

Show  $T(n) = 4n^2 + 2n + 1 \in \Theta(n^2)$

First show that  $T(n) \in O(n^2)$

$$\begin{aligned}4n^2 + 2n + 1 &\leq cn^2 \\n &= 1 \\4 + 2 + 1 &\leq 7 \\c = 7, n_0 &= 2 \\4n^2 + 2n + 1 &\leq 7n^2 \forall n \geq 1 \\ \therefore T(n) &\in O(n^2)\end{aligned}$$

and then  $T(n) \in \Omega(n^2)$

$$\begin{aligned}4n^2 + 2n + 1 &\geq cn^2 \\n &= 1, c = 1 \\4n^2 + 2n + 1 &\geq n^2 \forall n \geq 1\end{aligned}$$

$T(n) \in O(n^2)$  and  $T(n) \in \Omega(n^2) \therefore T(n) \in \Theta(n^2)$