch NTOBRA controls reading of the averages from the startup file. The value should be 0 for the first job and 1 for continuation jobs. The switch COPR defines the order parameter restraining force constant. With TAUOPR the coupling time is specified. The switch UPDOBR is only relevant if the averages are not calculated using the damped memory approach but as a running average covering the last TAUOPR picoseconds of the simulation. We note that window averaging shows no advantage over the damped memory approach while requiring a sizeable amount of RAM. Finally NTWOP controls how often the order parameters are written to the special trajectory. The actual settings of the switches NTOBRA, COPR and TAUOPR are defined in the joblist S2_restraining.jobs that has the following structure:

```
TITLE
S2 order parameter restraining
END
JOBSCRIPTS
job_id [...] NTOPR NTOBRA COPR TAUOPR [...]
  1   [...]  -1    0    10    200 [...]
  2   [...]  -1    1    300    200 [...]
  3   [...]  -1    1    300    200 [...]
...
END
```

In the first job we start with a small restraining force constant COPR since we want a gentle build-up of the time averages. From the second job onwards the force constant is unchanged. Similar settings of force constant and averaging time were used in previous work on this system [12]. The experimental order parameters used for the restraining are taken from Hall and Fushman [15] and are specified in the column S0 of the file order_exp.dat. In the latter file the atoms i and j defining the bond vector need to be specified as well as the average bond length R0. The column DS0 contains the width of the flat bottom region while WOPR allows the assignment of individual weights to the order parameters if the corresponding switch NTOPR in md.imd is selected. Now use the mk_script program to create the job scripts and input files:

```
$ mk_script @f md_mk_script.arg
```

The file order_exp.dat needs to be specified under the keyword order in the @files section of md_mk_script.arg. As

before the simulation is split into 21 jobs that may preferably run on a computer cluster. To run the jobs interactively type

```
$ ./md_GB3_1.run
```

3.1.9 Analysis

First, we analyse the energy trajectories of the unrestrained and restrained simulations. Go into the directory ana/ene_ana/unres and run the analysis program ene_ana by typing

```
$ ene_ana @f ene_ana_unres.arg >
    ene_ana_unres.out
```

The first trajectory is excluded from the analysis to account for the fact that the system needs some additional equilibration phase when switching from a constant volume to a constant pressure simulation. The file ene_ana_unres.out contains the averages while the time series of all specified properties are contained in the .dat files. The total intramolecular energy of the protein had to be defined in the ene_ana.md++.lib file located in the subdirectory above, see line 150 in that file. Repeat the analysis for the restrained simulation and compare the results. For the latter we additionally evaluate the total restraining energy in order to check whether the contribution of the restraints is small compared to the total intramolecular energy of the protein. Note that the file ene_ana.md++.lib has to be compatible with the GROMOS version used. If you use a newer version than 1.5.0, you will find the corresponding file in the directory md++-x.y.z/data.

Second, the atom positional root-mean-square deviation of the backbone atoms from a reference structure is calculated for the two trajectories using the GROMOS++ program rmsd. For the unrestrained simulation go to the directory ana/rmsd/unres and type

```
$ rmsd @f rmsd_unres.arg > rmsd_unres.out
```

Here, we use the last structure of the equilibration simulation as reference. The two resulting RMSD time series are shown in Figure 1.

Third, the root-mean-square fluctuation of the backbone N atoms is calculated using the program rmsf. For the unrestrained simulation go to the directory ana/rmsf/unres and type

```
$ rmsf @f rmsf_unres.arg > rmsf_unres.out
```

The two resulting plots are displayed in Figure 2 and show that the restrained simulation does not necessarily show less fluctuations compared to the unrestrained simulation.

Finally the N-H order parameters are calculated using the program nhoparam. For the unrestrained simulation go to the directory ana/nhoparam/unres/0.5 and type


```
$ nhoparam @f nhoparam_unres.arg >
  nhoparam_unres.out
```

We do the analysis using two averaging time windows of 0.5 ns and 1.0 ns, respectively. Since the order parameter is defined as long-time tail of the autocorrelation function of the bond vector, this comparison provides insight whether the corresponding autocorrelation functions have reached their plateau values. The `nhoparam` program also calculates order parameters averaged over the entire trajectory. These values may be considerably smaller than those calculated using 1 ns averaging time. If that is the case, conformational changes occur on larger time scales and a structural interpretation based on order parameters might be difficult. Figure 3 shows a relatively small influence of the averaging time on the resulting order parameters in the present case.

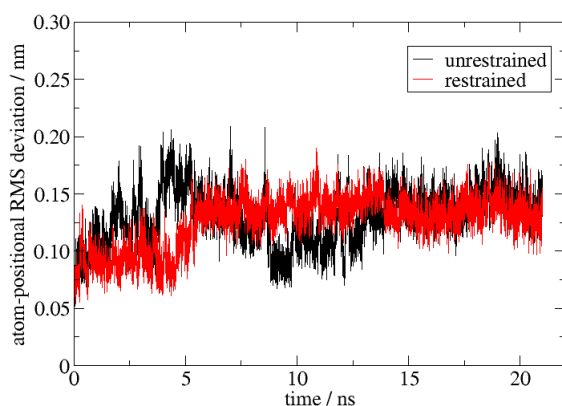


Figure 1. Backbone atom-positional root-mean-square deviation (RMSD) of GB3 with respect to the final structure of the equilibration simulation.

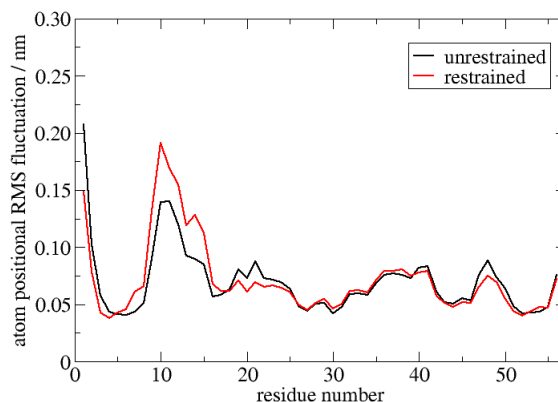


Figure 2. Backbone N atom-positional root-mean-square fluctuation (RMSF) of GB3.

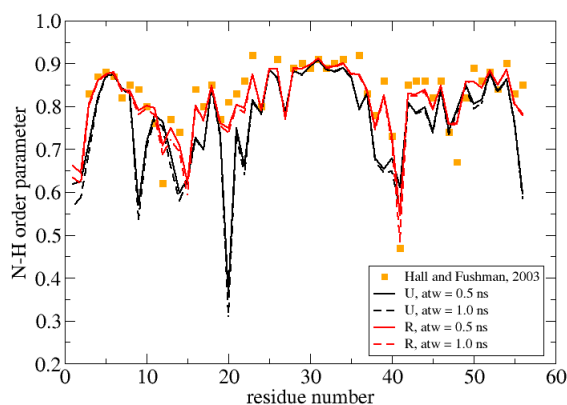


Figure 3. Comparison of backbone N-H order parameters for protein GB3, determined from unrestrained (U) and restrained (R) MD simulations using different averaging time windows (atw) in the analysis. The experimentally derived order parameters used for restraining were taken from the work of Hall and Fushman [15] (anisotropic model).

3.2 Tutorial 2: Double decoupling method & corrections for net-charge changes

The double decoupling method (DDM) [16] is an alchemical perturbation approach to compute binding free energies from molecular dynamics simulations by making use of a thermodynamic cycle (Figure 4). Two of the branches are determined by thermodynamic integration corresponding to the decoupling of the ligand from the system (perturbing the ligand into a non-interacting dummy molecule), free in solution and when bound to the host. In order to avoid sampling of non-relevant phase space in the complexed system, the

ligand is kept in a position that resembles that of the native bound conformation by gradually introducing a harmonic distance restraint. The free energy of the restraint removal can be evaluated analytically.

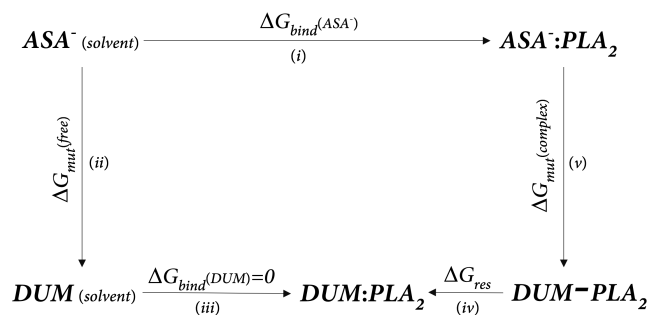


Figure 4. Thermodynamic cycle for the calculation of the standard binding free energy of aspirin (ASA^-) binding to the protein phospholipase A_2 (PLA_2). ASA^- is turned into a non-interacting dummy molecule (DUM), both in its complexed state (v) and free in solution (ii). The free energy of DUM binding to PLA_2 is zero (iii). An intermediate state (DUM-PLA_2) is introduced by linking both binding partners with a harmonic distance restraint. The free-energy contribution of this restraint can be calculated analytically (iv) via equation 6. The free energy differences of branches (ii) and (v) are determined via (extended) thermodynamic integration (TI), enabling the calculation of the standard binding free energy (i).

In this tutorial we will calculate the standard binding free energy of aspirin (ASA) to the protein phospholipase A_2 (PLA_2) using the DDM and extended-thermodynamic interaction (X-TI) [17].

3.2.1 Simulation setup

Preparation of topologies and coordinate files, energy minimization, solvation in SPC water and the addition of counter ions as well as the setup of equilibrations and simulations can be performed in analogy to tutorial 1. The Cartesian coordinates for the enzyme phospholipase A_2 with bound acetyl salicylic acid (ASA) can be obtained from the Protein Data-bank with accession code 1OXR [18]. The final equilibrated structures, `eq_ASA_Na_7.cnf` and `eq_PLA2_ASA_Ca_2Na_7.cnf`, are in subdirectories `eq/eq_ASA` and `eq/eq_PLA2_ASA` of the directory `t_02`.

3.2.2 Perturbation topology

Go into the subdirectory `topo`. The topologies for the ligand (`ASA.top`) and the ligand bound to the protein (`PLA2_ASA.top`) are already prepared. You can also find the combined topologies with sodium counter ions and a calcium ion that is important for the ligand binding (`ASA_Na.top` and `PLA2_ASA_Ca_2Na.top`). For ligand decoupling, the topology for ASA in the decoupled state (`DUM.top`) was generated by changing the integer atom code (IAC) to 22 corresponding

to dummy type for all the atoms and setting all the charges to 0. The program `make_pt_top` can convert topologies from state A and B into a perturbation topology. The `PERTATOMPARAM` block lists all atoms with their respective force field parameters that will be alchemically perturbed during the simulation.

3.2.3 Distance restraints

Distance restraints are introduced for the calcium ion to keep it bound in the active site. For this a distance restraint specification file `disres.dat` is set up in subdirectory `eq` containing the following block.

```
DISTANCERESSPEC
# DISH DISC
0.1 0.153
# i j k l type i j k l type r0 w0 rah
1208 0 0 0 0 309 0 0 0 0 0.223 1.0 0
1208 0 0 0 0 321 0 0 0 0 0.235 1.0 0
1208 0 0 0 0 339 0 0 0 0 0.246 1.0 0
1208 0 0 0 0 489 0 0 0 0 0.255 1.0 0
1208 0 0 0 0 490 0 0 0 0 0.248 1.0 0
END
```

The restraint is defined between the calcium ion and 5 atoms of residues coordinating the ion (3 amide oxygens and 2 carboxylate oxygens). `type 0` is referring to explicit/real atoms. `r0` is the distance between two atoms in nm. The restraint is defined with a weight factor `w0` of 1 by which the distance restraint interaction term `CDIR` of the `DISTANCERES` block in the `imd`-file gets multiplied (force constant). The parameter `rah` controls the form and dimension of the restraint, here it is set to zero which corresponds to a full harmonic potential in x, y, z dimensions. Parameters `DISH` and `DISC` are the hydrogen-carbon and carbon-carbon distances, respectively. GROMOS can also apply distance restraints on virtual or pseudo atoms by setting the appropriate type and a specification of additional atoms `j, k` and `l`.

To keep the ligand within the active site when getting decoupled, we gradually turn on a harmonic distance restraint simultaneously to the perturbation. Go into the subdirectory `DDM/md_TI` where you will find the `disres.dat` file which contains an additional block.

```
PERTDISRESSPEC
# DISH DISC
0.1 0.153
# i j k l type i j k l type n
m Ar0 Aw0 Br0 Bw0 rah
21 211 264 529 -1 1195 1199 1203 0 -1 0
0 0.0 0.0 0.0 1.0 0
END
```

The distance restraint is defined between the centre of geometry (type -1) of 4 backbone atoms (i, j, k and l) of PLA₂ around the active site and the centre of geometry of 3 atoms of the ligand's benzene ring with a distance of zero (A_r0=B_r0=0). At state A the restraint is turned off (A_w0=0), while at state B the restraint is retained with a weight factor of 1 (B_w0=1). Parameters n and m control hidden restraints [19]. Parameters DISH and DISC are not relevant for the centre of geometry and this type of pseudo atoms.

3.2.4 Extended-thermodynamic integration simulation

The thermodynamic integration approach uses the coupling parameter λ , which defines the system as a linear combination of the two end-states [20]. The coupling parameter approach formulates the Hamiltonian of the system dependent on λ by interpolating between the two states (scaling of force-field parameters).

$$V_{nb}(r_{ij}, \lambda) = (1 - \lambda)^n V^A(r_{ij}, \lambda) + \lambda^n V^B(r_{ij}, 1 - \lambda) \quad (1)$$

with

$$V^X(r_{ij}, \lambda) = \frac{C_{12}^X}{(\alpha_{lj}\lambda^2 C_{126}^X + r_{ij}^6)^2} - \frac{C_6^X}{\alpha_{lj}\lambda^2 C_{126}^X + r_{ij}^6} + \frac{q_i^X q_j^X}{4\pi\epsilon_0} \left[\frac{1}{(\alpha_{crf}\lambda^2 + r_{ij}^2)^{1/2}} - \frac{1/2 C_{rf} r_{ij}^2}{(\alpha_{crf}\lambda^2 + R_{rf}^2)^{3/2}} - \frac{1 - 1/2 C_{rf}}{R_{rf}} \right] \quad (2)$$

where C_6^X , C_{12}^X , q_i^X and q_j^X are the Lennard-Jones parameters and partial charges for state X (A or B). r_{ij} is the distance between particles i and j , C_{rf} and R_{rf} are parameters of the electrostatic reaction field assumed outside the cutoff sphere [21]. α_{crf} and α_{lj} are soft-core parameters [22].

Go into the subdirectory md_TI. The input files md_TI_ASA_Na.imd and md_TI_PLA2_ASA_Ca_2Na.imd contain two additional blocks that are relevant for the free energy calculations using X-TI integration. The PERTURBATION block controls the alchemical perturbation

```
PERTURBATION
#      NTG      NRDGL      RLAM      DLAMT
#      1         0        0.0        0.0
#  ALPHLJ  ALPHC    NLAM   NSCALE
#      1.0      1.0         1         0
END
```

NTG turns on the perturbation to calculate $\partial H/\partial \lambda$ and RLAM is the initial value for λ . The initial value of λ could also be read from the configuration when setting NRDGL=1. RLAM will be adjusted for several different λ points using the jobs file md_TI.jobs. DLAMT controls the increase of λ with time. The

parameters ALPHLJ and ALPHC are the soft-core parameters for Lennard-Jones (α_{lj}) and Coulomb (α_{crf}) interactions, respectively. NLAM controls the power dependence of the λ coupling (n in eq. 1) and NSCALE the use of interaction scaling for complete energy groups.

The PRECALCLAM block is relevant for the pre-calculation of intermediate non-simulated λ -points during the simulation as extension to standard TI.

```
PRECALCLAM
#  NRLAM  MINLAM  MAXLAM
#      81       0       1
END
```

With the settings in the above block, the energies and derivatives with respect to λ will be calculated on-the-fly at 81 points ranging from $\lambda=0$ to $\lambda=1$, which results in λ -steps of 0.0125.

The simulation is defined in the jobs file md_TI.jobs. Simulations will be performed at 11 equally spaced λ -points between $\lambda=0$ and $\lambda=1$ for 5 ns each in case of the complexed system, where ASA is bound to PLA₂. This system also requires the perturbed distance restraint. The simulations of ASA free in solution will also be performed at 11 λ -points each for 0.5 ns. Note that this tutorial can also be carried out using standard TI, in which case the PRECALCLAM block is not required. However, then, usually more than 11 λ -points are needed. To run the two simulations, copy the argument files required by the mk_script program into the two directories md_TI_ASA and md_TI_PLA2_ASA, respectively, and adapt the paths before generating the job files with the mk_script program and submitting the jobs to a cluster. If you prefer to continue directly, you will find the necessary energy and free-energy trajectories in the subdirectories L_*.

3.2.5 Free-energy analysis

The free energies can be determined via extended-thermodynamic integration (X-TI) [17] or the Bennett acceptance ratio (BAR) method [23]. The raw data for both methods can be extracted from the energy and free energy trajectory files using the gromos++ program ext_ti_ana.

Go into the subdirectory DDM/ana_TI/ana_TI_ASA and run the program ext_TI_ana via the bash-script by typing

```
$ ./ext_ti_ana_bar.sh
```

X-TI requires the pre-calculation of free energies at non-simulated points. Free-energy derivatives at requested non-simulated λ_p values can be reweighed to obtain ensemble averages for λ_p from simulated λ_s points. The predictions from multiple simulations at λ_s points can be merged into a single TI profile by a linear reweighting scheme using the program ext_TI_merge. Run the program via the bash-script by typing


```
$ ./ext_ti_merge.sh
```

The program calculates the integral of the final TI-curve using the trapezoidal rule in order to obtain the free-energy estimate. The results of X-TI for both systems, ASA and PLA2_ASA, are shown in Figure 5.

BAR estimates free energies from the free energy differences between two adjacent λ points i and j , using

$$\Delta G(\lambda_i \rightarrow \lambda_j) = k_B T \ln \frac{\langle f(E(\lambda_i) - E(\lambda_j) + C) \rangle_{\lambda_j}}{\langle f(E(\lambda_j) - E(\lambda_i) - C) \rangle_{\lambda_i}} + C \quad (3)$$

with

$$f(x) = \frac{1}{1 + \exp(x/k_B T)} \quad (4)$$

C is determined iteratively to ensure that the two ensemble averages from λ_i and λ_j are identical. To calculate error estimates, a bootstrap sampling can be conducted. Run the program `bar` via the bash-script by typing

```
$ ./bar.sh
```

BAR is computationally more efficient and converges relatively fast compared to regular TI. The efficiency of X-TI is comparable with the added advantage of a direct visualization of the entire free-energy profile [24].

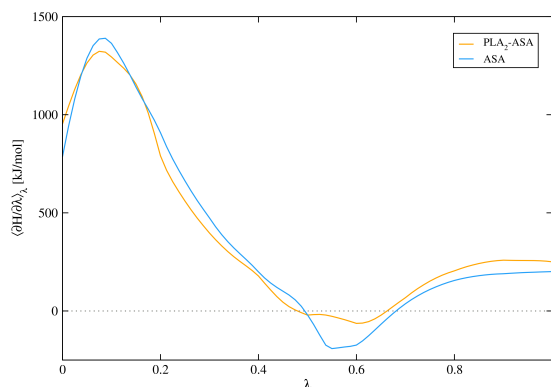


Figure 5. The reweighted property $\langle \frac{\partial H}{\partial \lambda} \rangle$ for $\lambda=0$ to $\lambda=1$ for both systems ASA and PLA2_ASA.

3.2.6 Thermodynamic cycle

The free energy of binding is determined according to the thermodynamic cycle shown in Figure 4 as

$$\Delta G_{\text{bind}}(\text{ASA}^-) = \Delta G_{\text{mut}}(\text{free}) + \Delta G_{\text{bind}}(\text{DUM}) - \Delta G_{\text{res}} - \Delta G_{\text{mut}}(\text{complex}) \quad (5)$$

The free energy associated with the removal of the restraint (ΔG_{res}) for a dummy particle can be calculated analytically,

including a standard state correction [25, 26]:

$$\Delta G_{\text{res}} = -k_B T \ln \frac{V^\circ}{(2\pi k_B T/K)^{3/2}} \quad (6)$$

where K is the force constant of the harmonic distance restraint and V° is the accessible solution volume corresponding to the standard-state definition. For a molar reference concentration it is given by $V^\circ = 1.661 \text{ nm}^3$. Equation 6 corrects for restricted mobility and can be derived from the partition function associated with the restraining potential energy function, given that the restraint is so strong that the integration volume can be extended to the entire space [27].

3.2.7 Correction terms for net-charge changes

Due to finite box sizes, periodic boundary conditions and simplifications in the calculations of the electrostatic interactions, the calculated free energies are artifacted. In the following paragraphs, we will refer to these energies as raw free energies. We will quantify and correct these artifacted components using a free-energy correction ΔG_{cor} to yield methodology-independent values ΔG as

$$\Delta G = \Delta G_{\text{raw}} + \Delta G_{\text{cor}} \quad (7)$$

Analogous to Reif and Oostenbrink [28], ΔG_{cor} is a combination of multiple free-energy corrections for a spurious solvent-polarization (ΔG_{pol}), the impracticality of calculating the zero of the potential under periodic boundary conditions using discrete solvent molecules (ΔG_{dsm}) and artifacted direct interactions between the ligand and the host molecule (ΔG_{dir}). The free-energy correction is calculated as

$$\Delta G_{\text{cor}} = \Delta G_{\text{pol}} + \Delta G_{\text{dir}} + \Delta G_{\text{dsm}} \quad (8)$$

These three correction terms will be calculated in the following paragraphs. A general scheme about the calculation of the corrections based on λ -generated trajectories can be found in Figure 6 [29]. Note that within this tutorial, only the information needed for the practical part is provided, further details about the theory can be found elsewhere [28, 30, 31]. The set of the three correction terms needs to be calculated for both branches of the thermodynamic cycle. Have a look into the directory `corrections`. It contains subdirectories for Aspirin free in solution and the complex of Phospholipase A2 with Aspirin. The correction procedure will only be explained for Aspirin free in solution, the procedure for the complex is similar. Go into the directory `corrections/ASA`. First, we need to create a set of topologies for intermediate states. These topologies will have full, unperturbed VdW parameters but charges that scale with λ . Go further into the subdirectory `correction_topologies`. The python script `interpolate_topocharges.py` takes three

input parameters: topologies at states A and B and a specific λ -value. A new topology with charges that correspond exactly to the given λ -value is written out. All other parameters remain unperturbed and are taken from topology A. We do not have to use it directly but can use the bash script `do_interpolate_topocharges.bash` instead. It creates six topologies at equidistant λ -points. These will be used for the individual correction terms explained in the following paragraphs.

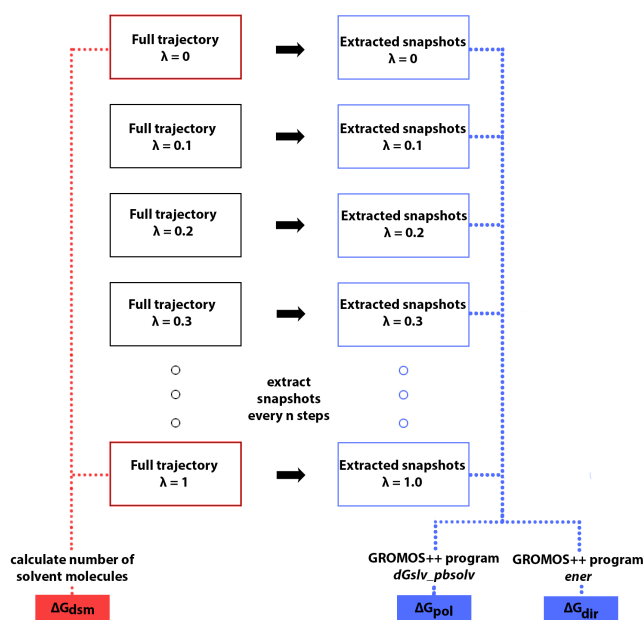


Figure 6. Schematic representation of the corrections. ΔG_{dsm} is calculated over full trajectories of the end states (however, if one of the end states has zero charges, it can be skipped). ΔG_{pol} and ΔG_{dir} are both calculated on individual snapshots only. In this tutorial, only the final snapshots of 6 chosen λ -points are used for these calculations.

3.2.8 Solvent polarisation

First, we calculate the correction estimate ΔG_{pol} for the spurious solvent polarisation. We will use a set of continuum-electrostatics calculations on configurations extracted from trajectories that were sampled at different λ points. For each of these configurations, the electrostatic potential at the atom sites of the Aspirin molecule will be calculated twice - using a cutoff scheme with a reaction-field contribution under periodic boundary conditions and using full Coulombic charges under non-periodic boundary conditions. The integrated differences between both potentials will give an estimate of ΔG_{pol} , which can be directly applied to the raw free energies that were calculated in the simulation. Note that for the sake of simplicity, in this tutorial we will use only the last configurations of six λ -generated trajectories. However, when used

for “real” research questions, a more complete set of configurations should be analysed in order to achieve more reliable results.

Go into the subdirectory `corrections/ASA/dGpol`. It contains argument files for the GROMOS++ program `dGslv_pbsolv`. There are six argument files for six different λ points. Since the continuum-electrostatics calculations are computationally demanding, the output files are already provided. However, if you prefer to run the continuum-electrostatics calculations yourself, you can run them by typing

```
$ dGslv_pbsolv @f dGslv_pbsolv_L_0.0.arg >
  dGslv_pbsolv_L_0.0.out
$ dGslv_pbsolv @f dGslv_pbsolv_L_0.2.arg >
  dGslv_pbsolv_L_0.2.out
...
$ dGslv_pbsolv @f dGslv_pbsolv_L_1.0.arg >
  dGslv_pbsolv_L_1.0.out
```

Let’s have a look at one of the output files. It contains four rows for the individual atoms of the charged acetyl group of the Aspirin molecule. There are several columns. Next to basic information for the individual atoms, there are six columns with potentials created under non-periodic boundary conditions in solvation (NPBC_SLV), non-periodic boundary conditions in vacuum (NPBC_VAC), periodic boundary conditions in solvation (PBC_SLV), periodic boundary conditions in vacuum (PBC_VAC), a fast Fourier transform result for the lattice-summation method under periodic boundary conditions (FFT_LS_PBC) and a fast Fourier transform result for the reaction-field method under periodic boundary conditions (FFT_RF_PBC). The potential that has to be integrated over λ reads (NPBC_SLV - NPBC_VAC) - (PBC_SLV - PBC_VAC) - (FFT_LS_PBC - FFT_RF_PBC). Note that the last term has to be used only if a cutoff scheme with reaction field contribution was applied in the simulation. You can simply use the script `integrate.py`. Type

```
$ ./integrate.py
```

We are interested in the result NPBC - PBC, which is the correction term ΔG_{pol} .

3.2.9 Direct ligand-protein interactions

In the actual MD simulation, the interaction between the ligand and the protein atoms was calculated by a cutoff scheme with a reaction field contribution. A correct scheme would involve no cutoff and purely Coulombic interactions. ΔG_{dir} accounts for the difference between the simulated and the real case. Note that in order to minimize the dependence of the correction terms on the conformations of the molecules the same configurations have to be used for ΔG_{dir} that were

used for the calculations of ΔG_{pol} . Go into the subdirectory `correctionsASAdGdir`. It contains argument files for the GROMOS++ program `ener`. There are 12 argument files for six different λ -points, one for Coulombic interactions under non-periodic boundary conditions (NPBC) and one for Coulomb/Reaction-field interactions under periodic boundary conditions (PBC). You can use the provided output files or generate them yourself by typing

```
$ ener @f ener_PBC_L_0.0.arg >
    ener_PBC_L_0.0.out
$ ener @f ener_NPBC_L_0.0.arg >
    ener_NPBC_L_0.0.out
$ ener @f ener_PBC_L_0.2.arg >
    ener_PBC_L_0.2.out
...
$ ener @f ener_NPBC_L_1.0.arg >
    ener_NPBC_L_1.0.out
```

We are interested in the integrated energies NPBC-PBC. You can do it yourself or use a provided Python script. Simply type

```
$ ./integrate.py
```

The integrated result is the correction term ΔG_{dir} .

3.2.10 Potential from discrete solvent molecules

Another artifact stems from the impossibility of calculating the absolute zero potential in a periodic simulation box and the convention to average the solvent-generated potential over the exterior and the interior of the solvent molecules. As a consequence, the calculated potential differs from the “real” potential by an offset. For a rigid solvent model with a single van der Waals interaction site and any scheme relying on molecular-cutoff truncation based on this specific site, it can be shown that this offset is related to the quadrupole moment trace of the solvent model used. The free-energy correction is furthermore proportional to the water-molecule density inside the box (LS - lattice summation schemes) or within the cutoff radius (cutoff schemes with reaction-field correction - RF) and reads

$$\Delta G_{\text{dsm}}(\text{LS}) = -N_A(6\epsilon_0)^{-1} \gamma_s \Delta Q N_S V_B^{-1} \quad (9)$$

for the LS scheme and

$$\Delta G_{\text{dsm}}(\text{RF}) = -N_A(6\epsilon_0)^{-1} \frac{2(\epsilon_{\text{RF}} - 1)}{2\epsilon_{\text{RF}} + 1} \gamma_s \sum_{i=1}^n \Delta q_i \langle N_S(R_{C,i}) \rangle V_C^{-1} \quad (10)$$

for the RF scheme, where N_A is the Avogadro constant, ϵ_0 is the vacuum dielectric permittivity, ϵ_{RF} is the (relative) reaction-field dielectric permittivity, ΔQ is the net-charge change in the system, Δq_i is the net-charge change of the perturbed atom i , N_S is the number of solvent molecules in the box, $\langle N_S(R_{C,i}) \rangle$ is the average number of solvent molecules in the

cutoff sphere of the perturbed atom i , V_B is the volume of the computational box and V_C is the volume of the cutoff sphere. γ_s is the quadrupole moment trace relative to the van der Waals interaction site. Values for typically used water models can be found in table 1. Hint: the reaction-field permittivity used in the simulations can be found in the `NONBONDED` block in one of the `imd` files, parameter `EPSRF`.

Table 1. Quadrupole-moment traces [e nm^2] for typical solvent models

model	γ_s
SPC [14]	0.008200
SPC/E [32]	0.008476
TIP3P [33]	0.007641
TIP4P [33]	0.009295
TIP5P [34]	0.002054
ST2 [35]	0.001754

Go into the subdirectory `corrections/ASA/dGdsm`. First, we need to calculate the average number of water molecules in the cutoff sphere that was used in the simulation. We will calculate this number using a radial distribution function (`rdf`) over the trajectory that was generated with full charges on the perturbed atoms. The argument file for the GROMOS++ program `rdf` is already provided, as is the output file for the case your simulation did not finish yet. You can run `rdf` by typing

```
$ rdf @f rdf.arg > rdf.out
```

The output file contains the densities of water particles as function of the distance of all the perturbed atoms. To obtain the total number of water molecules, these densities need to be integrated over the distance and multiplied by the water number density $\rho = N/V_B$ in the simulation box. Equation 10 then gives the final correction term ΔG_{dsm} . You can calculate it by typing

```
$ ./integrate.py
```

This script reads the file `rdf.out` as well as `system.info` that contains relevant information about the box size, the cutoff, the correction field and the solvent model. Relevant information about the box size can be found by looking into one of the configuration files - the `POSITION` block contains the number of solvent molecules and the `GENBOX` block provides the box dimensions. Settings for the electrostatics can be found in the `NONBONDED` block in the `imd` files.

3.2.11 Corrected results

Above, the three correction terms for Aspirin free in solution were calculated. According to equation 8, the sum of these three correction terms constitutes the total correction for

this branch of the thermodynamic cycle. The same set of correction terms has to be calculated for the ligand bound to the host (directory `corrections/PLA2_ASA`). Both corrections can be directly added to the raw free energies to yield methodologically independent results (see table 2). The final calculated estimate $\Delta G_{\text{bind}}^{\circ} = \Delta G(\text{PLA}_2\text{-ASA}) - \Delta G(\text{ASA}) = -32.3$ kJ/mol agrees quite well with the experimentally determined estimate of $\Delta G_{\text{bind,exp}} = -29.6$ kJ/mol [18].

Table 2. Results from Double Decoupling with corrections. All values are reported in kJ/mol.

System	ΔG_{raw}	ΔG_{res}	ΔG_{pol}	ΔG_{dir}	ΔG_{dsm}	ΔG
ASA	-371.2	-	12.3	-9.1	77.5	-290.5
PLA ₂ _ASA	-383.2	18.2	-13.3	23.4	32.1	-322.8

3.3 Tutorial 3: Using HREMD and distance-field

Another way to calculate the binding free energy of a ligand to a protein is to pull the ligand out of the active site. There are several methods available to perform such calculations, however, most of them require the *a priori* knowledge of the dissociation path. Even if the dissociation path is determined during the simulation, it is often assumed that it is linear, or that only a single dissociation path exists. For an accurate estimate of the binding free energy the simulations should be performed such that the binding and unbinding of the ligand can be sampled reversibly. In this tutorial we will use the distance-field (DF) distance as the reaction coordinate and combine this with Hamiltonian-replica-exchange molecular dynamics (HREMD) simulations [36]. The advantage of the DF distance is that we will be able to pull the ligand back into the active site, even if it moved to the other side of the protein. The HREMD simulations allow for multiple paths to be sampled reversibly.

3.3.1 Preparations

As in the tutorial above, we will use the PLA₂ - ASA complex as a test system. The preparation of the topology, coordinates, the energy minimization and the equilibration of the system are very similar to the tutorial above. The only difference is that we will use a larger cubic box to allow the ligand to move freely in the solvent. The final equilibrated structure can be found in the directory `eq` with the name `eq_PLA2_ASA_Ca_2Na_7.cnf`.

3.3.2 Slow-growth

In order to get some initial coordinates for each of the replicas of the HREMD simulations, we will perform a short slow-growth simulation where the ligand is pulled out of the active site in a non-equilibrium manner. The exact pulling speed and

force constant are not relevant in this case as we are not trying to calculate the binding free energy from the slow-growth simulations. It is, however, important that the structure of the protein does not get disrupted during this initial simulation. The slow-growth simulation is started from the final configuration of the equilibration. Go to the directory `slowgrowth` and have a look at the `PERTURBATION` block in the input file `slowgrowth.imd`.

```
PERTURBATION
#      NTG      NRDGL      RLAM      DLAMT
#          1          0        0.0      0.001
#  ALPHLJ  ALPHC      NLAM  NSCALE
#          0.0        0.0          1          0
END
```

With `NTG` set to 1, you specify that a free energy calculation will be performed. The starting λ point `RLAM` is set to 0. With each timestep during the simulation, λ will be increased. The rate of increase in ps^{-1} is set to `DLAMT` = 0.001. Together with `NSTLIM` = 500000 (from the `STEP` block) and an integration time step of 0.002 ps this results in a simulation of 1ns where λ is continuously changed from 0 to 1. `ALPHLJ` and `ALPHC` are the softness parameters of the Lennard-Jones and Coulombic interactions, respectively. These are set to 0 here, because we are not changing any nonbonded interactions, only distance restraints. In addition to that, we have to specify which kind of restraints will be used. In this case we will use distance-field distance restraints:

```
DISTANCEFIELD
#  NTDFR
#          1
#  GRID  PROTEINOFFSET  PROTEINCUTOFF  PROTECT
#    0.2         15          0.2          0
#  UPDATE  SMOOTH    RL    NTWDF    PRINTGRID
#    100         1    1.0    1000          0
END
```

With `NTDFR` set to 1, we turn on distance-field (DF) restraining during the simulation. Typically the grid size (`GRID`) for the DF calculation is set to 0.2 nm. `PROTEINOFFSET` is the penalty which is added to the DF distance if the path crosses the host. This value has to be large enough, such that paths through the protein always result in larger DF distances than around the protein. Here we have chosen `PROTEINOFFSET` = 15. `PROTEINCUTOFF` = 0.2 determines that any grid point which is within 0.2 nm of a protein atom will be flagged as protein. In cases where the binding site is quite small, it can happen that the zero distance point is often flagged as protein, in these cases it might be necessary to use `PROTECT` > 0. This is the radius around the zero-distance point in which a grid point will not be flagged as protein. For our simulation,

we will leave this value at 0.

In order to speed up the simulation, the grid is calculated only every `UPDATE = 100` steps. The `SMOOTH` parameter is used to prevent very large forces acting at the surface of the protein due to the large penalties. With each smoothening step the non-protein grid points are identified which have a direct neighbouring grid point flagged as protein. These are on the edge of the protein and we will recalculate their DF distance but now without the protein penalty. This removes the large forces pointing away from the protein, but because the smoothening steps are performed after the updating step, they do not influence the optimal route. We will set the number of smoothening rounds to 1. Forces change linearly for distances larger than 1 nm as set by `RL`. We will write DF distances and forces to an external file (special trajectory file, `*.trs`) every `NTWDF = 1000` steps. We will not print the grid to the final configuration, so we use `PRINTGRID=0`. The definition of the distance restraint that will be modified during the slow-growth simulation, is specified in the distance restraint specification file `disres.dat`. There are two blocks in this file. The first one, `DISTANCERESSPEC` specifies the distance restraints between the Ca^{2+} ion and its surrounding residues, which prevents the Ca^{2+} from drifting away. The second block `PERTDFRESSPEC` specifies the perturbed distance-field restraints.

```
PERTDFRESSPEC
# DISH DISC
  0.1   0.153
# PROTEINATOMS  A_R0  K_A  B_R0  K_B  M  N
                1190   0.0  500   5.0  500  0  0
#  TYPE_I  NUM_I  ATOM_I [0]  ..  ATOM_I [NUM_I]
    -1      7    16 190 249 312 486 632
                1208
#  TYPE_J  NUM_J  ATOM_J [0]  ..  ATOM_J [NUM_J]
    -1      2   1194 1203
END
```

`DISH = 0.1` specifies the carbon - hydrogen distance and `DISC = 0.153` specifies the carbon-carbon distance in nm. These are used to compute the position of some types of pseudo or virtual atoms, respectively, from the positions of explicitly represented atoms. `PROTEINATOMS` specifies the last atom number of the protein which will be used to flag protein atoms. `A_R0` and `B_R0` are the restraining distances in nm at $\lambda = 0$ and $\lambda = 1$, respectively. We will use a force constant of $500 \text{ kJ mol}^{-1} \text{ nm}^{-2}$ which remains the same upon changing λ ($K_A = K_B = 500$). We will not use hidden distance restraints, so `M = N = 0`.

The distance between pseudo atom *i* and pseudo atom *j* will be restrained, where pseudo atom *i* is defined as the center of geometry of 7 atoms (`NUM_I = 7`) with atom numbers

16, 190, 249, 312, 486, 632 and 1208. These atom numbers correspond to the C_α atoms of residues L2, W18, A22, C28, D48, Y63 (residue numbers according to the topology) and the calcium ion. Pseudo atom *j* is the center of geometry of atoms C2 and C7 (topology names) of the aspirin ligand. All input files are now prepared and we can generate the run file with:

```
$ mk_script @f mk_script.arg
```

Make sure the generated `slowgrowth_PLA2_ASA_1.run` file is ready to be submitted to a cluster. After running the slow-growth simulation, we can analyze the system by using `trs_ana`. We will use this program to read out the DF distances and forces from the special trajectory, `*.trs`, file. An example of the argument file is prepared in `trs_ana.arg`. You can run the program with

```
$ trs_ana @f trs_ana.arg
```

The DF distance as a function of time is written out to the file `df_dist.dat`. Have a look at the file with e.g. `Xmgrace` and make sure no sudden jumps are present. We also need to make sure that the protein was not disrupted during the pulling process. For this, calculate the root-mean-square deviation (RMSD) as a function of time with

```
$ rmsd @f rmsd_bb.arg > rmsd_bb.dat
$ rmsd @f rmsd_all.arg > rmsd_all.dat
```

Have a look at the RMSD of the backbone atoms (`rmsd_bb.dat`) as well as for all protein atoms (`rmsd_all.dat`). When both the `df_dist.dat` and the RMSD plots look normal, we can continue to prepare the starting structures for the replica-exchange simulations. If not, the slow-growth simulation should be performed again with some variables modified. For example, you can decrease `DLAMT` (and increase `NSTLIM` accordingly) in order to pull slower. Changing the force constant of the DF restraints (`K_A` and `K_B` in the `PERTDFRESSPEC` block) or choosing different atoms to apply the DF restraints to can also help to avoid any disruption of the protein.

3.3.3 Hamiltonian-replica-exchange simulations

One of the first choices that we have to make when starting a HREMD simulation, is how many replicas will be used. For performance issues it is best to keep the number of replicas equal to the number of CPUs available (preferably on a single computational node). In the prepared example, we used 24 replicas. Have a look at the prepared input file for the replica-exchange simulation (`HREMD.imd` in the directory `HREMD`). You will find that the `PERTURBATION` block is still present, but with `DLAMT` now set to 0. This means we are still calculating free energies, but we are no longer changing the λ parameter

during a single simulation. The DISTANCEFIELD block is pretty much unchanged, apart from NTWDF because we will write out the DF data more often. You will also find an additional block:

```
REPLICA
# NRET
1
# RET(1..NRET)
298.0
# LRESALE
0
# NRELAM
24
# RELAM(1..NRELAM)
0.0000 0.0435 0.0870 0.1304 0.1739 0.2174
0.2609 0.3043 0.3478 0.3913 0.4348
0.4783 0.5217 0.5652 0.6087 0.6522
0.6957 0.7391 0.7826 0.8261 0.8696
0.9130 0.9565 1.0000
# RETS(1..NRELAM)
0.002 0.002 0.002 0.002 0.002 0.002
0.002 0.002 0.002 0.002 0.002
0.002 0.002 0.002 0.002 0.002
0.002 0.002 0.002 0.002 0.002
0.002 0.002 0.002
# NERTRIAL
100
# NREQUIL
0
# CONT
1
END
```

Because we will perform Hamiltonian-replica-exchange and not temperature replica exchange, the number of replica exchange temperatures are set to NRET=1. We thus also only have one RET value which is the temperature of each replica, in this case equal to 298 K. We do not need to scale temperatures after exchange trials, so LRESALE=0. NRELAM is the number of replica-exchange lambda values, which is set to 24 here. For each of the replicas you have to specify at which λ value it should be simulated. These values are given at RELAM. We do not know the optimal spread of the λ values of the replicas before actually running the simulations, so as an initial guess we just spread them evenly between $\lambda = 0$ and 1. We will keep the standard timestep of 0.002 ps for each λ -replica, as given by RETS. In order to keep the simulation time per run short, we set the number of exchange trials per run to NERTRIAL=100. Prolonging the simulations can then be done by performing multiple runs sequentially. NREQUIL sets the number of exchange periods for equilibration, during which no switches between the replicas are allowed. This would

be especially beneficial if you start the HREMD simulations from a single configuration and you need time to equilibrate. Since we start from multiple configurations which are close to their respective λ values, we will set this to 0. CONT=1, as we start from multiple configuration files, instead from a single configuration. The next step will be to select the appropriate configurations from the slow-growth simulation as initial configurations for each of the replicas.

The script `write_start_files.py` in the directory `starting_coordinates` will help with this. The program will find the λ values of the replicas, look for the DF restraint in the PERTDFRESSPEC block in the distance restraints file and determine the restraining distances for each of the replicas from this information. It will then search for the frame in the slow-growth simulation which has a DF distance which is closest to the restraining distance of this replica. This frame will be written to a separate file for each of the replicas, named `start_{X}.cnf`, where X will be the replica number. An example argument file is provided which lists the topology of the system, the DF distances over time of the slow-growth simulation (`df_dist.dat`), the coordinate trajectory from the slow-growth simulation, the HREMD input file and the distance restraint specification file as will be used for the HREMD simulation. To run the script:

```
$ ./write_start_files.py
@write_start_files.arg
```

The starting coordinates for the HREMD simulation are now available and we can prepare the run files with `mk_script`:

```
$ mk_script @f mk_script.arg
```

The HREMD simulations are split into quite a few runs, in order to prevent an extremely long single simulation. Go to the first directory, `run1` and submit `HREMD_1.run` to a computer cluster, preferable with the same number of CPUs as we have replicas, which would be 24 in the prepared example.

3.3.4 Analysis of HREMD

All analyses for HREMD simulations will be performed in the subfolder `analysis`. In order to make sure the choice of replicas is appropriate, we will analyze whether there were sufficient switches between the replicas. This can be done already after only a few runs have finished. The switching information of the replicas is written out to the `replica.dat` file for each of the runs separately. You can combine them into a single file by using the provided script:

```
$ ./gather_replica_data.sh [nr_runs]
[nr_trials]
```

Here, you need to replace `[nr_runs]` with the number of runs which have been performed already and `[nr_trials]` with the

number of exchange trials per run, which was set to 100 in the example files. This script results in the file `replica_all.dat`. The switches of the replicas can now be visualized by running

```
$ ./rep_ana_mpi.py replica_all.dat
```

The resulting `rep_change.out` file can be opened with Xmgrace. An example of such file is shown in Figure 7.

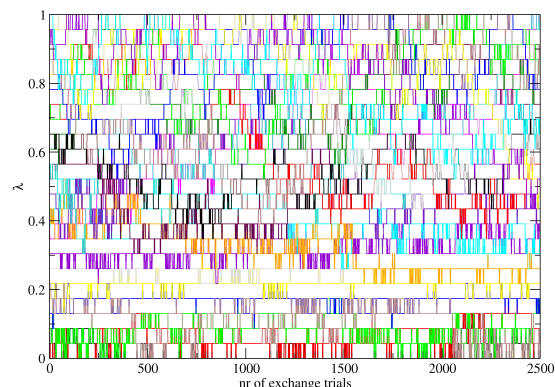


Figure 7. Replica exchanges during time. Different colors represent different replicas.

In case there is a pair of λ points for which not enough switches are occurring, you have two options to resolve this. You can either insert another λ point or make the difference between the λ points smaller. The former option is maybe quicker to set up, but requires longer simulation time because of the additional replica. The latter option does not require more replicas, but it is not guaranteed that your small change improves the switching probabilities and that you do not introduce another region of low switching probability due to the change. Of course you can also use more elaborate methods to optimize the λ -spacing [37].

If you are happy with the switching probabilities, you can start preparing for the calculation of the Free Energy Curve (FEC). First, we have to write out the measured DF distances for each of the replicas. Then we calculate the distributions of these and on this data we can perform the weighted histogram analysis method (WHAM) which will result in the FEC. We will again use the program `trs_ana` to extract the DF distance from the special trajectories (`*trs.gz`). A small script is provided which runs this program for each of the replicas, thereby collecting data from each of the runs.

```
$ ./do_all_trs_ana.sh [nr_runs]
                    [nr_replicas]
```

This will generate a subdirectory called `df_dist` which then contains `df_dist_X.dat` files for each replica X. From these

distance files, we will first generate the distributions, which can then be used to determine the FEC by applying WHAM. The program `tcf` can generate distributions for each of the `df_dist` files. We will set the boundaries to 0 and 5 nm (the same range as the restraining distances) and use 200 bins. Especially the boundaries should be adapted when working on different systems. Again, a small script is prepared which will perform the program `tcf` on each of the replicas:

```
$ ./do_tcf.sh [nr_replicas]
```

One should always check whether the distributions at adjacent λ -values are sufficiently overlapping and whether the individual distributions are sufficiently sampled. We can then determine the FEC $F(r)$ by using the WHAM program. Note that the FEC contains the Jacobian contribution, whereas a PMF does not [38]. As input parameters, the WHAM program needs the temperature of the simulation, the restraining distance for each replica and the force constant of the restraints. All this information is read from the `HREMD.imd` and `disres.dat` files as specified in the `do_wham.sh` file:

```
$ ./do_wham.sh
```

This script also moves the final FEC on the y-axis such that its minimum is placed at 0 kJ/mol. The file `wham_FEC_200bins_5000iter_min0.dat` now contains the final FEC, which is shown in Fig. 8. As you can see, the curve is not completely flat at larger distances, but is rather noisy. Ideally, you would have to change the spacing of the replicas, add more replicas in the unbound range, or lower the maximum distance which you restrain such that the replicas are placed more densely in the unbound range. However, we can still see where the plateau of the unbound range is, so we will go ahead with the calculation of the binding free energy.

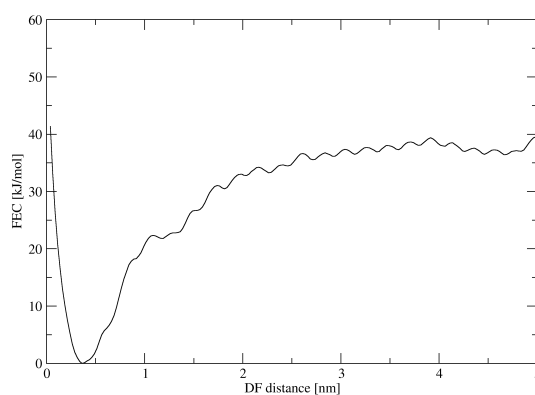


Figure 8. Free Energy Curve (FEC) along the DF distance as obtained from HREMD simulations, for the PLA2-ASA system.

3.3.5 Calculation of binding free energy

To derive the binding free energy from the FEC in Fig. 8 we cannot simply take the value of ΔG at the plateau around the unbound state. We will need to integrate the bound and unbound ranges of the FEC and we will need to include the standard state correction of

$$\Delta G_{\text{std}} = -k_B T \ln \left(\frac{V_u}{V^\circ} \right) \quad (11)$$

Here, V° is the standard state volume of 1.661 nm^3 and V_u is the unbound volume which is sampled by the ligand in the unbound range. This range is defined by the plateau observed in the FEC curve.

In order to determine V_u we need to select the configurations of the trajectory which contributed to the plateau range of the FEC. In this example, the plateau can be observed between 3 and 5 nm. The script `select_frames_unbound_region.sh` (which you can find in the subdirectory `unboundVolume`) will select the appropriate frames by reading in the `df_dist_X.dat` files which were generated using `do_all_trs_ana.sh`. Since the DF distances are written out every 50 steps (`NTWDF=50`) and the coordinates only every 1000 steps (`NTWE=1000`), the script filters the `df` distance file such that it matches the timesteps of the coordinate trajectory. In order to run the program, specify the number of replicas, the number of runs and the boundaries of the unbound range:

```
$ ./select_frames_unbound_region.sh 24
[nr_runs] 3.0 5.0
```

A list of the selected configurations (`list_frames_unbound_region.txt`) as well as the trajectory with only these configurations (`unbound_region_frames.trj`) are written to separate directories for each of the replicas. We will now combine all the configurations from the unbound range and determine how much volume was sampled by the ligand by using the program `iondens`. `iondens` calculates the average density of ions (ligand in our case) from a trajectory file. For the example, here you can start it with

```
$ ./do_iondens.sh
```

where we use the final configuration from the equilibration run as a reference configuration. Some parameters in `do_iondens.sh` have been set as appropriate for the current system. For example, the particle that we will be monitoring now, will not be an ion, but the centre of geometry (cog) of the atoms C2 and C3 of the aspirin ligand. The grid spacing is set to 0.1 nm, such that a single grid point corresponds to 1 \AA^3 . The thresholds are set very low, such that we pick up single occupancies of the grid points. The results are written out to multiple files, but we are interested only in the

file `grid.pdb`. This file contains one line for each of the grid points that have been sampled by the particle at least once. Since we have chosen the grid spacing such that each point corresponds to 1 \AA^3 , the number of different grid points that have been visited (number of lines in the file) corresponds to the unbound volume (in Å^3) which was sampled by the ligand during the simulations. For the current example (5 ns HREMD simulation with the unbound range chosen between 3 and 5 nm), the number of visited grid points is 11 258 which equals to a sampled unbound volume of 11.3 nm^3 .

We can now determine the raw binding free energy from the WHAM results and determine the standard state correction with the sampled unbound volume which we have just obtained. To perform this calculation, we will use the program `calc_dG_corrected.py` which you can find in the `analysis` directory. Before running the program, be sure to modify the argument file `calc_dG_corrected.arg` to your data. It should contain the file name of the WHAM results, the start of the bound range (in nm), the end of the bound range (in nm), the start of the unbound range (in nm), the end of the unbound range (in nm) and the sampled unbound volume (in nm^3), each on a separate line. You can now run the program with

```
$ ./calc_dG_corrected.py
@calc_dG_corrected.arg
```

This program will determine the raw binding free energy from the FEC $F(r)$ obtained with WHAM, the standard state correction and the final binding free energy:

$$\begin{aligned} \Delta G_{\text{bind}}^\circ &= \Delta G_{\text{bind}}^{\text{raw}} + \Delta G_{\text{std}} \\ &= -k_B T \ln \left(\frac{\int_b dr e^{-F(r)/k_B T}}{\int_u dr e^{-F(r)/k_B T}} \right) - k_B T \ln \left(\frac{V_u}{V^\circ} \right) \end{aligned} \quad (12)$$

It also prints the standard state correction and the final binding free energy. Note that in [36], $F(r)$ is referred to as $\Delta G_{\text{WHAM}}(r)$. The expression (Eq. 21) used in that paper to calculate the binding free energy is obtained when shifting $F(r)$ to become $\hat{F}(r) = F(r) + C$, such that $\int_b dr e^{-\hat{F}(r)/k_B T}$ becomes equal to 1. This is achieved for

$$C = k_B T \ln \int_b dr e^{-F(r)/k_B T} \quad (13)$$

Note that the minus sign in Eq. 21 of ref [36] should actually be a plus sign.

We have performed the prepared HREMD simulations for 5 ns and obtained $\Delta G_{\text{bind}}^{\text{raw}} = -31.9 \text{ kJ/mol}$, $\Delta G_{\text{std}} = -4.7 \text{ kJ/mol}$ and $\Delta G_{\text{bind}}^\circ = -36.7 \text{ kJ/mol}$. The final result is similar to what we found in the previous tutorial (-32.2 kJ/mol), but deviates a bit more from the experimental estimate of -29.6 kJ/mol [18]. As mentioned before, the spacing of the replicas is not optimal in the current example. This can influence both

the convergence of the FEC and final binding free energies. An improvement of the accuracy of the final binding free energy can thus likely be obtained by optimizing the spacing of the replicas, adding more replicas and/or prolonging the simulations.

4 Author Contributions

JG and NH prepared Tutorial 1, BL, CÖ, AdR and CO prepared Tutorials 2 and 3. All authors contributed to manuscript writing.

5 Other Contributions

This work has profited from the experiences of various members of the research groups of WFvG, NH and CO using the methods explained in this tutorial.

6 Potentially Conflicting Interests

WFvG, CO and NH are developers of the GROMOS simulation package.

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Author Information

ORCID:

Wilfred F. van Gunsteren: [0000-0002-9583-7019](https://orcid.org/0000-0002-9583-7019)

Chris Oostenbrink: [0000-0002-4232-2556](https://orcid.org/0000-0002-4232-2556)

Niels Hansen: [0000-0003-4366-6120](https://orcid.org/0000-0003-4366-6120)

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