

show $T(n) = 4n^2 + 2n + 1 \in O(n^2)$

$$4n^2 + 2n + 1 \leq cn^2$$

$$4 + \frac{2}{n} + \frac{1}{n^2} \leq c$$

$$n_0 = 1$$

$$5 \leq c$$

$$c = 7$$

$$\therefore 4n^2 + 2n + 1 \leq 7n^2$$

$$\forall n \geq 1$$

show $T(n) = 4n^2 + 2n + 1 \in \Omega(n^2)$

$$4n^2 + 2n + 1 \geq cn^2$$

$$4 + \frac{2}{n} + \frac{1}{n^2} \geq c$$

$$n_0 = 1$$

$$5 \geq c$$

$$c = 4$$

$$\therefore 4n^2 + 2n + 1 \geq 4n^2$$

$$\forall n \geq 1$$

$$\Theta(n^2) = \Omega(n^2) \cap (n^2)$$

$$\therefore T(n) \in \Theta(n^2)$$

(b) $O(n^2)$